

W6.SES Forecast

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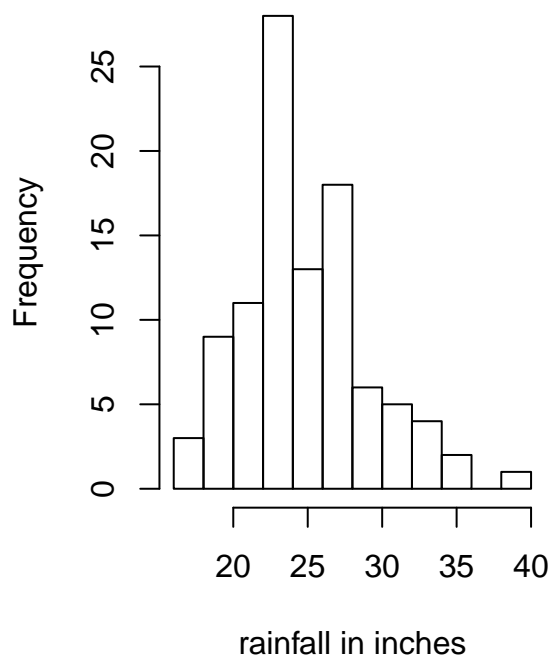
5/28/2020

Dataset source:<https://robjhyndman.com> Dataset description:<https://pkg.robjhyndman.com/fma/reference/index.html> Simple Exponential Smoothing -dataset:total annual rainfall recorded-during the years 1813-1912-in inches-for London,England -scan:go to website-grab data-store in array

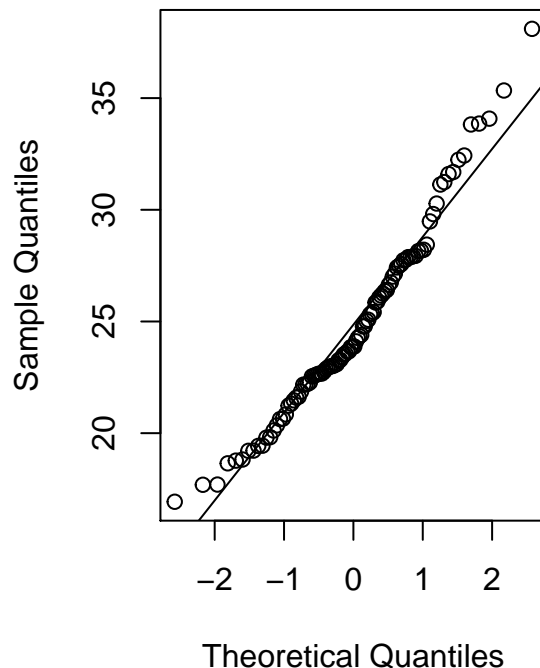
```
rm(list = ls(all=TRUE))
rain.data=scan('https://robjhyndman.com/tsdldata/hurst/precip1.dat',skip = 1)
rain.ts=ts(rain.data,start = c(1813))
#rain.ts

#plot-summarize data nature
par(mfrow=c(1,2))
hist(rain.data,main = 'Annual London Rainfall 1813-1912',xlab = 'rainfall in inches')
#histogram:mound shaped-not quite symmetrical
qqnorm(rain.data,main='Normal Plot of London Rainfall')
qqline(rain.data)
```

Annual London Rainfall 1813-19



Normal Plot of London Rainfall



```
#normal distributed test
#skew-not quite normal-systematic departure from normality
```

```

#close-not extreme

#plot-data, ACF
par(mfrow=c(2,1))
plot.ts(rain.ts,main='Annual London Rainfall 1813-1912',
        xlab='year',ylab='rainfall in inches')
acf(rain.ts,main='ACF:London Rainfall')
#time series->sequence-see ACF
#dataset-noise-no structure
#autocorrelations week-cannot fit obvious model

library(forecast)

