

# Lucas ciardullo

1) a) 10111

$$2^0 \times 1 + 2^1 \times 1 + 2^2 \times 1 + 2^3 \times 1 = 23$$

b) 11111

$$2^0 \times 1 + 2^1 \times 1 + 2^2 \times 1 + 2^3 \times 1 + 2^4 \times 1 = 31$$

c) 10000001  ~~$2^0 \times 1$~~

$$2^0 \times 1 + 2^7 \times 1 = 128$$

d) 10,1

$$1 \times 2^0 + 0,1 \times 2 = 2$$

$$1 \times 2^1 + 1 \times 2^{-1} = 2,5$$

e) 10,101

$$1 \times 2^1 + 2^{-1} \times 1 + 2^{-3} \times 1 = 2,625$$

f) 100,011

$$1 \times 2^2 + 2^{-2} \times 1 + 2^{-3} \times 1 = 4,375$$

g) 1011,0101

$$1 \times 2^0 + 1 \times 2^1 + 2^3 \times 1 + 2^{-2} \times 1 + 2^{-4} \times 1 = 11,3125$$

h) 1100,011

$$1 \times 2^2 + 1 \times 2^3 + 2^{-2} \times 1 + 2^{-3} \times 1 = 12,375$$

2) a) 55

$$\begin{array}{r} 55 \overline{) 2} \\ 1 \quad 27 \overline{) 2} \\ \quad 1 \quad 13 \overline{) 2} \\ \quad \quad 1 \quad 6 \overline{) 3} \\ \quad \quad \quad 0 \quad 2 \overline{) 2} \\ \quad \quad \quad \quad 1 \quad 1 \overline{) 2} \\ \quad \quad \quad \quad \quad 1 \quad 0 \end{array}$$

110111

$$\begin{array}{r} 48 \overline{) 2} \\ 0 \quad 24 \overline{) 2} \\ \quad 0 \quad 12 \overline{) 8} \\ \quad \quad 0 \quad 6 \overline{) 2} \\ \quad \quad \quad 0 \quad 3 \overline{) 2} \\ \quad \quad \quad \quad 1 \quad 2 \overline{) 2} \\ \quad \quad \quad \quad \quad 1 \quad 0 \overline{) 5} \\ \quad \quad \quad \quad \quad \quad 1 \quad 0 \end{array}$$

1010000

c) 204

$$\begin{array}{r}
 204 \div 2 = 102 \\
 102 \div 2 = 51 \\
 51 \div 2 = 25 \text{ r } 1 \\
 25 \div 2 = 12 \text{ r } 1 \\
 12 \div 2 = 6 \text{ r } 0 \\
 6 \div 2 = 3 \text{ r } 0 \\
 3 \div 2 = 1 \text{ r } 1 \\
 1 \div 2 = 0 \text{ r } 1
 \end{array}$$

110 01100

d) 237

$$\begin{array}{r}
 237 \div 2 = 118 \text{ r } 1 \\
 118 \div 2 = 59 \\
 59 \div 2 = 29 \text{ r } 1 \\
 29 \div 2 = 14 \text{ r } 1 \\
 14 \div 2 = 7 \text{ r } 0 \\
 7 \div 2 = 3 \text{ r } 1 \\
 3 \div 2 = 1 \text{ r } 1 \\
 1 \div 2 = 0 \text{ r } 1
 \end{array}$$

111101101

e) 255,75

$$\begin{array}{r}
 255 \div 2 = 127 \text{ r } 1 \\
 127 \div 2 = 63 \text{ r } 1 \\
 63 \div 2 = 31 \text{ r } 1 \\
 31 \div 2 = 15 \text{ r } 1 \\
 15 \div 2 = 7 \text{ r } 1 \\
 7 \div 2 = 3 \text{ r } 1 \\
 3 \div 2 = 1 \text{ r } 1 \\
 1 \div 2 = 0 \text{ r } 1
 \end{array}$$

0,75 x 2 = 1,5  
 0,5 x 2 = 1  
 0 x 2 = 0

1111111,110

f) 10,4

$$\begin{array}{r}
 10 \div 2 = 5 \\
 5 \div 2 = 2 \text{ r } 1 \\
 2 \div 2 = 1 \\
 1 \div 2 = 0 \text{ r } 1 \\
 0 \div 2 = 0 \text{ r } 0
 \end{array}$$

0,4 x 2 = 0,8

0,8 x 2 = 1,6

0,6 x 2 = 1,2

0,2 x 2 = 0,4

0,4 x 2 = 0,8

1010,0110

g) 83,45

$$\begin{array}{r}
 83 \div 2 = 41 \text{ r } 1 \\
 41 \div 2 = 20 \text{ r } 1 \\
 20 \div 2 = 10 \text{ r } 0 \\
 10 \div 2 = 5 \text{ r } 0 \\
 5 \div 2 = 2 \text{ r } 1 \\
 2 \div 2 = 1 \text{ r } 0 \\
 1 \div 2 = 0 \text{ r } 1
 \end{array}$$

