Predicting stock returns using lags with regression models

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Introduction

We have always been wondering how the lagged stock returns explain the real stock return so in this report, supervised machine learning models with Ridge regressions are come up with to make predictions of stock returns using 5 previous-day stock returns. The entire model building process starts with a data overview, and is followed by a simple stock model built with only one stock and finally a general stock model built with several stocks after taking consideration of the fixed effect inside each stock through one-hot encoding. 5-fold cross validation is used for selecting the optimal parameter in the loss function. And this report will be structured by discussing data in the Data section, model in the Model section, results in the Result section, and limitations in the Limitation Section.

Data

The package "rugarch" in R and the data set "dji30ret" are used in this report for analysis, which contains the closing value log returns for the Dow Jones 30 constituents from 1987-03-16 to 2009-02-03. A brief summary of the data set is as follows:

```
##
          AA
                                AXP
                                                       BA
##
    Min.
            :-0.2745595
                          Min.
                                  :-0.3034304
                                                 Min.
                                                         :-0.1938568
    1st Qu.:-0.0114593
                          1st Qu.:-0.0109291
                                                 1st Qu.:-0.0098007
    Median : 0.0000000
                          Median : 0.0000000
                                                 Median: 0.0000000
##
            : 0.0001608
                                  : 0.0001687
##
    Mean
                          Mean
                                                 Mean
                                                         : 0.0003058
##
    3rd Qu.: 0.0116377
                          3rd Qu.: 0.0114812
                                                 3rd Qu.: 0.0105709
##
    Max.
            : 0.2087337
                          Max.
                                  : 0.1712035
                                                 Max.
                                                         : 0.1439727
         BAC
                                 C
                                                      CAT
##
##
            :-0.3420588
                                  :-0.3056056
                                                         :-0.244156
    Min.
                          Min.
                                                 Min.
    1st Qu.:-0.0093365
                                                 1st Qu.:-0.010575
##
                          1st Qu.:-0.0111602
##
    Median: 0.0000000
                          Median: 0.0000000
                                                 Median: 0.000000
##
            : 0.0001149
                          Mean
                                  : 0.0000796
                                                         : 0.000378
##
    3rd Qu.: 0.0100293
                          3rd Qu.: 0.0116803
                                                 3rd Qu.: 0.011141
##
            : 0.2698774
                                  : 0.4572902
                                                         : 0.137371
                                                 Max.
         CVX
                                 DD
                                                      DIS
##
##
            :-0.1812526
                                  :-0.2018984
                                                         :-0.3426451
    Min.
                          Min.
                                                 Min.
    1st Qu.:-0.0082829
##
                          1st Qu.:-0.0093255
                                                 1st Qu.:-0.0102932
##
    Median: 0.0000000
                          Median: 0.0000000
                                                 Median: 0.0000000
##
    Mean
            : 0.0004538
                          Mean
                                  : 0.0001774
                                                 Mean
                                                         : 0.0002886
    3rd Qu.: 0.0095239
                          3rd Qu.: 0.0095836
                                                 3rd Qu.: 0.0105821
##
            : 0.1894765
                                  : 0.1086964
                                                         : 0.1756133
##
    Max.
                          Max.
                                                 Max.
          GE
##
                                 GM
                                                       HD
            :-0.1947441
                                  :-0.3727220
                                                         :-0.3386365
##
    Min.
                          Min.
                                                 Min.
```

```
1st Qu.:-0.0083683
                         1st Qu.:-0.0119502
                                              1st Qu.:-0.0115889
                         {\tt Median} \,:\, 0.0000000
                                              Median : 0.0000000
##
   Median: 0.0000000
   Mean : 0.0002751
                         Mean :-0.0002715
                                              Mean : 0.0006922
   3rd Qu.: 0.0093459
                         3rd Qu.: 0.0115692
                                              3rd Qu.: 0.0127656
##
##
   Max.
          : 0.1275967
                         Max. : 0.3009365
                                              Max. : 0.1315251
        HPQ
                              IBM
                                                  INTC
##
##
   Min.
           :-0.2263815
                                :-0.268161
