In Class Assignment 4

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Summary of Data

Below is a summary of the data set "big_missing.csv". As you can see, each x column has missing data points.

```
summary(data_set)
```

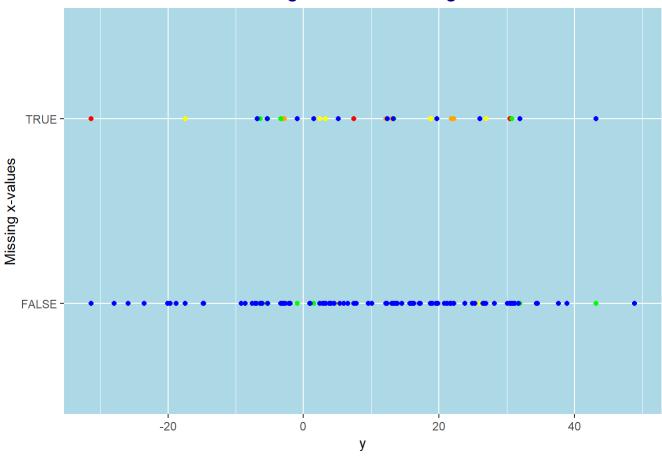
```
##
          x1
                               x2
                                                    х3
##
    Min.
            :-2.85696
                                :-2.40106
                                             Min.
                                                     :-2.018833
##
    1st Ou.:-0.76317
                        1st Ou.:-0.57819
                                             1st Ou.:-0.457711
    Median :-0.12731
                        Median : 0.06486
##
                                             Median :-0.008622
##
    Mean
            :-0.03669
                        Mean
                                : 0.03498
                                                     : 0.018659
##
    3rd Qu.: 0.86817
                         3rd Qu.: 0.64943
                                             3rd Qu.: 0.453366
           : 2.66424
##
    Max.
                        Max.
                                : 2.64657
                                                     : 1.784673
                                             Max.
    NA's
            :10
                         NA's
                                :12
                                             NA's
##
                                                     :10
##
          x4
                              x5
                                                   х6
##
    Min.
            :-1.1089
                       Min.
                               :-3.10974
                                            Min.
                                                    :-2.78223
##
    1st Qu.:-0.4835
                       1st Qu.:-0.69247
                                            1st Qu.:-0.72309
##
    Median :-0.1036
                       Median : 0.12553
                                            Median :-0.23559
            :-0.0474
                               : 0.01172
                                                    :-0.08153
##
    Mean
                       Mean
                                            Mean
##
    3rd Ou.: 0.3514
                       3rd Ou.: 0.72377
                                            3rd Ou.: 0.64835
                                                    : 2.37292
##
    Max.
            : 1.4986
                       Max.
                               : 2.15504
                                            Max.
    NA's
                       NA's
                               :11
                                                    :13
##
            :8
                                            NA's
##
                               x8
                                                  х9
          x7
                                                                     x10
##
    Min.
            :-2.52170
                        Min.
                                :-3.9179
                                            Min.
                                                    :-2.2041
                                                               Min.
                                                                       :-2.06412
    1st Qu.:-0.58542
                        1st Qu.:-0.8708
                                            1st Qu.:-0.6859
                                                                1st Qu.:-0.79520
##
##
    Median : 0.04912
                        Median :-0.2553
                                            Median : 0.1682
                                                               Median :-0.11243
##
            :-0.06950
                        Mean
                                :-0.1843
                                            Mean
                                                    : 0.1111
                                                                       : 0.03711
                         3rd Qu.: 0.6912
                                            3rd Qu.: 0.8439
                                                                3rd Ou.: 0.83159
##
    3rd Ou.: 0.44330
##
    Max.
            : 1.63941
                        Max.
                                : 2.8479
                                            Max.
                                                    : 2.4595
                                                               Max.
                                                                       : 2.30761
                                                    :7
##
    NA's
           :10
                         NA's
                                            NA's
                                                                NA's
                                                                       :15
                                :15
##
          У
##
    Min.
            :-31.360
    1st Qu.: -2.881
##
    Median : 12.345
##
##
    Mean
              9.810
##
    3rd Ou.: 21.667
            : 48.838
##
    Max.
##
```

