formalising choreographic programming

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the goal

long-term

a certified framework for choreographic programming

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in this talk

the first steps

- a core choreographic language
- a proof of turing completeness
- a core process calculus
- certified choreography compilation

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very brief summary

initially presented at types'19, publications at itp'21 & ictac'21

choreographic programming, conceptually

what are choreographies?

high-level global specifications of concurrent and distributed systems

a new programming paradigm

implementations for the local endpoints are automatically generated

- guaranteed to be deadlock-free
- guaranteed to satisfy the specification

an example

authentication choreography

```
c.credentials --> ip.x;
If ip.(check x)
Then ip --> s[left]; ip --> c[left]; s.token --> c.t
Else ip --> s[right]; ip --> c[right]
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local implementations

```
c :  ip!credentials; ip & {left:  s?t; right:  0 }
s :  ip & {left:  c!token; right:  0 }
ip:  c?x; If (check x) Then (s(+)left; c(+)left)
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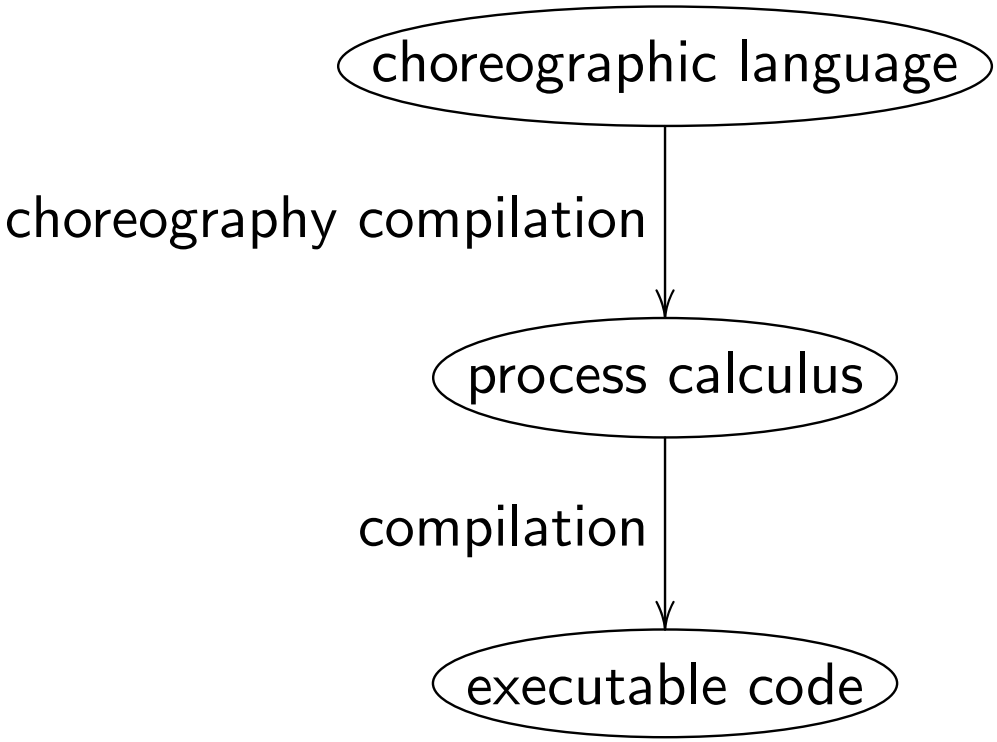
(gets tricky in the presence of recursion. . .)

