Stack

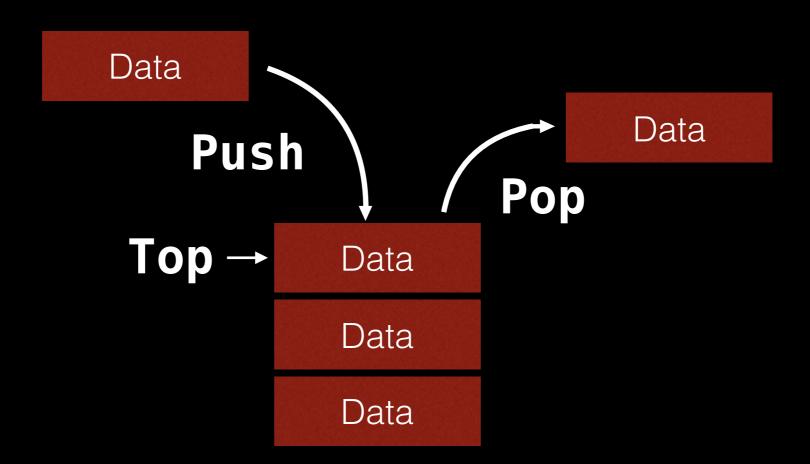
William Fiset

Outline

- Discussion about Stacks
 - What is a Stack?
 - When and where is a Stack used?
 - Complexity Analysis
 - Stack usage examples
- Implementation details
 - Pushing elements on stack
 - Popping elements from stack
- Code Implementation

DISCUSSION

A stack is a one-ended linear data structure which models a real world stack by having two primary operations, namely push and pop.



Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Apple

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
pop()
push('Lettuce')
```

Apple

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
pop()
push('Lettuce')
```

Apple



Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
pop()
push('Lettuce')
```

Onion



Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Celery



Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
pop()
push('Lettuce')
```

Celery

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')

push('Watermelon')
pop()
pop()
pop()
push('Lettuce')
```

Watermelon



Celery

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')

push('Watermelon')
pop()
pop()
push('Lettuce')
```

Watermelon

Celery

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Watermelon

Celery

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Watermelon



Celery

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Celery

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Celery

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Celery



Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Lettuce



Onion

Potato

Cabbage

Instructions

```
pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')
```

Lettuce

Onion

Potato

Cabbage

When and where is a Stack used?

- Used by undo mechanisms in text editors.
- Used in compiler syntax checking for matching brackets and braces.
- Can be used to model a pile of books or plates.
- Used behind the scenes to support recursion by keeping track of previous function calls.
- Can be used to do a Depth First Search (DFS) on a graph.

Complexity Analysis

Complexity

Pushing	0(1)
Popping	0(1)
Peeking	0(1)
Searching	O (n)
Size	0(1)

Problem: Given a string made up of the following brackets: ()[]{}, determine whether the brackets properly match.

Bracket Sequence:

 $[\ [\ \{\}\]\ (\)\]$

Current Bracket: Ø

Reversed Bracket: Ø

Bracket Sequence:

[{}]

Current Bracket: [

Reversed Bracket:]

Bracket Sequence:

[{}]()]

Current Bracket: [

Reversed Bracket:]

Bracket Sequence:

```
[[{}]()]
```

Current Bracket: {

Reversed Bracket: }

Bracket Sequence:

```
[[{}]()]
```

Current Bracket: }

Reversed Bracket: {

Bracket Sequence:

```
[[{}]()]
```

Current Bracket: }

Reversed Bracket: {

Bracket Sequence:

[[{}]()]

Current Bracket:]

Reversed Bracket: [

Bracket Sequence:

```
[[{}]()]
```

Current Bracket:]

Reversed Bracket: [

Bracket Sequence:

```
[[{}]()]
```

```
Current Bracket: (
```

Reversed Bracket:)

Bracket Sequence:

```
[[{}]()]
```

```
Current Bracket: )
```

Reversed Bracket: (

Bracket Sequence:

```
[[{}]()]
```

```
Current Bracket: )
```

Reversed Bracket: (

Bracket Sequence:

```
[[{}]()]
```

Current Bracket:]

Reversed Bracket: [

Bracket Sequence:

 $[[\{\}]()]$

Current Bracket:]

