

Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

#### Lecture 15: Decision Trees & Random Forest

### COMP90049 Knowledge Technologies

Hasti Samadi & Sarah Erfani & Karin Verspoor, CIS

Semester 2, 2019





## From Decision Stumps to Decision Trees

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Decision Tree
Definition
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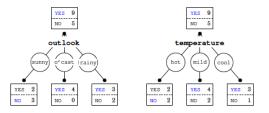
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More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources We have seen decision stumps in action in the context of 1-R



 Based the same concept we can build a more complex model with the ability to capture complex feature interaction



### **Decision Tree**

Decision Tree & Random Forest

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<u>Decision Tree</u> <u>Definition</u> <u>Hunt Algorithm</u> <u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

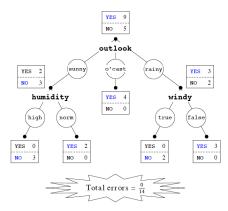
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Summary Resources

#### A flow-chart-like tree structure

- Internal node denotes a test on an attribute
- Branch represents an outcome of the test (attribute value)
- <u>Leaf nodes represent class labels</u> or class distribution





### **Decision Tree**

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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

## Advantages:

- Basic classification model
- Fast
- Scalable
- Interpretable

### Disadvantage:

Not highest accuracy (Random Forest to the rescue)



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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources Let D<sub>t</sub> be the set of training records that reach a node t



Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

### **General Procedure:**



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Decision Tree
Definition

Hunt Algorithm
Predicting by DT

Attribute Selection
Information Gian

Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

#### **General Procedure:**

Outlook	Temperature	Humidity	Windy	Play
sunny	hot	high	FALSE	no
sunny	hot	high	TRUE	no
overcast	hot	high	FALSE	yes
rainy	mild	high	FALSE	yes
rainy	cool	normal	FALSE	yes
rainy	cool	normal	TRUE	no
overcast	cool	normal	TRUE	yes
sunny	mild	high	FALSE	no
sunny	cool	normal	FALSE	yes
rainy	mild	normal	FALSE	yes
sunny	mild	normal	TRUE	yes
overcast	mild	high	TRUE	yes
overcast	hot	normal	FALSE	yes
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Technologies

Decision Tree
Definition

Hunt Algorithm
Predicting by DT

Attribute Selection

Information Gian Gain Ratio

More DT Algorithms

**Overfitting** 

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

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Technologies

Decision Tree
Definition
Hunt Algorithm

Predicting by DT

Attribute Selection
Information Gian

Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

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Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

**Overfitting** 

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

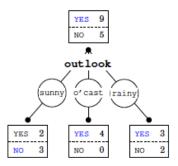
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**Overfitting** 

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

- If D<sub>t</sub> contains records that belong to more than one class, use an attribute to split the data into smaller subsets.
- Recursively apply the procedure to <u>each subset</u>.



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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

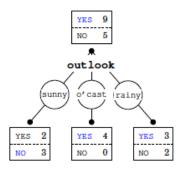
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Classifier Combination Bagging Random Tree

Random Forest
Summary

Resources

- If D<sub>t</sub> contains records that belong to more than one class, use an attribute to split the data into smaller subsets.
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  - If D<sub>t</sub> contains records that ALL belong to the same class y<sub>t</sub>, then t is a leaf node labelled as y<sub>t</sub>





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Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

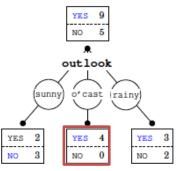
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Combination
Bagging
Random Tree
Random Forest

Summary Resources

#### **General Procedure:**

- If D<sub>t</sub> contains records that belong to more than one class, use an attribute to split the data into smaller subsets.
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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

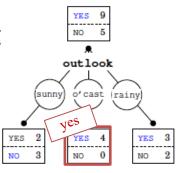
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Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

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<u>Decision Tree</u> <u>Definition</u> <u>Hunt Algorithm</u> <u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

