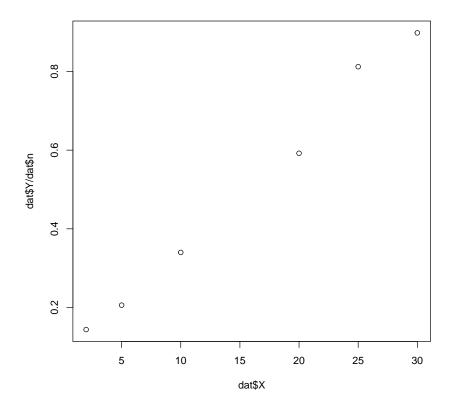
Stat 207 HW7

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```
(a) dat = read.table("CH14PR11.txt")
    names(dat) = c("X", "n", "Y")
    plot(dat$X, dat$Y/dat$n)
```



The plot support the analyst's belief that the logistic response functiion is appropriate.

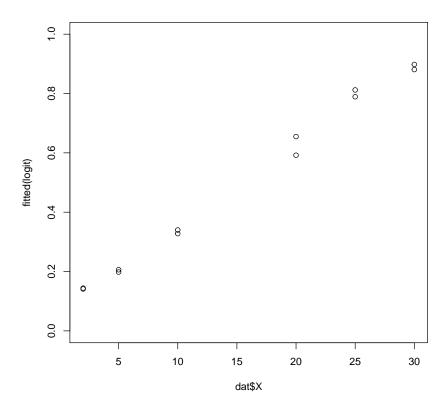
```
(b) logit = glm(Y/n ~ X, data = dat, weight = n , family = "binomial")
    summary(logit)

##
## Call:
## glm(formula = Y/n ~ X, family = "binomial", data = dat, weights = n)
##
## Deviance Residuals:
```

```
1 2 3 4 5
##
   0.1754 0.4330
                  0.5784 -2.9193
                                  1.2710
                                           1.2209
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -2.076565
                        0.084839 -24.48 <2e-16 ***
             0.135851
                        0.004772 28.47 <2e-16 ***
## X
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 1108.171 on 5 degrees of freedom
## Residual deviance: 12.181 on 4 degrees of freedom
## AIC: 53.419
## Number of Fisher Scoring iterations: 3
```

From the summary, the maximum likelihood estimates of $\hat{\beta}_0 = -2.0766,$ $\hat{\beta}_1 = 0.1359,$

$$\hat{\pi} = \frac{exp(\beta_0 + \beta_1 X)}{1 + exp(\beta_0 + \beta_1 X)} = \frac{exp(-2.0766 + 0.1359X)}{1 + exp(-2.0766 + 0.1359X)}$$



The fitted logistic response function appears to be well.

```
(d) exp(0.1359)
## [1] 1.145567
```

 $exp(\beta_1)=1.145567$, so that the odds of the bottles being returned is increased by 14.5567% with each one deposit level increased.

```
(e) newdat = data.frame(X = 15)
    predict(logit, newdata = newdat, type = "response")

## 1
## 0.4903005
```

The estimated probability that a bottle will be returned when the deposit is 15 cents is 0.4903005.

```
(f) newpi = 0.75
  pi_2 = log(newpi/(1-newpi))
  (pi_2 - (-2.0766))/0.1359
## [1] 23.36433
```

Estimate the amount of deposit for which 75% of the bottles are expected to be returned is 23.36433.

$2 \quad 14.14$