0,45 x 2 = 0,9

0,9 x 2 = 1,8

0,8 x 2 = 1,6

0,6 x 2 = 1,2

0,2 x 2 = 0,4

0,4

1010011,01110110



3) a)  $310,10_{(16)}$

Si, es posible, ya que  $2^4 = 16$  es potencia exacta por lo tanto cada número se agrupa en 4 bits

3      1      0  
0011    0001    0000

$0,1 \times 2 = 0,2$   
 $0,2 \times 2 = 0,4$   
 $0,4 \times 2 = 0,8$   
 $0,8 \times 2 = 1,6$

$$310,10_{(16)} = 001100010000,0001_{(2)}$$

b)  $310,10_{(2)}$

No, ~~es~~ no es un número válido en binario

c)  $\underbrace{10100111101}_{(2)}$

Si, por lo mismo que en el punto A

A 7 D

4) a)  $\in \mathbb{Z}$

$$16^0 \times 2 + 14 \times 16^1 = 226$$

$$\begin{array}{r} 226 \div 2 = 113 \\ 113 \div 2 = 56 \text{ r } 1 \\ 56 \div 2 = 28 \\ 28 \div 2 = 14 \\ 14 \div 2 = 7 \\ 7 \div 2 = 3 \text{ r } 1 \\ 3 \div 2 = 1 \text{ r } 1 \\ 1 \div 2 = 0 \text{ r } 1 \end{array}$$

11100010

b) 3D

$$16^0 \times 13 + 16^1 \times 3 = 61$$

$$\begin{array}{r} 61 \div 2 = 30 \text{ r } 1 \\ 30 \div 2 = 15 \\ 15 \div 2 = 7 \text{ r } 1 \\ 7 \div 2 = 3 \text{ r } 1 \\ 3 \div 2 = 1 \text{ r } 1 \\ 1 \div 2 = 0 \text{ r } 1 \end{array}$$

0d11101



c) A 0

$$16^0 \times 0 + 16^1 \times 10 = 160$$

$$\begin{array}{r} 160 \overline{) 2} \\ 0 \ 80 \overline{) 2} \\ 0 \ 40 \overline{) 2} \\ 0 \ 20 \overline{) 2} \\ 0 \ 10 \overline{) 2} \\ 0 \ 5 \overline{) 2} \\ 1 \ 2 \overline{) 2} \\ 0 \ 1 \overline{) 2} \\ 1 \ 0 \end{array}$$

10100000

d) 2,1

$$2 \cdot 16^0 + 1 \cdot 16^{-1} = 2,0625$$

$$\begin{array}{r} 2 \overline{) 2} \\ 0 \ 1 \overline{) 2} \\ 1 \ 0 \end{array}$$

$$0,0625 \times 2 = 0,125$$

$$0,125 \times 2 = 0,25$$

$$0,25 \times 2 = 0,5$$

$$0,5 \times 2 = 1$$

10010,0001

e) F, 01

$$16^0 \times 15 + 16^{-2} \times 1 = 15,00390625$$

$$\begin{array}{r} 15 \overline{) 2} \\ 1 \ 7 \overline{) 2} \\ 1 \ 3 \overline{) 2} \\ 1 \ 1 \overline{) 2} \\ 1 \ 0 \end{array}$$

$$0,00390625 \times 2 = 0,0078125$$

$$0,0078125 \times 2 = 0,015625$$

$$0,015625 \times 2 = 0,03125$$

$$0,03125 \times 2 = 0,0625$$

1111,00000001



f) 1,5

$$16^0 \times 1 + 15 \cdot 16^{-1} = 1,9375$$

10001,1111

$$0,9375 \times 2 = 1,875$$

$$0,875 \times 2 = 1,75$$

$$0,75 \times 2 = 1,5$$

$$0,5 \times 2 = 1$$

2) >  $\begin{array}{r} 1111 \\ 101101 \\ + 100011 \\ \hline 1010000 \end{array}$

b)  $\begin{array}{r} 11111 \\ 110110011 \\ 1110 \\ 11 \\ \hline 111101110 \end{array}$

c)  $\begin{array}{r} 101110111 \\ 10010101 \\ \hline \end{array}$

$\begin{array}{r} 111111111 \\ 1011101111 \\ 100010101 \\ \hline 10000000100 \end{array}$

d)  $\begin{array}{r} 1111111 \\ 1110010 \\ + 110111 \\ \hline 111 \\ 10110000 \end{array}$

e)  $\begin{array}{r} 1111 \\ 11101 \\ 1100 \\ 1101 \\ \hline 110110 \end{array}$

f)  $\begin{array}{r} 1111 \\ 10110111 \\ 00100111 \\ \hline 11011110 \end{array}$

g)  $\begin{array}{r} 1111111 \\ 000111101 \\ 01010110 \\ \hline 01110011 \end{array}$