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  - If D<sub>t</sub> is an empty set, then t is a leaf node labelled by the default class, y<sub>d</sub> (majority class in the data)



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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

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## Hunt's Algorithm: Example

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

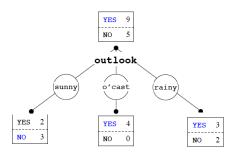
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Overfitting

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Combination
Bagging
Random Tree
Random Forest





## Hunt's Algorithm: Example

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Decision Tree

Definition

Hunt Algorithm

Predicting by DT

Attribute Selection Information Gian Gain Ratio

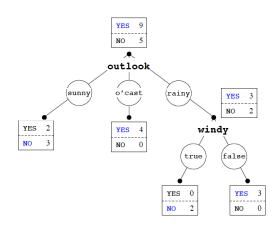
More DT Algorithms

Overfitting

Classifier

Combination Bagging

Random Tree Random Forest





## Hunt's Algorithm: Example

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<u>Decision Tree</u>
<u>Definition</u>
<u>Hunt Algorithm</u>
<u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

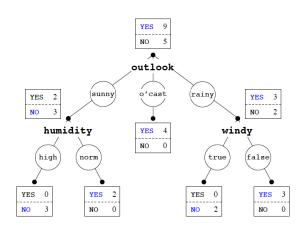
More DT Algorithms

Overfitting

Classifier

Combination Bagging

Random Tree Random Forest





Decision Tree & Random Forest

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<u>Decision Tree</u>
<u>Definition</u>
<u>Hunt Algorithm</u>
<u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Outlook	Temperature	Humidity	Windy	Play
Rainy	High	Mild	true	?



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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

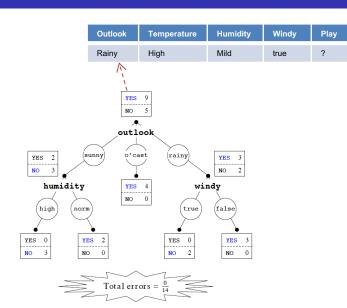
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Overritting

Classifier Combination

Bagging Random Tree

Random Forest





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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

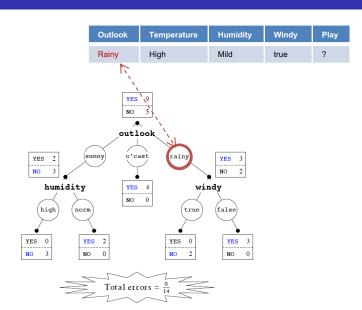
More DT Algorithms

Overfitting

Classifier

Combination Bagging

> Random Tree Random Forest





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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

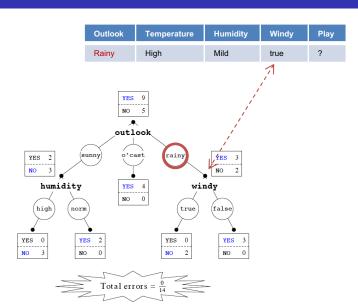
More DT Algorithms

Overfitting

Classifier

Combination Bagging

> Random Tree Random Forest





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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

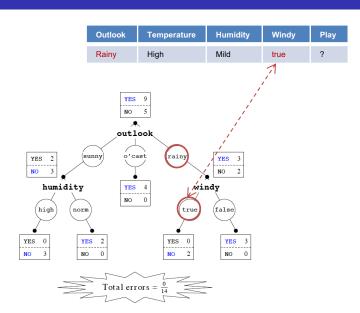
More DT Algorithms

Overfitting

Classifier

Combination Bagging

Random Tree Random Forest





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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

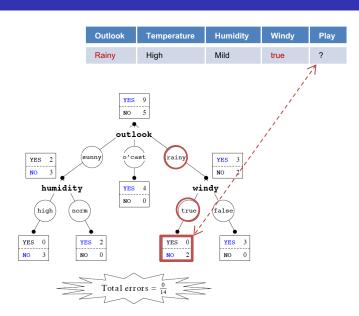
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Overfitting

