



# Introduction to Data Science and Analytics

## Levels of Measurement



# Varieties of Data and Measurements

- Type of measurement determines the statistical techniques that are applicable
- For instance:
  - Which types of measurements are suitable in a regression analysis
    - for the independent / predictor variables?
    - for the dependent / predicted variables?
  - What about data used in classification?

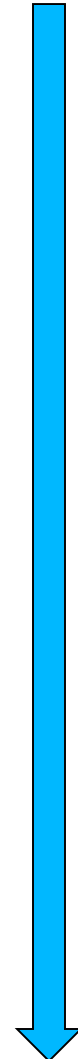


# Varieties of Data and Measurements

- Nominal measurements
  - Classes or factors of a data set
- Ordinal measurements
  - Ordered or ranked measures of a data set
- Interval measurements
  - Difference measured from end points
- Ratio measurements
  - Continuous magnitude compared to a unit magnitude

Low  
Precision

High  
Precision



# Varieties of Data and Measurements

- Levels of measurements – lowest precision
  - Example: Temperature
    - When you walked into work, was the temperature:
      - Cold ?
      - Cool ?
      - Warm ?
      - Hot ?
- These are *Nominal* measures



# Varieties of Data and Measurements

- Levels of measurements – lower but not lowest precision
- Example: Temperature
  - When you walked into work, was the temperature:
    - Coldest day of the year?
    - Hottest day of the year?
    - 5<sup>th</sup> coldest day of the year?

These are *Ordinal* measures

# Varieties of Data and Measurements

- Levels of measurements – better but not best precision
- Example: Temperature
  - When you walked into work, was the temperature:
    - 20° F ?
    - 35° F ?
    - 99° F ?

These are *Interval* measures

(e.g. relative to 0°F end point)

# Varieties of Data and Measurements

- Levels of measurements – better but not best precision
- Example: Temperature
  - Is  $98^{\circ}\text{F}$  twice (2X) as hot as  $49^{\circ}\text{F}$  degrees?
  - If you say yes ....
    - Then what is twice cold as  $32^{\circ}\text{F}$  ?
    - Where does  $0^{\circ}\text{F}$  fit in ?  $-10^{\circ}\text{F}$  &  $-20^{\circ}\text{F}$ ?

There is a lack of precision in the  $^{\circ}\text{F}$  measurement is because the  $0^{\circ}$  reference point is arbitrary



# Varieties of Data and Measurements

- Central tendency (e.g. mean) and dispersion (e.g. standard deviation) are descriptive statistics
- How central tendency is measured varies per the measurement level



# Central Tendencies

- Nominal
  - The most common value, i.e., mode
- Ordinal
  - The middle rank, i.e., median
  - Other percentile/quantile
  - Also mode



# Central Tendencies

- Interval
  - Arithmetic mean, i.e., average
  - Also mode, median, and percentile/quantile
- Ratio
  - Mode, median, percentile/quantile, and arithmetic mean
  - Additional measures: geometric and harmonic means

# Continuous vs. Discrete Variables

- Nominal and ordinal are discrete
  - Values come from a *limited set of values*
- Interval and ratio are continuous
  - Values have *infinite possible values*
- These variable types define suitable models for inferential statistics
  - Example : Regression vs. Classification

# Inferring Continuous Variables

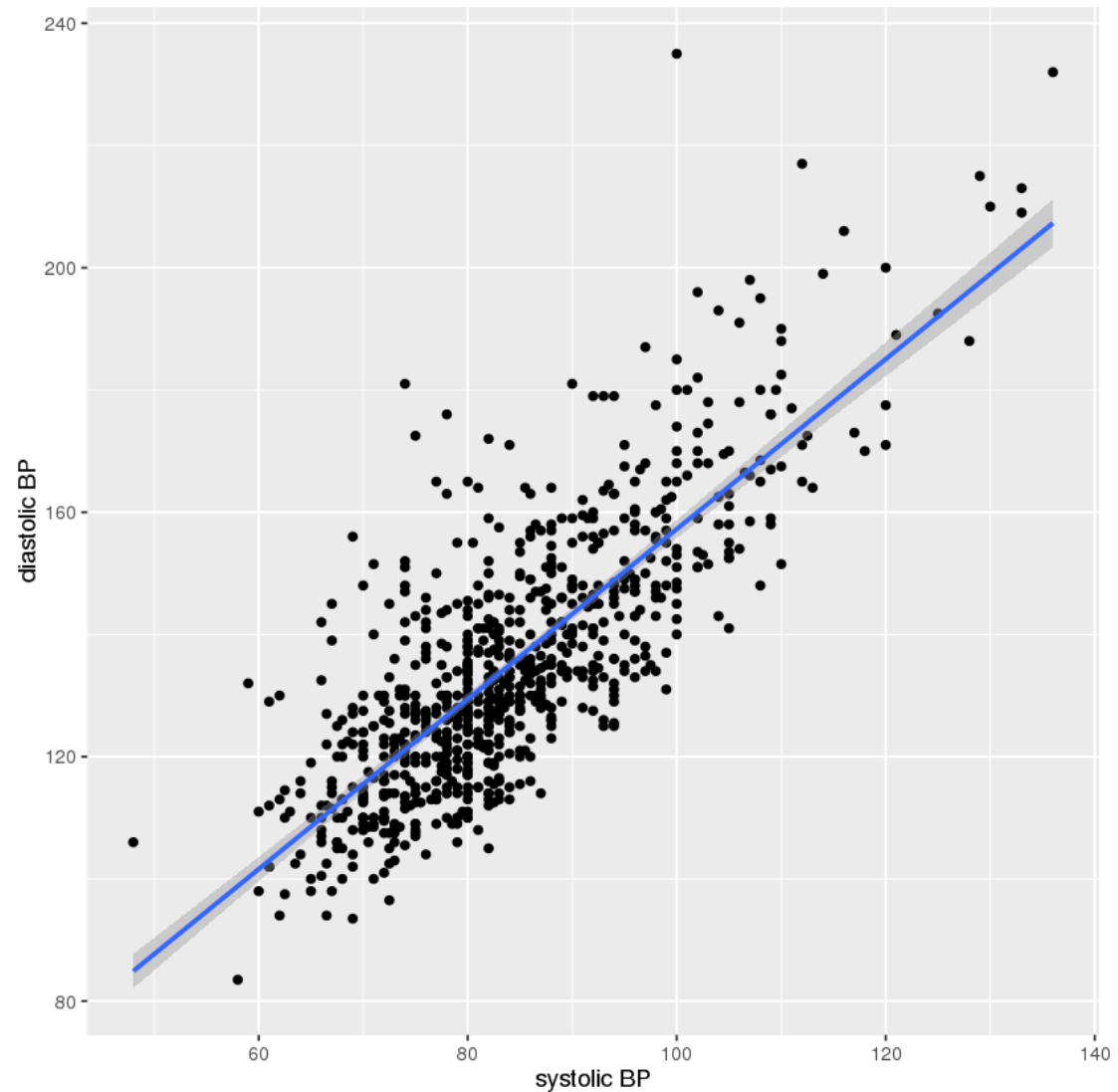
- Interval and ratio measurements are typically predicted through inferential statistics using a form of *regression analysis*
- A formula of independent (predictor) variables (x-axis) and model coefficients compute a dependent (predicted) value (y-axis)

