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### **Algorithms Lab**

#### **Exercise** – Poker Chips

You regularly meet with your friends on Thursdays for poker night. Three hours into the evening, and slightly drunk already, you get bored of the game and start stacking up the chips in various ways. This gets you thinking. What if you played a solitaire game with the chips?

The rules are as follows. First distribute the chips randomly into several stacks. Then repeat until no chips are left:

- For any subset (of your choosing) of stacks remove the topmost chip from each of its stacks, provided these chips all have the same colour.
- If you removed k > 1 chips, award yourself  $2^{k-2}$  points. If you only removed one chip, 0 points.

Your score is the sum of points gained in each step. The goal, of course, is to score the maximum possible number of points.

On the next morning, sober again, you decide to solve the problem once and for all with a program.

**Input** The first line of the input contains the number  $t \le 60$  of test cases. Each of the t test cases is described as follows.

- It starts with a line that contains one integer n, representing the number of stacks you formed ( $1 \le n \le 5$ ).
- The next line contains n positive integers  $m_1 \ldots m_n$ , separated by a space, such that  $1 \le m_i \le 2000$ , for  $i \in \{1, \ldots n\}$ , and  $\prod_i (m_i + 1) \le 2^{16}$ . Here  $m_i$  denotes the number of chips in the i-th stack.
- The following n lines list the chips in the stacks. The i-th such line contains integers  $c_{i1} \ldots c_{im_i}$ , separated by a space. Each  $c_{ij}$  ( $1 \le c_{ij} \le 2^{10}$ ) represents the colour of one chip.  $c_{im_i}$  is the chip at the top of the stack (removed first) and  $c_{i1}$  is the chip at the bottom (removed last).

**Output** For every test case the corresponding output appears on a separate line. Each output consists of one integer p: the maximum number of points you can score in the game according to the rules above.

**Points** There are three groups of test sets, worth 100 points in total.

- 1. For the first group of test sets, worth 30 points, you may assume that  $n \le 2$ .
- 2. For the second group of test sets, worth 30 points, you may assume that  $m_i \leq 12$  for all  $i \in \{1, ..., n\}$ .

3. For the third test set, worth  $40\ \mathrm{points},$  there are no additional assumptions.

# **Sample Input**

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# Sample Output

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