Reversed Bracket: [

Bracket Sequence:

```
[[{}]()] —— Valid
```

Current Bracket:]

Reversed Bracket: [

Bracket Sequence:

 $[\{\})[]$

Current Bracket: Ø

Reversed Bracket: Ø

Bracket Sequence:

```
[{})[]
```

Current Bracket: [

Reversed Bracket:]

Bracket Sequence:

```
[{})[]
```

```
Current Bracket: {
```

Reversed Bracket: }

```
{
```

Bracket Sequence:

```
[{})[]
```

```
Current Bracket: }
```

Reversed Bracket: {

```
{
```

Bracket Sequence:

```
[{})[]
```

Current Bracket: }

Reversed Bracket: {

Bracket Sequence:

```
[{})[]
```

```
Current Bracket: )
```

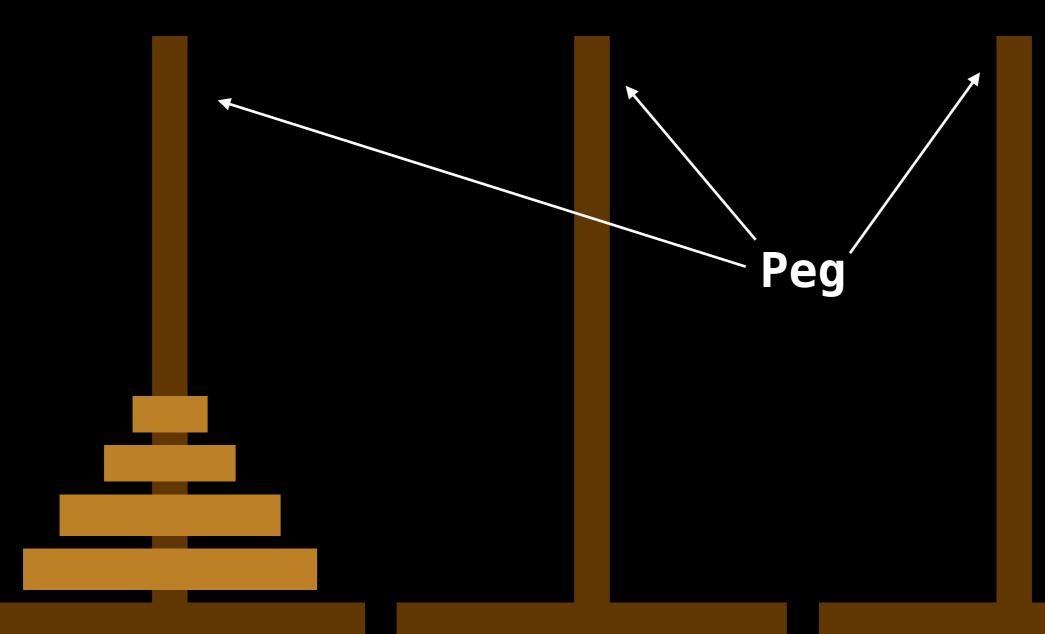
Reversed Bracket: (

Bracket Sequence:

```
Current Bracket: )
```

Reversed Bracket: (

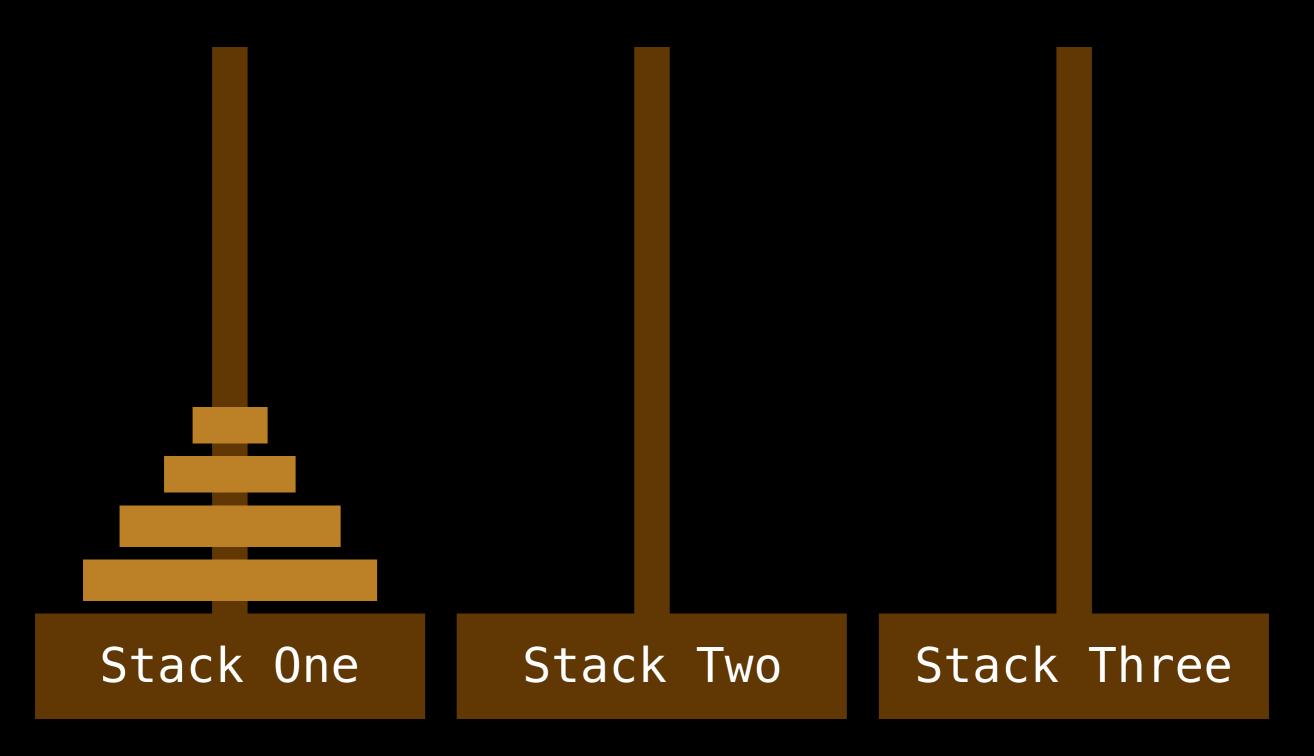
```
Let S be a stack
For bracket in bracket string:
    rev = getReversedBracket(bracket)
    If isLeftBracket(bracket):
        S.push(bracket)
    Else If S.isEmpty() or S.pop() != rev:
        return false // Invalid
return S.isEmpty() // Valid if S is empty
```