```

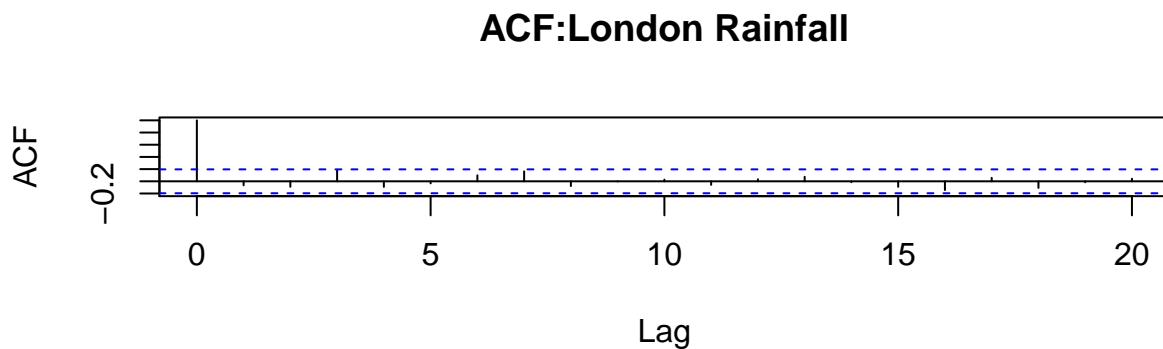
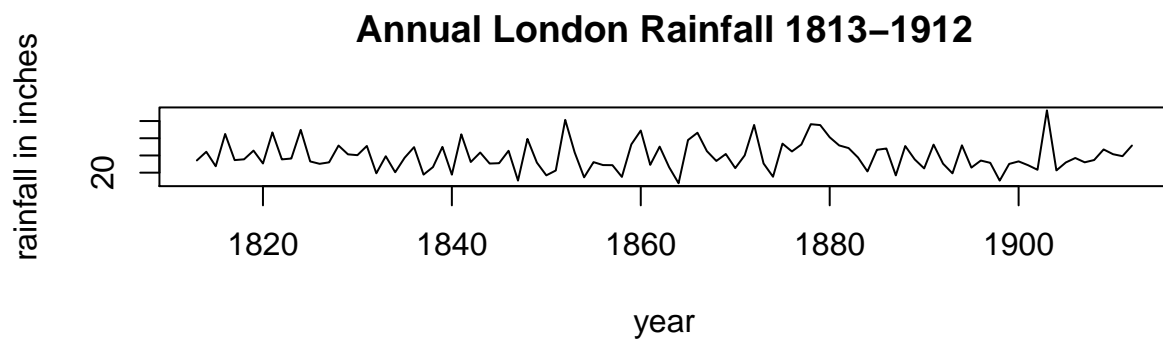
```

## Registered S3 method overwritten by 'xts':
##   method      from
##   as.zoo.xts zoo

## Registered S3 method overwritten by 'quantmod':
##   method      from
##   as.zoo.data.frame zoo

## Registered S3 methods overwritten by 'forecast':
##   method      from
##   fitted.fracdiff fracdiff
##   residuals.fracdiff fracdiff

```



```
auto.arima(rain.ts)
```

```
## Series: rain.ts
## ARIMA(0,0,0) with non-zero mean
##
## Coefficients:
##          mean
##       24.8239
## s.e.    0.4193
##
## sigma^2 estimated as 17.76:  log likelihood=-285.25
## AIC=574.49   AICc=574.61   BIC=579.7
```

```
# no fit model-no coef
```

Forecast Naive method -data:previous year's=current year's-last few year's annual rainfall -forecast-predict future value:current time n_{th} -h lags away-future time: $n+h$ - $x_{n,n+h}$ - $x_{n,n+1}=x_n$

seasonal naive method -seasonality-predict future value-value previous season -n predict next period $n+1$ -1 season ago-week: $s=7$ - $x_{n,n+1}=x_{n+1-s}$

Average method-Simple Moving Average -average all past values, weighted equally-predict future value

```
mean(rain.ts)
```

```
## [1] 24.8239
```

```
#forecast:rainfall in 1913
```