Classifier

Combination Bagging

Random Tree Random Forest





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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

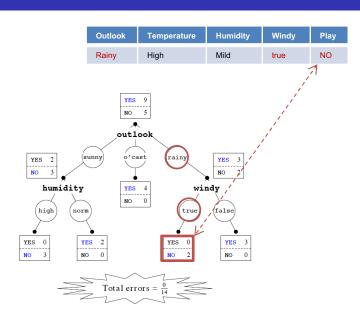
More DT Algorithms

Overfitting

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Classifier Combination

> Bagging Random Tree Random Forest





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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources There could be more than one tree that fits the same data!



Decision Tree & Random Forest

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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- There could be more than one tree that fits the same data!
- How do we choose the attribute to partition the instances at a given node?



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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- There could be more than one tree that fits the same data!
- How do we choose the attribute to partition the instances at a given node?
- We want to get the smallest tree



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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- There could be more than one tree that fits the same data!
- How do we choose the attribute to partition the instances at a given node?
- We want to get the smallest tree
- Prefer attributes that create more homogeneous (pure) nodes



Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- There could be more than one tree that fits the same data!
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- We need to measure node purity



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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

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- One Measure is Entropy



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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

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- We want to get the smallest tree
- Prefer attributes that create more homogeneous (pure) nodes
- We need to measure node purity
- One Measure is Entropy (measure of predictability)



# Entropy (Recap)

Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources The entropy of a discrete random event x with possible states 1,..,n is:

$$H(x) = -\sum_{i=1}^{n} P(i) \log_2 P(i)$$

(where  $0 \log_2(0)$  is 0)



# Entropy (Recap)

Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

## When **Entropy** is <u>low</u>

➤ The event is <u>predictable</u> (more homogeneous)

### When **Entropy** is high

➤ The event is <u>unpredictable</u> (less homogeneous)



# Entropy (Recap)

Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

#### When **Entropy** is <u>low</u>

The event is <u>predictable</u> (more homogeneous)

#### When **Entropy** is <u>high</u>

➤ The event is <u>unpredictable</u> (less homogeneous)

#### In developing a **Decision Tree**:

✓ We prefer attributes (for splitting the dataset) that reduce the entropy more.



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Decision Tree

Definition

Hunt Algorithm

Predicting by DT

Attribute Selection
Information Gian
Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources  The expected reduction in entropy caused by knowing the value of an attribute.

- Compare:
  - the entropy <u>before</u> splitting the tree using the attribute's values
  - the <u>weighted average</u> of the entropy over the children <u>after the split</u> (Mean Information)
- If the entropy decreases, then we have a better tree (more predictable)



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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

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- the entropy <u>before</u> splitting the tree using the attribute's values
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- If the entropy decreases, then we have a better tree (more predictable)
- Information Gain is the <u>difference</u> between the entropy at the root (before splitting) and the Mean Information



Decision Tree & Random Forest

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<u>Decision Tree</u> <u>Definition</u> <u>Hunt Algorithm</u> <u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources We calculate the **Mean Information** for a tree stump with m attribute values as:

Mean Info
$$(x_1, ..., x_m) = \sum_{i=1}^m P(x_i)H(x_i)$$

where  $H(x_i)$  is the entropy of the class distribution for the instances at node  $x_i$ 



Decision Tree & Random Forest

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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources • We calculate the **Mean Information** for a tree stump with *m* attribute values as:

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where  $H(x_i)$  is the entropy of the class distribution for the instances at node  $x_i$ 

Information Gain

$$IG(R_A|R) = H(R) - \sum_{i=1}^{m} P(x_i)H(x_i)$$

$$IG(R_A|R) = H(R) - Mean Info(x_1,...,x_m)$$



Decision Tree & Random Forest

COMP90049 Knowledge Technologies

<u>Decision Tree</u>
<u>Definition</u>
<u>Hunt Algorithm</u>
<u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