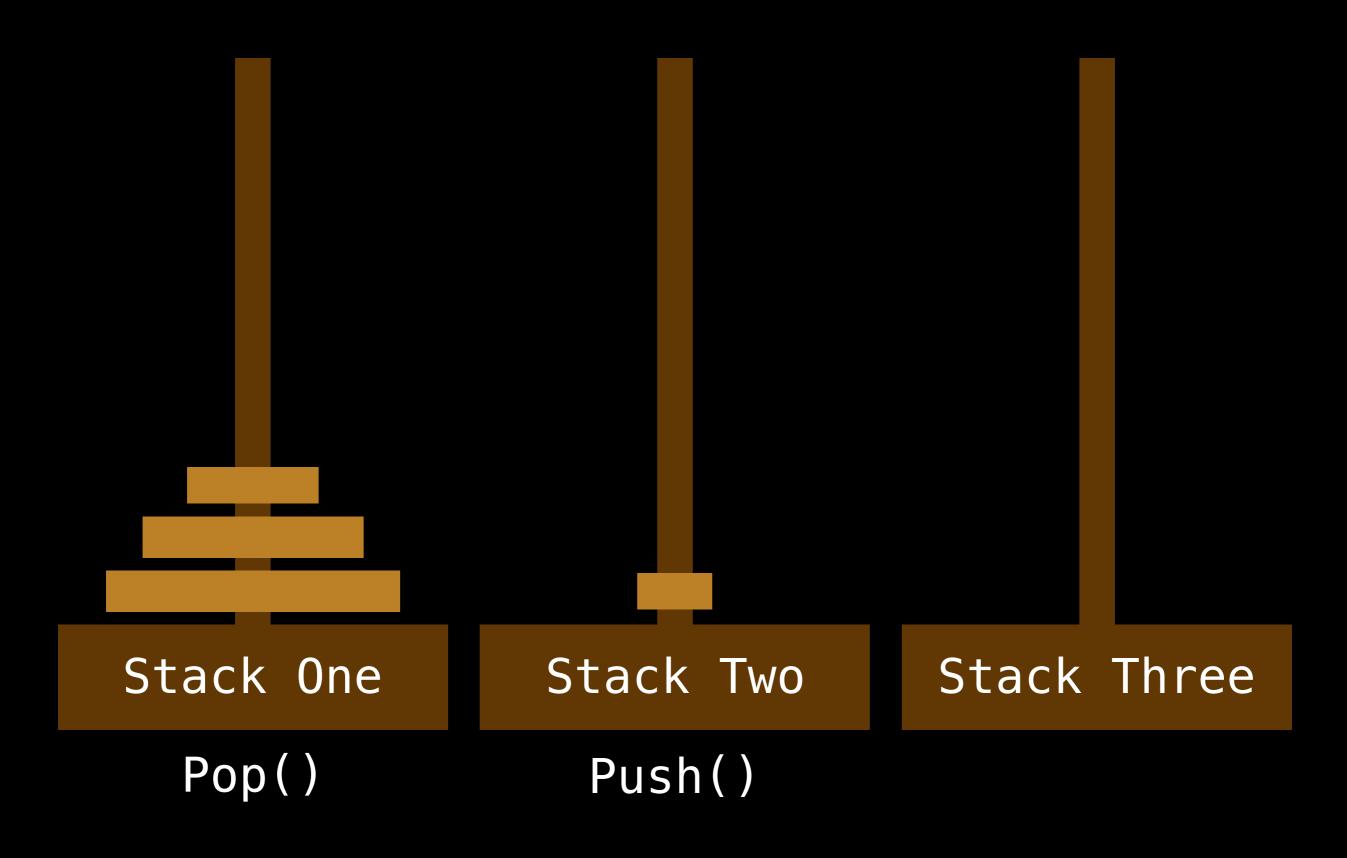


