

# Program Certification by Higher-Order Model Checking

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**Abstract.** Model checking of higher-order recursion schemes or (collapsible) higher-order pushdown automata (higher-order model checking, for short) is a generalization of finite state and pushdown model checking, which has been extensively studied in the last decade [1–11, 15–17]. Higher-order recursion schemes are essentially terms of the simply-typed  $\lambda$ -calculus with recursion and tree constructors; therefore, they serve as good models for higher-order functional programs. Indeed, various verification problems for higher-order functional programs can be easily reduced to higher-order model checking, and automated verification tools have been developed based on the reduction [9, 12–14, 18].

In the talk, I will first provide a brief introduction to higher-order model checking and its applications to higher-order program verification. I will then discuss higher-order model checking from the viewpoint of certificates. In particular, I plan to discuss the following questions: (i) How can we certify the result of program verification based on higher-order model checking? (ii) Why does higher-order model checking work at all, despite its extremely high worst-case complexity?

## References

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