Plots of Missing Data

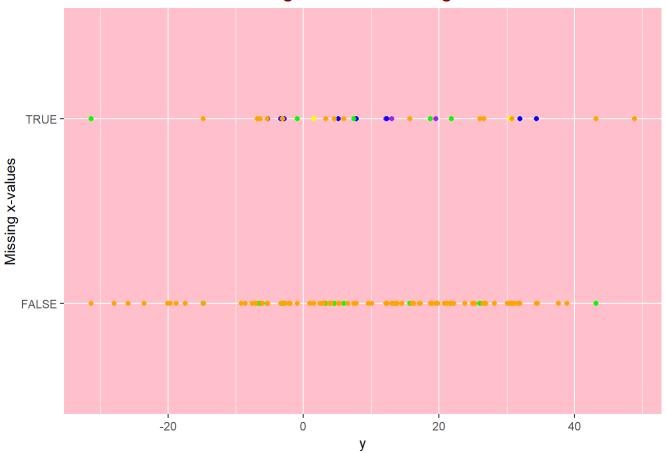
We can see that the data is missing completely at random by looking at the graphs below. The first graph shows the missing values of x1 through x5 for all the values of y and the second shows the missing values of x6 through x10 (these are split into two graphs for easier interpretation). Each color represents a different x. As you can see,

the missing data does not appear in any sort of pattern.

Missing Data for x1 Through x5



Missing Data for x6 Through x10



Regression Techniques

There are a few techniques to bypass missing data. First we will try a regression with line deletion:

```
data_set_delete = na.omit(data_set)
delete_model = lm(y~.,data=data_set_delete)
summary(delete_model)
```

```
##
## Call:
## lm(formula = y \sim ., data = data set delete)
##
## Residuals:
##
        Min
                  1Q
                      Median
                                    3Q
                                            Max
## -22.6805 -5.1175 -0.2035
                                6.8746 15.0412
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 8.9932
                            1.4355
                                     6.265 1.26e-07 ***
                 3.9131
                            1.9325
                                     2.025 0.04883 *
## x1
## x2
                -1.6148
                            2.3013 -0.702 0.48648
## x3
                 7.1822
                            3.1157
                                     2.305 0.02583 *
                -3.4870
                            2.6064 -1.338 0.18765
## x4
## x5
                -0.2990
                            2.1386 -0.140 0.88943
## x6
                 5.3380
                            2.1329
                                   2.503 0.01603 *
                 0.4504
                            2.9189
                                     0.154 0.87806
## x7
                                     3.136 0.00302 **
## x8
                 5.0405
                            1.6074
## x9
                -0.6487
                            2.0402 -0.318 0.75198
## x10
                 2.9116
                            1.7447
                                     1.669 0.10210
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.551 on 45 degrees of freedom
## Multiple R-squared: 0.7514, Adjusted R-squared: 0.6961
## F-statistic: 13.6 on 10 and 45 DF, p-value: 1.372e-10
```

The intercept has a very statistically significant p-value (<0.001). There is one other coefficient with a p-value <0.01 (x8), three others that are less than 0.05 (x1, x3, and x6), but the rest are not statistically significant.

We do not have a feasible way to do single imputation, but we can use multiple imputation and pool the regressions.

```
data_set_mi = mice(data_set,m=15,print=FALSE)
mi_fit = with(data_set_mi,lm(y~x1+x2+x3+x4+x5+x6+x7+x8+x9+x10))
mi_fit_pooled = pool(mi_fit)
```

```
## Warning: package 'bindrcpp' was built under R version 3.5.2
```

```
summary(mi_fit_pooled)
```

```
##
                                                  df
                estimate std.error
                                   statistic
                                                         p.value
## (Intercept) 10.1471228
                         1.141787
                                   8.8870566 61.67217 1.214140e-12
## x1
               3.8705918
                         1.321033
                                  2.9299738 56.20675 4.747239e-03
## x2
              -2.0346881
                         1.869253 -1.0885033 50.67492 2.806084e-01
## x3
               5.8819805
                         ## x4
              -4.0739424
                         2.269327 -1.7952209 59.17539 7.751847e-02
## x5
              -0.4568413
                         1.810999 -0.2522593 46.78148 8.016795e-01
## x6
               4.1941364
                         1.929256
                                  2.1739657 44.90982 3.355477e-02
                         2.766361 -0.2245657 25.42956 8.230595e-01
## x7
              -0.6212299
               4.2653447
                         1.395200 3.0571569 50.90258 3.301505e-03
## x8
## x9
              -2.3672672
                         1.582793 -1.4956268 58.78711 1.398509e-01
## x10
               4.7848644 1.415433 3.3804951 51.78205 1.259825e-03
```

Again, the intercept has a very statistically significant p-value (<0.001). There are now three coefficients with p-values <0.01 (x1, x8, and x10) and one that is less than 0.05 (x3). This leads me to believe that x1 and x8 are definitely significant. x3 also seems fairly significant. x10 appears to be significant too, although it did not appear to be significant in the regression with line deletion. Finally, x6 is possibly significant since its first p-value was <0.05, and its second was <0.1.