- 3.1 (a) 0.
  - $q_1 \, 0 \, \sqcup$
  - $\sqcup q_2 \sqcup$
  - $\sqcup \sqcup q_{accept}$
  - (b) 00.
    - $q_1 \, 0 \, 0 \, \sqcup$
    - $\sqcup q_2 0 \sqcup$
    - $\sqcup x q_3 \sqcup$
    - $\sqcup q_5 x \sqcup$
    - $q_5 \sqcup x \sqcup$
    - $\sqcup q_2 x \sqcup$
    - $\sqcup x q_2 \sqcup$
    - $\sqcup x \sqcup q_{accept}$
  - (c) 000.
    - $q_1 \, 0 \, 0 \, 0 \, \sqcup$
    - $\sqcup q_2 0 0 \sqcup$
    - $\sqcup x q_3 0 \sqcup$
    - $\sqcup x 0 q_4 \sqcup$
    - $\sqcup x 0 \sqcup q_{reject}$

- (d) 000000.
  - $q_1 \, 0 \, 0 \, 0 \, 0 \, 0 \, 0 \, \Box$
  - $\sqcup q_2 0 0 0 0 0 \sqcup$
  - $\sqcup x 0 q_4 0 0 0 \sqcup$
  - $\sqcup x 0 x q_3 0 0 \sqcup$
  - $\sqcup x 0 x 0 q_4 0 \sqcup$
  - $\sqcup x 0 x 0 x q_3 \sqcup$
  - $\sqcup x 0 x 0 q_5 x \sqcup$
  - $\sqcup x 0 x q_5 0 x \sqcup$
  - $\sqcup x \circ q_5 x \circ x \sqcup$
  - $\sqcup x q_5 0 x 0 x \sqcup$
  - $\sqcup q_5 x 0 x 0 x \sqcup$
  - $q_2 \sqcup x \, 0 \, x \, 0 \, x \, \sqcup$
  - 12
  - $\sqcup q_2 x 0 x 0 x \sqcup$
  - $\sqcup x q_2 0 x 0 x \sqcup$
  - $\sqcup x x q_3 x 0 x \sqcup$
  - $\sqcup x x x 0 q_4 x \sqcup$
  - $\sqcup xxx0xq_4\sqcup$
  - $\sqcup xxx0x \sqcup q_{reject}$
- 3.2 (a) 11.
  - $q_1 11 \sqcup$
  - $x q_3 1 \sqcup$
  - $x 1 q_3 \sqcup$
  - $x \, 1 \, q_{reject} \, \sqcup$

- (b) 1#1.
  - $q_1 1 \# 1 \sqcup$
  - $x q_3 \# 1 \sqcup$
  - $x \# q_5 1 \sqcup$
  - $x q_6 \# x \sqcup$
  - $q_7 x \# x \sqcup$
  - $x q_1 \# x \sqcup$
  - $x \# q_8 x \sqcup$
  - $x \# x q_8 \sqcup$
  - $x \# x \sqcup q_{accept}$
- (c) 1##1.
  - $q_1\,1\,\#\,\#\,1\sqcup$
  - $x \# q_5 \# 1 \sqcup$
  - $x \# q_{reject} \# 1 \sqcup$
- (d) 10#11.
  - $q_1 \, 1 \, 0 \, \# \, 1 \, 1 \, \sqcup$
  - $x q_3 0 \# 11 \sqcup$
  - $x \, 0 \, q_3 \, \# \, 1 \, 1 \, \sqcup$
  - $x \ 0 \# q_5 \ 1 \ 1 \ \sqcup$
  - $x \ 0 \ q_5 \# x \ 1 \sqcup$
  - $x \, 0 \, q_6 \, \# \, x \, 1 \, \sqcup$
  - $x q_7 0 \# x 1 \sqcup$
  - $q_7 \, x \, 0 \, \# \, x \, 1 \, \sqcup$
  - $x q_1 0 \# x 1 \sqcup$
  - $x x q_2 \# x 1 \sqcup$
  - $x x \# q_4 x 1 \sqcup$
  - $x x \# x q_4 1 \sqcup$
  - $x \, x \, \# \, x \, q_{reject} \, 1 \, \sqcup$

(e) 10#10.

$$q_1 10 # 10 \sqcup x q_3 0 # 10 \sqcup x 0 q_3 # 10 \sqcup x 0 q_6 # x 0 \sqcup x 0 q_6 # x 0 \sqcup x 0 q_7 x 0 # x 0 \sqcup x 0$$

- 3.3 Solution in book.
- 3.4 An enumerator  ${\cal E}$  can be defined as a 2-tape Turing machine with the transition function:

$$\delta: Q \times \Gamma_{tape} \longrightarrow Q \times \Gamma_{tape} \times \Gamma_{print} \times \{L, R, S\} \times \{R, S\}$$

The language enumerated by the enumerator is  $L \subseteq \Gamma_p *$ .