a bird's-eye view



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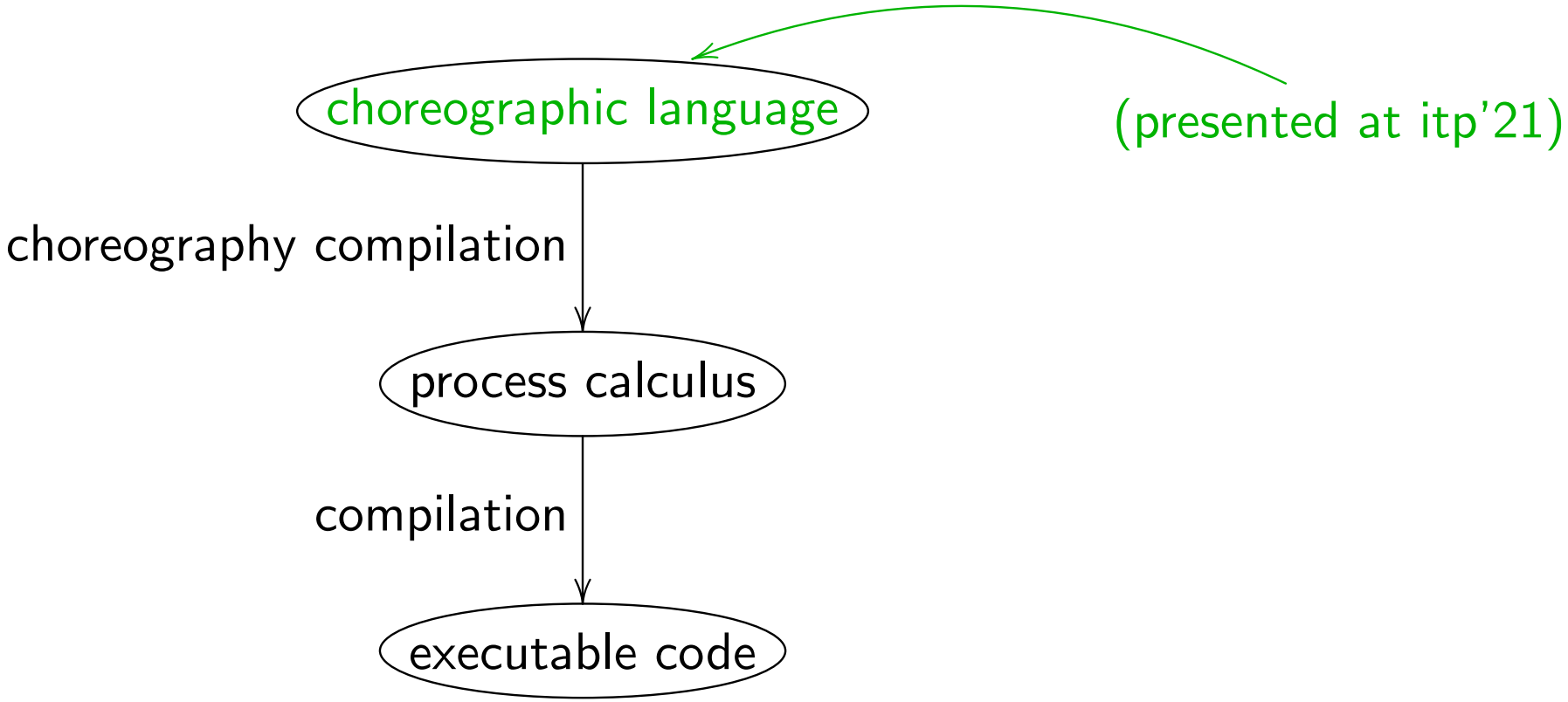