8) >  $\begin{array}{r} 01 \\ 110111 \\ 1111 \\ 1000000 \\ 1101011 \\ 1111 \\ \hline 1011100 \end{array}$

b)  $\begin{array}{r} 00 \\ 11011 \\ 011000 \end{array}$

c)  $\begin{array}{r} 11000 \\ 111 \\ 01 \\ 11000 \\ 111 \\ \hline 01 \end{array}$



$$\begin{array}{r}
 \begin{array}{ccccccc}
 & & 0 & 1 & 1 & & \\
 & & 10 & 10 & 10 & & \\
 c) & 1 & 1 & 0 & 0 & 0 & \\
 & & 1 & 1 & 1 & & \\
 \hline
 & 1 & 0 & 0 & 0 & 1 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{cccccccccccccccc}
 & & & & 0 & 1 & 10 & 0 & 1 & 10 & 10 & 0 & 1 & 1 & 0 & 1 \\
 & & & & 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 \\
 d) & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 1 \\
 & & & & & & & & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & \\
 \hline
 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccccccc}
 & & 0 & 1 & 10 & 0 & 10 & 10 & 10 & 10 \\
 & & 10 & 10 & 10 & 10 & 10 & 10 & 10 & 10 \\
 e) & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & \\
 & & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 1 \\
 \hline
 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{cccc}
 & & 1 & \\
 9) a) & 1 & 5 & 2 & 7 \\
 & 1 & 3 & 3 & \\
 \hline
 & 1 & 6 & 6 & 2 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{cccc}
 & & 1 & \\
 b) & 1 & 7 & 4 & 0 & 6 \\
 & 6 & 3 & 0 & 5 & 4 \\
 \hline
 & 1 & 0 & 2 & 4 & 6 & 2 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & 1 & 1 \\
 c) & 3 & 6 & 5 \\
 & 2 & 3 & \\
 \hline
 & 4 & 9 & 0 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & 1 & 1 \\
 d) & 2 & 7 & 3 & 2 \\
 & 1 & 2 & 6 & 5 \\
 \hline
 & 4 & 2 & 1 & 7 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & & 1 \\
 10) a) & B & 3 & 5 & 9 \\
 & 8 & 3 & A & \\
 \hline
 & D & 8 & 9 & 3 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & & 1 \\
 b) & A & 8 & 3 & 5 & 0 \\
 & + & 0 & 1 & 2 & 3 \\
 \hline
 & A & B & 4 & 7 & 3 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & 1 & \\
 c) & A & F \\
 & C & 3 & \\
 \hline
 & 1 & 7 & 2 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & & 1 \\
 d) & 1 & 7 & 4 \\
 & 3 & C & \\
 \hline
 & 1 & B & 0 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & 1 & 1 \\
 e) & 2 & 0 & F & 3 \\
 & 3 & 1 & B & \\
 \hline
 & 2 & 4 & 1 & 0 & 
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc}
 & & 1 \\
 f) & 2 & E & 7 & 0 \\
 & 1 & 4 & A & 7 & F \\
 \hline
 & 1 & D & 8 & E & F & 
 \end{array}
 \end{array}$$

$$(1) \quad a = 10011110$$

$$b = 01101101$$

$$\begin{array}{r} 11111 \\ a) \quad 10011110 \\ \quad 01101101 \\ \hline 100001011 \end{array}$$

$$\begin{array}{r} b) \quad 10011110 \\ \quad 01101101 \\ \hline 11112211 \end{array}$$

$$\begin{array}{r} c) \quad 10011110 \\ \quad 01101101 \\ \hline 11112211 \end{array}$$

$$\begin{array}{r} d) \quad 10011110 \\ \quad 01101101 \\ \hline 11112211 \end{array}$$

$$e) a) \quad 2^0 \times 1 + 2^1 \times 1 + 2^3 \times 1 + 2^8 \times 1 = 267_{(10)}$$

$$b) \quad 11112211_{(10)}$$

$$c) \quad 8^0 \times 4 + 8^1 \times 1 + 8^2 \times 2 + 8^3 \times 2 + 8^4 \times 1 + 8^5 \times 1 + 8^6 \times 1 + 8^7 \times 1 = 2397326_{(10)}$$

$$d) \quad 16^0 + 16^1 + 16^2 \times 2 + 16^3 \times 2 + 16^4 + 16^5 + 16^6 + 16^7 = 286335505_{(10)}$$