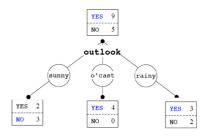
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Overfitting

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Random Tree Random Forest





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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

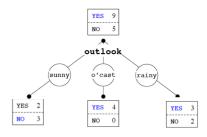
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**Overfitting** 

Classifier Combination

Bagging Random Tree Random Forest

Summary Resources



entropy before splitting the tree (entropy at root)

$$H(R) = -((9/14)\log_2(9/14) + (5/14)\log_2(5/14)) = -(-.4098 - 0.5305) = 0.940$$



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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

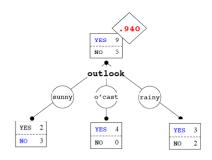
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Overfitting

Classifier Combination

> Bagging Random Tree

Random Forest
Summary
Resources



entropy before splitting the tree (entropy at root)

$$H(R) =$$
 $-((9/14)\log_2(9/14) + (5/14)\log_2(5/14)) =$ 
 $-(-.4098 - 0.5305) = 0.940$ 



Decision Tree & Random Forest

COMP90049 Knowledge Technologies

<u>Decision Tree</u> <u>Definition</u> Hunt Algorithm <u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination

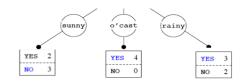
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Summary Resources entropies after splitting the tree (outlook)

$$\begin{array}{l} H(rainy) = \\ -(3/5)\log_2(3/5) + (2/5\log_2(2/5))) = \\ -(-0.4422 - 0.5288) = 0.971 \end{array}$$

$$\begin{array}{l} H(overcast) = \\ -((4/4)\log_2(4/4) + (0/4\log_2(0/4))) = 0 \end{array}$$

$$H(sunny) = -((2/5)\log_2(2/5) + (3/5\log_2(3/5))) = 0.971$$





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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination Bagging

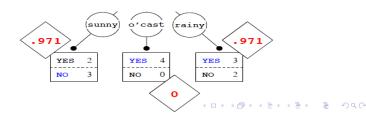
Random Tree Random Forest

Summary Resources entropies after splitting the tree (outlook)

$$H(rainy) = -(3/5)\log_2(3/5) + (2/5\log_2(2/5))) = -(-0.4422 - 0.5288) = 0.971$$

$$\begin{array}{l} \textit{H(overcast)} = \\ -((4/4)\log_2(4/4) + (0/4\log_2(0/4))) = 0 \end{array}$$

$$H(sunny) = -((2/5)\log_2(2/5) + (3/5\log_2(3/5))) = 0.971$$





Decision Tree & Random Forest

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Decision Tree

Definition

Hunt Algorithm

Predicting by DT

Attribute Selection Information Gian Gain Ratio

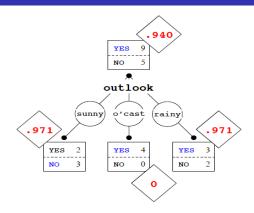
More DT Algorithms

Overfitting

#### Classifier

Combination
Bagging
Random Tree
Random Forest

Summary Resources



#### Mean Information for Outlook

$$Mean\_info(outlook) = P(rainy)H(rainy) + P(overcast)H(overcast) + P(sunny)H(sunny) = 5/14 * 0.971 + 0 + 5/14 * 0.971 = 0.693$$



Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

#### Information Gain

$$IG(R_A|R) = H(R) - Mean Info(x_1,...,x_m)$$



Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination

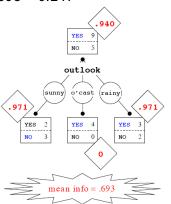
Bagging Random Tree Random Forest

Summary Resources

#### Information Gain

$$IG(R_A|R) = H(R) - Mean Info(x_1,...,x_m)$$

$$IG (outlook | R) = 0.94 - 0.693 = 0.247$$





Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

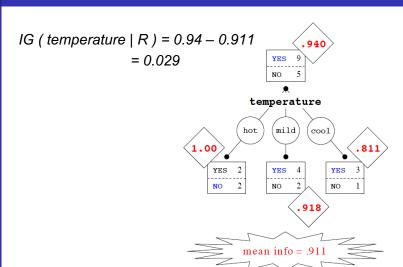
More DT Algorithms

Overfitting

Classifier

Combination
Bagging
Random Tree

Random Forest
Summary
Resources





Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

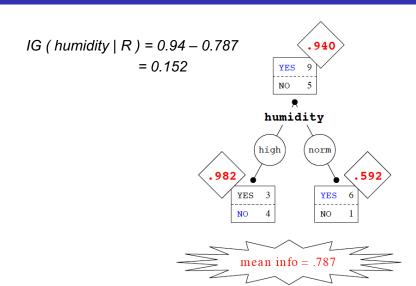
Overfitting

Classifier

Resources

Combination
Bagging
Random Tree

Random Forest
Summary





Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

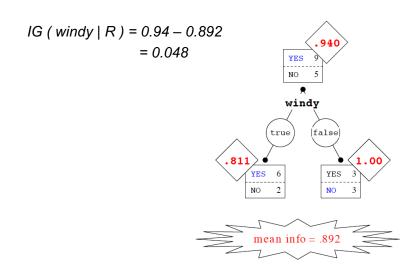
Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination

Bagging Random Tree Random Forest





Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources IG (outlook  $\mid R$ ) = 0.247 IG (temperature  $\mid R$ ) = 0.029 IG (humidity  $\mid R$ ) = 0.152

IG(windy | R) = 0.048



Decision Tree & Random Forest

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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources IG (outlook | R) = 0.247 higher Information Gain

IG ( temperature | R ) = 0.029

IG (humidity | R) = 0.152

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Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

ID	Outlook	Temperature	Humidity	Windy	Play
1	sunny	hot	high	FALSE	no
2	sunny	hot	high	TRUE	no
3	overcast	hot	high	FALSE	yes
4	rainy	mild	high	FALSE	yes
5	rainy	cool	normal	FALSE	yes
6	rainy	cool	normal	TRUE	no
7	overcast	cool	normal	TRUE	yes
8	sunny	mild	high	FALSE	no
9	sunny	cool	normal	FALSE	yes
10	rainy	mild	normal	FALSE	yes



Decision Tree & Random Forest

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<u>Decision Tree</u> <u>Definition</u> <u>Hunt Algorithm</u> <u>Predicting by DT</u>

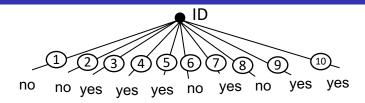
Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination Bagging

Random Tree Random Forest



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Decision Tree & Random Forest COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- Information gain tends to prefer <u>highly-branching</u> <u>attributes</u>:
  - A subset of instances is more likely to be homogeneous (all of a single class) if there are only a few instances
  - Attribute with many values will have fewer instances at each child node



Decision Tree & Random Forest

COMP90049

Knowledge
Technologies

Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources  Information gain tends to prefer <u>highly-branching</u> <u>attributes</u>:

- A subset of instances is more likely to be homogeneous (all of a single class) if there are only a few instances
- Attribute with many values will have fewer instances at each child node
- This may result in overfitting/fragmentation



Decision Tree & Random Forest

COMP90049

Knowledge
Technologies

<u>Decision Tree</u> <u>Definition</u> <u>Hunt Algorithm</u> <u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources  Information gain tends to prefer <u>highly-branching</u> <u>attributes</u>:

- A subset of instances is more likely to be homogeneous (all of a single class) if there are only a few instances
- Attribute with many values will have fewer instances at each child node
- This may result in overfitting/fragmentation
- Solution → Gain Ratio