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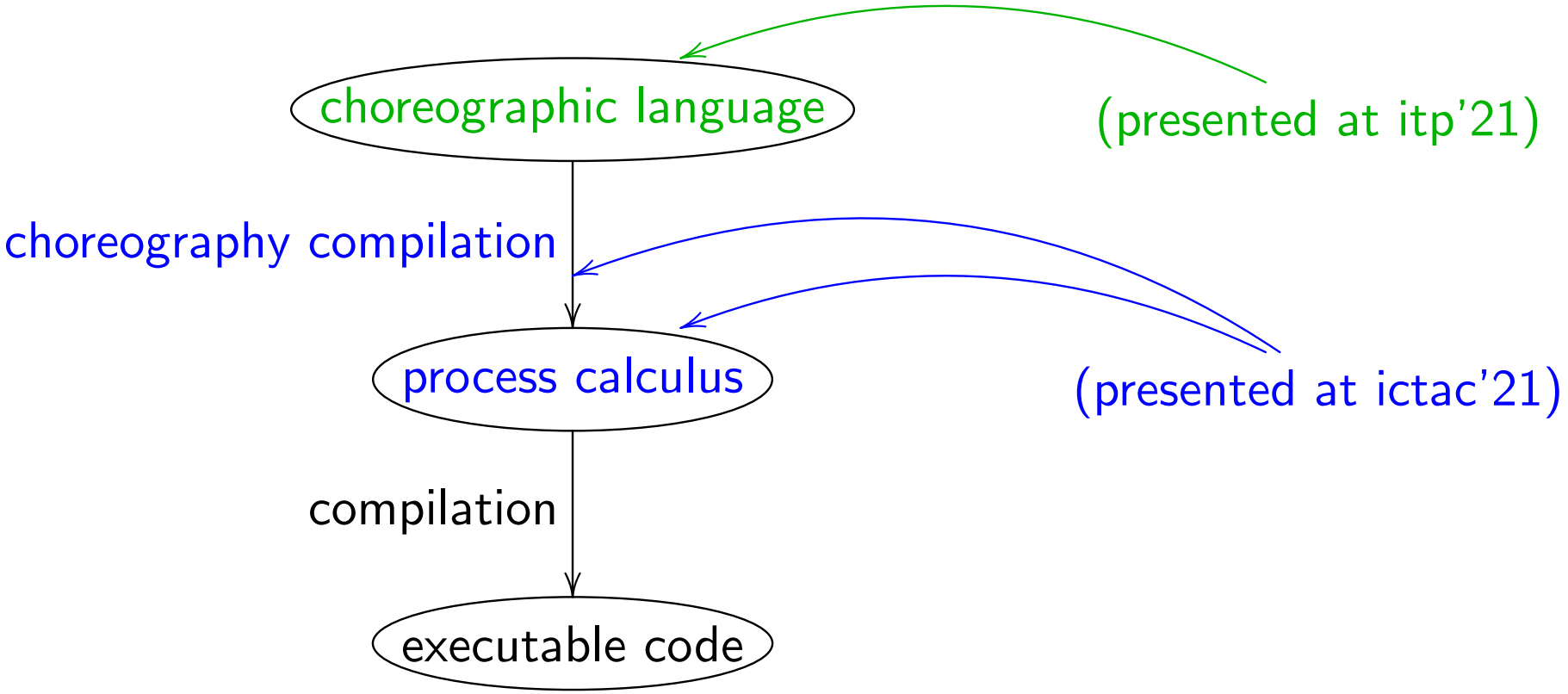