Simple Exponential Smoothing(SES) greater weight->closer values-decaying sequence of weights-lesser weight to further past -geometric series-decrease at a constant ratio - $x_{n,n+1}=\alpha x_n+(1-\alpha)x_{n-1}$ - $\alpha=1$:naive forecast - $\alpha>1$:series decay rapidly, emphasis on 'near' observations - $\alpha>0$:series decay slowly, emphasis on further past points

```
alpha=0.2 #increase alpha-more rapid decay
forecast.values=NULL #establish array-forecast values

n=length(rain.data)

#naive first forecast
forecast.values[1]=rain.data[1]

#loop to creat all forecast values
for (i in 1:n) {
  forecast.values[i+1]=alpha*rain.data[i]+(1-alpha)*forecast.values[i]
}
paste('forecast for time',n+1,'=',forecast.values[n+1])
```

```
## [1] "forecast for time 101 = 25.3094062064236"
```

Moving Towards a Least Squares Approach-find level:alpha

```

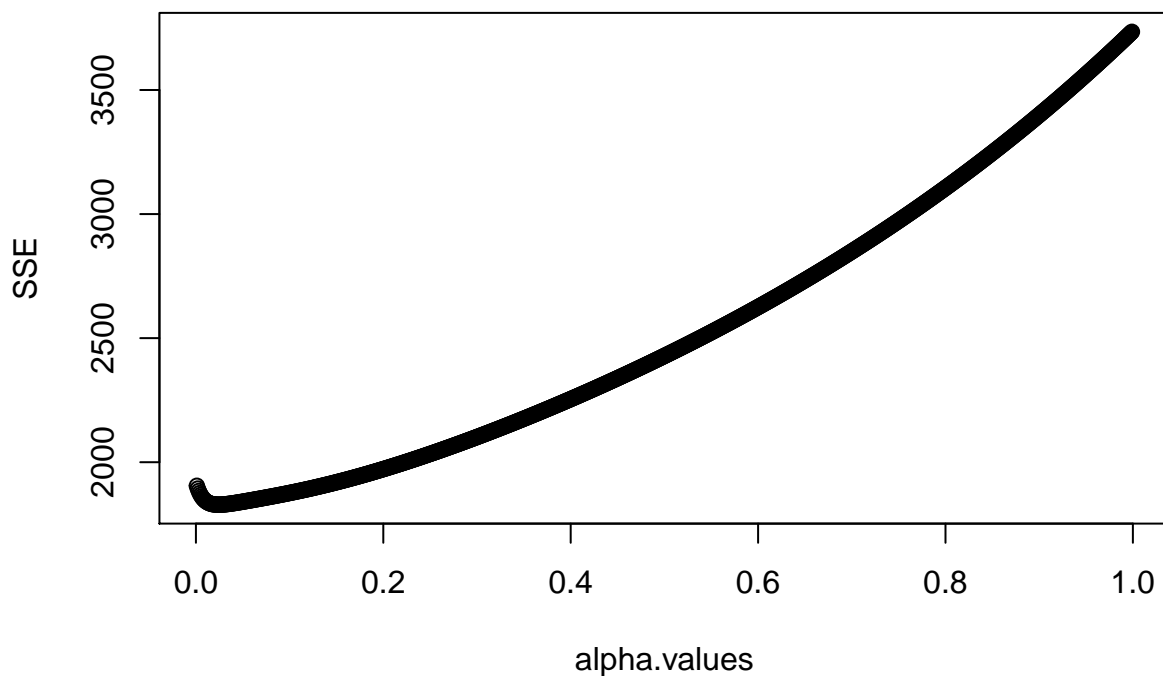
SSE= NULL
alpha.values=seq(0.001,0.999,by=0.001)
number.alphas=length(alpha.values)

for (k in 1:number.alphas) {
  forecast.values=NULL
  forecast.values[1]=rain.data[1]
  n=length(rain.data)
  alpha=alpha.values[k]

  for (i in 1:n) {
    forecast.values[i+1]=alpha*rain.data[i]+(1-alpha)*forecast.values[i]
  }
  SSE[k]=sum((rain.data-forecast.values[1:n])^2)
}
plot(SSE~alpha.values,main='Optimal alpha value Minimize SSE')

