# Infinite-State High-Level MSCs: Model-Checking and Realizability \*

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#### Abstract

Message sequence charts (MSC) and High-Level MSC (HMSC) is a visual notation for asynchronously communicating processes and a standard of the ITU. They usually represent incomplete specifications of required or forbidden properties of communication protocols. We consider in this paper two basic problems concerning the automated validation of HMSC specifications, namely model-checking and synthesis. We identify natural syntactic restrictions of HMSCs for which we can solve the above questions. We show first that model-checking for globally-cooperative (and locally-cooperative) HMSCs is decidable within the same complexity as for the restricted class of bounded HMSCs. Furthermore, model-checking local-choice HMSCs turns out to be as efficient as for finite-state (sequential) systems. The study of locally-cooperative and local-choice HMSCs is motivated by the synthesis question, i.e., the question of implementing HMSCs through communicating finite-state machines (CFM) with additional message data. We show that locally-cooperative and local-choice HMSCs are always implementable. Furthermore, the implementation of a local-choice HMSC is deadlock-free and of linear size.

 $\mathit{Key\ words:}\ \mathrm{Concurrency},\ \mathrm{MSC},\ \mathrm{Model\text{-}Checking},\ \mathrm{Synthesis},\ \mathrm{Communicating}$  Automata.

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#### 1 Introduction

Message sequence charts (MSC for short) is a visual notation for asynchronously communicating processes and a standard of the ITU [15]. The usual application of MSCs in telecommunication is for capturing requirements of communication protocols in form of scenarios at early design stages. MSCs usually represent incomplete specifications, obtained from a preliminary view of the system that abstracts away several details such as variables or message contents. High-level MSCs (HMSCs for short) combine basic MSCs using choice and iteration, thus describing possibly infinite collections of scenarios. They have a graphical representation by means of directed graphs, with nodes labeled by finite MSCs.

Model-checking and synthesis are the two basic problems considered in this paper. High-level MSCs are infinite-state systems, since the semantics implies that communication channels are unbounded. Another important feature is that high-level MSCs have a global control structure, that comes from the diagram representation of MSCs and the graph structure of the HMSC. This makes the model-checking problem undecidable, and it also raises serious problems for synthesis, where the control must be distributed. Our goal is to propose relaxed restrictions of high-level MSCs that ensure both decidability of model-checking and synthesis, while preserving the infinite-state character of high-level MSCs, i.e. without restricting the channels.

Model-checking. The detection of possible design failures of a protocol at early stages is of critical importance, and the utility of HMSCs can be greatly enhanced by automatic validation methods. A preliminary specification of a protocol can suffer from several deficiencies, either related to the partial order of events (e.g. race conditions [3, 26]) or to the violation of user-defined properties specified for instance in logics such as LTL or MSO. However, model-checking HMSCs against such logics is either undecidable (for LTL see [4]) or extremely time consuming (non elementary complexity for MSO interpreted on MSCs [20]). A common approach is to specify the property by a set of MSCs given by an HMSC, as usually done by engineers. The property HMSC can be interpreted as the bad behaviors which have to be avoided by the model [4, 26]. Unfortunately, this kind of model-checking is undecidable, even if we impose bounded communication channels. This undecidability result motivated the definition of regular (bounded) HMSCs [4, 26, 14]. A regular HMSC has the property that the set of all linearizations of its MSCs is regular. With this restriction, model-checking HMSC or LTL properties becomes of course decidable. However, the situation is not at all satisfactory since regularity imposes a bound on message channels, or equivalently, that each message has to be somehow acknowledged. This is a strong restriction, excluding very simple HMSCs such as a producer-consumer scenario, where a message is sent

an arbitrary number of times from a producer to a consumer. Such a simple scenario is often needed, for instance to describe asynchronous transfers (see e.g. the USB 1.1 specification [30]). More generally, any protocol involving a read- or write-only process cannot be described by regular HMSCs.

The first objective of the paper is to show that we do not need to restrict the channel size for obtaining a class with a decidable model-checking problem. We propose in this paper *globally-cooperative HMSCs* and show that their model-checking problem is decidable, actually within the same asymptotic complexity bounds as for regular HMSCs.

Synthesis. A second basic validation step in protocol design is to know whether the specification is implementable in a machine-oriented model—the synthesis problem, see e.g. [29]. For HMSC specifications, synthesis has a specific flavor. First, we seek for fully distributed implementations, which are in general much harder to obtain than sequential ones [29, 21, 18]. Second, HMSCs usually describe a set of possibly incomplete requirements, which means that the model can be refined compared to the specification. Notice finally that an implementable model can be itself model-checked using for instance SDL tools (Specification and description languages, ITU Z.100). There is a large body of papers considering the implementability of HMSC specifications. Previous work considered implementations by statecharts as state-based model [17, 11]. Another line of research used communicating finite state machines (CFM or message passing automata) [1, 2, 25], which is also the model used in this paper. In both models, no global control is available, contrary to an HMSC description. In order to install a distributed control, the machine realization may need further message data or even exchange additional control or synchronization messages.

Our second goal is to exhibit general techniques for synthesizing such a distributed control. For this, we adopt a moderate view of implementation: we allow additional message contents while ruling out extra control messages. The reason is that additional messages mean additional process synchronization, which is not desirable (or even impossible) in a given environment. On the other hand, additional message contents make sense since message data (e.g. call parameters) is often abstracted away in the specification. Still, our implementation semantics by CFMs is more general than the one introduced in [1] and used in [2, 24] where a parallel product of communicating finite-state automata is employed to realize the (linear) behavior of each process of the given HMSC. In particular, the possibility of adding information through messages is explicitly ruled out in [1]. Actually, the implementation semantics of [1, 2] was shown to be undecidable even for regular HMSCs, which was the motivation for considering safe implementations in [1, 19].

We propose in this paper three classes of HMSCs that do not restrict the com-

munication channels: globally-cooperative and two subclasses thereof, locally-cooperative and local-choice HMSCs. Globally-cooperative HMSCs have been introduced independently in [24], whereas locally-cooperative HMSCs are defined in this paper. The local-choice property has been considered in [12]. Globally-cooperative HMSCs extend the well studied class of regular HMSCs [26, 4, 14]. In a nutshell, globally-cooperative HMSCs rule out arbitrary repetitions of communications patterns involving two non-communicating groups of active processes. (In particular, regular HMSCs correspond exactly to globally-cooperative HMSCs that use only bounded communication channels.) This restriction makes it possible, given a globally-cooperative HMSC, to construct an automaton accepting a word language representing the set of distributed behaviors described by the HMSC. This property is a crucial point for the design our model-checking algorithms.

In the first part of the paper (Section 4) we consider the model-checking problem stated as intersection (negative property) or inclusion (positive property) of HMSCs. That is, the property to be tested is also described by an HMSC. We show that negative and positive model-checking for globally-cooperative HMSCs are PSPACE- and EXPSPACE-complete, respectively, which is as good as the model-checking for regular HMSCs while being applicable to a much larger class of infinite-state HMSCs. For locally-cooperative HMSCs, negative model-checking is still PSPACE-complete, whereas positive model-checking lies between PSPACE and EXPSPACE. For the third subclass, local-choice HMSCs, we are able to obtain better complexities. Namely, we show that negative model-checking can be solved in quadratic time, whereas positive model-checking is PSPACE-complete.

In the second part of the paper we consider the synthesis of communicating finite-state machines from locally-cooperative, resp. local-choice HMSCs (Sections 5.1 and 5.2). We show that both HMSCs classes are always implementable by CFMs, however the quality of the implementations differs considerably. Locally-cooperative HMSCs can be implemented with an exponential overhead in the finite control and the message contents, and the implementation is in general not deadlock-free. For local-choice HMSCs we present a linear-size, deadlock-free implementation by CFMs. For globally-cooperative HMSCs we conjecture that they are implementable, too, albeit with a lot of deadlocks.

The last contribution of this paper considers the question whether a CFM is deadlock-free (Section 6). We note that CFMs obtained from HMSCs have the property that for each execution there is an equivalent one that uses only bounded channels. We call such CFMs existentially-bounded and we show that reachability and deadlock-freeness for existentially-bounded CFMs is decidable (PSPACE-complete). In contrast, both problems are undecidable for general CFMs [5]. Therefore, we are able to test whether a CFM implementation of

an HMSC is deadlock-free or not.

A preliminary version of this paper was presented in [10].

Related work. Model-checking regular HMSCs against HMSC properties was shown to be decidable in [4, 26]. For partial-order logics, decidability of model-checking was obtained w.r.t. MSO [20] and TLC [28].

Synthesis (realizability, inference) of CFM from MSC specifications has been introduced in [1], where it is shown that the problem is co-NP complete for finite sets of finite MSCs, however solvable in polynomial time for deadlockfree (safe) realizability. In [2] this question is considered for HMSCs and it is shown that realizability is in general undecidable (even for regular HMSCs), however deadlock-free realizability of regular HMSCs is in EXPSPACE. The matching lower bound is shown in [19], where it is also shown that the upper bound still holds for globally-cooperative HMSCs. The implementation model considered in these papers consists of CFMs with no additional message data, i.e. a parallel product of communicating finite-state machines corresponding to the exact behavior of the single processes. A weaker framework (only messages with same content are FIFO-ordered) is used in [24], where it it is shown that it is decidable whether a given globally-cooperative HMSC is realizable. Our approach is similar to the one used in [25] for implementing regular HMSCs. Finally, [6] considers the implementation of HMSCs by Petri nets with a larger set of behaviors and [12] identifies particular classes of HMSCs that are implementable by CFMs without additional message data.

## 2 Preliminaries

In this section we recall the specification formalism of message sequence charts (MSC) and high-level message sequence charts (HMSC) based on the ITU standard Z.120 [15]. Each message sequence chart describes a scenario or an execution of a communication protocol in which processes communicate with each other over point-to-point, error-free FIFO channels. An MSC scenario consists in a description of the messages sent and received, the local events, and the ordering between them. The event ordering is based on a process ordering and a message ordering. In the visual description of MSCs, each process is represented by a vertical line, which gives a total order on the events belonging to that process. Messages are usually represented by horizontal or slanted arrows from the sending process to the receiving one.

**Definition 1.** An MSC over process set  $\mathcal{P}$  is a tuple  $M = \langle E, <, \mathcal{P}, t, \mathcal{C}, m \rangle$  where:

- $E = \bigcup_{p \in \mathcal{P}} E_p$  is the disjoint union of the sets  $E_p$ , comprising the events located on process p. We denote by  $P(e) \in \mathcal{P}$  the location of event e.
- Every event is either a communication event (send or receive) or a local event. We write  $E = S \cup R \cup L$  as a disjoint union, with S denoting the sends, R the receives and L the local events.
- ullet C is a finite set of message contents and local action names.
- $t: E \to A = \{p!q(a), p?q(a), l_p(a) \mid p, q \in \mathcal{P}, p \neq q, a \in \mathcal{C}\}$  labels each event by its  $type\ t(e)$ , with t(e) = p!q(a) if  $e \in E_p \cap S$  is a send event of message a from p to q, t(e) = p?q(a) if  $e \in E_p \cap R$  is a receive event of message a by p from q and  $t(e) = l_p(a)$  if  $e \in E_p \cap L$  is a p-local event describing the local action a.
- $m: S \longrightarrow R$  is a bijection that pairs up send and receive events (matching function). If m(e) = f, then t(e) = p!q(a) and t(f) = q?p(a) for some  $p, q \in \mathcal{P}$  and  $a \in \mathcal{C}$ .
- $< \subseteq E \times E$  is the relation defined by the two conditions below:
  - · The restriction of < to  $E_p$  is a total order, for every process  $p \in \mathcal{P}$ .
  - · For all  $e, f \in E$ , m(e) = f implies e < f.