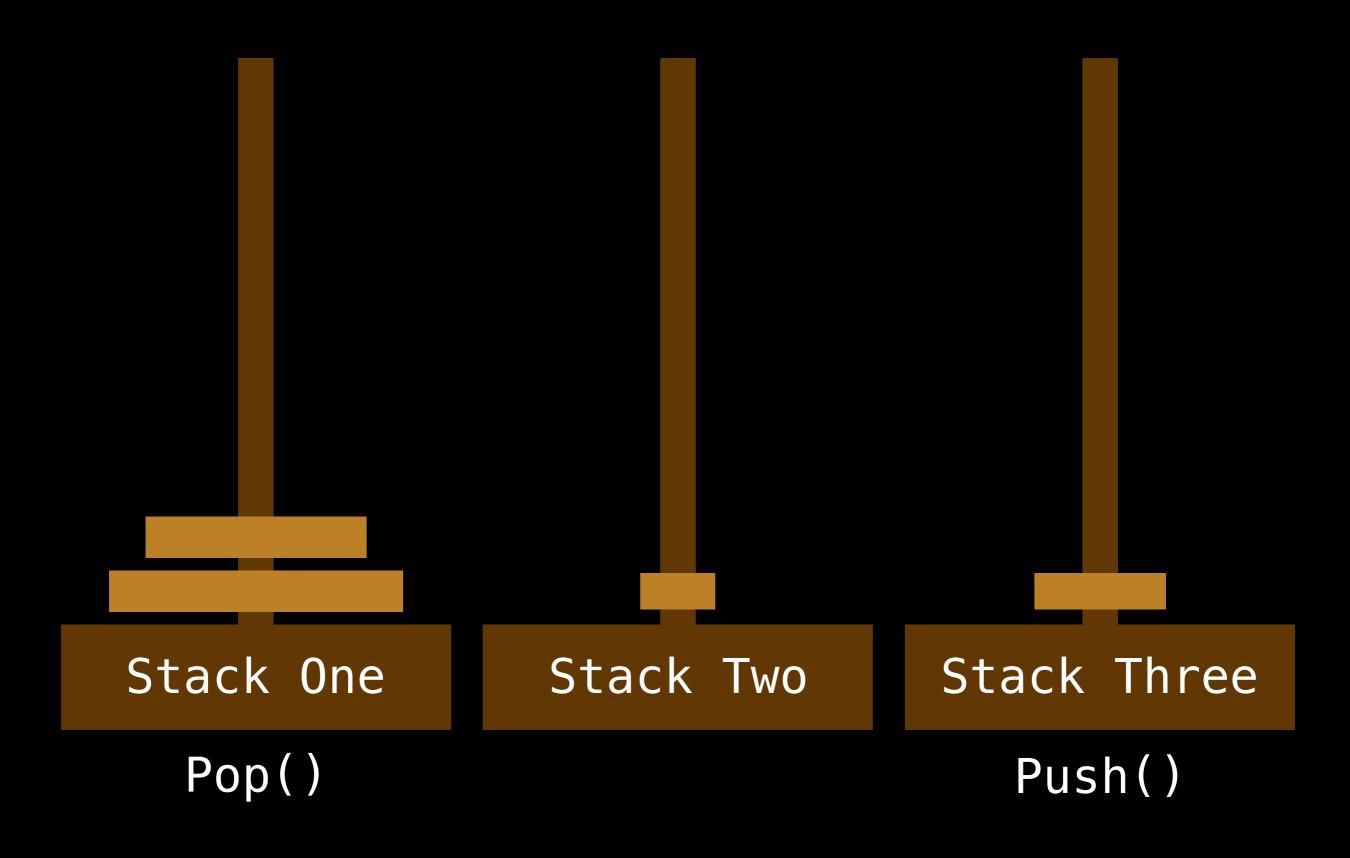
Disk Pile 1