Decision Tree & Random Forest

Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination Bagging Random Tree Random Forest

- Gain ratio (GR) reduces the bias for information gain towards highly-branching attributes by normalizing relative to the <u>split information</u>
- Split info (SI) is the entropy of a given split (evenness of the distribution of instances to attribute values)

$$GR(R_{A}|R) = \frac{IG(R_{A}|R)}{SI(R_{A}|R)} = \frac{IG(R_{A}|R)}{H(R_{A})}$$
$$= \frac{H(R) - \sum_{i=1}^{m} P(x_{i})H(x_{i})}{-\sum_{i=1}^{m} P(x_{i}) \log_{2} P(x_{i})}$$



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<u>Decision Tree</u>

<u>Definition</u>

<u>Hunt Algorithm</u>

Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

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$$= \frac{H(R) - \sum_{i=1}^{m} P(x_{i})H(x_{i})}{-\sum_{i=1}^{m} P(x_{i}) \log_{2} P(x_{i})}$$

 Note: Split Info is entropy of distribution of instances to attribute values (<u>disregarding classes</u>, unlike Mean Info)



Decision Tree & Random Forest

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<u>Decision Tree</u> <u>Definition</u> Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Mean Info
$$(x_1, ..., x_m) = \sum_{i=1}^m P(x_i)H(x_i)$$
  
Split Info $(x_1, ..., xm|R) = -\sum_{i=1}^m P(x_i)\log_2 P(x_i)$ 



Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

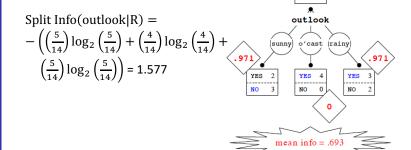
Classifier Combination

Bagging Random Tree Random Forest

Summary Resources

Mean Info
$$(x_1,...,x_m) = \sum_{i=1}^m P(x_i)H(x_i)$$

Split Info(x<sub>1</sub>,...,xm|R) = 
$$-\sum_{i=1}^{m} P(x_i) \log_2 P(x_i)$$



940

YES



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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree

Random Tree Random Forest

$$IG(\text{outlook}|R) = 0.247$$

$$IG(\text{humidity}|R) = 0.152$$

$$IG(temperature|R) = 0.029$$

$$IG(\text{windy}|R) = 0.048$$



Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination

Bagging Random Tree Random Forest

Summary Resources IG(outlook|R) = 0.247SI(outlook|R) = 1.577

IG(humidity|R) = 0.152SI(humidity|R) = 1.000

IG(temperature|R) = 0.029SI(temperature|R) = 1.557

IG(windy|R) = 0.048SI(windy|R) = 0.985



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<u>Decision Tree</u>
<u>Definition</u>
<u>Hunt Algorithm</u>
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination

Bagging Random Tree Random Forest

Summary Resources

```
IG(\text{outlook}|R) = 0.247

SI(\text{outlook}|R) = 1.577

GR(\text{outlook}|R) = 0.156
```

IG(humidity|R) = 0.152 SI(humidity|R) = 1.000GR(humidity|R) = 0.152

IG(temperature|R) = 0.029 SI(temperature|R) = 1.557GR(temperature|R) = 0.019

IG(windy|R) = 0.048 SI(windy|R) = 0.985 GR(windy|R) = 0.049



Decision Tree & Random Forest

COMP90049
Knowledge

Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination

> Bagging Random Tree Random Forest

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IG(\text{outlook}|R) = 0.247

SI(\text{outlook}|R) = 1.577

GR(\text{outlook}|R) = 0.156
```

$$IG(\text{humidity}|R) = 0.152$$
  
 $SI(\text{humidity}|R) = 1.000$   
 $GR(\text{humidity}|R) = 0.152$ 

$$IG(\text{temperature}|R) = 0.029$$
  
 $SI(\text{temperature}|R) = 1.557$   
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$$IG(\text{windy}|R) = 0.048$$
  
 $SI(\text{windy}|R) = 0.985$   
 $GR(\text{windy}|R) = 0.049$ 



Decision Tree & Random Forest

COMP90049

Knowledge
Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination

Bagging Random Tree Random Forest

Summary Resources