                                                    :-0.2488610
                         Min.
                                             Min.
##
    1st Qu.:-0.0125577
                         1st Qu.:-0.009243
                                             1st Qu.:-0.0139915
##
   Median : 0.0000000
                         Median: 0.000000
                                             Median: 0.0000000
##
   Mean : 0.0003792
                         Mean : 0.000249
                                             Mean : 0.0005553
    3rd Qu.: 0.0135366
                         3rd Qu.: 0.009469
                                             3rd Qu.: 0.0158734
                                                  : 0.2265276
##
   Max. : 0.1591410
                         Max. : 0.123635
                                             Max.
##
        JNJ
                              JPM
                                                   AIG
          :-0.2043813
                                :-0.3234769
##
   Min.
                                              Min.
                                                     :-0.9362581
    1st Qu.:-0.0078036
                         1st Qu.:-0.0111299
##
                                              1st Qu.:-0.0089217
##
   Median : 0.0000000
                         Median: 0.0000000
                                              Median: 0.0000000
         : 0.0004993
##
                         Mean : 0.0002586
                                                   :-0.0002978
   Mean
                                              Mean
    3rd Qu.: 0.0084695
                         3rd Qu.: 0.0111094
                                              3rd Qu.: 0.0094814
                         Max. : 0.2239172
                                              Max. : 0.3585320
##
         : 0.1153126
   Max.
##
          ΚO
                              MCD
                                                   MMM
##
   Min.
          :-0.2828628
                                :-0.1827990
                                                     :-0.2257926
                         Min.
                                              Min.
    1st Qu.:-0.0080020
                         1st Qu.:-0.0093024
                                              1st Qu.:-0.0074074
   Median : 0.0000000
                         Median : 0.0000000
                                              Median: 0.0000000
##
   Mean : 0.0004333
                         Mean : 0.0004514
                                              Mean : 0.0003322
##
##
    3rd Qu.: 0.0089027
                         3rd Qu.: 0.0099834
                                              3rd Qu.: 0.0082499
##
   Max. : 0.1791113
                         Max.
                              : 0.1030806
                                              Max. : 0.1049975
        MRK
                              MSFT
                                                  PFE
##
##
          :-0.3119154
                                :-0.379490
                                                    :-0.1892420
   Min.
                         Min.
                                             Min.
##
    1st Qu.:-0.0090772
                         1st Qu.:-0.010643
                                             1st Qu.:-0.0096386
   Median: 0.0000000
                         Median: 0.000000
                                             Median: 0.0000000
##
   Mean : 0.0003447
                         Mean : 0.000787
                                             Mean : 0.0003885
                         3rd Qu.: 0.012848
##
    3rd Qu.: 0.0100307
                                             3rd Qu.: 0.0107528
##
   Max.
         : 0.1224923
                         Max. : 0.178465
                                                  : 0.0989399
                                             Max.
         PG
                               Т
                                                   UTX
##
          :-0.3598917
                               :-0.1352280
                                                     :-0.3029024
##
   Min.
                         Min.
                                              Min.
##
    1st Qu.:-0.0074074
                         1st Qu.:-0.0087377
                                              1st Qu.:-0.0083770
   Median: 0.0000000
                         Median: 0.0000000
                                              Median: 0.0000000
   Mean : 0.0004917
                         Mean : 0.0003364
                                              Mean : 0.0004517
##
    3rd Qu.: 0.0085107
                         3rd Qu.: 0.0096619
                                              3rd Qu.: 0.0098064
##
         : 0.1980376
                         Max. : 0.1505242
                                                     : 0.1278841
##
   Max.
                                              Max.
          ٧Z
##
                              WMT
                                                   MOX
                                                     :-0.2676996
##
   Min. :-0.1931448
                         Min.
                                :-0.1249721
                                              Min.
##
   1st Qu.:-0.0087802
                         1st Qu.:-0.0100137
                                              1st Qu.:-0.0078818
##
   Median : 0.0000000
                         Median: 0.0000000
                                              Median: 0.0000000
   Mean
         : 0.0002848
                         Mean : 0.0004985
                                              Mean
                                                    : 0.0004964
    3rd Qu.: 0.0089366
                         3rd Qu.: 0.0104713
                                              3rd Qu.: 0.0090419
##
   Max. : 0.1365130
                         Max. : 0.1146918
                                              Max. : 0.1653925
```

There are 5521 observations and 30 stocks inside the data set.