```

Optimal alpha value Minimize SSE



```

#retrieve SSE position, alpha
index.of.smallest.SSE=which.min(SSE)
index.of.smallest.SSE #return position 24

```

```
## [1] 24
```

```
alpha.values[which.min(SSE)] #return alpha=0.024
```

```
## [1] 0.024
```

```
alpha=0.024
forecast.values=NULL
forecast.values[1]=rain.data[1]
n=length(rain.data)

for (i in 1:n) {
  forecast.values[i+1]=alpha*rain.data[i]+(1-alpha)*forecast.values[i]
}
paste('forecast at time:',n+1,'=',forecast.values[n+1])
```

```
## [1] "forecast at time: 101 = 24.6771392918524"
```

```
# HoltWinters for SES-turn off seasonal,trend effects
HoltWinters(rain.ts,beta = FALSE, gamma = FALSE)
```

```
## Holt-Winters exponential smoothing without trend and without seasonal component.
##
## Call:
## HoltWinters(x = rain.ts, beta = FALSE, gamma = FALSE)
##
## Smoothing parameters:
##   alpha: 0.02412151
##   beta : FALSE
##   gamma: FALSE
##
## Coefficients:
##           [,1]
## a 24.67819
```

Holt-Winters for level,Trend-alpha,beta -ACF:slow decay, PACF:cut off sharply-accommodate trend -non-seasonal data-level,trend -SES:forecast value at step,n+1-smoothed value at step n

```
#set up transformed data,smoothing parameters
data=rain.data
N=length(data)
alpha=0.7
beta=0.5

#prepare empty array-store values
forecast=NULL
level=NULL
trend=NULL

#initialize level,trend in a very simple way
level[1]=data[1]
trend[1]=data[2]-data[1]

#initialize forecast to get started
forecast[1]=data[1]
```

```

forecast[2]=data[2]

#loop to build forecast
for (n in 2:N) {
  level[n]=alpha*data[n]+(1-alpha)*(level[n-1]+trend[n-1])
  trend[n]=beta*(level[n]-level[n-1])+(1-beta)*trend[n-1]
  forecast[n+1]=level[n]+trend[n]
}

#display calculated forecast value
forecast[3:N]

```

```

## [1] 28.58000 24.03400 31.75830 25.92469 23.61996 25.67606 22.62277
## [8] 31.19431 25.71777 23.68708 31.96190 24.97968 21.55863 21.33779
## [15] 26.97731 26.29711 25.49906 27.92697 20.25991 23.01382 19.56516
## [22] 23.15575 27.88142 20.75862 20.45976 26.93269 20.60663 30.58199
## [29] 25.32440 25.86308 22.66011 21.80068 25.66561 17.97513 28.28719
## [36] 24.68979 19.09914 18.94475 34.93377 29.95016 19.43202 20.63337
## [43] 20.95060 21.45506 18.27962 27.41063 34.66121 25.52046 27.20557
## [50] 21.55966 14.98350 26.86943 33.57491 29.27783 23.93647 24.26730
## [57] 20.46499 23.50855 34.23263 25.56993 17.91365 26.03498 26.91914
## [64] 29.02919 35.56699 36.73488 32.34804 27.83017 25.68725 22.67584
## [71] 18.12337 24.14145 27.20987 19.87044 26.39396 24.73763 21.17906
## [78] 27.39532 23.70733 19.26637 26.66785 22.54005 23.07969 22.70269
## [85] 17.21615 20.82853 23.28826 22.85779 21.09142 38.59651 25.35176
## [92] 22.16872 22.84875 22.23420 23.01436 26.71189 26.37498 25.32017

