Partial-Autocorrelation-and-the-PACF-First-Examples

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2020年5月19日 星期 Objectives
                       After this lecture, you will be able to
                       Use the acf() function to obtain a Partial
                     Autocorrelation Coefficient plot(PACF)
                        Use the PACF to determine the likely order of an
                         AR(p) process
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                       ▶ Use the ar() function to estimate coefficients in an
db3af01...
                         AR(p) process
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Thistleton and Sadigov Partial Autocorrelation and the PACF Week 3

The Partial Autocorrelation Function

Let's suppose you have time series data in front of you, and you have plotted the series as well as the time series data alone just what the generating process is.

plotted the ACF. Unless you have created the data yourself, say with arima.sim(), or if you have & obvious how woold it. good knowledge of the physical process that generated your time series, it's not easy to tell from we det the physical process that generated your time series, it's not easy to tell from Now the ACF is one of our primary tools for characterizing an autoregressive or moving average

process. We've already seen how to find the ACF as a formula for MA(q) and AR(p) processes and learned to predict the characteristic shapes which occur in the ACF for these simple processes. First, the "good news":

A moving average process of order q has an ACF that cuts off after q lags. So, if you have an MA() process with enough terms that you believe the ACF is well estimated,

and the ACF cuts off after 4 lags, you can be reasonably sure you have an MA(4) process.

How about an AR(p) process? That is, if you know you have an AR(p) process, can you tell what

the *order* of the process is? It would be terrific if we had a plot that would function for an AR(p)

More "good news"! As we develop in this lecture, the Partial Autocorrelation Function, or PACF

Generating Data and Observing the Partial Autocorrelation Function

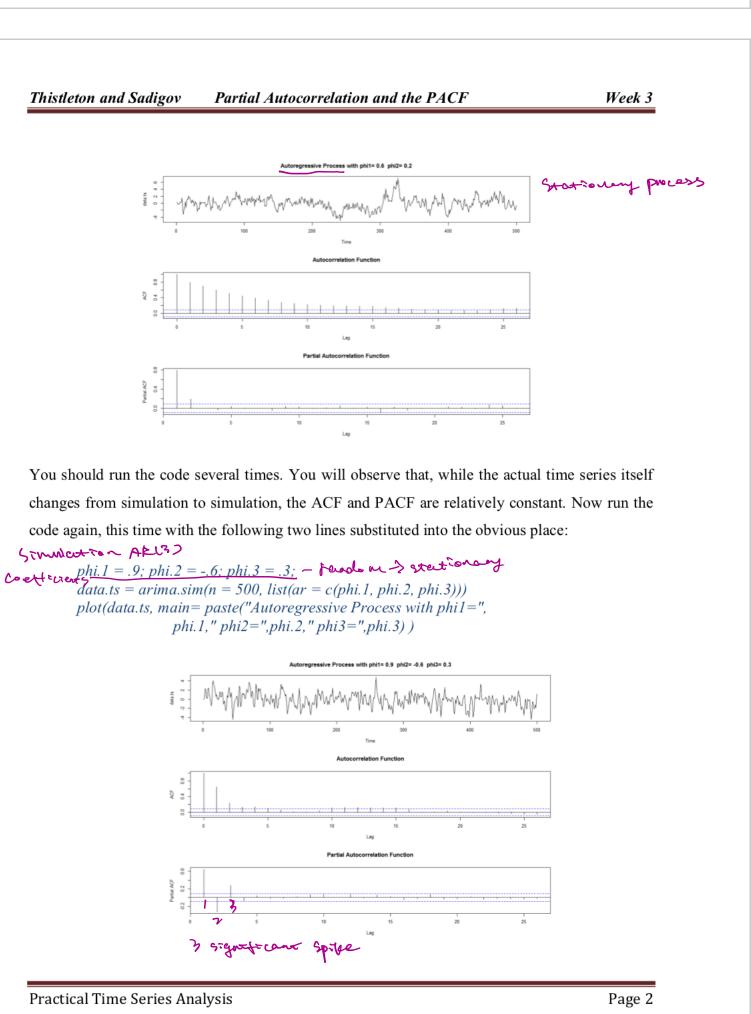
process the way the ACF does for the MA(q) process.

will help us to find the order of an AR(p) process. We will develop this graph in the lecture below. First, let's create some data and look at some pictures. (ARLO) PICCESS Simulation ARC>) Xt= Zt+ & Xt-1+ -- + Pp Xt-p