The relation < is required to be acyclic and is called *visual order*.

A message (e, f) is a pair of matching send and receive events, i.e., m(e) = f. We assume that channels are FIFO, that is, whenever m(e) = f, m(e') = f', e < e' and t(e) = p!q(a), t(e') = p!q(a') for some  $p, q \in \mathcal{P}$ ,  $a, a' \in \mathcal{C}$ , we also have f < f'.

The results of this paper are independent of this assumption. For non FIFO channels we have to add some information in the type t(e) of an event e. Formally, we have to extend the set of types A to  $A \times \mathbb{N}$  and we require that m(e) = f only if t(e) = (p!q(a), k) and t(f) = (q?p(a), k) for some p, q, a and  $k \in \mathbb{N}$ .

Since the visual order is required to be acyclic, its reflexive-transitive closure  $<^*$  is a partial order on E. For sake of simplicity we will use the same notation  $\leq$  for the partial order  $<^*$ . A *linearization* of < is a total order  $\leq$  extending  $\leq$ . For any MSC M we denote by Lin(M) the set of labeled linearizations of M:

$$\operatorname{Lin}(M) = \{t(e_1) \cdots t(e_k) \mid e_1 \cdots e_k \text{ is a linearization of } M\}.$$

Note that with the FIFO property, any labeled linearization  $x \in \text{Lin}(M)$  suffices to reconstruct the MSC M, since the type mapping  $t : E \to A$  encodes all the information needed.

If the matching m is a partial, injective function then we speak about a partial MSC. For every  $x \in A^*$  we denote by  $\mathrm{msc}(x)$  the partial MSC defined by pairing the k-th event of type p!q(a) with the k-th event of type q?p(a) (if they exist).

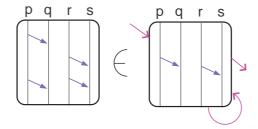


Fig. 1. The left part of the figure depicts an MSC on 4 processes p, q, r, s consisting of 4 messages. It is generated by the HMSC on the right side.

The *size* of an MSC is the number of events it contains.

Since the specification of a communication protocol includes many scenarios, a high-level description is needed for combining them together and defining infinite sets of (finite or infinite) scenarios. The standard description of the norm Z.120 uses non deterministic branching, concatenation and iteration for defining finite or infinite sets of MSCs (see the examples in Figures 1, 4). Formally, a high-level MSC (HMSC)  $G = \langle V, R, v^0, v^f, \lambda \rangle$  is a finite transition system  $(V, R, v^0, v^f)$  with transition set  $R \subseteq V \times V$ , initial node  $v^0$  and terminal node  $v^f$ . Each node v is labeled by the finite MSC  $\lambda(v)$ . We assume that each  $\lambda(v)$  is non empty, except possibly for  $v = v^f$ . We also assume that every node is accessible from  $v^0$  and from each node there is a path to  $v^f$ . An execution of G is the labeling  $\lambda(v_0)\lambda(v_1)\cdots\lambda(v_k)$  of some path  $v^0=v_0,v_1,\ldots,v_k=v^f$  in G, i.e.,  $(v_i,v_{i+1}) \in R$  for every  $0 \le i < k$ . The set of executions of G is denoted by  $\mathcal{L}(G)$ , the set of linearizations of executions of G is denoted by  $\mathcal{L}(G)$ . The size of an HMSC is the sum of the sizes of its nodes.

Of course, the semantics of HMSCs depends on the definition of the MSC product. We consider the usual weak product of MSCs, as defined in the following. Let  $M_1 = \langle E_1, <_1, \mathcal{P}, t_1, \mathcal{C}_1, m_1 \rangle$  and  $M_2 = \langle E_2, <_2, \mathcal{P}, t_2, \mathcal{C}_2, m_2 \rangle$  be MSCs over the same set of processes  $\mathcal{P}$ . Their product  $M_1M_2$  is defined as the MSC  $\langle E_1 \cup E_2, <, \mathcal{P}, t_1 \cup t_2, \mathcal{C}_1 \cup \mathcal{C}_2, m_1 \cup m_2 \rangle$  over the disjoint union of event sets, with the visual order given by:

$$< = <_1 \cup <_2 \cup \{(e, f) \in E_1 \times E_2 \mid P(e) = P(f)\}.$$

That is, events of  $M_1$  precede the events of  $M_2$  for each process, respectively. Note that there is no synchronization between different processes when moving from one node to the next one (this is called *weak sequencing*). Hence, it is possible that one process is still involved in some actions of  $M_1$ , while another process has advanced to an event of  $M_2$ . We also say that  $M_1$  is a *prefix* of  $M_1M_2$ .

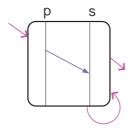


Fig. 2. A globally-cooperative HMSC.

## 3 A Panorama of HMSC Classes

In this section we introduce two of the subclasses of infinite-state HMSCs defined in this paper, globally-cooperative and locally-cooperative HMSCs. As mentioned in the introduction, both variants of model-checking HMSCs (intersection and inclusion) are undecidable for general HMSCs, even with bounded channels. The very reason for undecidability is that loops can simulate counting, as explained below.

Let us denote for an MSC M the set of processes that occur in M by P(M). Clearly, we have  $M_1M_2 = M_2M_1$  for any MSCs  $M_1, M_2$  with  $P(M_1) \cap P(M_2) = \emptyset$ . We write in this case  $M_1 \parallel M_2$  and we say that  $M_1, M_2$  are independent. Notice that  $(M_1M_2)^* = \{M_1^nM_2^n \mid n \geq 0\}$  if  $M_1 \parallel M_2$ .

The communication graph of an MSC M is a directed graph with a node p for each process  $p \in P(M)$  that sends or receives a message, together with edges  $p \to q$  whenever M contains a message from p to q.

**Definition 2** (globally-cooperative). An HMSC  $\langle V, R, v^0, v^f, \lambda \rangle$  is called *globally cooperative* if every MSC labeling a loop of the transition system (V, R) has a weakly connected communication graph.

The HMSC in Figure 1 is not globally cooperative, since the communication graph of the loop has two weakly connected components, one over  $\{p,q\}$  and the other over  $\{r,s\}$ . The HMSC in Figure 2 is globally cooperative, since the communication graph of its loop consists of one edge  $p \to s$ .

Compared with globally-cooperative HMSCs, the previously defined regular HMSCs impose a more severe restriction on communication. As said in the introduction, some existing protocols, such as USB 1.1 in isochronus transfer mode, contain cycles with messages sent without being acknowledged.

**Definition 3** (regular). [26, 4] An HMSC  $\langle V, R, v^0, v^f, \lambda \rangle$  is called *regular* if every MSC labeling a loop of the transition system (V, R) has a *strongly connected* communication graph.

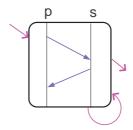


Fig. 3. A regular HMSC.

For example, the HMSC in Figure 3 is regular, unlike the HMSC of Figure 2, which has no acknowledgment message from s to p.

The link between globally-cooperative and regular HMSCs is summarized by the proposition below. An HMSC has universally-bounded channels if there exists some integer B such that for every  $x \in \text{Lin}(G)$  and every prefix  $y \leq x$ , the difference between the number of send symbols and receive symbols in y is at most B.

**Proposition 4.** An HMSC G is regular if and only if it is globally cooperative and it has universally bounded channels.

*Proof.* Assume first that G is regular. By definition, the communication graph of each loop is strongly connected, hence also weakly connected. Moreover, since Lin(G) is regular [4, 26], the second property also follows.

Conversely, let G be globally cooperative and assume that channels are universally bounded. Consider a loop in the transition system, say labeled by M. Since every state is reachable from the initial node, and the final node is reachable from every state, we find MSCs  $M_1$ ,  $M_2$  such that  $M_1M^*M_2 \subseteq \mathcal{L}(G)$ . We want to show that the communication graph of M must be strongly connected.

Suppose by contradiction that this is not the case, and let  $p \to q$  be an edge such that p,q do not belong to the same strongly connected component. The edge  $p \to q$  corresponds to a message from p to q in M, say to (e,f). Consider the two occurrences of the message (e,f) in MM. The event f in the first M and the event e in the second M cannot be ordered, since otherwise there would be a path from q to p in the communication graph of M (which is the same as the graph of MM). Hence, MM has a linearization where the two occurrences of e appear before the two occurrences of e appear before the occur

A natural subclass of globally-cooperative HMSCs is obtained by requiring that for every transition  $(v, v') \in R$  the two MSCs labeling v, v' are not inde-

pendent. Intuitively, this restriction avoids mixing the parallel product with the sequential transition relation of the underlying HMSC graph.

**Definition 5** (locally-cooperative). An HMSC  $\langle V, R, v^0, v^f, \lambda \rangle$  is called *locally cooperative*, if for every  $(v, v') \in R$ , the MSCs  $\lambda(v), \lambda(v'), \lambda(v)\lambda(v')$  all have weakly connected communication graphs.

Since local and global cooperativeness and regularity are structural restrictions, we can test whether a HMSC satisfies one of these restrictions.

**Proposition 6.** Checking whether an HMSC is globally cooperative (or regular) is co-NP-complete, whereas checking whether it is locally cooperative can be done in linear time.

*Proof.* We first show how to check whether an HMSC is globally cooperative. We guess a subgraph H of G. Then we check (in polynomial time) that there exists a loop passing through each node of H at least once. Moreover, the communication graph is checked to be not weakly connected. This algorithm is clearly co-NP.

For the lower bound we reduce 3-SAT to our problem. Let  $\phi = C_1 \wedge \cdots \wedge C_m$  be a 3-SAT formula over n variables  $x_1, \ldots, x_n$ , and disjunctive clauses  $C_i = l_i^1 \vee l_i^2 \vee l_i^3$ . The formula  $\phi$  is satisfiable iff there exists a valuation such that for every  $i \leq m$ , at least one literal among  $l_i^1, l_i^2, l_i^3$  is true for the valuation.

The MSC-graph G contains two vertices  $NT_i, NF_i$  for each variable  $x_i$ , plus one initial and final node  $N_0$ . Transitions go from from each  $NX_i$  to each  $NX_{i+1}$ , for  $X \in \{T, F\}$  and  $1 \le i < n$ . Moreover, G contains transitions from  $N_0$  to  $NT_1$  and  $NF_1$ , resp. from  $NT_n$  and  $NF_n$  back to  $N_0$ . Hence, a simple loop of G around  $N_0$  corresponds to a valuation of the variables:  $x_i$  true means that the loop goes through  $NT_i$ , and  $x_i$  false means that the loop goes through  $NF_i$ .

We describe now the MSCs used in the construction. There will be 3m + 2 processes  $(P_j^1, P_j^2, P_j^3)_{1 \leq j \leq m}$ , where  $P_j^1, P_j^2, P_j^3$  correspond to the clause  $C_j$ , plus two extra processes  $P_0, P_{m+1}$ .

Let  $M_0$  be an MSC consisting of two local actions, one on  $P_0$  and one on  $P_{m+1}$ , and let  $N_0$  be labeled by  $M_0$ .

We define now MSCs  $LT_j^k$ ,  $LF_j^1$ : The MSC  $LF_j^1$  consists of a message from  $P_0$  to  $P_j^1$ . The MSC  $LF_j^2$  consists of a message from  $P_j^1$  to  $P_j^2$ . The MSC  $LF_j^3$  consists of a message from  $P_j^2$  to  $P_{m+1}$ . The MSCs  $LT_j^1$  and  $LT_j^2$  are both empty, while  $LT_j^3$  consists of one message from  $P_0$  to  $P_j^2$ .