```

```

#verify with HoltWinters() output
par(mfrow=c(2,1))
m=HoltWinters(data,alpha=0.7,beta=0.5,gamma=FALSE)
m$fitted[,1]

```

```

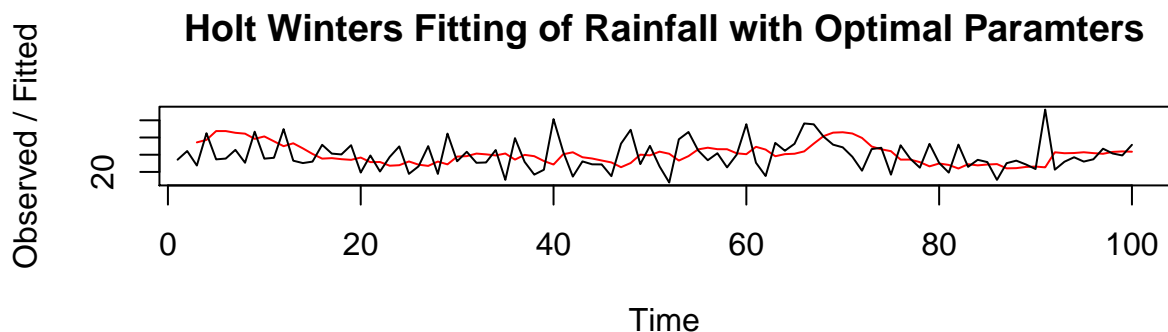
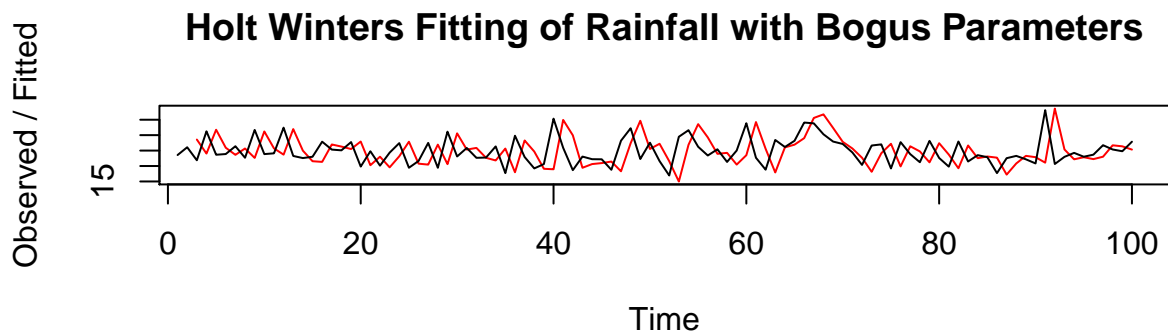
## Time Series:
## Start = 3
## End = 100
## Frequency = 1
## [1] 28.58000 24.03400 31.75830 25.92469 23.61996 25.67606 22.62277
## [8] 31.19431 25.71777 23.68708 31.96190 24.97968 21.55863 21.33779
## [15] 26.97731 26.29711 25.49906 27.92697 20.25991 23.01382 19.56516
## [22] 23.15575 27.88142 20.75862 20.45976 26.93269 20.60663 30.58199
## [29] 25.32440 25.86308 22.66011 21.80068 25.66561 17.97513 28.28719
## [36] 24.68979 19.09914 18.94475 34.93377 29.95016 19.43202 20.63337
## [43] 20.95060 21.45506 18.27962 27.41063 34.66121 25.52046 27.20557
## [50] 21.55966 14.98350 26.86943 33.57491 29.27783 23.93647 24.26730
## [57] 20.46499 23.50855 34.23263 25.56993 17.91365 26.03498 26.91914
## [64] 29.02919 35.56699 36.73488 32.34804 27.83017 25.68725 22.67584
## [71] 18.12337 24.14145 27.20987 19.87044 26.39396 24.73763 21.17906
## [78] 27.39532 23.70733 19.26637 26.66785 22.54005 23.07969 22.70269
## [85] 17.21615 20.82853 23.28826 22.85779 21.09142 38.59651 25.35176
## [92] 22.16872 22.84875 22.23420 23.01436 26.71189 26.37498 25.32017