```
IG(\text{outlook}|R)
                    = 0.247
SI(\text{outlook}|R)
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IG(\text{humidity}|R)
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                    = 1.000
GR(\text{humidity}|R)
                    = 0.152
IG(temperature|R)
                          = 0.029
SI(temperature|R)
                          = 1.557
GR(\text{temperature}|R)
                          = 0.019
```

IG(windy|R) = 0.048 SI(windy|R) = 0.985GR(windy|R) = 0.049



### Other Decision Tree Implementations

Decision Tree & Random Forest

Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination Bagging Random Tree

Random Forest
Summary
Resources

#### Ross Quinlan

- ID3 uses the Hunt's algorithm with <u>information gain</u> <u>criterion</u> and <u>gain ratio</u>
  - Available in WEKA (no discretization, no missing values)
- C4.5 improves ID3
  - Needs entire data to fit in memory
  - Handles missing attributes and continuous attributes
  - Performs tree post-pruning
  - Available in WEKA as J48



### Other Decision Tree Implementations

Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination Bagging Random Tree Random Forest

Summary Resources

#### Breiman et al.

- CART builds multivariate decision (binary) trees
  - Supports numerical target variables (regression)
  - Available in WEKA as SimpleCART



# Determine When to Stop Splitting

<u>Decision Tree &</u> <u>Random Forest</u>

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources When a node is homogenous



# Determine When to Stop Splitting

Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- When a node is homogenous
- When the subsample size is smaller than a threshold



# Determine When to Stop Splitting

Decision Tree & Random Forest

COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

- When a node is homogenous
- When the subsample size is smaller than a threshold

**Remember**: our goal is not to sub-divide the data perfectly

Over-subdivision leads to a complicated decision boundary (over-fitting)





# Determine When to Stop Splitting

Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources Metrics to control the complexity of the tree

- Total number of nodes
- Tree depth
- Minimum number of data points for a split
- IG/GR is smaller than a threshold



## So far..

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Technologies

Decision Tree
Definition
Hunt Algorithm

Predicting by DT

Attribute Selection
Information Gian

Gain Ratio

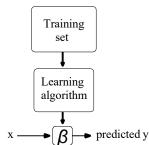
More DT Algorithms

Overfitting

Classifier Combination Bagging

> Random Tree Random Forest

- We have discussed individual classification algorithms and considered each of them in isolation
- We have discussed ways of comparing the performance of individual classifiers over a given dataset/task, which allows us to choose the "dataset optimal" classifier





## So far..

Decision Tree & Random Forest COMP90049 Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

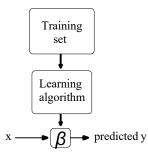
Classifier Combination

Bagging Random Tree Random Forest

Summary Resources

- We have discussed individual classification algorithms and considered each of them in isolation
- We have discussed ways of comparing the performance of individual classifiers over a given dataset/task, which allows us to choose the "dataset optimal" classifier
- Classifier combination (ensemble learning)

constructs a set of base classifiers from a given set of training data and aggregates the outputs into a single meta-classifier





### **Classifier Combination**

Decision Tree & Random Forest COMP90049 Knowledge

Technologies

Decision Tree

Definition
Hunt Algorithm

Predicting by DT

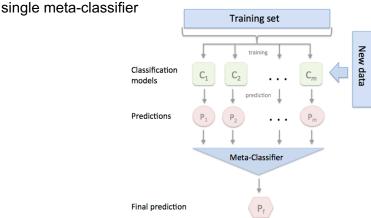
Attribute Selection
Information Gian
Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources Classifier combination (ensemble learning)
 constructs a set of base classifiers from a given set of training data and aggregates the outputs into a





### **Classifier Combination**

Decision Tree & Random Forest COMP90049 Knowledge Technologies

