# University of Toronto Department of Computer & Mathematical Sciences STAB57: an Introduction to Statistics

### Week 7 Assignment

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-email me

-website

-textbook

This week's list of problems is based on the material from: Chapter 6,  $\S 3$ 

You are expected to work on this list of problems prior to the upcoming tutorial.

Problems have the following tags:

 $\stackrel{\circ}{\mathbf{g}}$ : difficult,  $\stackrel{\circ}{\mathbf{g}}$ : Book exercise,  $\Theta$ : extra exercise

#### Terminology and Concepts to learn:

- confidence intervals
- likelihood intervals
- t-statistic
- z- and t-confidence intervals
- hypothesis testing
- p-values

#### Problem 1 🖹

Practice your skills on hypothesis testing 6.3.1,2,3,4,6

#### Problem 2 🖹

Go over example 6.3.7 explaining how the central limit theorem can be used to infer a confidence interval for the Bernouilli model. Then do problem 6.3.11 and 6.3.13

## Problem 3 $\S$

Recall the  $\Gamma$ -function from week 3. The t-distribution is defined as follows:

$$f_U(u)\frac{\Gamma(\frac{n+1}{2})}{\sqrt{\pi}\Gamma(\frac{n}{2})}\left(1+\frac{u^2}{n}\right)^{-(n+1)/2}\frac{1}{\sqrt{n}}$$

Give a simple description of this distribution if the parameter is n = 1.

## Problem 4 🖁

Let S be the Poisson-model where  $P_{\lambda} \sim \text{Poisson}(\lambda)$ .

- Write down what a likelihood interval looks like in this case
- $\bullet$  Ue the above to find a 95%-confidence interval