```
dat = read.table("CH14PR14.txt")
  names(dat) = c("Y", "X1", "X2", "X3")
 logit = glm(Y ~ X1 + X2 + X3, data = dat, family = "binomial")
  summary(logit)
##
## Call:
## glm(formula = Y ~ X1 + X2 + X3, family = "binomial", data = dat)
##
## Deviance Residuals:
      Min
##
           1Q Median
                                  3Q
                                          Max
## -1.4037 -0.5637 -0.3352 -0.1542
                                       2.9394
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -1.17716
                          2.98242 -0.395 0.69307
                          0.03038
## X1
               0.07279
                                   2.396 0.01658 *
              -0.09899
## X2
                          0.03348 -2.957 0.00311 **
               0.43397
                          0.52179
                                   0.832 0.40558
## X3
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 134.94 on 158 degrees of freedom
## Residual deviance: 105.09 on 155 degrees of freedom
## AIC: 113.09
##
## Number of Fisher Scoring iterations: 6
```

From the summary, the maximum likelihood estimates $\hat{\beta}_0 = -1.17716$,

```
\hat{\beta}_1 = 0.07279, \ \hat{\beta}_2 = -0.09899, \ \hat{\beta}_4 = 0.43397 \hat{\pi} = \frac{exp(\beta_0 + \beta_1 X1 + \beta_2 X2 + \beta_3 X3)}{1 + exp(\beta_0 + \beta_1 X1 + \beta_2 X2 + \beta_3 X3)} = \frac{exp(-1.17716 + 0.07279X1 - 0.09899X2 + 0.43397X3)}{1 + exp(-1.17716 + 0.07279X1 - 0.09899X2 + 0.43397X3)}
```

```
(b) exp(0.07279)

## [1] 1.075505

exp(-0.09899)

## [1] 0.9057518

exp(0.43397)

## [1] 1.543373
```

- $exp(\beta_1) = 1.075505$, so that the odds of getting a flu shot is increased by 7.5% with each one age increased.
- $exp(\beta_2) = 0.9057518$, so that the odds of getting a flu shot is decreased by 9.4% with each one health awareness index increased.
- $exp(\beta_3) = 1.543373$, so that the odds of getting a flu shot is increased by 54.3% from woman to man.

The estimated probability with X1=55, X2=60 and X3=1 is 0.06422197

3 14.17

(a) dat = read.table("CH14PR11.txt")
 names(dat) = c("X", "n", "Y")
 logit = glm(Y/n ~ X, weight=n, data = dat, family = "binomial")
 summary(logit)

```
##
## Call:
## glm(formula = Y/n ~ X, family = "binomial", data = dat, weights = n)
##
## Deviance Residuals:
                  2
                          3
                                                      6
##
       1
                                             5
##
   0.1754
           0.4330 0.5784 -2.9193
                                       1.2710
                                                 1.2209
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -2.076565
                          0.084839 -24.48
                                              <2e-16 ***
## X
                0.135851
                           0.004772
                                     28.47
                                              <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1108.171 on 5 degrees of freedom
##
## Residual deviance: 12.181 on 4 degrees of freedom
## AIC: 53.419
##
## Number of Fisher Scoring iterations: 3
  b1 = 0.1359
  s1 = 0.004772
  z = qnorm(1-0.05/2)
  c(b1-s1*z, b1+s1*z)
## [1] 0.1265471 0.1452529
  c(exp(b1-s1*z), exp(b1+s1*z))
## [1] 1.134903 1.156332
```

From summary(logit), we get $s(b_1) = 0.004772$, $b_1 = 0.1359$, based on $b_k \pm z(1-\alpha/2)sb_k$, we conclude that we are 95 % confident that β_1 is between 0.1265471 and 0.1452529, and corresponding confidence limits for the odds ratio $exp(\beta_1)$ is between 1.134903 and 1.156332.