We label  $NT_i$  by the product of all MSCs  $LT_j^k$  such that  $l_j^k = x_i$ , and of

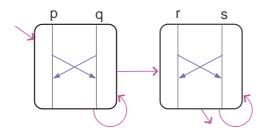


Fig. 4. Regular HMSC which is not locally cooperative.

all MSCs  $LF_j^k$  such that  $l_j^k = \overline{x_i}$ . Symmetrically, let  $NF_i$  be labeled by the product of all MSCs  $LT_j^k$  such that  $l_j^k = \overline{x_i}$ , and of all MSCs  $LF_j^k$  such that  $l_j^k = x_i$ .

Thus, the processes  $P_0$  and  $P_{m+1}$  are connected in the communication graph of a simple loop around  $N_0$  iff there exists a clause where all three literals are false. Moreover, notice that if  $P_0$  and  $P_{m+1}$  are connected in some loop, then all processes occurring in that loop are connected (in the communication graph): if  $LF_j^1$ ,  $LF_j^3$  or  $LT_j^3$  appear in the loop, their processes are connected either to  $P_0$  or to  $P_{m+1}$ . Concerning  $LF_j^2$ , its processes are either connected to  $P_0$  because of  $LT_j^3$  (i.e.,  $l_j^3$  is true) or to  $P_{m+1}$  because of  $LF_j^3$  (i.e.,  $l_j^3$  is false).

Hence,  $\phi$  is satisfiable iff there exists a valuation such that for all  $1 \leq j \leq m$ , one of  $l_j^1, l_j^2, l_j^3$  is true in the valuation, iff there exists a simple loop with a non connected communication graph.

Note that we can change slightly the construction for the lower bound for regular HMSCs. It suffices to replace each message by a pair of messages, back and forth.  $\Box$ 

We have defined three subclasses of HMSCs: locally-cooperative, globally-cooperative, and regular HMSCs. Any locally-cooperative or regular HMSC is also globally cooperative by the definition of these classes. Locally-cooperative HMSCs and regular HMSCs are expressively incomparable, see e.g. Figure 2 that depicts a locally-cooperative HMSC which is not regular. On the other hand, Figure 4 depicts a regular HMSC which is not locally cooperative.

We will show in Section 4 that the model-checking problem of the bigger class of globally-cooperative HMSCs is decidable within the very same complexity as for locally-cooperative or regular HMSCs. An implementation through CFMs (albeit with deadlocks) is known for regular HMSCs [25]. In Section 5 we show how to implement locally-cooperative HMSCs. However, the implementability for globally-cooperative HMSCs remains open.

We end this section by explaining some motivation behind the definition of globally-cooperative HMSCs. The main idea is that one can model-check an

HMSC w.r.t. a property given by another HMSC, provided that we are able to obtain a regular set of representatives for the set Lin(H) of one HMSC H, that is compatible with the relation  $\parallel$ . We call  $X \subseteq \text{Lin}(H)$  a set of representatives for H, if for every MSC  $M \in \mathcal{L}(H)$ , we have  $\text{Lin}(M) \cap X \neq \emptyset$ . We will explain in the next section how to provide for any globally-cooperative HMSC such a suitable set of representatives.

## 4 Model-Checking

Bounding message channels by forcing acknowledgments as required for regular HMSCs is a severe restriction, excluding such simple and common scenarios as the one depicted in Figure 2. Such a scenario is however a locally-cooperative HMSC. Although globally-cooperative HMSCs are much more general than regular HMSCs, we can show that we are still able to do automata-based model-checking with the same complexities. The underlying idea is that the executions of a globally-cooperative HMSC can be captured by a suitable regular set of representative linearizations. As an example reconsider the HMSC G of Figure 2. The set Lin(G) of linearizations of executions of G is obviously non regular. However, the representative set  $X = (p!s \, s?p)^*$  captures all the information needed for doing model-checking against an HMSC property.

The plan of this section is as follows. First, we recall some basic facts from the theory of Mazurkiewicz traces [22, 7], that are crucial for our definition of globally-cooperative HMSCs. Then we discuss the model-checking problem for globally-cooperative and locally-cooperative HMSCs, respectively.

## 4.1 Mazurkiewicz Traces

Mazurkiewicz traces were proposed as a formal model for concurrent executions, where the concurrency is made explicit by describing the independence between possible actions in the system. Formally, let  $\| \subseteq A \times A$  be a symmetric, irreflexive independence (commutation) relation on the alphabet of actions A. A Mazurkiewicz trace is just a set of words that can be obtained from a given word  $\sigma \in A^*$  by exchanging adjacent symbols a, b with  $a \parallel b$ .

We are interested here in computing closure sets under the independence relation  $\parallel$ . Let  $K \subseteq A^*$  be a set of words. The  $\parallel$ -closure of  $K \subseteq A^*$  is the smallest set  $[K]_{\parallel}$  containing K such that  $\sigma ab\sigma' \in [K]_{\parallel}$  iff  $\sigma ba\sigma' \in [K]_{\parallel}$ , for all  $\sigma, \sigma' \in A^*$  and  $a \parallel b$ .

Unfortunately, the \|-\closure\ does not preserve regularity in general. Consider

for instance two letters a, b with  $a \parallel b$ . Then  $[(ab)^*]_{\parallel}$  is the set of words over  $\{a, b\}$  with equally many a's and b's.

Mazurkiewicz trace theory provides a syntactical condition ensuring that the  $\parallel$ -closure of a regular language remains regular. Given an automaton  $\mathcal{A}$ , this condition states that each loop of  $\mathcal{A}$  is labeled by a connected word [23, 27]. A word w is called *connected* if its set of letters cannot be partitioned into non empty subsets X, Y such that  $a \parallel b$  for all  $a \in X, b \in Y$ . If the condition is true, then we can construct a non deterministic automaton recognizing the set  $[\mathcal{L}(\mathcal{A})]_{\parallel}$  which is of size at most  $2^{O(n \cdot \wp)}$ , where  $n = |\mathcal{A}|$  and  $\wp$  is the minimal number of cliques covering the graph  $(A, (A \times A) \setminus \parallel)$  [26].

## 4.2 Model-checking globally-cooperative and locally-cooperative HMSCs

It is easy to obtain an automaton  $\mathcal{A}$  from an HMSC G such that  $\mathcal{L}(\mathcal{A}) \subseteq \operatorname{Lin}(G)$  is a set of representatives. For this, it suffices to replace each node by some linearization of the associated MSC and view the graph thus obtained as a (word) automaton. Unfortunately, this set does not suffice for deciding for instance whether  $\mathcal{L}(G) \cap \mathcal{L}(H) \neq \emptyset$  for some HMSCs G, H. Consider for instance the HMSC G in Figure 1. The representative set obtained from G could be  $X = (p!q \, q?p \, r!s \, s?r)^*$ . However, for the MSC shown in the left part, one might choose the linearization  $(p!q \, q?p)^2(r!s \, s?r)^2$ , that does not belong to X.

The idea is to consider a sort of message alphabet with an independence relation on it, and apply the construction of [26] for closing it under commutation. Notice that defining the message alphabet is not easy. For instance, consider the MSC labeling one of the nodes in Figure 4. Its two messages cannot be split into two MSCs, and they must be considered together. Formally, a non empty MSC is called *atomic* (atom, for short) if it cannot be written as  $M = M_1M_2$  for non empty MSCs  $M_1, M_2$ . For instance, the two MSCs in Figure 8 are not atomic, since the atoms correspond to single messages. It is not hard to see that any MSC has a unique factorization into atomic MSCs, up to commuting adjacent independent atoms, i.e. atoms  $M_1, M_2$  such that  $M_1 \parallel M_2$ . The decomposition of M can be obtained in linear time by computing the strongly connected components in a directed graph obtained from the partial order graph of M by adding back edges from r to s whenever (s, r) represents a message, [13].

We are now ready to define the suitable set of representatives that allows us to perform model-checking of an HMSC w.r.t. a property expressed by another HMSC. For sake of simplicity and efficiency we rather define this set of representatives (denoted  $\mathcal{L}^a(G)$  below) on a sort of message alphabet (atoms) instead of the event type alphabet.

**Definition 7.** Let  $G = \langle V, R, v^0, v^f, \lambda \rangle$  be an HMSC. We define Atom(G) as the (finite) set of atoms occurring in the decomposition of MSCs from  $\lambda(V)$ . We view Atom(G) as an alphabet, respectively  $\parallel$  as an independence relation on this alphabet. Let also  $\mathcal{L}^a(G) = \{A_1 \cdots A_k \mid A_1 \cdots A_k \in \mathcal{L}(G) \text{ and } A_i \in Atom(G) \text{ for all } i\}.$ 

Consider as an example the HMSC G in Figure 4, and let a, b denote the atomic MSCs labeling the initial and final node, respectively. We have  $\mathcal{L}^a(G) = \{a, b\}^+ \setminus (a^* \cup b^*)$ , with  $a \parallel b$ .

**Proposition 8.** Let G be a globally-cooperative HMSC of size s and over  $\wp$  processes. Then  $\mathcal{L}^a(G)$  is recognized by a non deterministic automaton of size at most  $2^{O(\wp s)}$ .

*Proof.* We first transform G into an equivalent automaton  $\mathcal{B}$  with nodes labeled by symbols from Atom(G). Formally, each node v is first replaced by a path  $v_1, \ldots, v_k$ , with  $v_i$  labeled by an atom  $M_i$  such that  $\lambda(v) = M_1 \cdots M_k$ . It is easy to see that this transformation preserves the property of being globally cooperative.

Note that  $[L(\mathcal{B})]_{\parallel} = \mathcal{L}^a(G)$ . In the example in Figure 4 we have for instance  $\mathcal{L}(\mathcal{B}) = a^+b^+$  and  $[L(\mathcal{B})]_{\parallel} = \{a,b\}^+ \setminus (a^*+b^*)$ . Since G is globally cooperative, each loop of  $\mathcal{B}$  is labeled by a connected word, hence we can apply the construction of [26] mentioned in Section 4.1. We obtain a non deterministic automaton  $\mathcal{A}$  recognizing  $[L(\mathcal{B})]_{\parallel} = \mathcal{L}^a(G)$ , of size at most  $2^{O(\wp s)}$ .

For locally-cooperative HMSCs G we obtain a smaller automaton recognizing  $\mathcal{L}^a(G)$ . More precisely, the size of the automaton is exponential in the number of processes, but polynomial in the size of the transition system.

**Proposition 9.** Let G be a locally-cooperative HMSC with n nodes and  $\wp$  processes. Let k be the maximal size of an MSC labeling a node of G. Then  $\mathcal{L}^a(G)$  is recognized by a non deterministic automaton of size at most  $(kn)^{2\wp}(\wp+1)^\wp$ .

*Proof.* Let  $G = \langle V, R, v^0, v^f, \lambda \rangle$ . First note that we cannot replace G by an equivalent locally-cooperative HMSC with nodes labeled by atoms, since this does not preserve local cooperativeness. Let  $x \in \mathcal{L}^a(G)$  and consider some accepting path  $\sigma = v_1 \cdots v_m$  of G labeled by x. Let also  $x_1$  be some prefix of x. We decompose the path  $v_1 \cdots v_m \in V^*$  with respect to  $x_1$  as follows: Let

$$\sigma = v_1 \cdots v_m = \alpha_1 \beta_1 \alpha_2 \cdots \beta_{k-1} \alpha_k \beta_k$$

with  $\alpha_1, \beta_k \in V^*$ ,  $\alpha_i, \beta_j \in V^+$  for all  $1 < i \le k$ ,  $1 \le j < k$ , such that the nodes occurring in  $\alpha_1 \cdots \alpha_k$  are precisely the nodes of  $\sigma$  that have at least one atom appearing in  $x_1$ . We call a node w of some subpath  $\alpha_i$  half-full, if the MSC  $\lambda(w)$  appears in  $x_1$ , but not completely. Otherwise it is called full. A node of a subpath  $\beta_i$  is called empty.