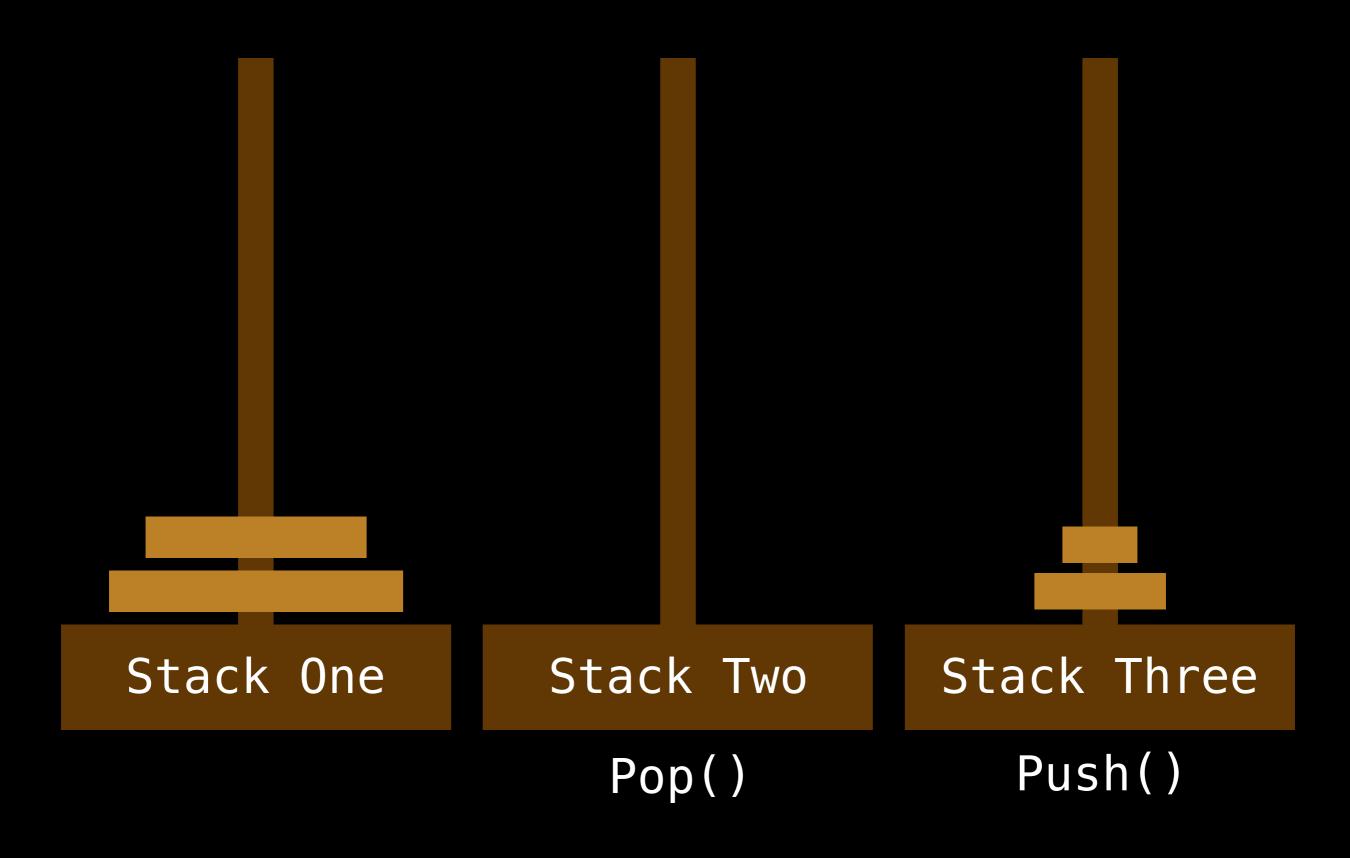
Disk Pile 2

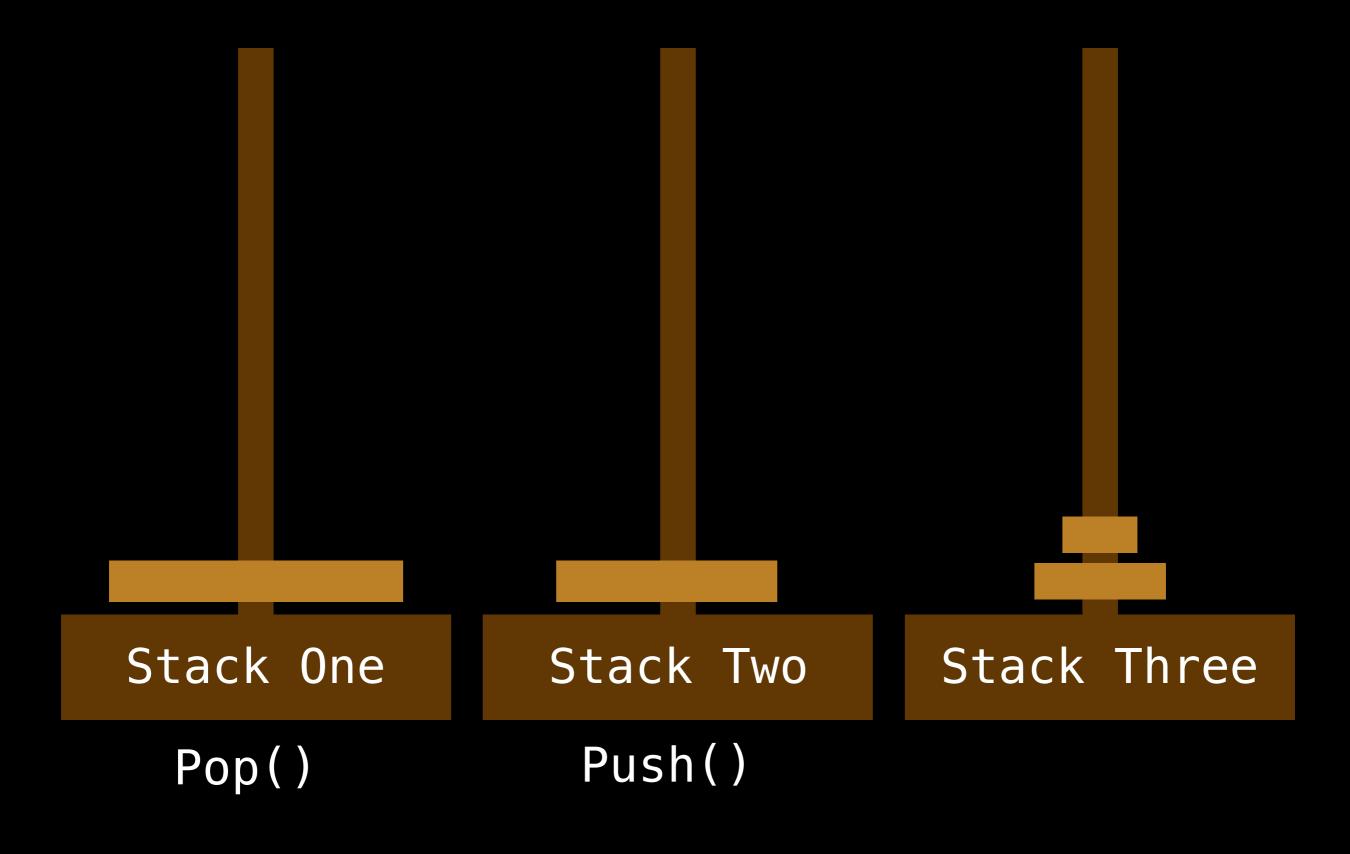
