

Secant and False Position Method
Numerical Computation
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Project #3

The Secant Method was used to find a root of an equation by finding a point and determined it if had a root by proximity to the x-axis. The secant method requires two points, which we used from our given interval, $[-7, -5]$ and $[-5, -3]$. The secant method was used to find a root of $f(x)=0$. The false position method also uses two points. The false position differs from the secant in this case with the amount of intervals.

Results: For intervals $[-7, -5]$, using the secant method, the maximum amount of iterations were 5, while the least were 4 using the Absolute relative error. The root came out to be -5.78 as shown in Figure1. With interval $[-5, -3]$, the maximum amount of iterations before finding the root was using the Absolute error, taking 7 iterations, while the shortest was 6, both the absolute relative and true error. The root for the second interval using the secant method was -3.66, as seen in figure 1. For the False Position method there was a slight convergence issues where the repeated error did not stop, until I adjusted the code, if the error calculation kept repeating to break. The iterations are shown in following figures but as seen for intervals $[-7, -5]$, it took 16 iterations for both the absolute error and relative while only 7 for the absolute true error. Also converging to root= -5.759. For interval $[-5, -3]$, there were less iterations but again the absolute error and absolute relative error where the maximum with 9 iterations while the true error gave us the least of 5 iterations, all converges to -3.668. Overall both methods are faster than the bisection method but I had the most complications with the false proposition method.

```
Case 0: Absolute Error
1      -5.737312      0.170092
2      -5.760588      0.023276
3      -5.759122      0.001466
4      -5.759131      0.000009
5      -5.759131      0.000000
Root:  -5.759131
```

```
-----
Case 1: Absolute Relative
1      -5.737312      0.029647
2      -5.760588      0.004041
3      -5.759122      0.000254
4      -5.759131      0.000002
5      -5.759131      0.000000
Root:  -5.759131
```

```
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Case 2: Absolute True Error
1      -5.737312      0.037524
2      -5.760588      0.002522
3      -5.759122      0.000016
4      -5.759131      0.000000
Root:  -5.759131
```

```
-----
Case 0: Absolute Error
1      -1.310773      2.860438
2      -3.623605      2.312832
3      -3.686597      0.062992
4      -3.669105      0.017491
5      -3.668876      0.000230
6      -3.668877      0.000001
7      -3.668877      0.000000
Root:  -3.668877
```

```
-----
Case 1: Absolute Relative
1      -1.310773      2.182252
2      -3.623605      0.638268
3      -3.686597      0.017087
4      -3.669105      0.004767
5      -3.668876      0.000063
6      -3.668877      0.000000
Root:  -3.668877
```

```
-----
Case 2: Absolute True Error
1      -1.310773      3.000171
2      -3.623605      0.079545
3      -3.686597      0.030579
4      -3.669105      0.000397
5      -3.668876      0.000002
6      -3.668877      0.000000
Root:  -3.668877
-----
```

The Following is the same function, Testing with The False Proposition Method, $[-7,-5]$ & $[-5,-3]$

Case 0: Absolute Error

1	-5.162685	1.837315
2	-5.634320	1.365680
3	-5.746782	1.253218
4	-5.758210	1.241790
5	-5.759065	1.240935
6	-5.759126	1.240874
7	-5.759131	1.240869
8	-5.759131	1.240869
9	-5.759131	1.240869
10	-5.759131	1.240869
11	-5.759131	1.240869
12	-5.759131	1.240869
13	-5.759131	1.240869
14	-5.759131	1.240869
15	-5.759131	1.240869
16	-5.759131	1.240869

Root: -5.759131

Case 1: Absolute Relative

1	-5.162685	0.355884
2	-5.634320	0.242386
3	-5.746782	0.218073
4	-5.758210	0.215656
5	-5.759065	0.215475
6	-5.759126	0.215462
7	-5.759131	0.215461
8	-5.759131	0.215461
9	-5.759131	0.215461
10	-5.759131	0.215461
11	-5.759131	0.215461
12	-5.759131	0.215461
13	-5.759131	0.215461
14	-5.759131	0.215461
15	-5.759131	0.215461
16	-5.759131	0.215461

Root: -5.759131

Case 2: Absolute True Error

1	-5.162685	0.799205
2	-5.634320	0.207672
3	-5.746782	0.021298
4	-5.758210	0.001594
5	-5.759065	0.000115
6	-5.759126	0.000008
7	-5.759131	0.000001

Root: -5.759131

Case 0: Absolute Error

1	-4.253147	2.424359
2	-3.744706	1.915917
3	-3.665346	0.079359
4	-3.668960	0.003613
5	-3.668877	0.003530
6	-3.668877	0.003530

Case 0: Absolute Error

1	-4.253147	2.424359
2	-3.744706	1.915917
3	-3.665346	0.079359
4	-3.668960	0.003613
5	-3.668877	0.003530
6	-3.668877	0.003530
7	-3.668877	0.003530
8	-3.668877	0.003530
9	-3.668877	0.000000

Root: -3.668877

Case 1: Absolute Relative

1	-4.253147	1.325664
2	-3.744706	1.047643
3	-3.665346	0.021651
4	-3.668960	0.000986
5	-3.668877	0.000963
6	-3.668877	0.000963
7	-3.668877	0.000963
8	-3.668877	0.000963
9	-3.668877	0.000000

Root: -3.668877

Case 2: Absolute True Error

1	-4.253147	0.789223
2	-3.744706	0.128507
3	-3.665346	0.006130
4	-3.668960	0.000144
5	-3.668877	0.000000

Root: -3.668877