Model

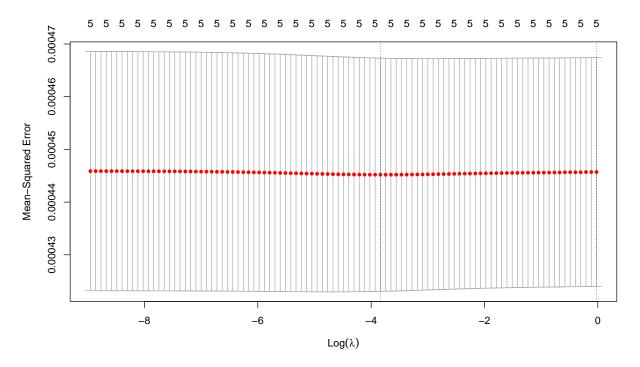
The simple model using only "AA" stock

To start a simple model, we take the Alcoa Corporation stock as an instance first, which is denoted by "AA" and we create 5 lagged stock returns as inputs for our model and use the real stock return as the output. A brief summary of the variables of the model is as follows:

```
##
      AA_return
                               lag_1
                                                    lag_2
           :-0.2745595
                                  :-0.274560
                                                        :-0.2745595
##
    Min.
                          Min.
                                                Min.
    1st Qu.:-0.0114625
                           1st Qu.:-0.011463
                                                1st Qu.:-0.0114461
##
##
    Median : 0.0000000
                          Median: 0.000000
                                                Median: 0.0000000
            : 0.0001576
                                  : 0.000149
                                                        : 0.0001552
##
    Mean
                          Mean
                                                Mean
    3rd Qu.: 0.0116305
                                                3rd Qu.: 0.0116305
##
                          3rd Qu.: 0.011618
            : 0.2087337
                                  : 0.208734
                                                        : 0.2087337
##
    Max.
                          Max.
                                                {\tt Max.}
##
        lag_3
                               lag_4
                                                     lag_5
                                                         :-0.2745595
##
    Min.
            :-0.2745595
                          Min.
                                  :-0.2745595
                                                 Min.
##
    1st Qu.:-0.0114343
                          1st Qu.:-0.0114295
                                                 1st Qu.:-0.0114343
##
    Median : 0.0000000
                          Median : 0.0000000
                                                 Median : 0.0000000
                                  : 0.0001807
                                                         : 0.0001733
##
            : 0.0001697
                          Mean
    Mean
                                                 Mean
##
    3rd Qu.: 0.0116305
                           3rd Qu.: 0.0116378
                                                 3rd Qu.: 0.0116305
##
            : 0.2087337
                          Max.
                                  : 0.2087337
                                                 Max.
                                                         : 0.2087337
```

The data to date 2002-12-31 are used as the training data and the data from date 2003-01-02 to date 2009-02-03 are used as the testing data. The training set is fit into a ridge regressing to predict the target variable using the features (the lagged five returns).

The optimal lambda of the Ridge regression is found via 5-fold cross validation and a plot of the lambda parameter vs. the Mean Squared Error is shown as follows:



The optimal lambda parameter is 0.02156627 and the model after fitting the Ridge regression using the optimal parameter chosen above (use the entire Training Set) is summarized as follows:

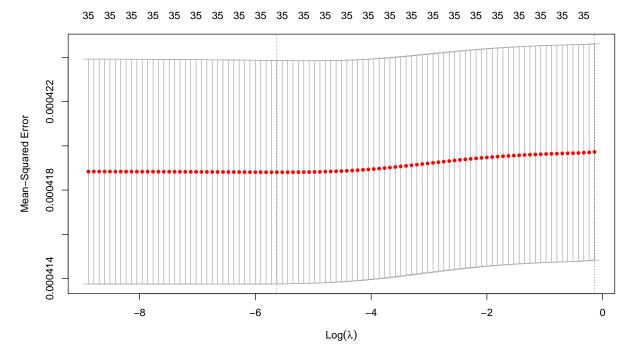
##		Length	Class	Mode
##	a0	1	-none-	numeric
##	beta	5	${\tt dgCMatrix}$	S4
##	df	1	-none-	numeric
##	dim	2	-none-	numeric
##	lambda	1	-none-	numeric
##	${\tt dev.ratio}$	1	-none-	numeric
##	nulldev	1	-none-	numeric
##	npasses	1	-none-	numeric
##	jerr	1	-none-	numeric
##	offset	1	-none-	logical
##	call	5	-none-	call
##	nobs	1	-none-	numeric

The general model using all the stocks

Similarly, 5 lagged stock returns are added as input variables. Besides this, dummy variables are added to realize one-hot encoding to get rid of the fix effects in different stocks. After preprocessing, the data frame has 165480 observations with 36 columns(5 lagged values, 1 true return and 30 dummy columns).

