

Complete each of the problems below for both of the following affine semigroups:

$$S = \mathbb{N}\{2, 3\}$$

$$S = \mathbb{N}^2\{(4, 0), (3, 1), (1, 3), (0, 4)\}$$

(1) Compute the saturation \overline{S} of S .

(2) Describe $\text{Spec } S$ geometrically: What dimension is it? Can you embed it in an affine space?

(3) Describe $\text{Spec } \overline{S}$. [hint: Look back at a previous worksheet and at textbook examples 1.1.6 and 1.1.22.]

(4) Define a map $\text{Spec } \overline{S} \rightarrow \text{Spec } S$.