We show first that every subpath  $\alpha_i$ , i > 1, starts with a half-full node. Indeed, with G being locally cooperative, there can be no transition from an empty node to a full node, since two nodes linked by a transition share at least one process.

In a second step, we show that the number of half-full nodes is at most  $\wp$  (see also Figure 5, where half-full nodes are grey, and full ones are black).



Fig. 5. Path decomposition in locally-cooperative HMSC.

Let w be a half-full node with  $\lambda(w) = YZ$ , where Y is the prefix of  $\lambda(w)$  appearing in  $x_1$ . By definition, Y and Z are both non empty. Since the communication graph of  $\lambda(w)$  is weakly connected there is some process  $p \in P(Y) \cap P(Z)$ . Suppose that w' is some half-full node occurring after w in  $\sigma$ , and let  $\lambda(w') = Y'Z'$  be the decomposition of w' w.r.t.  $x_1$ . Then  $P(Z) \cap P(Y') = \emptyset$ , since Z is executed after Y' in x. Hence,  $p \notin P(Y')$ . This shows the claim.

We obtain a non deterministic automaton  $\mathcal{B}$  recognizing  $\mathcal{L}^a(G)$  as follows. A state of  $\mathcal{B}$  records the first and the last node of each  $\alpha_i$ , as well as the processes that occurred so far in each  $\alpha_i$ . Moreover, we need to store the ordering and the configurations corresponding to the half-full nodes of the subpaths  $\alpha_i$ . Each transition of  $\mathcal{B}$  either adds an atom to a half-full node of some  $\alpha_i$ , or creates a new subpath  $\alpha_i$  (guessing a node). Whenever a node becomes full, the automaton can choose (non deterministically) to join two adjacent subpaths. The size of  $\mathcal{B}$  is bounded by  $k^{\wp}n^{2\wp}(\wp+1)^{\wp}$ , where  $n^{2\wp}$  stands for the possible first/last node of each subpath  $\alpha_i$  and the ordering of half-full nodes,  $k^{\wp}$  stands for the configurations of half-full nodes and  $(\wp+1)^{\wp}$  for the processes occurring in the  $\alpha_i$ .

**Theorem 10.** Model-checking globally-cooperative HMSCs is decidable. More precisely, let  $G_1, G_2$  be globally-cooperative HMSCs. Then,

- (1) Deciding whether  $\mathcal{L}(G_1) \cap \mathcal{L}(G_2) \neq \emptyset$  is PSPACE-complete.
- (2) Deciding whether  $\mathcal{L}(G_1) \subseteq \mathcal{L}(G_2)$  is EXPSPACE-complete.

Moreover, the lower bound for the intersection problem also holds when  $G_1, G_2$  are locally cooperative.

*Proof.* Using the unique decomposition of MSCs into atoms it can be easily checked that:

- (1)  $\mathcal{L}(G_1) \cap \mathcal{L}(G_2) \neq \emptyset$  iff  $\mathcal{L}^a(G_1) \cap \mathcal{L}^a(G_2) \neq \emptyset$ .
- (2)  $\mathcal{L}(G_1) \subseteq \mathcal{L}(G_2)$  iff  $\mathcal{L}^a(G_1) \subseteq \mathcal{L}^a(G_2)$ .

Hence, we obtain the upper bounds using the exponential size, non deterministic automata recognizing  $\mathcal{L}^a(G_i)$ .

The lower bound of the inclusion problem for globally-cooperative HMSCs can be directly obtained from the EXPSPACE-hardness of the universality problem for loop-connected automata, see [26].

For the intersection problem we encode accepting computations of a polynomially space-bounded Turing machine T as executions in  $\mathcal{L}(G_1) \cap \mathcal{L}(G_2)$ , with  $G_1$  and  $G_2$  locally cooperative. Let  $\Gamma$  be the tape alphabet of T and let w be an input of T. The proof idea is well known: we encode a finite computation  $C_0 \vdash C_1 \vdash \cdots \vdash C_m$  of T on w by using two copies  $C_i$  and  $\bar{C}_i$  of each configuration and by grouping factors in two different ways (see Figure 6). The HMSC  $G_1$  then ensures that  $C_i$  and  $\bar{C}_i$  are identical. The HMSC  $G_2$  ensures that for each i,  $\bar{C}_i$  and  $C_{i+1}$  are successor configurations, and that  $C_0$  (resp.  $\bar{C}_m$ ) is the initial (resp. final) configuration.

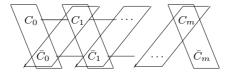


Fig. 6. TM computation.

The first issue is how to encode configurations. Let k be the length of any configuration (filled with blanks if necessary) reached by T on input w. We have k = p(|w|) for some polynomial p. We use k+2 processes  $P, \bar{P}, (P_i)_{1 \leq i \leq k}$ . If the i-th symbol of a configuration C is a, then we encode it by the MSC  $M_a^i$  consisting of a single message named a from  $P_i$  to P. The encoding h(C) of a configuration C is the concatenation of the encodings of symbols of C. Similarly, if the i-th symbol of  $\bar{C}$  is  $\bar{a}$ , then we encode it by the MSC  $\bar{M}_a^i$  consisting of a message from  $P_i$  to  $\bar{P}$  named a, and we let  $h(\bar{C})$  be the encoding of  $\bar{C}$ . The encoding of a sequence of configurations  $C_0, \ldots, C_m$  is  $h(C_0)h(\bar{C}_0)\cdots h(C_m)h(\bar{C}_m)$ .

Let  $M_i = \sum_a M_a^i$ ,  $\bar{M}_i = \sum_a \bar{M}_a^i$  and  $X_i = \sum_a M_a^i \bar{M}_a^i$ , where the sum means a choice. We easily construct  $G_1$  such that  $\mathcal{L}(G_1) = (X_1 \cdots X_k)^*$  (see Figure 7). Its node set is the disjoint union of nodes of  $X_1, \ldots, X_k$ , the nodes of  $X_1$  are initial, the nodes of  $X_k$  are final, and there is a transition from any node of  $X_j$  (resp. of  $X_k$ ) to any node of  $X_{j+1}$  (resp. of  $X_1$ ). Executions of  $G_1$  are exactly encodings of finite sequences  $C_0, \ldots, C_m$  with  $C_i \in \Gamma^k$ . Formally, we add a

unique initial node comprising all processes, and a unique final node. Note that  $G_1$  is locally cooperative.

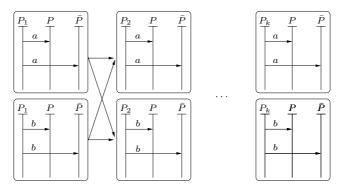


Fig. 7. The HMSC  $G_1$  for the intersection problem

The definition of  $G_2$  is slightly more complicated since we have to consider transitions of T. Assume that each configuration has the form  $\triangleleft uqv \triangleright$  where q is the current state of T, uv is written on the tape, and the head scans the first symbol of v. Thus, the transitions are of the form  $aqb \rightarrow qab'$  (left move) or  $aqb \rightarrow ab'q$  (right move). A transition  $t = xyz \rightarrow x'y'z'$  performed at head position i in a configuration is coded by the MSC  $T_{t,i} = \bar{M}_x^{i-1}\bar{M}_y^i\bar{M}_z^{i+1}M_{x'}^{i-1}M_y^iM_{z'}^{i+1}$ , and we let  $\delta_i = \{T_{t,i} \mid t \text{ transition of } T\}$ . Denote by  $s_1 \cdots s_k$  the initial configuration of T on w and by  $f_1 \cdots f_k$  its accepting configuration. Let  $Y_i = \sum_a \bar{M}_a^i M_a^i$ . It is again straightforward to construct a locally-cooperative HMSC  $G_2$  such that

$$\mathcal{L}(G_2) = M_{s_1}^1 \cdots M_{s_k}^k \left[ \bigcup_{i=2}^{k-1} Y_1 \cdots Y_{i-2} \cdot \delta_i \cdot Y_{i+2} \cdots Y_k \right]^* \bar{M}_{f_1}^1 \cdots \bar{M}_{f_k}^k$$

Both  $G_1$  and  $G_2$  are of size O(k). Finally, an execution of  $\mathcal{L}(G_1) \cap \mathcal{L}(G_2)$  is an encoding of a sequence  $C_0, \ldots, C_m$ . Since it is an execution of  $G_2$ ,  $G_2$  is the initial configuration of  $G_2$  on  $G_3$  is the final configuration, and  $G_4 \vdash G_{i+1}$ . Hence  $\mathcal{L}(G_1) \cap \mathcal{L}(G_2) \neq \emptyset$  iff the computation of  $G_3$  on  $G_4$  is accepting.  $G_4$ 

Note that the lower bounds for locally-cooperative HMSCs do not hold anymore if we assume that all nodes are labeled by *atomic* MSCs. In this case we can use the fact that any execution has a unique decomposition in atomic MSC, hence both questions can be rephrased in terms of finite word automata.

**Proposition 11.** Let  $G_1$ ,  $G_2$  be locally-cooperative HMSCs such that each node is labeled by an atomic MSC. We have:

- (1) Deciding whether  $\mathcal{L}(G_1) \cap \mathcal{L}(G_2) \neq \emptyset$  is a NLOGSPACE-complete problem.
- (2) Deciding whether  $\mathcal{L}(G_1) \subseteq \mathcal{L}(G_2)$  is an PSPACE-complete problem.

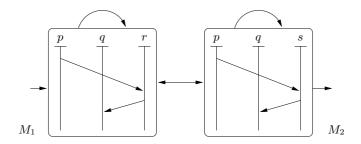


Fig. 8. A locally-cooperative HMSC G.

## 4.3 Local-choice HMSCs

A potential deficiency of HMSC specifications is the distributed choice along branching paths, when a node has more than one successor, each with possibly several minimal processes. The *local choice* property [12] ensures precisely that branching between executions is always controlled by a unique process. We define local HMSCs below, as a slightly different variant of local-choice HMSCs. Local HMSCs simplify the model-checking and implementation algorithms. Moreover, we show that our definition has the same expressiveness as the original definition of [12].

**Definition 12** (local HMSCs). An HMSC  $\langle V, R, v^0, v^f, \lambda \rangle$  is called *local* if

- (1)  $v^0$  has a single minimal event
- (2) for each node  $v \in V$ , there is a process  $\text{root}(v) \in P(v)$  such that every node w with  $(v, w) \in R$  has a unique minimal event, and this event is located on root(v).

For instance, the HMSC of Figure 8 is local. Figure 7 depicts an HMSC which is not local although every node has a unique minimal event, since this event does not belong to the processes of each predecessor node. It is easy to see that any local HMSC is locally cooperative.

Local-choice was defined by different syntactic conditions in [12, 9], but all these definitions are easily seen to yield the same class of HMSCs. We have chosen the simplest definition here, since it is easier to handle and it is compatible with local cooperativeness. Proposition 14 shows how to transform a local-choice HMSC into a local one. Since this construction can be achieved with a quadratic blow-up only, the complexity results for model-checking will not be affected too much. Actually, the results stated for negative model-checking (intersection) can be seen to hold with the very same complexity for local-choice HMSC.

We call a node with at least two outgoing edges a branching node.

**Definition 13** (local-choice HMSCs, [12]). An HMSC  $\langle V, R, v^0, v^f, \lambda \rangle$  is called

local-choice if the following conditions are satisfied:

- (1) Each path starting in  $v^0$  has a single minimal event.
- (2) For each branching node  $v \in V$  and for  $v = v^f$ , there is a process root(v) such that every path from a node w with  $(v, w) \in R$  has a single minimal event, and that event is located on root(v).