```

```
plot(m,main = 'Holt Winters Fitting of Rainfall with Bogus Parameters')
m2=HoltWinters(data,gamma = FALSE)
m2
```

```
## Holt-Winters exponential smoothing with trend and without seasonal component.
##
## Call:
## HoltWinters(x = data, gamma = FALSE)
##
## Smoothing parameters:
##  alpha: 0.1973985
##  beta : 0.3469287
##  gamma: FALSE
##
## Coefficients:
##      [,1]
## a 26.2701189
## b  0.2851515
```

```
plot(m2,main = 'Holt Winters Fitting of Rainfall with Optimal Paramters')
```



Airline Dataset -Monthly Airline Passenger Number 1949-1960

```
#AirPassengers
```

```

par(mfrow=c(2,1))
plot.ts(AirPassengers,main='Number of Monlthly Air Passengers(in thousand)')
#strong seasonality-12 month
#strong trend-go up
#increasing variability in later years

#tranform-log10-stablize variation
log10(AirPassengers)

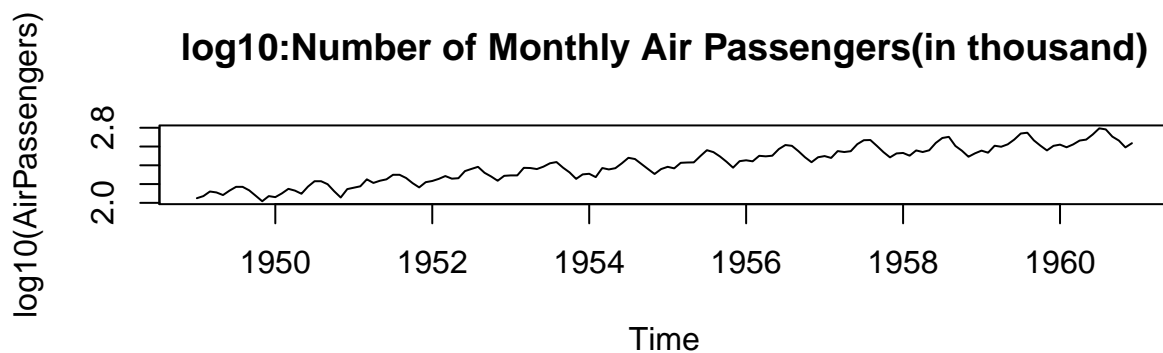
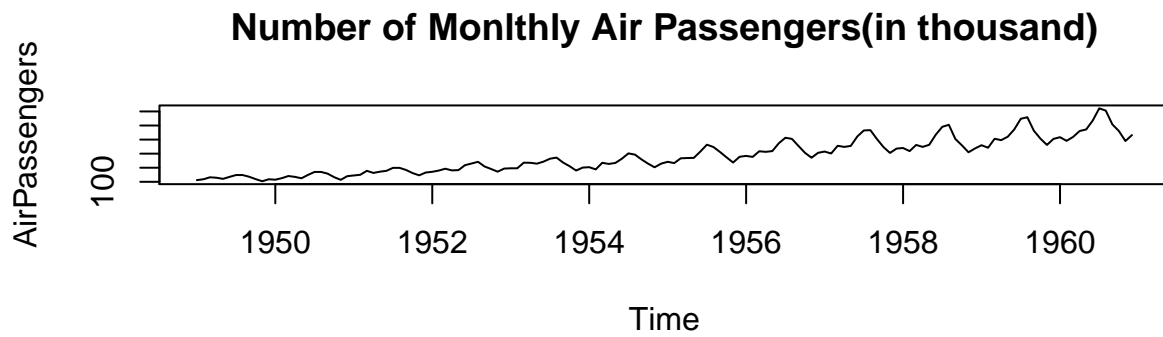
```