```
(b) qnorm(1-0.05/2)
## [1] 1.959964
```

$$H_0:\beta_1=0$$

```
\label{eq:VS.} \begin{array}{l} {\rm VS.}\ H_1{:}\beta_1\neq 0 \\ \\ z^*=\frac{b_1}{s(b_1)}=0.1359/0.004772=28.47863 \end{array}
```

we can reject H_0 if $|z^*| > Z(1-0.05/2)=1.959964$, otherwise reject H_1 so that reject H_0 because $|z^*|>1.959964$,

therefore, X1 can not be dropped from the regression model, and the P-value is 2e-16

```
(c) logLik(logit)

## 'log Lik.' -24.70937 (df=2)

logitR = glm(Y/n ~ 1, weight = n, data = dat, family = "binomial")
logLik(logitR)

## 'log Lik.' -572.7044 (df=1)

qchisq(1-0.05, 2-1)

## [1] 3.841459

pchisq(1095.99, 1, lower.tail = FALSE)

## [1] 2.457179e-240
```

$$H_0:\beta_1=0$$
 VS. $H_1:\beta_1\neq 0$ The full model: $\pi=[1+exp(-(\beta_0+\beta_1X1))]^{-1}$ $\ln(\mathcal{L}(\mathcal{F}))=-24.70937$ The reduced model: $\pi=[1+exp(-(\beta_0))]^{-1}$ $\ln(\mathcal{L}(\mathcal{R}))=-572.7044$ $G^2=-2(\ln(\mathcal{L}(\mathcal{R})-\ln(\mathcal{L}(\mathcal{F}))))=1095.99$ we can reject H_0 if $G^2>\chi^2(1-0.05,2-1)=3.8415$, otherwise reject H_1 so that reject H_0 because $G^2>3.8415$,

therefore, X1 cannot be dropped from the regression model, and the P-value is 2.457179e-240. And the result is different from the result we get in (b).

```
dat = read.table("CH14PR14.txt")
(a)
     names(dat) = c("Y", "X1", "X2", "X3")
     logit = glm(Y ~ X1 + X2 + X3, data = dat, family = "binomial")
     summary(logit)
   ##
   ## glm(formula = Y ~ X1 + X2 + X3, family = "binomial", data = dat)
   ##
   ## Deviance Residuals:
         Min 1Q Median
                                     3Q
                                              Max
   ## -1.4037 -0.5637 -0.3352 -0.1542
                                           2.9394
   ##
   ## Coefficients:
   ##
                  Estimate Std. Error z value Pr(>|z|)
   ## (Intercept) -1.17716 2.98242 -0.395 0.69307
   ## X1
                  ## X2
                 -0.09899 0.03348 -2.957 0.00311 **
   ## X3
                 0.43397
                              0.52179 0.832 0.40558
   ## ---
   ## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
   ## (Dispersion parameter for binomial family taken to be 1)
   ##
   ##
          Null deviance: 134.94 on 158 degrees of freedom
   ## Residual deviance: 105.09 on 155 degrees of freedom
   ## AIC: 113.09
   ##
   ## Number of Fisher Scoring iterations: 6
       z(1 - \frac{0.1}{2*2}) = 0.975, s(b_1) = 0.03038, s(b_2) = 0.03348
    exp(30(0.07280.030381.96)) < exp(30\beta_1) < exp(30(0.0728 + 0.030381.96))
                      1.4878 < exp(30\beta_1) < 52.9837
    exp(25(0.0990.033481.96)) < exp(25\beta_2) < exp(25(0.0728 + 0.033481.96))
                      0.0163 < exp(25\beta_2) < 31.824
(b) qnorm(1-0.05/2)
   ## [1] 1.959964
```

```
H_0: \beta_3 = 0 VS. H_1: \beta_3 \neq 0 z^* = \frac{b_3}{s(b_3)} = 0.43397/0.52179 = 0.8316947 we can reject H_0 if |z^*| > Z(1 - 0.05/2) = 1.959964, otherwise reject H_1 so that reject H_1 because |z^*| < 1.959964, therefore, X3 can be dropped from the regression model, and the P-value in 0.40559
```

is 0.40558

```
(c) logLik(logit)

## 'log Lik.' -52.54659 (df=4)

logitR = glm(Y ~ X1+X2, data = dat, family = "binomial")
logLik(logitR)

## 'log Lik.' -52.89769 (df=3)

qchisq(1-0.05, 4-3)