# Inferring Continuous Variables

Regression Plot  
Example

Understanding  
Variable  
Relationships

Example: Blood  
Pressure  
Measurements



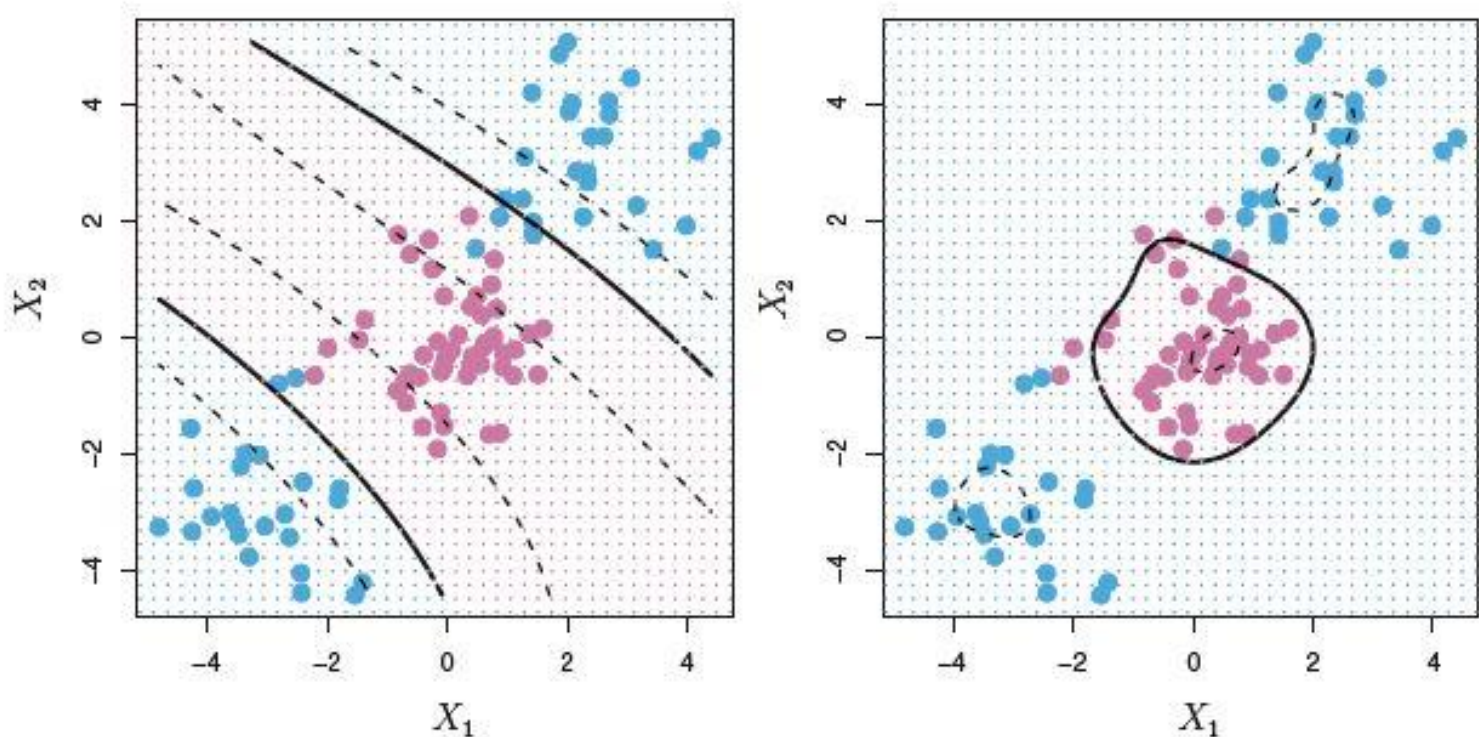
# Inferring Discrete Variables

- Nominal measurements are typically predicted through inferential statistics using *classification techniques* (e.g. neural networks)
- A formula of independent (predictor) variables and model coefficients determine a dependent (predicted) value based on decision planes derived from statistical models

# Inferring Nominal Variables

There are numerous ways to predict nominal values given input measurements

Classification examples from 2D scatter plot with decision boundaries



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