



MATLAB

Variables & Data Types

Week 2

Loosely follows Chapter 2



Variables

- Used to store information
- Can hold numerical values or text values and you don't need to declare them
- Can be recalled later
- Always use informative names
- Standard conventions
 - `speedOfLightKPH`
 - `speed_of_light_kph`
 - `SPEED_OF_LIGHT_KPH`

Variable Naming Rules

- Must begin with a letter
- Must only contain letters, numbers, and underscores
- Cannot contain spaces or punctuation marks
- Names exceeding 63 characters are truncated
 - Please don't create variables 63 characters long (30 is a good limit)
- Case sensitive but try **NOT** to use two variables of the same name
 - X and x is acceptable
 - BALANCE and balance is not acceptable

The Workspace

- Contains current variables
- I refer to this as the “environment”
- `who` displays a list of current variables
- `whos` displays current variables, data types, and sizes
- `Workspace` in the UI also displays current variables

Data Types

- MATLAB has 15 different data types

- `str = 'Hello World!'`
- `n = 2345`
- `d = double(n)`
- `un = uint32(789.50)`
- `rn = 5678.92347`
- `c = int32(rn)`

```
str = Hello World!  
n = 2345  
d = 2345  
un = 790  
rn = 5678.9  
c = 5679
```

- All operations are performed with double precision by default

Variables as arrays

All variables in MATLAB are arrays

Scalar

1×1

Vector

$n \times 1$ or $1 \times n$

Matrix

$n \times m$

Vectors and Matrices are mathematical objects, Arrays are lists or tables.

Scalars

- Scalars are simply 1x1 arrays
- They contain a single value, such as the following:

radius = 6

height = 12

width = 2

Vectors

- A vector is a collection of values represented in a 1-dimensional array
- A vector can be $n \times 1$ or $1 \times n$
- Rows are separated by semicolons (Column Vector)
 - `heights = [144; 13; 25; 108; 96; 61; 73; 60; 48; 109]`
- Columns are separated by commas or spaces (Row Vector)
 - `heights = [3, 141, 140, 6, 7, 137, 136, 10, 11, 133]`

column vector	row vector																				
<table><tr><td>144</td></tr><tr><td>13</td></tr><tr><td>25</td></tr><tr><td>108</td></tr><tr><td>96</td></tr><tr><td>61</td></tr><tr><td>73</td></tr><tr><td>60</td></tr><tr><td>48</td></tr><tr><td>109</td></tr></table>	144	13	25	108	96	61	73	60	48	109	<table><tr><td>3</td><td>141</td><td>140</td><td>6</td><td>7</td><td>137</td><td>136</td><td>10</td><td>11</td><td>133</td></tr></table>	3	141	140	6	7	137	136	10	11	133
144																					
13																					
25																					
108																					
96																					
61																					
73																					
60																					
48																					
109																					
3	141	140	6	7	137	136	10	11	133												

Matrices

- A matrix is a collection of values represented as a 2-dimensional array
- Defining a matrix is done so with both commas (for columns) and semicolons (for rows)

```
matrix = [ 3.0, 1.8, 3.6;  
          4.6, -2.0, 21.3;  
          0.0, -6.1, 12.8;  
          2.3, 0.3, -6.1 ]
```

		COLUMNS		
		1	2	3
ROWS	1	3.0	1.8	3.6
	2	4.6	-2.0	21.3
	3	0.0	-6.1	12.8
	4	2.3	0.3	-6.1

Scalar & Array Operations

Operation	Algebraic Syntax	MATLAB Syntax
Addition	$a + b$	a + b
Subtraction	$a - b$	a - b
Multiplication	$a \times b$	a .* b
Division	$a \div b$	a ./ b
Exponentiation	a^b	a .^ b

Hierarchy of Operations

- Remember good old PEMDAS?
- **IMPORTANT:** calculations are performed left to right after PEMDAS

Example breakdown

$c = 2 + 3^2 + 1 / (1 + 2)$	→	$c = 2 * 3^2 + 1 / 3$	
$c = 2 + 3^2 + 1 / (1 + 2)$	→	$c = 2 * 9 + 1 / 3$	
$c = 2 * 3^2 + 1 / (1 + 2)$	→	$c = 18 + 1 / 3$	(left to right)
$c = 2 * 3^2 + 1 / (1 + 2)$	→	$c = 18 + 0.33333$	
$c = 2 * 3^2 + 1 / (1 + 2)$	→	$c = 18.33333$	

Array Operations

- Matrix operations can be performed on an array
- To perform matrix calculations, use the standard operators (+, -, *, /, ^)
- To perform operations to each discrete element, use the dot/element-wise operator. (+, -, .*, ./, .^)
- Use the dot-operator anytime unless you intend to perform matrix math.

Matrix Operations

Operation	Algebraic Syntax	MATLAB Syntax
Addition	$A + B$	A + B
Subtraction	$A - B$	A - B
Multiplication	$A \times B$	A * B
Division	$A \div B$	A / B
Exponentiation	A^b	A ^ b

Array vs Matrix Arithmetic Example

- Enter the following:

- `>> x = [2, 1; 3, 4]`
- `>> y = [5, 6; 7, 8]`
- `>> zMat = x * y`
- `>> zDot = x .* y`

zMat should contain [17, 20; 43, 50]

due to **matrix** multiplication

zDot should contain [10, 6; 21, 32]

due to **array** multiplication

$$\begin{pmatrix} A & B \\ C & D \end{pmatrix} \times \begin{pmatrix} E & F \\ G & H \end{pmatrix} = \begin{pmatrix} AE+BG & AF+BH \\ CE+DG & CF+DH \end{pmatrix}$$

Explicitly Defining & Assigning Arrays

- An array can be defined by typing in a list of numbers enclosed in square brackets.