Disk Pile 3

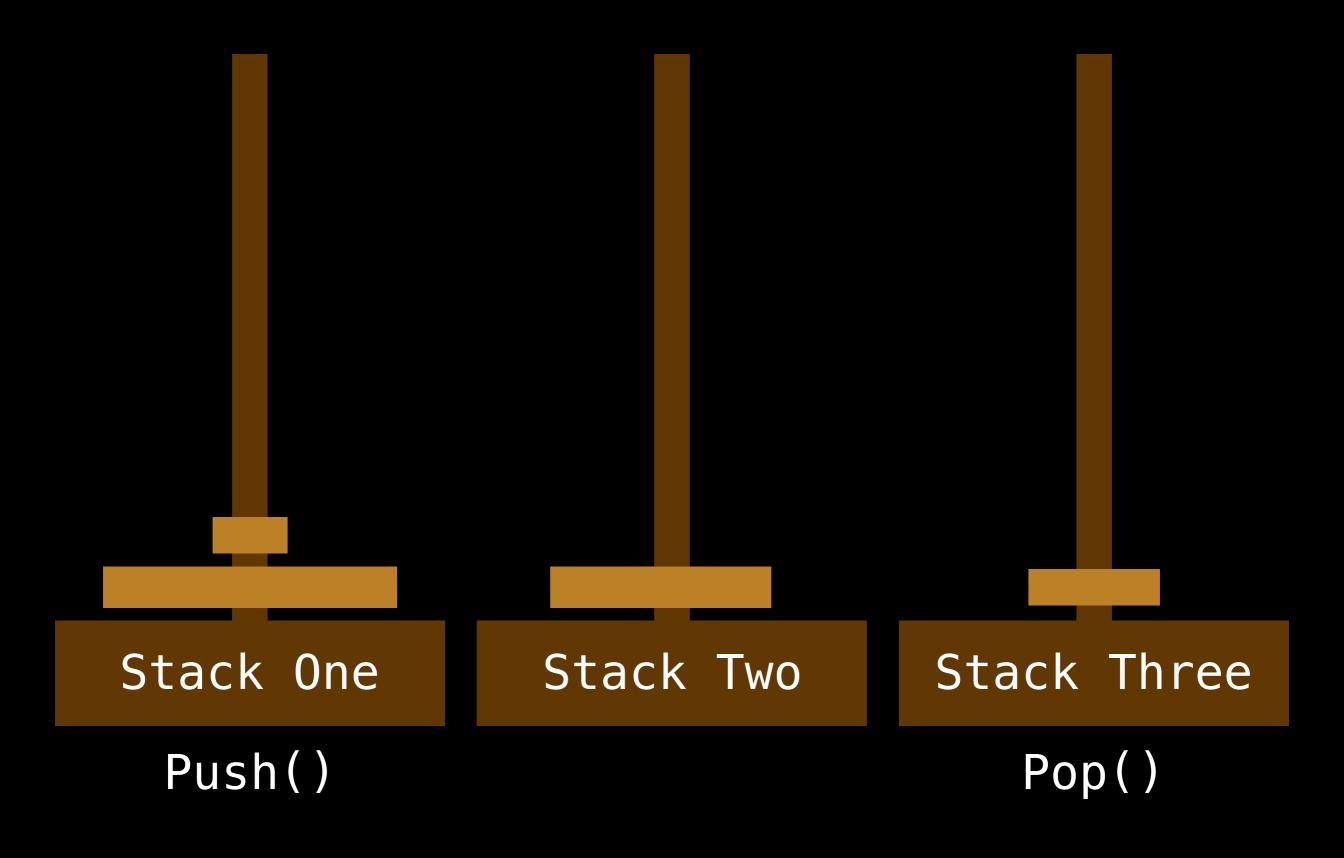