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generate data rm( list=ls(all = TRUE))
 Phi. 1 = .6; phi. 2 = .2; data.ts = arima.sim(n = 500, list(ar = c(phi.1, phi.2)))
                          paste("Autoregressive Process with phi1=",phi.1," phi2=",phi.2))
                   acf(data.ts, main="Autocorrelation Function")
                   acf(data.ts, type="partial", main="Partial Autocorrelation Function")
```

Practical Time Series Analysis

Page 1



Thistleton and Sadigov

beveridge

Week 3

in your simulations. Do you have any conjectures?

Partial Autocorrelation and the PACF

You can continue to play with the code, changing the number of terms and the coefficients used

Here is a classic data set in Time Series Analysis, the good old Beveridge Wheat Price Index. You can get the numbers at the Time Series Data Library...just visit the website: http://datamarket.com/data/list/?q=provider:tsdl

The data set originally appeared in a paper called "Weather and Harvest Cycles" (Beveridge, 1921)

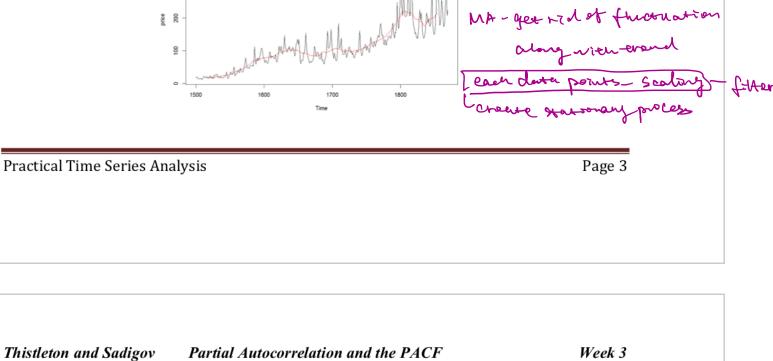
and has also been discussed in subsequent papers critiquing the original analysis, for example

(Sargan, 1953) and (Granger & Hughes, 1971). While we note that there are issues with Beveridge's analysis, we present the data as a nice illustration of the topic at hand.

Partial Autocorrelation Function and the Beveridge Wheat Price Data Set

Can you follow along on this code? I have downloaded the data into a text file, removing some header information. Next, I create a time series with the data in the second column (the actual prices, starting in the year 1500) and create a "filter" with the simple moving average that uses 15 data points on either side of a given year to introduce some smoothing. We plot the original series and the smoothed series on the same axes.

ente t.S. entrour Sur Col. = ts(beveridge[,2]) start=1500) your or your low plot(beveridge.ts, ylab="price", main="Beveridge Wheat Price Data") beveridge.MA = filter(beveridge.ts, rep(1/31, 31), sides = 2)lines(beveridge.MA, col="red")



scale at each data point by ma process

Some dawa - beginning & end - & represented in Y - NA

main="Autocorrelation Function of Transformed Beveridge Data") acf(na.omit(Y), type="partial",main="Partial Autocorrelation Function of Transformed Beveridge Data") - Prec

plot(Y, ylab="scaled price", main="Transformed Beveridge Wheat Price Data")

acf(na.omit(Y), get rid et clara points x meaningful

Now Beveridge transformed his data by scaling each data point by its corresponding smoothed

value. I've done this with the following lines, and plotted the usual graphs.

par(mfrow=c(3,1))

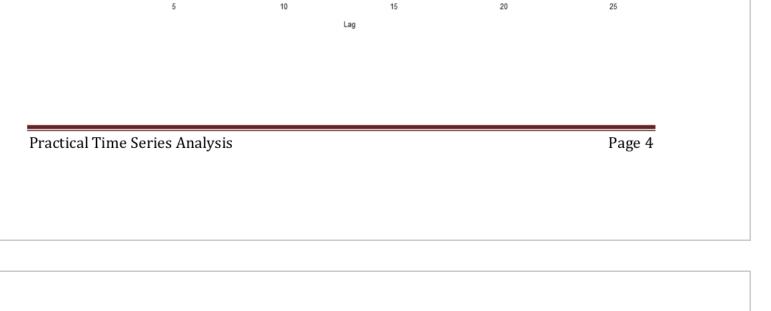
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Y = beveridge.ts/beveridge.MA

The acf() function doesn't like missing data, so the first and last 15 numbers are ignored or omitted with the clean-up function *na.omit()*. What do you notice about the Partial Autocorrelation function?

Partial Autocorrelation Function of Transformed Beveridge Data

Transformed Beveridge Wheat Price Data **Autocorrelation Function of Transformed Beveridge Data**



We will use the routine ar() to estimate the coefficients of our model. In other lectures we describe how to do this; for now, just think of this as similar to a call to lm() when we are doing a regression curve fitting. We believe we have a model $X_t = Z_t + \phi_1 X_{t-1} + \dots + \phi_n X_{t-n}$ AR(p) process:

We let the ar() function find the coefficients for us. We discuss selecting a model using quality

criteria such as the Akaike Information Criterion (AIC) in other lectures. As R will tell you, the

ar() routine will "Fit an autoregressive time series model to the data, by default selecting the

Partial Autocorrelation and the PACF

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complexity by AIC." By complexity we mean how many terms to take, or what the value of p is.
If we will allow up to 5 terms in our model (a reasonable number) we call
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openewate coefficients in the process $\frac{ar(na.omit(Y), order.max = 5)}{Ur \text{ free look for cychousiz process param up to 5}}$ And obtain a second order model Coefficients:

2 0.7239 -0.2957sigma² estimated as 0.02692 = PACF plan

That's handy! Now that we know one of the ways we use a PACF, let's discuss the intuition behind the PACF

An autoregressive process of order p, an AR(p), has a PACF that cuts off after p lags.

and how to calculate it for a stochastic process and how to estimate it for some given time series

data.

Just to state the obvious at this point:

Week 3