## [1] 3.841459

pchisq(0.70236, 1, lower.tail = FALSE)

## [1] 0.4019918
```

$$H_0{:}\beta_3 = 0$$
 VS. $H_1{:}\beta_3 \neq 0$ The full model: $\pi = [1 + exp(-(\beta_0 + \beta_1 X 1 + \beta_2 X 2 + \beta_3 X 3))]^{-1} \ln(L(F)) = -52.54659$ The reduced model: $\pi = [1 + exp(-(\beta_0 + \beta_1 X 1 + \beta_2 X 2))]^{-1} \ln(L(R)) = -52.89769$
$$G^2 = -2(\ln(L(R)-\ln(L(F)))) = 0.70236$$
 we can reject H_0 if $G^2 > \chi^2(1 - 0.05, 4 - 3) = 3.8415, otherwise reject H_1 so that reject H_1 because $G^2 < 3.8415$,$

therefore, X3 can be dropped from the regression model, and the P-value is 0.4019918. And the result is the same as the result we get in (b).

```
logitF = glm(Y \sim X1+X2+I(X1^2)+I(X2^2)+I(X1*X2), data = dat, family = "binomial")
  logLik(logitF)
## 'log Lik.' -52.13072 (df=6)
  logitR = glm(Y ~ X1+X2, data = dat, family = "binomial")
  logLik(logitR)
## 'log Lik.' -52.89769 (df=3)
  qchisq(1-0.05, 6-3)
## [1] 7.814728
  pchisq(1.53394, 3, lower.tail = FALSE)
## [1] 0.6744594
                            H_0: \beta_3 = \beta_4 = \beta_5 = 0
                       VS. H_1:notall\beta_3, \beta_4, \beta_5 equal0
                               The full model:
 \pi = [1 + exp(-(\beta_0 + \beta_1 X1 + \beta_2 X2 + \beta_3 X1^2 + \beta_4 X2^2 + \beta_5 X1 * X2))]^{-1}
                            ln(L(F)) = -52.13072
       The reduced model: \pi = [1 + exp(-(\beta_0 + \beta_1 X 1 + \beta_2 X 2))]^{-1}
                            ln(L(R)) = -52.89769
                   G^2 = -2(\ln(L(R)-\ln(L(F)))) = 1.53394
we can reject H_0 if G^2 > \chi^2(1 - 0.05, 6 - 3) = 7.814728, otherwise reject H_1
                 so that reject H_1 because G^2 < 7.814728,
   therefore, X1^2, X2^2, I(X1 * X2) can be dropped from the regression
  model, and the P-value is 0.6744594. And the result is the same as the
                            result we get in (b).
```

```
(a) dat = read.table("CH14PR14.txt")
    names(dat) = c("y", "x1", "x2", "x3")
    dat.new = scale(dat[, 2:4], scale = FALSE)
    dat.new = as.data.frame(cbind(dat$y, dat.new))
    names(dat.new) = c("y", "x1", "x2", "x3")
```

```
alpha = .1
  wrap.foo = function(formula, dat.new. = dat.new)
    model = glm(formula, family = binomial, data = dat.new.)
    p.val = summary(model)$coef
    p.val[nrow(p.val), 4]
  tmp = c(wrap.foo(y ~ x1),
          wrap.foo(y ~ x2),
         wrap.foo(y ~ I(x1*x2)),
         wrap.foo(y \tilde{I}(x1^2)),
         wrap.foo(y \tilde{1}(x2^2)),
         wrap.foo(y ~ I(x1^2):I(x2^2)))
  any(tmp < alpha)</pre>
## [1] TRUE
  which.min(tmp)
## [1] 1
  tmp = c(wrap.foo(y ~x1 + x2),
          wrap.foo(y \sim x1 + I(x1*x2)),
          wrap.foo(y \sim x1 + I(x1^2)),
          wrap.foo(y \sim x1 + I(x2^2))
  any(tmp < alpha)</pre>
## [1] TRUE
  which.min(tmp)
## [1] 1
 wrap.foo(y ~ x1 + x2 + I(x2^2))
          )
  any(tmp < alpha)</pre>
## [1] FALSE
```

X1 enters in step 1; X2 enters in step 2; no variables satisfy criterion

for entry in step 3.

