Homework4

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Problem 1: Error Functions for Tree Classification

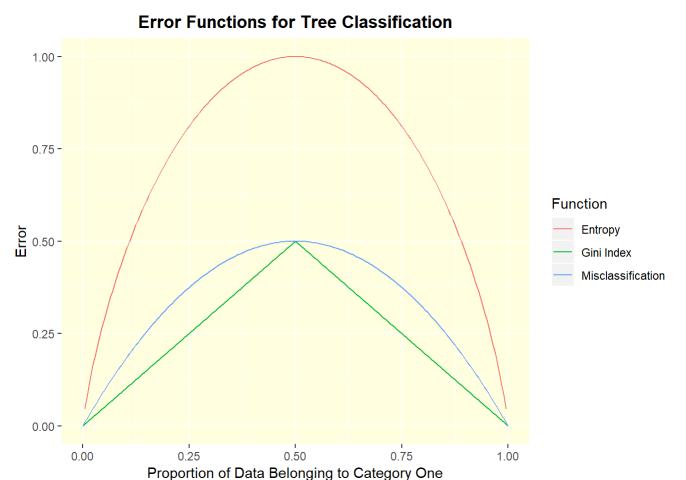
Below is a graph depicting three different error functions in a two-category classification problem:

```
library(ggplot2)
```

```
## Warning: package 'ggplot2' was built under R version 3.5.2
```

```
#defining p (proportion of training data points in the mth leaf that belong to category 1)
p=seq(0,1,0.005)
Gini = 2*p*(1-p)
Entropy=(p-1)*log2(1-p)-p*log2(p)
#misclassification
E=0.5-abs(p-0.5)
Error=data.frame(p,E,Gini,Entropy)
ggplot()+geom_line(data=Error,aes(x=p,y=E,col="purple"))->p1
p1+geom_line(data=Error,aes(x=p,y=Gini,col="salmon"))->p2
p2+geom_line(data=Error,aes(x=p,y=Entropy,col="blue"))->p3
p3+theme(panel.background=element_rect(fill="lightyellow"))->p4
p4+theme(plot.title=element text(hjust=0.5,face="bold"))->p5
p5+labs(title="Error Functions for Tree Classification",y="Error",
        x="Proportion of Data Belonging to Category One")->p6
p6+scale_colour_discrete(name="Function",breaks=c("blue", "purple", "salmon"),
                       labels=c("Entropy", "Gini Index", "Misclassification"))
```

```
## Warning: Removed 2 rows containing missing values (geom_path).
```



It is much better to use the Gini index or entropy instead of misclassification error to train trees because of their concave, *curved* shape. Since the algorithm used is greedy (recursive binary splitting), it will only split the tree if the average error of the child nodes is less than the error of the parent node (so that each split lowers the total objective). The average always falls on a straight line between the two child nodes. When using misclassification error, the average error of the child nodes could easily equal the error of the parent node, causing the algorithm to stop prematurely. On the other hand, a line drawn between two points on the Gini index or entropy curve is always under the curve, so the average error will likely not be equal to the parent node.

Problem 2: Predicting Titanic Survivors Using Trees (Kaggle Competition)