##	Jan	Feb	Mar	Apr	May	Jun	Jul
## 1949	2.049218	2.071882	2.120574	2.110590	2.082785	2.130334	2.170262
## 1950	2.060698	2.100371	2.149219	2.130334	2.096910	2.173186	2.230449
## 1951	2.161368	2.176091	2.250420	2.212188	2.235528	2.250420	2.298853
## 1952	2.232996	2.255273	2.285557	2.257679	2.262451	2.338456	2.361728
## 1953	2.292256	2.292256	2.372912	2.371068	2.359835	2.385606	2.421604
## 1954	2.309630	2.274158	2.371068	2.356026	2.369216	2.421604	2.480007
## 1955	2.383815	2.367356	2.426511	2.429752	2.431364	2.498311	2.561101
## 1956	2.453318	2.442480	2.501059	2.495544	2.502427	2.572872	2.615950
## 1957	2.498311	2.478566	2.551450	2.541579	2.550228	2.625312	2.667453
## 1958	2.531479	2.502427	2.558709	2.541579	2.559907	2.638489	2.691081
## 1959	2.556303	2.534026	2.608526	2.597695	2.623249	2.673942	2.738781
## 1960	2.620136	2.592177	2.622214	2.663701	2.673942	2.728354	2.793790
##	Aug	Sep	Oct	Nov	Dec		
## 1949	2.170262	2.133539	2.075547	2.017033	2.071882		
## 1950	2.230449	2.198657	2.123852	2.056905	2.146128		
## 1951	2.298853	2.264818	2.209515	2.164353	2.220108		
## 1952	2.383815	2.320146	2.281033	2.235528	2.287802		
## 1953	2.434569	2.374748	2.324282	2.255273	2.303196		
## 1954	2.466868	2.413300	2.359835	2.307496	2.359835		
## 1955	2.540329	2.494155	2.437751	2.374748	2.444045		
## 1956	2.607455	2.550228	2.485721	2.432969	2.485721		
## 1957	2.669317	2.606381	2.540329	2.484300	2.526339		
## 1958	2.703291	2.606381	2.555094	2.491362	2.527630		
## 1959	2.747412	2.665581	2.609594	2.558709	2.607455		
## 1960	2.782473	2.705864	2.663701	2.591065	2.635484		

```

plot(log10(AirPassengers),main='log10:Number of Monthly Air Passengers(in thousand)')

```

Exponential Smoothing with Trend, Seasonality seasonal differences -additive:Jan-add a constant amount-June projection -multiplicative-multiply a constant amount

```
#transform data-SES
```

```
Airpassengers.SES=HoltWinters(x=log10(AirPassengers),beta=FALSE,gamma = FALSE)
```

```
Airpassengers.SES$SSE
```

```
## [1] 0.3065102
```

```
#additive seasonality
```

```
Airpassengers.HW=HoltWinters(log10(AirPassengers))
```

```
Airpassengers.HW$SSE
```

```
## [1] 0.0383026
```

```
#smoothing parameters
```

```
Airpassengers.HW$alpha
```

```
##      alpha
```

```
## 0.326612
```

```
Airpassengers.HW$beta
```

```
##      beta
```

```
## 0.005744246
```

```
Airpassengers.HW$gamma
```

```
##      gamma  
## 0.8207255
```

```
Airpassengers.HW$coefficients
```

```
##           a           b           s1           s2           s3  
## 2.680598830 0.003900787 -0.031790733 -0.061224237 -0.015941495  
##           s4           s5           s6           s7           s8  
## 0.006307818 0.014138008 0.067260071 0.127820295 0.119893006  
##           s9           s10          s11          s12  
## 0.038321663 -0.014181699 -0.085995400 -0.044672707
```

```
rm(list = ls(all=TRUE))  
library('forecast')  
Airpassengers.HW=HoltWinters(log10(AirPassengers))  
AirPassengers.forecast=forecast(Airpassengers.HW)  
plot(AirPassengers.forecast)
```

Forecasts from HoltWinters