```
(b) wrap.foo = function(formula, dat.new. = dat.new)
       model = glm(formula, family = binomial, data = dat.new.)
      p.val = summary(model)$coef
      p.val = p.val[, 4]
       p.val[-1]
     tmp = wrap.foo(y ~ x1 + x2 + I(x1*x2) + I(x1^2) + I(x2^2))
     any(tmp > alpha)
   ## [1] TRUE
     which.max(tmp)
   ## I(x1^2)
   ##
     tmp = wrap.foo(y ~ x1 + x2 + I(x1*x2) + I(x2^2))
     any(tmp > alpha)
   ## [1] TRUE
     which.max(tmp)
   ## I(x1 * x2)
   ##
     tmp = wrap.foo(y ~ x1 + x2 + I(x2^2))
     any(tmp > alpha)
   ## [1] TRUE
     which.max(tmp)
   ## I(x2^2)
   ## 3
     tmp = wrap.foo(y ~ x1 + x2)
     any(tmp > alpha)
   ## [1] FALSE
```

X11 is deleted in step 1; X12 is deleted in step 2; X3 is deleted in step 3; X22 is deleted in step 4; X1 and X2 are retained in the model.

```
model = glm(y ~ x1 + x2 + I(x1*x2) + I(x1^2) + I(x2^2) + I(x1^2*x2^2),
             family = binomial, data = dat.new)
  step(model)
## Start: AIC=116.67
## y \sim x1 + x2 + I(x1 * x2) + I(x1^2) + I(x2^2) + I(x1^2 * x2^2)
##
                  Df Deviance
                               AIC
## - I(x2^2)
                   1 102.68 114.68
## - I(x1^2)
                  1 103.56 115.56
## - I(x1 * x2)
                  1 103.84 115.84
## - I(x1^2 * x2^2) 1 104.26 116.26
## <none>
                       102.67 116.67
## - x2
                  1 107.48 119.48
## - x1
                  1 109.46 121.46
##
## Step: AIC=114.68
## y \sim x1 + x2 + I(x1 * x2) + I(x1^2) + I(x1^2 * x2^2)
##
                  Df Deviance
                               AIC
                  1 103.83 113.83
## - I(x1^2)
## - I(x1 * x2)
                  1 103.84 113.84
## <none>
                       102.68 114.68
## - I(x1^2 * x2^2) 1 105.71 115.71
## - x2
                  1 107.94 117.94
## - x1
                  1 109.50 119.50
##
## Step: AIC=113.83
## y \sim x1 + x2 + I(x1 * x2) + I(x1^2 * x2^2)
##
##
                  Df Deviance
                               AIC
## - I(x1 * x2)
               1 104.74 112.74
## - I(x1^2 * x2^2) 1 105.75 113.75
## <none>
                       103.83 113.83
## - x1
                  1 109.97 117.97
## - x2
                  1 111.00 119.00
## Step: AIC=112.74
## y \sim x1 + x2 + I(x1^2 * x2^2)
##
                  Df Deviance
## - I(x1^2 * x2^2) 1 105.80 111.80
```

```
## <none>
                      104.74 112.74
## - x1
                  1 109.97 115.97
## - x2
                    1 111.40 117.40
##
## Step: AIC=111.8
## y \sim x1 + x2
##
##
         Df Deviance
                      AIC
## <none>
             105.80 111.80
        1
## - x1
             113.20 117.20
## - x2 1 116.27 120.27
##
## Call: glm(formula = y ~ x1 + x2, family = binomial, data = dat.new)
##
## Coefficients:
## (Intercept)
                      x1
     -2.29705
                   0.07787
                             -0.09547
##
##
## Degrees of Freedom: 158 Total (i.e. Null); 156 Residual
## Null Deviance:
                   134.9
## Residual Deviance: 105.8 AIC: 111.8
```

The best model according to the AICp criterion is based on y $\,$ x1 + x2. AIC = 111.8.