Below are the data sets for training and testing a model to predict which passengers on the Titanic survived.

```
library(tree)

## Warning: package 'tree' was built under R version 3.5.2

library(MASS)
library(randomForest)

## Warning: package 'randomForest' was built under R version 3.5.2
```

```
## randomForest 4.6-14

## Type rfNews() to see new features/changes/bug fixes.

## ## Attaching package: 'randomForest'

## The following object is masked from 'package:ggplot2':
## ## margin

library(gbm)

## Warning: package 'gbm' was built under R version 3.5.2

## Loaded gbm 2.1.5

Titanic_train=read.csv("C:/Users/lydia/Documents/titanic/train.csv",header=TRUE)
Titanic_test=read.csv("C:/Users/lydia/Documents/titanic/test.csv",header=TRUE)
summary(Titanic_train)
```

```
PassengerId
                        Survived
                                           Pclass
##
##
    Min.
           : 1.0
                     Min.
                             :0.0000
                                               :1.000
                                       Min.
##
    1st Qu.:223.5
                     1st Qu.:0.0000
                                       1st Qu.:2.000
##
    Median :446.0
                     Median :0.0000
                                       Median :3.000
##
    Mean
           :446.0
                     Mean
                             :0.3838
                                       Mean
                                               :2.309
    3rd Qu.:668.5
                     3rd Ou.:1.0000
                                       3rd Qu.:3.000
##
##
    Max.
           :891.0
                     Max.
                             :1.0000
                                       Max.
                                               :3.000
##
##
                                         Name
                                                       Sex
                                                                      Age
                                           :
                                                   female:314
                                                                        : 0.42
##
    Abbing, Mr. Anthony
                                               1
                                                                 Min.
                                                                 1st Ou.:20.12
##
    Abbott, Mr. Rossmore Edward
                                               1
                                                   male :577
    Abbott, Mrs. Stanton (Rosa Hunt)
                                               1
                                                                 Median :28.00
##
##
    Abelson, Mr. Samuel
                                               1
                                                                 Mean
                                                                        :29.70
##
    Abelson, Mrs. Samuel (Hannah Wizosky):
                                               1
                                                                 3rd Qu.:38.00
    Adahl, Mr. Mauritz Nils Martin
                                               1
##
                                                                 Max.
                                                                        :80.00
##
    (Other)
                                            :885
                                                                 NA's
                                                                        :177
##
        SibSp
                         Parch
                                            Ticket
                                                             Fare
##
    Min.
            :0.000
                     Min.
                             :0.0000
                                       1601
                                                :
                                                   7
                                                       Min.
                                                               :
                                                                 0.00
    1st Qu.:0.000
                     1st Qu.:0.0000
                                       347082
                                                   7
                                                       1st Qu.: 7.91
##
    Median :0.000
                     Median :0.0000
                                                       Median : 14.45
##
                                       CA. 2343:
                                                   7
    Mean
           :0.523
                             :0.3816
                                                               : 32.20
##
                     Mean
                                       3101295 :
                                                   6
                                                       Mean
##
    3rd Ou.:1.000
                     3rd Ou.:0.0000
                                       347088
                                                       3rd Ou.: 31.00
##
    Max.
           :8.000
                     Max.
                             :6.0000
                                       CA 2144 :
                                                   6
                                                       Max.
                                                               :512.33
                                       (Other) :852
##
##
            Cabin
                       Embarked
##
                :687
                        : 2
    B96 B98
                   4
                       C:168
##
##
    C23 C25 C27:
                   4
                       Q: 77
##
    G6
                   4
                       S:644
    C22 C26
                   3
##
##
    D
                   3
##
    (Other)
                :186
```

We can remove the column "Passenger Id" from our model since this is, presumably, a number arbitrarily assigned to passengers to organize the data set. We will also remove the "Name" and "Ticket" columns since these inputs are unique and nonnumerical (although the information could be used to engineer new columns). Finally, we will remove the "Cabin" data since it is likewise hard to categorize and most of the information is missing.

We will begin with an AdaBoost model. There is more missing data but the package we use for boosting will take care of it.

```
#AdaBoost

#Take out columns: PassengerId, Name, Ticket, Cabin
Titanic_train_boost=Titanic_train[,-c(1,4,9,11)]
Titanic_test_boost=Titanic_test[,-c(1,3,8,10)]
```

First we tune hyper-parameters using 10-fold cross-validation on depths of 1, 2, and 3 to find the tree with the lowest cross-validation error.

```
set.seed(1)

#tuning hyper-parameters

#depth=1
boost.titanic1=gbm(Survived~.,data=Titanic_train_boost,distribution="adaboost",n.trees=2000,inte
raction.depth=1,cv.folds=10)
cv_err1=boost.titanic1$cv.error
#minimum error
min(cv_err1)
```

[1] 0.7352366

#best number of trees
which.min(cv_err1)

[1] 83

#depth=2
boost.titanic2=gbm(Survived~.,data=Titanic_train_boost,distribution="adaboost",n.trees=2000,inte
raction.depth=2,cv.folds=10)
cv_err2=boost.titanic2\$cv.error
#minimum error
min(cv_err2)

[1] 0.7047338

#best number of trees
which.min(cv_err2)

[1] 76

#depth=3
boost.titanic3=gbm(Survived~.,data=Titanic_train_boost,distribution="adaboost",n.trees=2000,inte
raction.depth=3,cv.folds=10)
cv_err3=boost.titanic3\$cv.error
#minimum error
min(cv_err3)

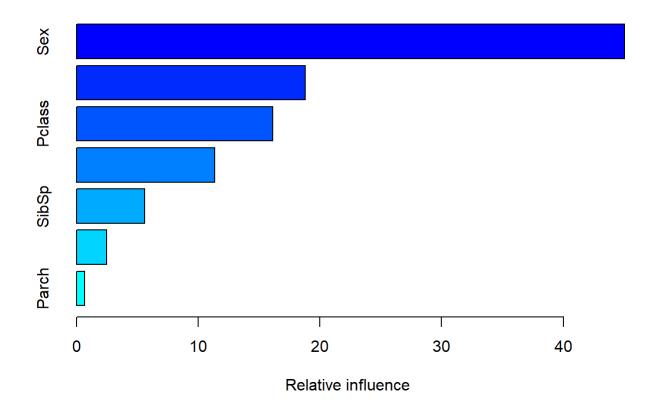
[1] 0.7075063

#best number of trees
which.min(cv_err3)

