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(A definite event is a finite class of finite inputs.) (4) There exists an indefinite event (a regular event that is not definite). (5) There exists a recursively enumerable class of binary-coded integers that is not a regular event.

The synthesis problem (the problem of constructing a net to represent specified regular events) is solved, although the solution is not of practical value.

W. L. DUDA

Edward F. Moore. Gedanken-experiments on sequential machines. Ibid., pp. 129-153.

This is a theoretical treatment of finite automata, and especially of the problem of obtaining information about an unknown automaton by imposing a sequence of inputs and observing the resulting outputs. There is no use of mathematical logic.

Author's corrections: p. 136, line 6 f.b., for "indistinguishable" read "distinguishable"; p. 151, in the last column of the tables of Machine H, for "Present Input" read "Present Output."

ALONZO CHURCH

Mochinori Goto, Yasuo Komamiya, Ryota Suekane, Masahide Takagi, and Shigeru Kuwabara. *Theory and structure of the automatic relay computer E. T. L. Mark II.* Researches of the Electrotechnical Laboratory, no. 556. Electrotechnical Laboratory, Agency of Industrial Science and Technology, Tokyo 1956, ix + 214 pp. and 37 plates.

Only Chapter III, Theory of relay networks, falls within the scope of this JOURNAL. The remarks of XX 285(2) are applicable. The theory of sequential circuits receives brief treatment relying on a few examples only. The authors stress a solution of equations of the form

$$\sum_{i=1}^{n} A_i = \sum_{i=0}^{\infty} d_i 2^i$$

where " \sum " denotes ordinary addition of natural numbers, and the parameters A_i as well as the d_j vary over 0, 1. The circuits "associated with" these solutions are claimed to possess novel self-checking features.

The solution which the authors give which recursively expresses the d_i 's as a propositional formula in the A_i 's is needlessly involved. A simpler recursive solution is readily given: d_0 is the modulo-two sum of the A_i 's and

$$\sum_{k=1}^{n-1} B_k = \sum_{i=0}^{\infty} d_{i+1} 2^i$$

where B_k is the Boolean product of A_{k+1} and the modulo-two sum of A_1 , A_2 , ..., A_k . An explicit solution may also be given: d_i is the modulo-two sum of all $\mathbf{\Pi}S$ where S varies through all subsets of $\{A_1, A_2, \ldots, A_n\}$ with 2^i elements and " $\mathbf{\Pi}S$ " denotes the product of the elements in S. This solution depends upon the fact that if $m = \binom{m}{k}$

$$\sum_{i=0}^{\infty} d_i 2^i$$
, then d_i is congruent modulo two to $\binom{m}{2^i}$.

Antonin Svoboda. Graphico-mechanical aids for the synthesis of relay circuits. Aktuelle Probleme der Rechentechnik, Deutscher Verlag der Wissenschaften, Berlin 1957, pp. 43-50.

The two graphico-mechanical aids are contact bones and contact grids. Contact bones are an aid in analyzing (i.e., finding a logical formula for) contact networks. The logical theory of contact network analysis has been generally understood for a long time, but there are practical difficulties, especially in the analysis of bridge networks (i.e., networks which are not of the series-parallel type). Contact grids are an aid in obtaining a normal formula for functions given in truth-table form. They are helpful in obtaining what are called (by others) prime implicants. The last para-