```
(d) step(model, k = log(159))
   ## Start: AIC=138.15
   ## y \sim x1 + x2 + I(x1 * x2) + I(x1^{\circ}2) + I(x2^{\circ}2) + I(x1^{\circ}2 * x2^{\circ}2)
   ##
                       Df Deviance
                                     AIC
   ##
   ## - I(x2^2)
                       1 102.68 133.10
   ## - I(x1^2)
                        1
                           103.56 133.97
                    1 103.84 134.25
   ## - I(x1 * x2)
   ## - I(x1^2 * x2^2) 1 104.26 134.68
   ## - x2
                       1 107.48 137.89
   ## <none>
                            102.67 138.15
   ## - x1
                        1 109.46 139.87
   ##
   ## Step: AIC=133.1
   ## y \sim x1 + x2 + I(x1 * x2) + I(x1^2) + I(x1^2 * x2^2)
   ##
   ##
                       Df Deviance
                      1 103.83 129.17
   ## - I(x1^2)
   ## - I(x1 * x2) 1 103.84 129.19
```

```
## - I(x1^2 * x2^2) 1 105.71 131.05
## <none>
                       102.68 133.10
## - x2
                  1 107.94 133.28
## - x1
                  1 109.50 134.84
##
## Step: AIC=129.17
## y \sim x1 + x2 + I(x1 * x2) + I(x1^2 * x2^2)
##
                  Df Deviance
                               AIC
## - I(x1 * x2)
                  1 104.74 125.02
## - I(x1^2 * x2^2) 1 105.75 126.03
## <none>
                       103.83 129.17
                  1 109.97 130.24
## - x1
## - x2
                  1 111.00 131.28
##
## Step: AIC=125.02
## y ^{\sim} x1 + x2 + I(x1^{\circ}2 * x2^{\circ}2)
##
##
                 Df Deviance
## - I(x1^2 * x2^2) 1 105.80 121.00
## <none>
                       104.74 125.02
## - x1
                  1 109.97 125.18
## - x2
                  1 111.40 126.61
##
## Step: AIC=121
## y \sim x1 + x2
##
##
       Df Deviance AIC
## <none> 105.80 121.00
## - x1 1 113.20 123.33
## - x2 1 116.27 126.41
##
## Call: glm(formula = y ~ x1 + x2, family = binomial, data = dat.new)
##
## Coefficients:
## (Intercept)
                      x1
##
   -2.29705
                 0.07787
                            -0.09547
##
## Degrees of Freedom: 158 Total (i.e. Null); 156 Residual
## Null Deviance:
                   134.9
## Residual Deviance: 105.8 AIC: 111.8
```

The best model according to the SBCp criterion is based on y x1 + x2. SBC = 121.