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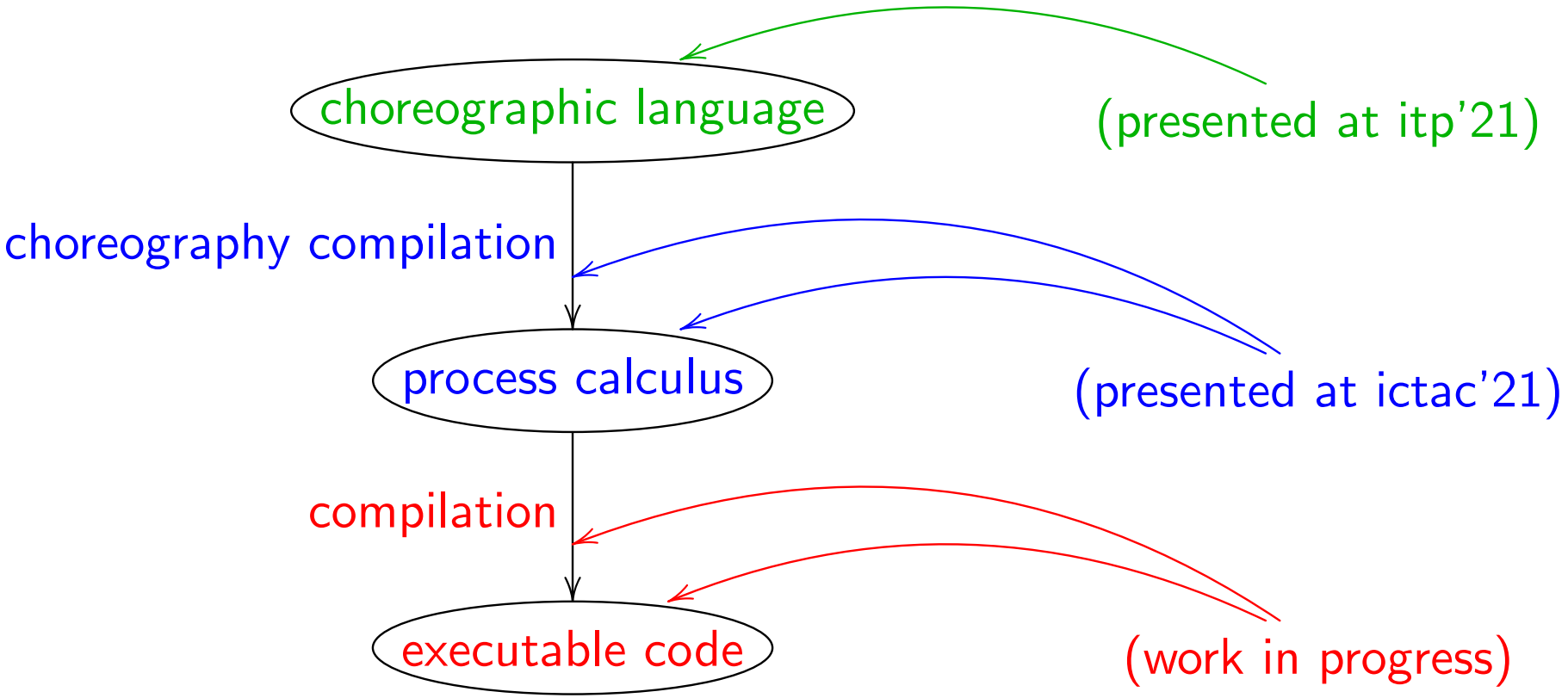