Also, the data to date 2002-12-31 are used as the training data and the data from date 2003-01-02 to date 2009-02-03 are used as the testing data. The training set is fit into a ridge regressing to predict the target variable using the features (the lagged five returns and dummy variables).

The optimal lambda of the Ridge regression is found via 5-fold cross validation and a plot of the lambda parameter vs. the Mean Squared Error is shown as follows:



The optimal lambda chosen in this model is 0.003593454 and after fitting the Ridge regression using the optimal parameter chosen above (use the entire Training Set), a summary of the fitted model is as follows:

Length Class Mode

##	a0	1	-none-	numeric
##	beta	35	${\tt dgCMatrix}$	S4
##	df	1	-none-	numeric
##	dim	2	-none-	numeric
##	lambda	1	-none-	numeric
##	${\tt dev.ratio}$	1	-none-	numeric
##	nulldev	1	-none-	numeric
##	npasses	1	-none-	numeric
##	jerr	1	-none-	numeric
##	offset	1	-none-	logical
##	call	5	-none-	call
##	nobs	1	-none-	numeric

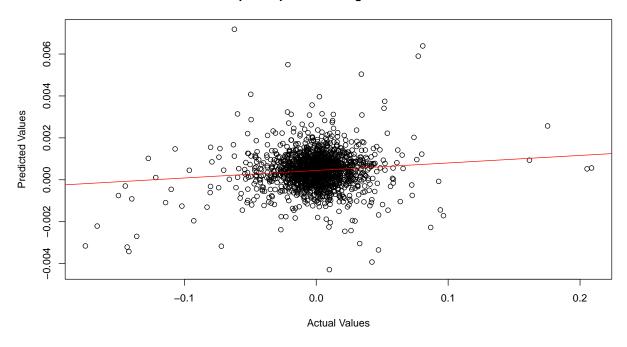
Result

The simple model using only "AA" stock

The mean absolute error using the fitted model above to predict the returns of AA in the Test Set is 0.01772329.

The scatterplot of predictions against the true values is as follows:

Scatterplot of predictions against the true values



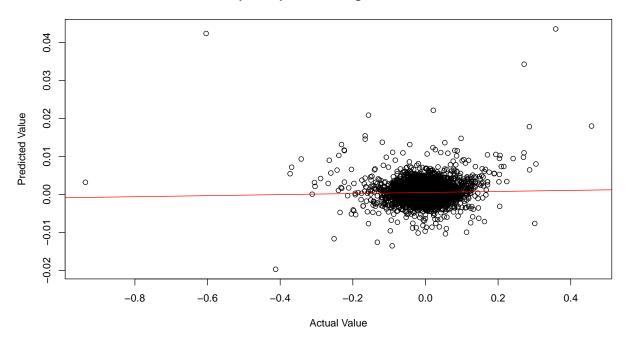
Conclusions can be drawn from the scatterplot that the model does not fit quite well from the scatterplot as the predicted values are not that close to actual values (the line is not close to a regressed diagonal line)

The general model using all the stocks

The mean absolute error using the fitted model above to predict the returns of all stocks in the Test Set is 0.0127128.

The scatterplot of predictions against the true values is as follows:

Scatterplot of predictions against the true values



Compared to the previous predicted value vs actual value graph, this model does not have a significant improvement from the above although MAE decreases since the predicted value range is still much narrower than the actual value range and the line is not regressed diagonally.

Limitations and next steps

There are several limitations in the models. One is multicollinearity and next step could be setting a baseline of the variables and dropping one dummy variable to avoid multicollinearity. Furthermore, if we consider using dummy variables to improve the model, we could incorporate factors that impact stock behaviors such as the size of the company(whether it is a large company or small company indicated by P/E ratio), whether the company is a value company or growth company, and so on. We can add dummy variables in these aspects and train our model to see whether there would be some improvements for the fitted model.

Reference

R Core Team. 2020. R: A Language and Environment for Statistical Computing. Vienna, Austria: R Foundation for Statistical Computing. https://www.R-project.org/ (https://www.R-project.org/).