<u>Decision Tree</u> <u>Definition</u> <u>Hunt Algorithm</u> <u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- Motivation 1: the combination of lots of weak <u>classifiers</u> can be at least <u>as good as one strong</u> <u>classifier</u>
  - Motivation 2: the combination of a selection of strong classifiers is (usually) at least <u>as good as the best of</u> the base classifiers



### **Classifier Combination**

Decision Tree & Random Forest

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Knowledge
Technologies

Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

- Instance manipulation: generate multiple training datasets through sampling, and train a base classifier over each
- Feature manipulation: generate multiple training datasets through different feature subsets, and train a base classifier over each
- Class label manipulation: generate multiple training datasets by manipulating the class labels in a reversible manner
- Algorithm manipulation: semi-randomly "tweak" internal parameters within a given algorithm to generate multiple base classifiers over a given dataset



# Bagging

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Decision Tree Definition Hunt Algorithm Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

#### Classifier Combination

Bagging Random Tree Random Forest

Summary Resources

- Basic intuition: the more data, the better the performance, so how can we get ever more data out of a fixed training dataset?
  - Method: Randomly sample the original dataset N times, with replacement

Original training dataset:

Bootstrap samples:





### Random Tree

Decision Tree & Random Forest

Knowledge Technologies

Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources A "Random Tree" is a Decision Tree where:

- At each node, <u>only some of the possible attributes</u> are considered
- For example, a fixed proportion of all of the attributes, except the ones used earlier in the tree
- Attempts to control for unhelpful attributes in the feature set
- Much faster to build than a "deterministic" Decision Tree, but increases model variance



### Random Forest

Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources

### A "Random Forest" is:

- An ensemble of Random Trees (many trees = forest)
- Each tree is built on a <u>random subset of records</u> of the data: **Tree bagging**
- Each tree is built on a <u>random subset of features</u> of the data: Random subspace
- Decision via majority voting



### Random Forest

Decision Tree & Random Forest

COMP90049 Knowledge Technologies

<u>Decision Tree</u>
<u>Definition</u>
<u>Hunt Algorithm</u>
<u>Predicting by DT</u>

Attribute Selection Information Gian Gain Ratio

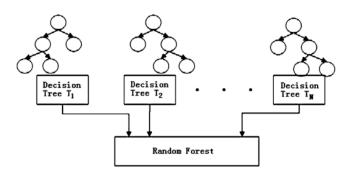
More DT Algorithms

Overfitting

Classifier Combination

Bagging Random Tree Random Forest

Summary Resources



Community of Experts



## **Practical Properties of Random Forests**

Decision Tree & Random Forest

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Decision Tree
Definition
Hunt Algorithm
Predicting by DT

Attribute Selection Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier Combination Bagging Random Tree Random Forest

- Generally a very strong performer
- Embarrassingly parallelisable
- Surprisingly efficient
- Robust to overfitting
- Interpretability sacrificed



### Tools and Resources

Decision Tree & Random Forest COMP90049 Knowledge

Technologies

Decision Tree

Definition
Hunt Algorithm
Predicting by DT

Attribute Selection

Information Gian Gain Ratio

More DT Algorithms

Overfitting

Classifier
Combination
Bagging
Random Tree
Random Forest

Summary Resources This lecture was prepared using some material adapted from:

- https://www-users.cs.umn.edu/~kumar/dmbook/ch4.pdf
- http://wwwusers.cs.umn.edu/~kumar/dmbook/dmslides/chap4\_basic classification.ppt
- Mitchell, Tom (1997). Machine Learning. Chapter 3: Decision Tree Learning.
- Tan et al (2006) Introduction to Data Mining. Section 4.3, pp 150-171.
- Pang-Ning Tan, Michael Steinbach, and Vipin Kumar.
   Introduction to Data Mining. Addison Wesley, 2006