[1] 53

We then use all the training data to build a tree using the best depth/tree combination.

```
#final model
boost.titanic=gbm(Survived~.,data=Titanic_train_boost,distribution="adaboost",n.trees=76,interac
tion.depth=2)
#summary info of final model
summary(boost.titanic)
```



```
##
                         rel.inf
                 var
                 Sex 45.0279381
## Sex
                 Age 18.8012406
## Age
              Pclass 16.1124694
## Pclass
## Fare
                Fare 11.3422033
## SibSp
               SibSp
                      5.5949740
## Embarked Embarked
                      2.4743680
## Parch
               Parch
                      0.6468066
```

Finally, we use our model to make predictions on the test set.

```
#Using test data
#prediction
boost.prediction = predict(boost.titanic,Titanic_test_boost,type="link",n.trees=76,interaction.d
epth=2)
boost.prediction01=ifelse(boost.prediction>0,1,0)

#creating a data frame of the predictions
boost.submission = data.frame(PassengerId = Titanic_test$PassengerId, Survived = boost.prediction01)
```

I used the following code to write the output to a csv file so I could upload it to Kaggle:

write.csv(boost.submission, file = "boost_submission.csv", row.names = FALSE, quote = FALSE)

Next, we will build a Random Forest model. The package for Random Forest does not deal with missing values very well so we will have to clean up the data a bit.

```
#Random Forest

#temporarily removing the Survived column from training data
Titanic_train2=Titanic_train[,-2]

#temorarily combining the test and train data
Titanic_all = rbind(Titanic_train2, Titanic_test)

#summary of data
summary(Titanic_all)
```

```
##
     PassengerId
                        Pclass
                                                                    Name
##
    Min.
           :
                    Min.
                           :1.000
                                    Connolly, Miss. Kate
                                                                           2
               1
    1st Qu.: 328
                    1st Qu.:2.000
                                     Kelly, Mr. James
                                                                           2
##
    Median : 655
                    Median :3.000
##
                                     Abbing, Mr. Anthony
##
    Mean
           : 655
                    Mean
                           :2.295
                                     Abbott, Mr. Rossmore Edward
    3rd Ou.: 982
                                     Abbott, Mrs. Stanton (Rosa Hunt):
##
                    3rd Ou.:3.000
                                                                           1
##
    Max.
           :1309
                    Max.
                           :3.000
                                     Abelson, Mr. Samuel
                                                                           1
##
                                     (Other)
                                                                       :1301
##
        Sex
                                       SibSp
                                                         Parch
                       Age
##
    female:466
                 Min.
                         : 0.17
                                          :0.0000
                                                    Min.
                                                            :0.000
                                  Min.
    male :843
                  1st Qu.:21.00
                                   1st Qu.:0.0000
                                                    1st Qu.:0.000
##
                  Median :28.00
                                  Median :0.0000
                                                    Median:0.000
##
##
                  Mean
                         :29.88
                                  Mean
                                          :0.4989
                                                    Mean
                                                            :0.385
##
                  3rd Qu.:39.00
                                   3rd Ou.:1.0000
                                                     3rd Qu.:0.000
##
                  Max.
                         :80.00
                                  Max.
                                          :8.0000
                                                    Max.
                                                            :9.000
##
                  NA's
                         :263
         Ticket
                                                    Cabin
                                                                Embarked
##
                          Fare
    CA. 2343: 11
                     Min.
                            :
                                                        :1014
                                                                 : 2
##
                               0.000
##
    1601
                 8
                     1st Qu.: 7.896
                                        C23 C25 C27
                                                                C:270
##
    CA 2144:
                 8
                     Median : 14.454
                                        B57 B59 B63 B66:
                                                                Q:123
    3101295 :
                 7
                                                            5
##
                     Mean
                            : 33.295
                                        G6
                                                                S:914
##
    347077 :
                 7
                     3rd Ou.: 31.275
                                        B96 B98
                                                            4
##
    347082 :
                            :512.329
                                        C22 C26
                 7
                     Max.
                                                            4
                                                        : 271
##
    (Other) :1261
                     NA's
                            :1
                                        (Other)
```

```
str(Titanic_all)
```

```
## 'data.frame':
                   1309 obs. of 11 variables:
## $ PassengerId: int 1 2 3 4 5 6 7 8 9 10 ...
## $ Pclass
                : int 3 1 3 1 3 3 1 3 3 2 ...
## $ Name
                : Factor w/ 1307 levels "Abbing, Mr. Anthony",..: 109 191 358 277 16 559 520 62
9 417 581 ...
   $ Sex
                : Factor w/ 2 levels "female", "male": 2 1 1 1 2 2 2 2 1 1 ...
##
                : num 22 38 26 35 35 NA 54 2 27 14 ...
##
  $ Age
##
   $ SibSp
                : int 1101000301...
  $ Parch
                : int 000000120...
##
                : Factor w/ 929 levels "110152", "110413",...: 524 597 670 50 473 276 86 396 345
## $ Ticket
133 ...
##
  $ Fare
                : num 7.25 71.28 7.92 53.1 8.05 ...
                : Factor w/ 187 levels "", "A10", "A14", ...: 1 83 1 57 1 1 131 1 1 1 ...
##
   $ Cabin
                : Factor w/ 4 levels "", "C", "Q", "S": 4 2 4 4 4 3 4 4 4 2 ...
   $ Embarked
```