It is easy to see that local HMSCs are local-choice HMSCs, while locally-cooperative and local-choice are syntactically incomparable.

An important observation is that every path in a local-choice HMSC  $G = \langle V, R, v^0, v^f, \lambda \rangle$  where all but the last node are non branching and different from  $v^f$ , is of length  $\leq |V|$ . Such a path will be called a *non branching path*. Moreover, for any node v, there is a unique maximal non branching path starting in v that ends either in a branching node or in the terminal node  $v^f$ . We denote this path by NPath(v). Consider now an accepting path  $\sigma$  of G. We decompose  $\sigma$  as

$$\sigma = \sigma_0 \sigma_1 \cdots \sigma_{k+1} \,,$$

where each  $\sigma_i$  is a maximal non branching path (note that this decomposition is unique). Let  $v_i$  be the last node of  $\sigma_{i-1}$  (see also Figure 9, where the triangles represent the partial order graphs of the subpaths  $\sigma_i$ ). Recall that  $v_i$  is branching (or  $v^f$ ) for all  $i \leq k$ . Let also  $w_i$  be the first node of  $\sigma_i$ , hence  $\sigma_i = \text{NPath}(w_i)$ . By definition,  $p_i = root(v_i) \in P(w_i)$  is the process on which the minimal event of  $\sigma_i$  is located. Moreover, the local-choice condition applied to the branching node  $v_{i-1}$  ensures that  $p_i$  also belongs to  $P(\sigma_{i-1})$ , since otherwise  $\sigma_{i-1}\sigma_i \cdots \sigma_k$  would have more than one minimal event.

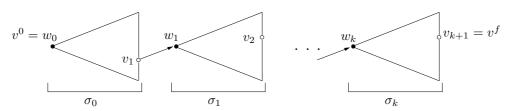


Fig. 9. Path decomposition in local-choice HMSC.

The above decomposition of paths in a local-choice HMSC will be used by the implementation algorithm (Section 5.2). Moreover, this decomposition yields a simple transformation of local-choice HMSC into local HMSCs:

**Proposition 14.** For each local-choice HMSC we can construct an equivalent local HMSC of quadratic size.

*Proof.* Let  $G = \langle V, R, v^0, v^f, \lambda \rangle$  be a local-choice HMSC. The nodes of the local-choice HMSC G' are all immediate successors of branching nodes, together with a new initial node  $w^0$  and a new final node  $w^f$ . A successor v of a branching node is labeled by  $\lambda(\text{NPath}(v))$  (see e.g.  $v = w_i$  in Figure 9).

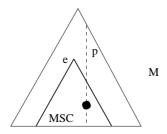


Fig. 10. p-decomposition of an MSC.

Similarly,  $w^0$  is labeled by NPath $(v^0)$ . Finally,  $\lambda(w^f)$  is the empty MSC. The transitions are given by:

- There is a transition  $(v, w) \in R'$  in G' whenever  $(x, w) \in R$ , where x is the last node of NPath(v) (for  $v = w^0$  we require that x is the last node of NPath $(v^0)$ ).
- There is a transition  $(v, w^f) \in R'$  for all v such that NPath(v) ends in  $v^f$  (for  $v = w^0$  we require that  $NPath(v^0)$  ends in  $v^f$ ).

It is obvious that the construction yields an equivalent, local HMSC G'. The number of nodes of G' is  $\leq |V| + 2$  and the size of each MSC labeling a node of G' is at most the size of G.

# 4.4 Model-checking local HMSCs

For the model-checking algorithms on local HMSCs we will transform a local HMSC such that it is non decomposable according to Definition 15 below. Intuitively, we will refine the MSCs labeling a path as much as possible, while preserving the local property. This will ensure a kind of uniqueness (see Lemma 17) when comparing two or more paths to each other.

Given an event e of an MSC M, we denote by  $e \downarrow$  the set of events  $\{f \in M \mid e \leq f\}$  lying in the future of e.

**Definition 15.** Let M be an MSC and p a process. We say that M is p-decomposable (see Figure 10) if there exists an event e of M such that  $e \downarrow$  is an MSC containing some event of process p, and  $M \neq e \downarrow$ . Note that  $e \downarrow$  is required to contain for every receive event the matching send, and vice-versa.

We say that a node v of an HMSC is p-decomposable, if the MSC labeling v is p-decomposable. A local HMSC is called *non decomposable*, if no node v is p-decomposable, with p = root(v).

For instance, the node  $M_1$  of the HMSC G of Figure 8 is not p-decomposable (but it is q- and r-decomposable). Similarly,  $M_2$  is not p-decomposable. Since

both nodes of G have root p, it follows that G is non decomposable.

On the other hand, if we modify  $M_1$  by adding a message from q to p as shown on Figure 11 (a), we still get a local HMSC, but its first node is p-decomposable. Factorizing this node according to its (unique) p-decomposition yields the equivalent, local HMSC of Figure 11 (b). Node  $N'_2$  in this HMSC is now  $q = \text{root}(N'_2)$ -decomposable and factorizing it according to this decomposition, we obtain the equivalent local and non decomposable HMSC of Figure 11 (c).

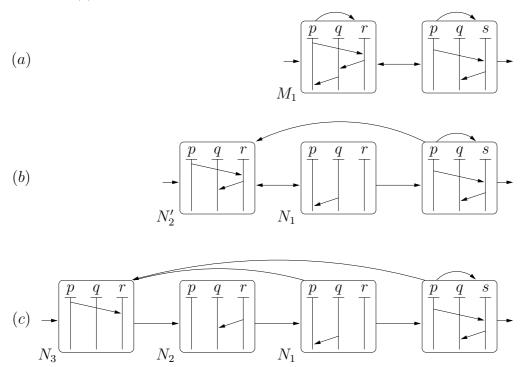


Fig. 11. (a) A decomposable HMSC. (c) An equivalent non decomposable HMSC.

We generalize this construction in the next statement.

**Proposition 16.** We can construct from a local HMSC G an equivalent, non decomposable local HMSC G' in time  $O(|G|^2)$ . Moreover, G' is of size |G|.

Proof. Let v be a node of  $G = \langle V, R, v^0, v^f, \lambda \rangle$  and  $M_1 = \lambda(v)$ . We show how to decompose inductively the node v. The decomposition is applied repeatedly to an MSC M w.r.t. a process p. We start with  $M_1$  and  $p_1 = root(v)$  (if  $v = v^f$  then we choose  $p_1 \in P(M_1)$  arbitrarily). If  $M_1$  is  $p_1$ -decomposable, then let  $M_1 = M_2N_1$  be a  $p_1$ -decomposition of  $M_1$  with  $|N_1|$  minimal. Hence  $N_1$  is not  $p_1$ -decomposable. Then we repeat the process with  $M = M_2$  and  $p_2$  being the process of the minimal event of  $N_1$ . The decomposition process stops as soon as M is not p-decomposable for the current process p. We obtain in this way a sequence  $N_\ell, \ldots, N_1$  of MSCs where  $M_1 = N_\ell \cdots N_1$  and every  $N_i$  has a unique

minimal event located on process  $p_{i+1}$ . Moreover,  $p_i \in P(N_i)$  for all  $\ell > i \geq 1$ . We replace now v by a new path  $w_{\ell}, \ldots, w_1$ , where  $w_i$  is labeled by the MSC  $N_i$  just defined. All edges of G ending at node v now end at  $w_{\ell}$  in the new HMSC, and all edges of G starting at node v now start at  $v_1$ . Note that the new path  $w_{\ell}, \ldots, w_1$  satisfies the requirement of local HMSCs. Moreover, the MSCs labeling the nodes of the new path are all non decomposable, by the minimality condition in each decomposition step.

Applying this algorithm for each node v of G, we obtain an equivalent non decomposable local HMSC G'. Since each event of G belongs to one and only one node of G', G' has at most |G| nodes. Since each decomposition step needs O(|G|) time, the algorithm is quadratic.

The next lemma says that for deciding whether two paths  $v_1, \ldots, v_k$  and  $w_1, \ldots, w_\ell$  of a non decomposable local HMSC are labeled by the same MSCs, we can proceed as follows. Assume that  $v_i$  is labeled by  $M_i$  and  $w_j$  is labeled by  $N_j$ . Assume that there exists some index i such that  $M_j = N_j$  for all  $j \leq i$ , but  $M_{i+1} \neq N_{i+1}$ . In this case, we show that  $N_{i+2} \cdots N_\ell$  is a suffix of  $M_{i+1}$ , resp.  $M_{i+2} \cdots M_k$  is a suffix of  $N_{i+1}$ . Notice that given  $v_{i+1}$  and  $w_{i+1}$ , we can decide effectively whether such factorizations of  $\lambda(v_{i+1})$  and  $\lambda(w_{i+1})$  exist.

**Lemma 17.** Let  $v_1, \ldots, v_k$  and  $w_1, \ldots, w_\ell$  be two paths of a non decomposable local HMSC G and suppose that  $v_i$  is labeled by  $M_i$  and  $w_j$  is labeled by  $N_j$ . Assume further that  $M_1 \cdots M_k = N_1 \cdots N_\ell$ . Then one of the following conditions is satisfied:

- (1)  $M_1 = N_1$ .
- (2)  $M_1 = XN_2 \cdots N_\ell$  and  $N_1 = XM_2 \cdots M_k$ , for some MSC X. Moreover,  $P(M_2 \cdots M_k) \cap P(N_2 \cdots N_\ell) = \emptyset$ .

*Proof.* If  $\ell = 1$  or k = 1, then we are in the second case of the claim. Else, let  $X = M_1 \cap N_1$  be the intersection of  $M_1, N_1$ , i.e., the greatest common prefix of  $M_1, N_1$ . We can write  $M_1 = XY$ ,  $N_1 = XY'$ , where  $P(Y) \cap P(Y') = \emptyset$  and X is an MSC. We can also write  $N_2 \cdots N_\ell = YZ$  for some MSC Z. Then,  $M_2 \cdots M_k = Y'Z$ .

We show first that at least one of the MSCs Y, Y', Z must be empty. Suppose by contradiction that all of Y, Y', Z are non empty. Let e be a minimal event of Z. Since  $YZ = N_2 \cdots N_\ell$  has a unique minimal event we must have  $P(e) \in P(Y)$ . By symmetry,  $P(e) \in P(Y')$ . But then  $P(Y) \cap P(Y') \neq \emptyset$ , a contradiction.

The case where Z is empty corresponds to the second case of the claim.

By symmetry we suppose now that Y is empty, thus  $M_1$  is a prefix of  $N_1$ . We want to show that Y' is also empty, i.e.,  $M_1 = N_1$ . We first show that  $N_1 = M_1 \cdots M_j$  for some j, and finally that j = 1.

Let j be the first index such that  $N_1 \subseteq M_1 \cdots M_j$ . By contradiction, assume that the minimal event e of  $N_2$  belongs to some  $M_i$ ,  $i \leq j$ . Let f be the minimal event of  $M_i$ . Suppose first that f = e. Using the local property of G, we infer that  $M_i \cdots M_j$  is a prefix of  $N_2 \cdots N_\ell$ , hence  $N_1 \subseteq M_1 \cdots M_{i-1}$ , contradicting the minimality of j. Because f < e, the event f belongs to  $N_1$ . Since e is a send event, and f < e in  $N_1N_2$ , there exists some event  $g \geq f$  in  $N_1$  with P(g) = P(e) = p. But this is a contradiction, since  $N_1$  is not p-decomposable. (Note that the restriction of the future of f to  $N_1$  is an MSC since f is the minimal event of  $M_i$ .) Therefore,  $N_1 = M_1 \cdots M_j$ .