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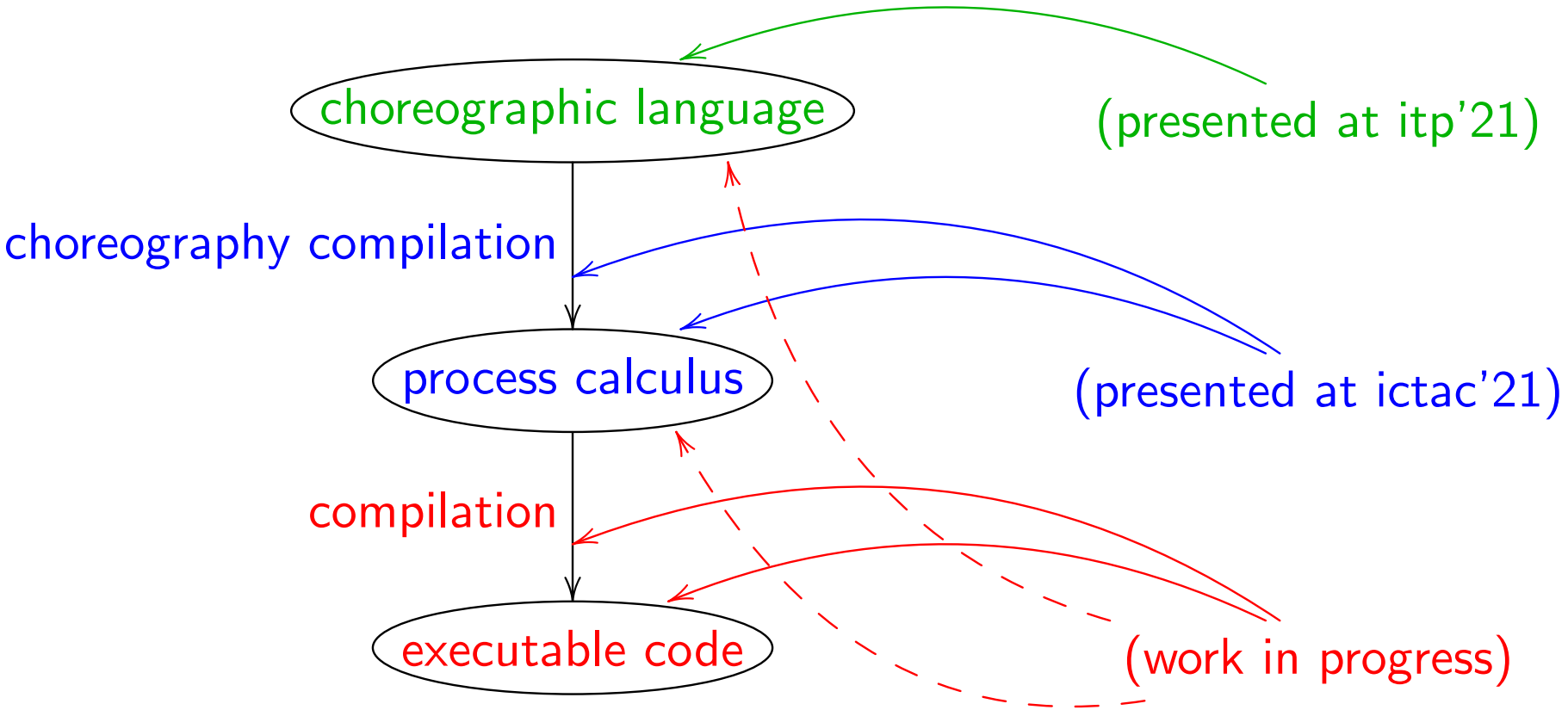

why bother formalizing?

choreographies are a popular topic...

- active research field
- many relevant applications
- potential in choreographic programming

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...but there are many disturbing signs

process calculus and session types plagued by wrong proofs

- complex definitions, long proofs by structural induction
- situation pointed out at itp'15
  - formalization of a published journal article
  - most proofs were wrong (but the theorems held)
- big revision of decidability results in the last few years
  - published proofs of both A and $\neg A$ for quite a few A...

the first step

formalization of a core choreography language

- parametric on expressions, values, &c
- syntax and semantics
- properties: progress, determinism, confluence, deadlock-freedom
- turing-completeness from the communication structure

(itp'21)

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(itp'21)

methodology

- closely followed a published reference
- formalizing took less time than getting **that** paper accepted
- no wrong proofs found, but...

the choreography language

a minimal language

- value communication
- label selections (for projection)
- conditionals
- trailing procedure calls (for recursion)

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agnostic language

- parametric on expressions and values
- only two labels

is this good or bad?

first attempt: a miserable failure

- bad model of *out-of-order execution*

  `p.e --> q.x; r.e' --> s.y` has two possible reduction paths

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- pen-and-paper definition by means of a structural precongruence (ugh)
- the number of auxiliary results exploded, with no end in sight

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two weird coincidences?