- Commas or spaces separate numbers or columns

■ $A = [12, 18, -3]$ OR $A = [12 \ 18 \ -3]$

A =

12 18 -3

- Semicolons separate rows

■ $B = [2, 5, 2; 1, 1, 2; 0, -2, 6]$

B =

2 5 2
1 1 2
0 -2 6

Dynamically Defining & Assigning Arrays

- Colon notation can be used to define evenly spaced vectors with **first:last**

- `H = 1:6`

H =

1 2 3 4 5 6

- The default increment is 1, you can specify with **first:increment:last**

- `I = 1:2:11`

I =

1 3 5 7 9 11

The *linspace()* and *logspace()* Functions

- *linspace(start, end, n)*
- Creates a finite linearly spaced set of *n* values between *start* and *end*
- Useful if you know the start, end, and number of values you want
 - *linspace(1,10,4)*
ans =
1 4 7 10
- *logspace(a,b,n)*
- Creates *n* points between 10^a and 10^b .
- Useful in signal processing

Array Inception

- You can define an array with other arrays

- $C = [A; B]$

C =

12	18	-3
2	5	2
1	1	2
0	-2	6

- $D = [C, C]$

D =

12	18	-3	12	18	-3
2	5	2	2	5	2
1	1	2	1	1	2
0	-2	6	0	-2	6

Recall:

A =

12	18	-3
----	----	----

B =

2	5	2
1	1	2
0	-2	6

Creating Arrays of Zeros & Ones

- For zeros use the `zeros(numRows, numCols)` function

- `E = zeros(3,5)`

E =

0	0	0	0	0
0	0	0	0	0
0	0	0	0	0

- For ones use the `ones(numRows, numCols)` function

- `F = ones(2,3)`

F =

1	1	1
1	1	1

NOTE: Placing a single number inside either function will return an nxn array

Accessing Values in an Array or Vector

- Referred to as a subscript
- An index is a number used to identify elements in an array
- Add parenthesis after your array name with row and col index (row,col)
 - `G = [1, 2, 3; 4, 5, 6; 7, 8, 9]`
G =

1	2	3
4	5	6
7	8	9
 - `G(2,1)` ← Retrieves the element from row 2, col 1
ans = 4

Changing/Setting Values in an Array

- Just as with retrieval, you can change values in an array with the same notation.

- `A = ones(2)` ← Create a 2x2 matrix of ones
- `A(2, 1) = 8` ← Sets the value of row two, col one to 8

A =

1	1
8	1

- You can extend an array by defining a new element

- `A(2, 3) = 10`

A =

1	1	0
8	1	10

NOTE: When defining a new element, notice any undefined values are filled with zeros

Retrieving an Entire Vector

- With retrieval notation, an entire row or column can be represented as a colon in place of an index value.

- $G = [1, 2, 3; 4, 5, 6; 7, 8, 9]$

$G =$

1	2	3
4	5	6
7	8	9

$G(:,1)$

ans =

1
4
7

$G(:,3)$

ans =

3
6
9

$G(2,:)$

ans =

4 5 6

More Extraction Methods with Colon

- The colon operator can also be used to extract a range of rows or columns

- `G = [1, 2, 3; 4, 5, 6; 7, 8, 9]`

`G =`

1	2	3
4	5	6
7	8	9

`G(2:3,:)`

`ans =`

4	5	6
7	8	9

`G(1,2:3)`

`ans =`

2	3
---	---

Manipulating Arrays & Vectors

- The transpose operator, a single apostrophe ' changes all of an array's rows to columns and columns to rows

- $J = [1, 3, 7]$

J =

1	3	7
---	---	---

- J'

J =

1
3
7

- $K = [1, 2, 3; 4, 5, 6; 7, 8, 9]$

K =

1	2	3
4	5	6
7	8	9

- K'

J =

1	4	7
2	5	8
3	6	9

Manipulating Arrays & Vectors (cont.)

- The functions `fliplr()` and `flipud()` flip an array left to right (`lr`) and upside-down (`ud`) respectively.

- `G = [1, 2, 3; 4, 5, 6; 7, 8, 9]`

`G =`

1	2	3
4	5	6
7	8	9

`fliplr(G)`

`ans =`

3	2	1
6	5	4
9	8	7

`flipud(G)`

`ans =`

7	8	9
4	5	6
1	2	3

Matrix Manipulation Exercises

- Create the following matrix using colon notation:

W =

1	2	3	4	5
10	12	14	16	18
6	5	4	3	2

- All three rows are evenly spaced
 - The first row ranges from 1 to 5 in increments of 1 (1:5 OR 1:1:5)
 - The second row ranges from 10 to 18 in increments of 2 (10:2:18)
 - The third row ranges from 6 to 2 in increments of -1 (6:-1:2)
 - Put them all together:
 - `W = [1:5; 10:2:18; 6:-1:2]`

Matrix Manipulation Exercises

- Create the following matrix using colon notation:

X =

1.2	2.3	3.4	4.5	5.6
1.9	3.8	5.7	7.6	9.5
0	-3	-6	-9	-12

- Transpose this matrix and assign it to variable Y
 - $Y = X'$
- Extract the 2nd row from Y and assign it to variable Z
 - $Z = Y(2, :)$