We have  $\ell \geq 2$ , thus j < k. Hence,  $root(M_j) = \min(M_{j+1}) = \min(N_2) = root(N_1)$ . Thus, there exists some event f in  $M_j$  with  $p = P(f) = \operatorname{root}(M_j)$ . So  $e = \min(M_j) \leq f$  and events e, f belong to  $N_1$ . But this means that  $N_1$  is p-decomposable, since  $e \downarrow$  restricted to  $N_1$  is an MSC. Therefore, we must have  $e = \min(N_1)$ , i.e. j = 1, and Y' is empty.

We can show now the main result of this section.

**Theorem 18.** Let G and G' be two local HMSCs. Then we have:

- (1) Deciding whether  $\mathcal{L}(G) \cap \mathcal{L}(G') \neq \emptyset$  is NLOGSPACE-complete. Moreover, this question can be solved deterministically in time  $O((|G| + |G'|)^2)$ .
- (2) Deciding whether  $\mathcal{L}(G) \subseteq \mathcal{L}(G')$  is PSPACE-complete.

*Proof.* Both lower bounds follow from classical results on finite word automata.

Let 
$$G = \langle V, R, v^0, v^f, \lambda \rangle$$
 and  $G' = \langle V', R', v'^0, v'^f, \lambda' \rangle$ .

**Intersection problem** We show that the intersection problem can be solved in time  $O((|G|+|G'|)^2)$ . By Proposition 16 applied to G and G', we can suppose that both HMSCs are local and non decomposable.

Assume that  $\mathcal{L}(G) \cap \mathcal{L}(G') \neq \emptyset$ . Then there exist two paths of G, G' labeled by  $M = M_1 \cdots M_k$  and  $N = N_1 \cdots N_\ell$  with M = N, thus satisfying the hypothesis of Lemma 17.

We define a graph  $G \times G'$  with set of states  $V \times V'$ . We let  $(v, v') \longrightarrow_{G \times G'} (w, w')$  in  $G \times G'$  if  $\lambda(v) = \lambda'(v'), (v, w) \in R$  in G and  $(v', w') \in R'$  in G'.

We will check the second condition of Lemma 17 using a set of target nodes T of  $G \times G'$ . Let  $(v, v') \in T$  iff:

- (1)  $\lambda(v) = XY$  and  $\lambda'(v') = XY'$ , where  $P(Y) \cap P(Y') = \emptyset$ .
- (2) Y' labels a path from a successor of v to a final state of G (if Y' is empty then  $v = v^f$  in G). Symmetrically, Y labels a path from a successor of v' to a final state of G' (if Y is empty then  $v' = v'^f$  in G').

We can determine whether (v, v') belongs to the target set using depth-first search in G, G' for finding a path from a successor of v' (if v' is not final) that is labeled by Y, and symmetrically for Y'. Hence, the target set T can be built in time  $O(|G \times G'|)$ .

By Lemma 17,  $\mathcal{L}(G) \cap \mathcal{L}(G') \neq \emptyset$  iff T is reachable from  $(v^0, v'^0)$ . Hence, this problem can be solved in time linear in the number of nodes of  $G \times G'$ , thus in time  $O(|G| \cdot |G'|)$ . This leads to the overall bound  $O((|G| + |G'|)^2)$ .

For the NLOGSPACE upper bound, we sketch the main ingredients of the proof. As usual for accessibility problems, it suffices to store one node of  $G \times G'$  at a time. Given two nodes v, w in a local HMSC such that  $(v, w) \in R$  and v (resp. w) has e (resp. f) as minimal event, the MSC labeling v is uniquely determined by (e, f). Precisely, it comprises the events that are in the future of e but not in that of f. Thus, a node of  $G \times G'$  can be represented by two pairs (e, f), (e', f') of events, one in G and one in G'. With similar arguments, we can test whether  $(v, v') \longrightarrow_{G \times G'} (w, w')$  holds in  $G \times G'$  in NLOGSPACE. For the target set, note that each of the MSCs X, Y, Y' occurring in the definition of T has a single minimal event. Hence we can reason as above for deciding in NLOGSPACE whether a node of  $G \times G'$  belongs to T.

Inclusion problem We show now that the inclusion problem is in PSPACE. We want to know whether there exists an accepting path in G labeled by M such that no path of G' labeled by M is accepting. This is done in the usual way, by guessing a path  $\rho$  in G and considering all possible paths in G' that may match. For this we define a graph  $\widehat{G} \times \widehat{G'}$  from  $G \times G'$ , that corresponds roughly to a subset construction on G'. The guessed path  $\rho$  in G determines all possibly matching paths in G', each of which is in one of the two cases of Lemma 17. At any time, we consider a node v of G and a set W' of nodes of G' according to case 1 of Lemma 17. Whenever (v, v') with  $v' \in W'$  belongs to the target set T, we store the suffix of v' which remains to be matched in G, according to case 2 of Lemma 17. Hence, a state of  $\widehat{G} \times \widehat{G'}$  is a triple (v, W', S) where v is a node of G, W' is a subset of nodes of G' and S is a set of suffixes of MSCs of nodes in G'.

Formally, let Suff be the set of suffixes of MSCs labeling the nodes of G'. The state set of  $\widehat{G} \times \widehat{G'}$  is  $V \times 2^{V'} \times 2^{\text{Suff}}$ . Transitions are defined as  $(v_1, W'_1, S_1) \longrightarrow (v_2, W'_2, S_2)$ , with

 $\bullet \ (v_1, v_2) \in R$ 

- $W_2' = \{v_2' \mid \exists v_1' \in W_1', (v_1, v_1') \longrightarrow_{G \times G'} (v_2, v_2')^4 \}$
- $S_2$  is defined by the following two conditions:
- (A) if  $M = \lambda(v_1)Y$  for some  $M \in S_1$ , then  $Y \in S_2$ ,
- (B) if  $(v_2, v_2') \in T$  for some  $v_2' \in W_2'$ , and  $\lambda(v_2') = XY'$  with  $X = \lambda(v_2) \cap \lambda'(v_2')$ , then  $Y' \in S_2$ .

Notice that in case B above, if  $\lambda(v_2) = \lambda(v_2')$ , then the empty MSC belongs to  $S_2$ . We define a set of final nodes  $\hat{T}$  of  $\widehat{G} \times \widehat{G}'$ : let  $(v, W', S) \in \hat{T}$  if v is final in G and the empty MSC does not belong to S. The initial state is  $(v^0, \{v'^0\}, \{Y'\})$ , where  $\lambda(v^0) = XY, \lambda'(v'^0) = XY'$  with  $P(Y) \cap P(Y') = \emptyset$ . If such an X does not exist, then clearly  $\mathcal{L}(G) \not\subseteq \mathcal{L}(G')$ .

We show now that a state of  $\hat{T}$  is reachable if and only if  $\mathcal{L}(G) \setminus \mathcal{L}(G') \neq \emptyset$ . As this question is a reachability problem in a graph of exponential size, the PSPACE upper bound follows directly.

Assume that there exists an accepting path  $\rho = v_0 \cdots v_\ell$  in G such that no matching path of G' is accepting. The path  $\rho$  uniquely defines a path  $\hat{\rho} = \hat{v}_0 \cdots \hat{v}_\ell$  of  $\widehat{G \times G'}$  with  $\hat{v}_i = (v_i, W'_i, S_i)$ , for all i. We show that  $\hat{v}_\ell \in \hat{T}$ . Assume by contradiction that the empty MSC belongs to  $S_\ell$ . Let us consider a transition  $\hat{v}_k \to \hat{v}_{k+1}$  that generates a suffix Y' in  $S_{k+1}$  (Case B above) leading to the empty MSC in  $S_\ell$  on  $\hat{\rho}$  (applying case A above). Thus, there exists a transition  $(v'_k, v'_{k+1}) \in R'$  in G' such that the pair  $(v_{k+1}, v'_{k+1}) \in T$ . Moreover  $\lambda(v'_{k+1}) = (\lambda(v_{k+1}) \cap \lambda'(v'_{k+1}))Y'$ . By the definition of the transitions (W'-component), we have  $\lambda(v_i) = \lambda'(v'_i)$  for all  $i \leq k$ . By the choice of k,  $\lambda'(v'_{k+1} \cdots v'_m) = \lambda(v_{k+1} \cdots v_\ell)$ , hence  $\lambda'(v'_0 \cdots v'_m) = \lambda(\rho)$  with  $v'_m$  final in G' (due to the definition of the target set T), a contradiction.

Conversely, assume that there exists an accepting path

$$(v_0, W'_0, S_0), \ldots, (v_\ell, W'_\ell, S_\ell)$$

in  $\widehat{G \times G'}$  and  $(v_{\ell}, W'_{\ell}, S_{\ell}) \in \widehat{T}$ . Let  $M = \lambda(v_0 \cdots v_{\ell})$ . Assume by contradiction that there exists an accepting path  $v'_0 \cdots v'_m$  of G' labeled by M. Then we can apply Lemma 17. So there exists an index k such that  $\lambda(v_i) = \lambda'(v'_i)$  for all  $i \leq k$ , and  $(v_{k+1}, v'_{k+1}) \in T$ . Then  $v'_{k+1} \in W'_{k+1}$ , and  $Y' \in S_{k+1}$ , where  $\lambda'(v'_{k+1}) = (\lambda'(v'_{k+1}) \cap \lambda(v_{k+1}))Y'$ . By the definition of T, the empty MSC belongs to  $S_{\ell}$ , a contradiction.

 $<sup>\</sup>overline{^4}$  That is,  $\lambda(v_1) = \lambda'(v_1')$  and  $(v_1', v_2') \in R'$ .

## 5 Implementing HMSC Specifications

The most natural implementation model for HMSCs are communicating finite state machines (CFM), as used for instance in the ITU Z.100 [16] specification language SDL.

A CFM  $\mathcal{A}$  consists of a network of finite state machines  $\mathcal{A} = (\mathcal{A}_p)_{p \in \mathcal{P}}$  that communicate over unbounded, error-free channels. In general we assume that channels are FIFO (if for instance the given HMSC is FIFO), but we can modify the semantics of receives if the MSCs contain overtaking of messages. The content of a channel is a word over a finite alphabet C. With each pair  $(p,q) \in \mathcal{P}^2$  of distinct processes we associate a channel  $B_{p,q}$ . Each finite state machine  $\mathcal{A}_p$  is described by a tuple  $\mathcal{A}_p = (S_p, A_p, \rightarrow_p, F_p)$  consisting of a set of local states  $S_p$ , a set of actions  $A_p$ , a set of local final states  $F_p$  and a transition relation  $\rightarrow_p \subseteq S_p \times A_p \times S_p$ . The computation begins in an initial state  $s^0 \in$  $\prod_{p\in\mathcal{P}} S_p$ . The actions of  $\mathcal{A}_p$  are either local actions or sending/receiving a message. We use the same notations as for MSCs. Sending message  $a \in \mathcal{C}$  from process p to process q is denoted by p!q(a) and it means that a is appended to the channel  $B_{p,q}$ . Receiving message a by p from q is denoted by p?q(a) and it means that a must be the first message in channel  $B_{q,p}$ , which will be then removed from  $B_{q,p}$  (supposing FIFO). In the non FIFO case we specify the type of the message that can be received next (cf. the semantics of a receive in the message queue of UNIX system V). A local action a on process p is denoted by  $l_p(a)$ .