```
dat = read.table("CH14PR11.txt")
 names(dat) = c("X", "n", "Y")
 logit = glm(Y/n ~ X, data = dat, family = "binomial")
## Warning: non-integer #successes in a binomial glm!
 0j1 = dat\$Y
 Ej1 = round(dat$n*fitted(logit), 1)
 0j0 = dat n - dat Y
 Ej0 = dat n-Ej1
 rbind(0j1, 0j0)
##
       [,1] [,2] [,3] [,4] [,5] [,6]
## Oj1 72 103 170 296 406 449
## Oj0 428 397 330 204
 rbind(Ej1, Ej0)
        1 2 3 4 5 6
## Ej1 70.6 99.1 163.9 327.4 394.6 440.3
## Ej0 429.4 400.9 336.1 172.6 105.4 59.7
 X.squ = sum((rbind(0j1, 0j0)-rbind(Ej1, Ej0))^2/rbind(Ej1, Ej0)); X.squ
## [1] 12.28748
```

$$H_0:E(Y) = [1 + exp(-\beta_0 - \beta_1 X1)]^{-1}$$
VS. $H_1:E(Y) \neq [1 + exp(-\beta_0 - \beta_1 X1)]^{-1}$

$$X^2 = \sum_j \sum_k \frac{(O_{jk} - E_{jk})^2}{E_{jk}} = 12.287$$
we can reject H_0 if $X^2 > \chi^2(0.99, 3) = 13.2767$, otherwise reject H_1 so that reject H_1 because $X^2 < 13.2767$,

$$\frac{exp(\beta_0 + \beta_1 Xi)}{1 + exp(\beta_0 + \beta_1 Xi)} = \frac{1}{\frac{1}{exp(\beta_0 + \beta_1 Xi)} + 1}$$
$$= \frac{1}{exp(0 - \beta_0 - \beta_1 Xi) + 1}$$
$$= [1 + exp(-\beta_0 - \beta_1 Xi)]^{-1}$$

$$\begin{split} lng(Y_1,...,Y_n) &= ln \prod_i \binom{n_i}{Y_i} \pi_i^{Y_i} (1-\pi_i)^{n_i-Y_I} \\ &= \sum_i [ln \binom{n_i}{Y_i} + Y_i ln(\pi_i) + (n_j - Y_j) ln(1-\pi_i)] \\ &= \sum_i [ln \binom{n_i}{Y_i} + Y_i ln(\pi_i/(1-\pi_i)) + (n_j) ln(1-\pi_i)] \\ &= \sum_i [ln \binom{n_i}{Y_i} + Y_i ln(\beta_0 + \beta_1 X_i)) - (n_j) ln(1 + exp(-\beta_0 - \beta_1 X_i))] \end{split}$$

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$$\pi_{i} = \frac{exp(\pi_{i}^{'})}{1 + exp(\pi_{i}^{'})}$$

$$1 - \pi_{i} = \frac{1}{1 + exp(\pi_{i}^{'})}$$

$$\frac{\pi_{i}}{1 - \pi_{i}} = exp(\pi_{i}^{'})$$

$$F_{L}^{-1}(\pi_{i}) = \pi_{i}^{'} = log_{e}(\frac{\pi_{i}}{1 - \pi_{i}})$$

$$\begin{split} \ln L(\beta_0,\beta_1) &= \sum_{i=1}^n y_i (\beta_0 + \beta_1 X_i) - \sum_{i=1}^n (1 + \exp(\beta_0 + \beta_1 X_i)) \\ \frac{\partial^2 lnL}{\partial \beta_0^2} &= -\sum_{i=1}^n \frac{\exp(\beta_0 + \beta_1 X_i)}{[1 + \exp(\beta_0 + \beta_1 X_i)]^2} \\ \frac{\partial^2 lnL}{\partial \beta_1^2} &= -\sum_{i=1}^n \frac{X_i^2 \exp(\beta_0 + \beta_1 X_i)}{[1 + \exp(\beta_0 + \beta_1 X_i)]^2} \\ \frac{\partial^2 lnL}{\partial \beta_0 \partial \beta_1} &= -\sum_{i=1}^n \frac{X_i \exp(\beta_0 + \beta_1 X_i)}{[1 + \exp(\beta_0 + \beta_1 X_i)]^2} \\ -E\{\frac{\partial^2 lnL}{\partial \beta_0^2}\} &= -g_{00} \\ -E\{\frac{\partial^2 lnL}{\partial \beta_1^2}\} &= -g_{11} \\ -E\{\frac{\partial^2 lnL}{\partial \beta_0 \partial \beta_1}\} &= -g_{01} = -g_{10}, \text{which is reduced to (14.51)} \end{split}$$