- oddly enough, this is also where students get stuck
- properties are very "intuitive" and actually never* proved

*to the best of the speaker's knowledge

is this good or bad? (cont'd)

second attempt: a success story with side-effects

- model out-of-order execution using an lts
- "intuitive" properties no longer needed (or can be proved)
- auxiliary lemmas disappeared
- final proof of confluence around 25% of the size of the previous (incomplete) development

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and the cherry on top of the cake

our students also liked the new definitions :-)

random thoughts

proof layering

as usual, the theory is developed in "layers", each depending on the previous

- confluence and determinism of the semantics were key ingredients for turing-completeness
- once the "right" definitions were there, the development was very smooth

random thoughts

very classical turing completeness

proved by showing that all partial recursive functions can be implemented as a choreography

- language where values are natural numbers, minimal set of expressions
- a choreography C implements a function $f : \mathbb{N}^n \to \mathbb{N}$ with input processes $p_1, \ldots, p_n$ and output process q if:
  - if $f(k_1, \ldots, k_n)$ is defined and each p_i initially stores k_i, then execution of C terminates in a state where q stores $f(k_1, \ldots, k_n)$
  - if $f(k_1, \ldots, k_n)$ is undefined and each p_i initially stores k_i, then execution of C never terminates

the second step

the epp theorem

- definition of a suitable process calculus
- formalisation of endpoint projection
- challenges: partial functions (branching terms, merging, projection)
- different solutions (dedicated terms, auxiliary types, indirect definitions)
- case explosion (partially) handled by automation

(ictac'21)

the process calculus

networks

finite sets of processes running in parallel

behaviours

local counterparts to the choreography actions

- send and receive
- choice and branching
- conditional
- trailing procedure calls

agnostic language as before

- parametric on expressions and values
- only two labels

compilation, informally

actions split in their components

- value communication $\rightsquigarrow$ send/receive pair
- label selection $\rightsquigarrow$ choice/branching pair
- conditional $\rightsquigarrow$ conditional
- procedure call $\rightsquigarrow$ procedure call

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knowledge of choice

when a process makes a choice, other processes' behaviours can only depend on it after it has been communicated to them

compilation and knowledge of choice

authentication choreography, wrong

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c.credentials --> ip.x;
If ip.(check x)
Then s.token --> c.t
Else 0
```

local implementations

```
ip:  c?x; If (check x) Then 0 Else 0
c :  ip!credentials; ???
s :  ???
```

compilation and knowledge of choice

authentication choreography, right

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compilation and knowledge of choice

authentication choreography, with logger

```
c.credentials --> ip.x;
If ip.(check x)
Then ip.(x,yes) --> l.y; (...)
Else ip.(x,no) --> l.y; (...)
```

local implementations

```
l :  ip?y
(...)
```

the challenges of partiality

compilation is a partial function

- failure can arise from trying to combine (merge) incompatible branches of a conditional

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all coq functions are total

- explicit terms for failure
- option monad
- proof terms where needed

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  (requires extended syntax, generates isomorphic structures)
- option monad
  (requires a lot of case analysis, horrible proofs)
- proof terms where needed
  (requires bookkeeping, proof irrelevance)

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$\rightsquigarrow$ no "best" solution, we use a bit of everything

the challenges of case explosion

the root of all problems

the main results require proofs by structural induction, often on two objects

- enormous amounts of cases (e.g. 512, with one subcase further dividing into 64)
- strong similarities among cases, but still slightly different proofs

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coq to the rescue!

automation features and tactic language

what's next?

implementation

using coq's extraction mechanism, we can obtain a certified compiler from choreographies to processes

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next step

build an (uncertified?) compiler to a real programming language

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build an (uncertified?) compiler to a real programming language

- ✓ requires additional syntax to be able to annotate the code with information to the compiler

conclusions

the eternal question

is it worthwhile to formalize current research?

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formalising choreographic programming:

- is feasible
- is useful
- can speed up things

conclusions

the eternal question

is it worthwhile to formalize current research?

formalising choreographic programming:

- is feasible
  - we did it (at least partially)
- is useful
  - our theory benefitted from it
- can speed up things
  - convincing the reviewers took three years
  - convincing coq took only two. . .

thank you!