A configuration C = (q, B) of a CFM  $\mathcal{A} = (\mathcal{A}_p)_{p \in \mathcal{P}}$  is described by a global state q of  $S = \prod_{p \in \mathcal{P}} S_p$  and the contents  $B \in (\mathcal{C}^*)^{\mathcal{P} \times \mathcal{P}}$  of all channels. The transition relation of the CFM is denoted by  $\rightarrow$ , its transitive-reflexive closure is denoted as usual by  $\stackrel{*}{\rightarrow}$ . The configuration with global state  $s^0$  and empty channels is the initial configuration. An execution  $\sigma = C_1 \stackrel{a_1}{\rightarrow} C_2 \stackrel{a_2}{\rightarrow} \cdots \stackrel{a_{m-1}}{\rightarrow} C_m$  of  $\mathcal{A}$  is a finite  $\rightarrow$ -path. The labeling of the execution  $\sigma$  is the sequence  $a_1 \cdots a_{m-1}$ . Note that the labeling of an execution  $\sigma$  defines in a natural way a partial MSC  $\operatorname{msc}(\sigma)$ .

We denote an execution of the CFM as successful, if each process p ends in some final state from  $F_p$  and all channels are empty. The set of successful executions of  $\mathcal{A}$  is denoted  $\mathcal{L}(\mathcal{A})$  and is a set of finite MSCs. A configuration C is a deadlock if there is no successful execution starting from C. The size of  $\mathcal{A}$  is  $\sum_{p} |\mathcal{A}_p|$ .

A CFM implementation of an HMSC will refine the HMSC specification by adding for instance data to the message contents. We will call  $\mathcal{A}$  a CFM implementation of the HMSC G if the projection of  $\mathcal{L}(\mathcal{A})$  on the original message contents of G coincides with  $\mathcal{L}(G)$ .

## 5.1 Locally-cooperative HMSCs

The simplest realization of an HMSC G by a CFM is the one where the automaton  $\mathcal{A}_p$  corresponding to process p generates the projection of  $\mathcal{L}(G)$  on p. This approach is used in [2, 24]. Consider again the HMSC  $G_1$  of Figure 8 (page 18), and let M be the MSC given by the projections  $\pi_p(M) = p!r$  p!s,  $\pi_q(M) = q?s$  q?r,  $\pi_r(M) = r?p$  r!q and  $\pi_s(M) = s?p$  s!q, pictured in Figure 12. Then M does not belong to  $\mathcal{L}(G_1)$  although  $\pi_t(M) \in \pi_t(\mathcal{L}(G_1))$  for all

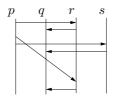


Fig. 12. An MSC  $M \notin \mathcal{L}(G_1)$ 

 $t \in \{p, q, r, s\}$ . Hence  $G_1$  is not realizable according to [2].

We describe our implementation of locally-cooperative HMSCs first on our example  $G_1$ . One can observe that  $G_1$  can be implemented if process p anticipates the next choice between the nodes  $M_1$  and  $M_2$  and sends the prediction with the current message. Processes r and s then forward the prediction to q. In this way, process q knows whether the next message should be received from r or from s. In the example above, this would mean that process p will send with the first message its next choice (node  $M_1$ ). Since predictions are forwarded, this will prevent process q to receive the message from s that corresponds to  $M_2$ .

The general solution will assign a leader process to each transition (p in the example) i.e., a process that occurs in both nodes of the transition, and decides about some nodes to be executed in the future (a kind of prediction).

For a node  $v \in V$  of  $G = \langle V, R, v^0, v^f, \lambda \rangle$ , let P(v) denote the processes occurring in  $\lambda(v)$ . For a path  $\sigma = v_0 v_1 \cdots v_k$  of G let  $P(\sigma) = \bigcup_i P(v_i)$  be the processes occurring in  $\sigma$ . Moreover, we define  $\operatorname{first}(\sigma, p)$  for all  $p \in \mathcal{P}$  as the first node containing p in  $\sigma$ :

$$\mathsf{first}(\sigma, p) = \begin{cases} \bot & \text{if } p \notin P(\sigma), \\ v_j, \text{ where } j = \min\{\ell \ge 0 \mid p \in P(v_\ell)\} & \text{otherwise.} \end{cases}$$

Similarly, if  $\sigma$  has at least i+1 nodes, let  $\mathsf{last}(\sigma,i,p)$  be the last node among the first (i+1) ones containing p:

$$\mathsf{last}(\sigma, i, p) = \begin{cases} \bot & \text{if } p \notin P(v_0 v_1 \cdots v_i), \\ v_j, \text{ where } j = \max\{\ell \le i \mid p \in P(v_\ell)\} & \text{otherwise.} \end{cases}$$

Let  $G = \langle V, R, v^0, v^f, \lambda \rangle$  be a locally-cooperative HMSC. A triple  $(v, \nu, l) \in V \times (V \cup \{\bot\})^{\mathcal{P}} \times \mathcal{P}$  is a realizable prediction if

- either  $\nu(p) = \bot$  for all  $p \in \mathcal{P}$  and  $v = v^f$ ,
- or there exist a path  $\sigma = v_0 v_1 \cdots v_k$  in G, and a transition  $(v, v_0) \in R$  such that
  - $\cdot l \in P(v) \cap P(v_0)$ , and

 $v = v'; \nu = \nu'; \ell = \ell';$ 

 $\nu(p) = \text{first}(\sigma, p)$  for each process p. In particular,  $\nu(l) = v_0$ .

The process l is called the *leader* of the transition  $(v, \nu(l))$  with respect to  $(v, \nu, l)$ . Note that realizable predictions can be precomputed iteratively in polynomial time.

From a locally-cooperative HMSC  $G = \langle V, R, v^0, v^f, \lambda \rangle$ , we build a communicating automaton  $\mathcal{A}_G$  as follows. Each process is initialized with the same input (realizable prediction)  $i_0 = (v_0, \nu_0, l_0)$ , with  $v_0 = v^0$ . The automaton associated with process p is described in Algorithm 1, written in pseudo-C.

```
Alg. 1 Code of process p in an implementation of a locally-cooperative HMSC.
(v, \nu, \ell) = (v_0, \nu_0, \ell_0);
while (true)
{
   m = (v, \nu, \ell);
   if (p \in P(v))
                        // Test useful only for the first node of p.
       execute(v, m); // Deadlocks if p receives a prediction
                         // different from m.
   v' = \nu(p);
   if (v' == \bot)
       halt();
   // Now, v' is the successor of v.
   if (v' == \nu(\ell))
       (\nu', \ell') = guess_next(v', \nu);
   else
       (\nu', \ell') = \operatorname{guess}(v');
```

The call guess\_next(v',  $\nu$ ) nondeterministically chooses a new pair (v',  $\ell'$ ) for the next node v', such that (v',  $\nu'$ ,  $\ell'$ ) is a realizable prediction and the new function  $\nu'$  is *compatible* with the old function  $\nu$  for processes not occurring in v':

$$\nu_{|\mathcal{P}\backslash P(v')} = \nu'_{|\mathcal{P}\backslash P(v')} \tag{C}$$

The call guess(v') guesses nondeterministically a pair (v',  $\ell'$ ) such that the prediction (v', v',  $\ell'$ ) is realizable. In this case, process p makes a prediction about a node p' that is not a direct R-successor of v. This prediction is needed

since all processes of a node must agree on some future information. The call halt() terminates the execution of p in an accepting state. Finally, the call execute(v, m) consists in executing the actions of p of the MSC labeling v, but overloading the messages to be sent or received with m. The weak connectivity of each MSC ensures that all processes executing a node must choose the same value for m in order to complete that node without deadlocking.

**Proposition 19.** Let G be a locally-cooperative HMSC. Then  $A_G$  is a CFM implementation of  $\mathcal{L}(G)$  of size  $n^{O(\wp)}$ , where n is the number of nodes of G and  $\wp$  is the number of processes.

*Proof.* Since  $A_G$  can simulate any execution of G by guessing precisely the path corresponding to a given execution we see that every execution of G corresponds to a successful execution of  $A_G$ . For the other direction let  $x \in \mathcal{L}(A_G)$  and let y be the MSC obtained from x by removing the additional message contents introduced by the algorithm. We will determine a path  $\sigma$  in G such that  $y = \lambda(\sigma)$ .

Since  $x \in \mathcal{L}(\mathcal{A}_G)$ , every process p executes a sequence of states, and halts when its prediction function  $\nu$  satisfies  $\nu(p) = \bot$ . We define the path  $\sigma$  inductively.

Let  $\sigma_0 = v_0 = v^0$ . If  $\nu_0 = \perp^{\mathcal{P}}$ , then we let  $\sigma = \sigma_0$ ; otherwise,  $\nu_0 \neq \perp^{\mathcal{P}}$  implies  $\nu_0(l_0) \neq \perp$ , since  $(v_0, \nu_0, l_0)$  is realizable. Assume now that we have constructed a sequence  $(v_k, l_k, \nu_k)_{0 \leq k \leq i}$  such that:

- a)  $\sigma_i = v_0 v_1 \cdots v_i$  is a path in G;
- b) for any process p, the sequence of events of process p along the path  $\sigma_i$ ,  $\pi_p(\sigma_i)$ , is a prefix of  $\pi_p(y)$ ;
- c) the common leader chosen during the execution of  $v_i$  is  $l_i \in P(v_i)$ ;
- d) the common prediction function chosen during the execution of  $v_i$  is  $\nu_i$ .

These conditions are fulfilled for i=0. Assume that they hold for a given i, and that  $\nu_i(l_i) \neq \bot$ . Then  $v_{i+1} = \nu_i(l_i)$  is a state of G and  $(v_i, v_{i+1}) \in R$  by by the definition of a realizable prediction. Hence  $\sigma_{i+1} = v_0 \cdots v_{i+1}$  is a path of G. Moreover,  $l_i \in P(v_{i+1})$ , and the algorithm for process  $l_i$  shows that  $l_i$  executes  $v_{i+1}$  immediately after having completed  $v_i$ .

We show first that every process  $p \in P(v_{i+1})$  executes  $v_{i+1}$  after  $\sigma_i$ . Assume that p executes some state  $v \neq v_{i+1}$  after its execution of  $\sigma_i$ . Let  $v_j = \mathsf{last}(\sigma_i, i, p)$  be the last node executed by p in  $\sigma_i$  and let  $\nu_j$  be the associated prediction. Then  $j \neq i$  since  $p \in P(v_i)$  would imply  $v = v_{i+1}$  since the execution did not deadlock. By assumption,  $v = \nu_j(p)$ . The prediction functions  $\nu_k$ ,  $j < k \leq i$  guessed by  $l_j$  satisfy the compatibility condition (C), so in particular  $\nu_k(p) = \nu_j(p)$  for  $j \leq k \leq i$ , so  $v = \nu_i(p)$ . Since  $\nu_i$  is realizable by a path  $\tau$  of G and  $p \in P(v_{i+1})$  we obtain that  $v = \nu_i(p) = \mathsf{first}(\tau, p) = v_{i+1}$ ,

a contradiction.

Since  $v_{i+1}$  is executed without deadlock, the new leader  $l_{i+1}$  and the new prediction function  $\nu_{i+1}$  are well defined.

Let now k be maximal such that  $\sigma_k$  satisfies conditions a) to d) above, and let  $\sigma = \sigma_k$ . We claim that  $y = \lambda(\sigma)$ . If this is not the case,  $\pi_p(\sigma)$  would be a strict prefix of  $\pi_p(y)$  for some  $p \in \mathcal{P}$ . Since p executes some actions after those of  $\pi_p(\sigma)$ , it has to execute at least the state  $v = \nu_j(p) = \nu_k(p)$ . But  $\nu_k(l_k) = \bot$  by maximality of k, so this is a contradiction to  $\sigma_k$  being executed without deadlock.

**Remark 20.** Note that we can fix a leader for each transition of the HMSC beforehand. This decreases the degree of nondeterminism and the possibility of deadlocking. We used a leader in our algorithm to simplify our implementation.

#### 5.2 Local-choice HMSCs

The implementation algorithm described in the previous section cannot avoid deadlocks for the resulting CFM, since future predictions are guessed by each process separately. An unavoidable problem is that branching in an HMSC is not controlled by a single process, as it is the case for local-choice HMSCs.