There is a missing fare that we will have to fill in. Since it is only one value (for a male in 3rd class), we will just replace the missing value with 0.

```
#Which passenger is missing fare?
which(is.na(Titanic_all$Fare))
```

```
## [1] 1044
```

```
#passenger missing fare
Titanic_all[1044,]
```

```
#replace missing value with 0
Titanic_all[1044,9] <-0</pre>
```

Random Forest can handle missing categorical data, so we don't have to worry about those columns, but there are many ages missing, so we will create age groups instead of using the numerical values.

As with AdaBoost, we will remove the columns we are not using and then separate the test and train data.

```
#Take out columns: PassengerId, Name, Ticket, Cabin, (Age)
Titanic_all_rf=Titanic_all_age[,-c(1,3,5,8,10)]

#Separate test and train
Titanic_train3=Titanic_all_rf[1:891,]
Titanic_train_rf=data.frame(Titanic_train3,Titanic_train$Survived)
Titanic_test_rf=Titanic_all_rf[892:1309,]
```

We then build the Random Forest model with our training data using a large number of trees and the default mtry (square root of m).

```
set.seed(1)

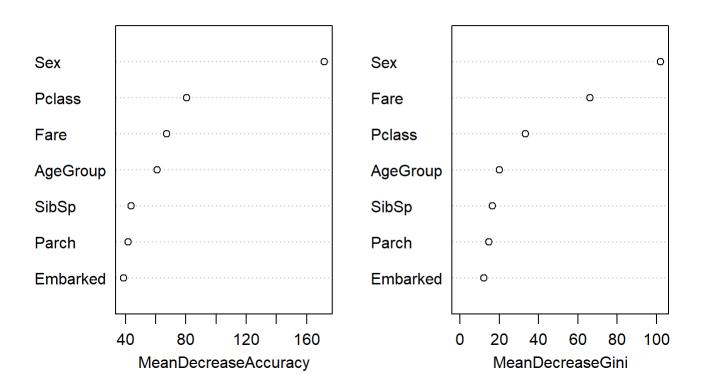
#Random Forest model
rf.titanic=randomForest(as.factor(Titanic_train.Survived)~.,data=Titanic_train_rf,ntree=2000,imp
ortance=TRUE)

#summary info
importance(rf.titanic)
```

```
##
                    0
                              1 MeanDecreaseAccuracy MeanDecreaseGini
             47.16101 61.47351
## Pclass
                                            80.61013
                                                             33.23189
## Sex
            124.09514 169.21993
                                           171.76763
                                                            102.04275
## SibSp
             39.97352 11.33856
                                            43.81349
                                                             16.39961
## Parch
             30.30626 28.89887
                                            41.65307
                                                             14.80877
## Fare
             45.86204 43.41121
                                            67.29572
                                                             66.26678
## Embarked 15.09956 35.52164
                                            38.73803
                                                             12.21297
## AgeGroup 33.96474 51.76402
                                            60.88153
                                                             20.04685
```

```
varImpPlot(rf.titanic)
```

rf.titanic



Finally, we use our model to make predictions on the test set and write the output to a csv file to upload to Kaggle.

```
#prediction
rf.prediction=predict(rf.titanic,Titanic_test_rf)

#data frame of prediction
rf.submission = data.frame(PassengerId = Titanic_test$PassengerId, Survived = rf.prediction)
```

Surprisingly, my Random Forest model did better than my AdaBoost model. My AdaBoost model performed worse than simple models that predict solely by gender. However, my Random Forest did pretty well.

Submission and Description	Public Score
rf_submission.csv a minute ago by Lydia Strebe	0.77033
add submission details	
boost_submission.csv 3 minutes ago by Lydia Strebe	0.74641
add submission details	

Results