Recall the definition of a branching node from Section 4.3: this is a node with at least two outgoing edges.

Algorithm 2 is a linear and deadlock-free CFM implementation of a local-choice HMSC. Roughly speaking, the idea of the algorithm is that after executing a branching node, the minimal process of the forthcoming execution has to choose the next node (through a call of  $choose\_successor()$  in Alg. 2 below). Processes that are not minimal after the branching will execute as their next event a receive action, so they stay in a *polling state* until receiving a message. A polling state means that the only possible actions are receives of arbitrary messages from arbitrary processes. The polling function is shown at the beginning of the pseudo-code for process p in Algorithm 2.

Messages are overloaded with the node that is currently executed: the call execute(w) means that process p executes the projection  $\pi_p(w)$  of w on process p, and that each message sent by p contains w as additional data. The current node is also stored in the variable current\_node, which is initialized to  $v^0$ . When a polling process receives a message overloaded with node v, its current node becomes v.

Finally, processes executing a non-branching node just jump to the next node

to execute their actions in this node (if any), and so on until reaching a branching node or the last node.

Alg. 2 Code of process p in an implementation of a local-choice HMSC.

```
// Polling function
void polling(void)
   while (true)
      if p receives a message containing v
         current_node = v;
         return;
      }
}
// Main algorithm
current_node = v_0;
while (true)
   execute(current_node);
   if (not_branching(current_node))
      current_node = successor_node(current_node);
   else if (p == root(current_node))
      current_node = choose_successor(current_node);
   else polling();
```

The correctness proof of the algorithm is easy, since each successor node of a branching node admits a unique minimal event on a process occurring in the previous node (and therefore, it is connected). After a branching node v, each process except root(v) begins its execution by receiving a message. Since messages are overloaded with node names, it gets informed about the current node. We obtain an implementation of linear size for local-choice HMSCs.

**Proposition 21.** For any local-choice HMSC, one can construct a deadlock-free CFM implementation of linear size.

## 6 Existentially-Bounded CFM and Deadlock Detection

In this section we consider a subclass of communicating finite state machines, called *existentially-bounded CFM*. Intuitively, a CFM is existentially-bounded if every execution can be simulated using bounded channels. Since implementations of HMSCs yield existentially-bounded CFMs, it is natural to ask whether a existentially-bounded CFM is deadlock-free. We show below how to

decide this question in polynomial space. Notice that for unrestricted CFMs this question is undecidable [5].

Recall that a CFM execution is successful if it ends with empty channels and each process reaches some local final state. A configuration C is a deadlock if there is no successful execution starting from C. Finally, for  $x \in A^*$  we let msc(x) denote the partial MSC defined by pairing the k-th event of type p!q(a) with the k-th event of type q?p(a) (if they exist).

Let  $A = \bigcup_{p \in \mathcal{P}} A_p$  be the set of possible actions of a CFM over process set  $\mathcal{P}$ . Two executions  $\sigma, \sigma'$  are called *equivalent* if  $\operatorname{msc}(\sigma) = \operatorname{msc}(\sigma')$  and  $\sigma, \sigma'$  start in the same configuration. In this case we write  $\sigma \sim \sigma'$ .

An execution  $\sigma$  of a CFM is called *existentially-b-bounded*, if every configuration of  $\sigma$  is such that the size of every channel is bounded by b. If  $C \stackrel{*}{\to} C'$  is b-bounded, then we say that C is b-reachable from C.

**Definition 22** (existentially-b-bounded CFM). Let b > 0. A CFM is said existentially-b-bounded if every successful execution  $\sigma$  starting in the initial configuration admits some successful, b-bounded equivalent execution  $\sigma'$ . A CFM is called existentially-bounded if it is existentially-b-bounded for some b.

**Proposition 23.** Let A be a existentially-b-bounded CFM and let C be b-reachable from the initial configuration of A. Then C is not a deadlock if and only if there is some b-bounded, successful execution starting from C.

Proof. We assume that C is not a deadlock configuration, that is, there exists some successful execution  $\sigma$  starting in C and labeled by  $v \in A^*$ . Moreover, let  $\tau = C_0 \stackrel{u}{\longrightarrow} C$  be a b-bounded execution, with  $u \in A^*$ . Since A is an existentially-b-bounded CFM there exists also a successful, b-bounded execution  $\sigma'$  such that  $\sigma' \sim \tau \sigma$ , that is,  $\sigma'$  and  $\tau \sigma$  are equivalent. Let  $w \in A^*$  be the labeling of  $\sigma'$ , hence  $\operatorname{msc}(w) = \operatorname{msc}(uv)$ . Hence, we can write  $w = u_0v_1u_1\cdots v_ku_kv_{k+1}$  with  $\operatorname{msc}(u) = \operatorname{msc}(u_0\cdots u_k)$ , and for all  $i \leq j$  and every process p, either  $\pi_p(u_j) = \epsilon$  or  $\pi_p(v_i) = \epsilon$ .

We show that the execution starting in C and labeled by  $v_1 \cdots v_{k+1}$  is b-bounded. Note first that  $v_1 \cdots v_{k+1}$  is well defined starting from C, since for any pair p,q of processes,  $|v_i|_a \neq \epsilon$  for some a = p?q(c) implies  $|u_i \cdots u_k|_{a'} = \epsilon$  for any a' = p?q(c'), thus a is possible after executing  $u_0 \cdots u_k v_1 \cdots v_{i-1}$ . Moreover, there can be no channel of size more than b in  $v_i$  after executing  $u_0 \cdots u_k v_1 \cdots v_{i-1}$ , since if  $|v_i|_a \neq \epsilon$  for some a = p!q(c) then  $|u_i \cdots u_k|_{a'} = \epsilon$  for any a' = p!q(c').

**Proposition 24.** The following problem is PSPACE-complete:

Input: Integer b (unary representation) and a existentially-b-bounded CFM A.

Question: Is  $\mathcal{A}$  deadlock-free?

*Proof.* The upper bound is provided by Proposition 23. For the lower bound we give a reduction from the non empty intersection problem for finite automata. Assume that  $A_1, \ldots, A_n$  are finite automata over a mutual alphabet  $\mathcal{M}$ . Without restriction, we suppose that for every  $\mathcal{A}_i$  and every state we can reach a final state. We use n processes  $p_1, \ldots, p_n$  that exchange messages over the alphabet  $\mathcal{M} \cup \{\#\}$ . Process  $p_1$  starts by sending a message # to  $p_n$ . Then  $p_1$  starts simulating  $A_1$  such that for each transition it sends a message to  $p_2$ corresponding to the transition label. Finally, from each final state of  $A_1$  it can go to a new state  $d_1$  after sending # to  $p_2$  (state  $d_1$  has no successor). For each i > 1 process  $p_i$  simulates the automaton  $A_i$  such that for each transition labeled by some  $a \in \mathcal{M}$  it must first receive the message a from  $p_{i-1}$ and then it sends a to  $p_{i+1}$ . Upon receiving # from  $p_{i-1}$  in a final state of  $\mathcal{A}_i$ it can move to a new state  $d_i$ , after sending # to  $p_{i+1}$ . If i = n then it also receives the message # from  $p_1$ . It can be easily checked that the intersection of  $A_1, \ldots, A_n$  is non empty if and only if there is some successful, 1-bounded execution starting from the initial configuration. 

## **Corollary 25.** The following problem is PSPACE-complete:

Input: Integer b (unary representation) and a existentially-b-bounded CFM A. Question: Is  $\mathcal{L}(A) \neq \emptyset$ ?

The last proposition allows to connect the model-checking problem and the implementation by CFMs. We first define the synchronized product of two CFM implementations of HMSCs  $G_1, G_2$ . Let  $\mathcal{A}_i = (\mathcal{A}_p^i)_{p \in \mathcal{P}}$ ,  $\mathcal{A}_p^i = (S_p^i, \rightarrow_p^i, s_i^0, F_p^i)$ , be a CFM implementation of  $G_i$ . The synchronized product  $\mathcal{A}_1 \times \mathcal{A}_2$  is the CFM  $\mathcal{A} = (\mathcal{A}_p)_{p \in \mathcal{P}}$  with  $\mathcal{A}_p = (S_p, \rightarrow_p, s^0, F_p)$  given by:

- $\bullet \ S_p = S_p^1 \times S_p^2,$
- $(s_1, s_2) \xrightarrow{a}_p (s'_1, s'_2)$  if  $s_1, s'_1 \in S^1_p$ ,  $s_2, s'_2 \in S^2_p$ ,  $s_i \xrightarrow{a_i}_p s'_i$  for each i = 1, 2. The actions  $a, a_1, a_2$  are either of the form  $a_i = p!q(c_i)$  and  $a = p!q(c_1, c_2)$ , or  $a_i = p?q(c_i)$  and  $a = p?q(c_1, c_2)$ . Moreover, the projection of  $c_1, c_2$  on the message contents of  $G_1, G_2$ , must be identical.
- The initial state of  $\mathcal{A}$  is  $s^0 = (s_1^0, s_2^0)$ , where  $s_i^0$  is the initial state of  $\mathcal{A}_i$ . Let also  $F_p = F_p^1 \times F_p^2$  be the set of local p-final states of  $\mathcal{A}$ .

**Theorem 26.** Let C be a class of CFM-implementable HMSCs. Then, the model-checking problem for C (intersection and inclusion, resp.) is decidable.

*Proof.* Suppose that  $A_i$  is a CFM implementation of  $G_i$ . Moreover, let  $b_i$  be the channel bound for  $G_i$ . That is, any atom in  $Atom(G_i)$  has some linearization such that the difference between send and receive symbols is at most

 $b_i$ , for any prefix. Then the CFMs  $\mathcal{A}_1, \mathcal{A}_2$  are existentially-b-bounded, with  $b = \max(b_1, b_2)$ .

Moreover, for the negative model-checking we have  $\mathcal{L}(G_1) \cap \mathcal{L}(G_2) \neq \emptyset$  iff  $\mathcal{L}(\mathcal{A}_1 \times \mathcal{A}_2) \neq \emptyset$ . For the positive model-checking we have  $\mathcal{L}(G_1) \not\subseteq \mathcal{L}(G_2)$  iff  $\mathcal{L}(\mathcal{A}_1 \times 2^{\mathcal{A}_2}) \neq \emptyset$ , where  $2^{\mathcal{A}}$  denotes the powerset CFM associated with  $\mathcal{A}$ , obtained by synchronizing on actions of same type and identical original contents.

#### Conclusion

We have shown that model-checking is decidable for a large class of infinite-state HMSCs, globally-cooperative HMSCs. Moreover, the complexity remains the same as for the more restricted class of regular HMSCs. For local-choice HMSCs, we have shown how to perform model-checking with the same complexity as for finite automata. The precise complexity of the inclusion problem for locally-cooperative HMSCs remains open, we only know that it lies between PSPACE and EXPSPACE. The implementation of locally-cooperative HMSCs raises the question whether we can decide for a given locally-cooperative HMSC if it can be implemented without deadlocks in our framework. Figure 13 summarizes our results.

Class $\mathcal{C}$	globally-cooperative	locally-cooperative	local-choice
$\in \mathcal{C}$ ?	co-NP	Р	Р
$\cap = \emptyset$	PSPACE	NLOG if $\wp$ is constant	NLOG
$\subseteq$	EXPSPACE	PSPACE if $\wp$ is constant	PSPACE
Implem.		$ G ^{O(\wp)}$	G

Fig. 13. Model-checking and implementation infinite-state HMSCs.

The present paper does not consider implementation of globally-cooperative HMSCs. It turns out that they are indeed implementable, see [8].

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