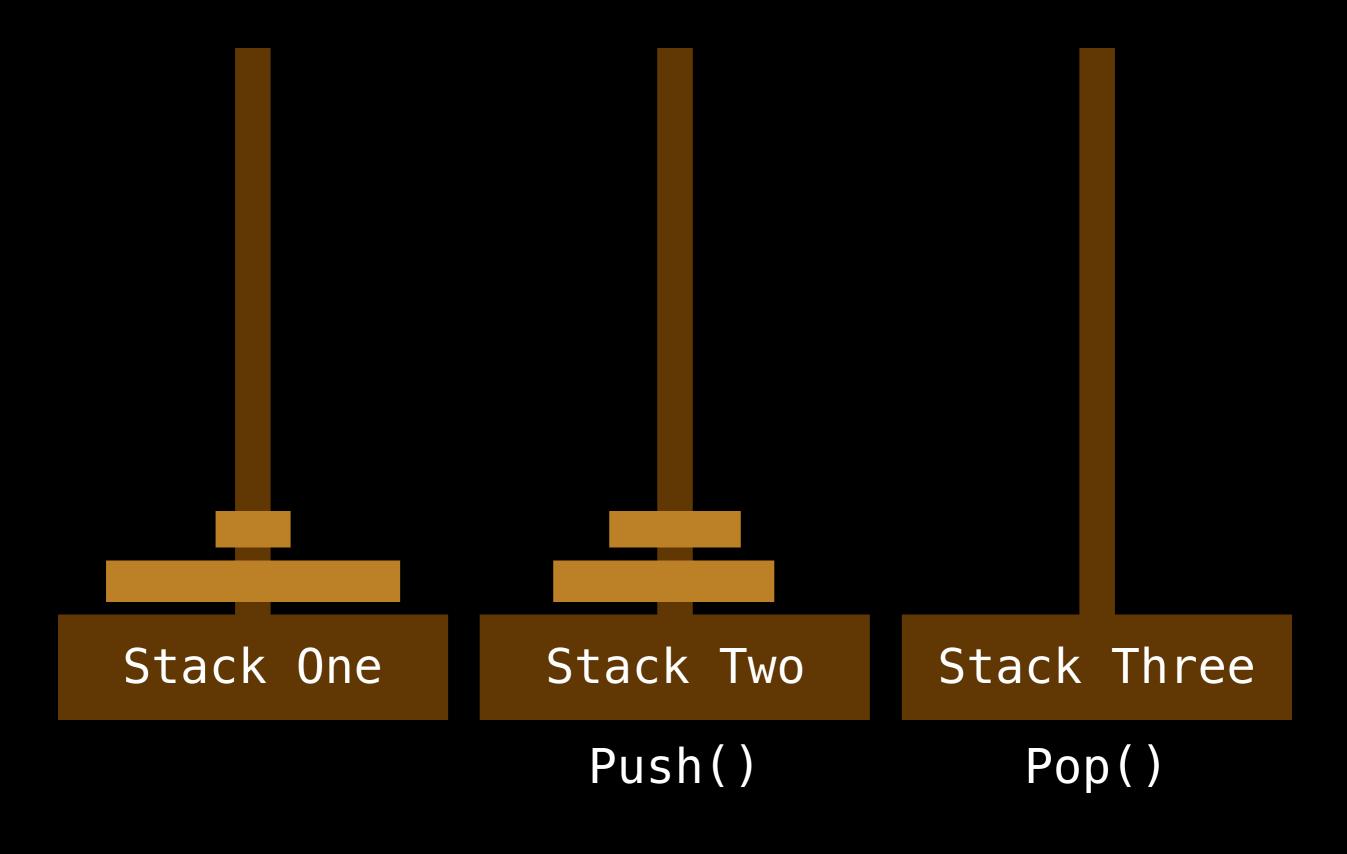


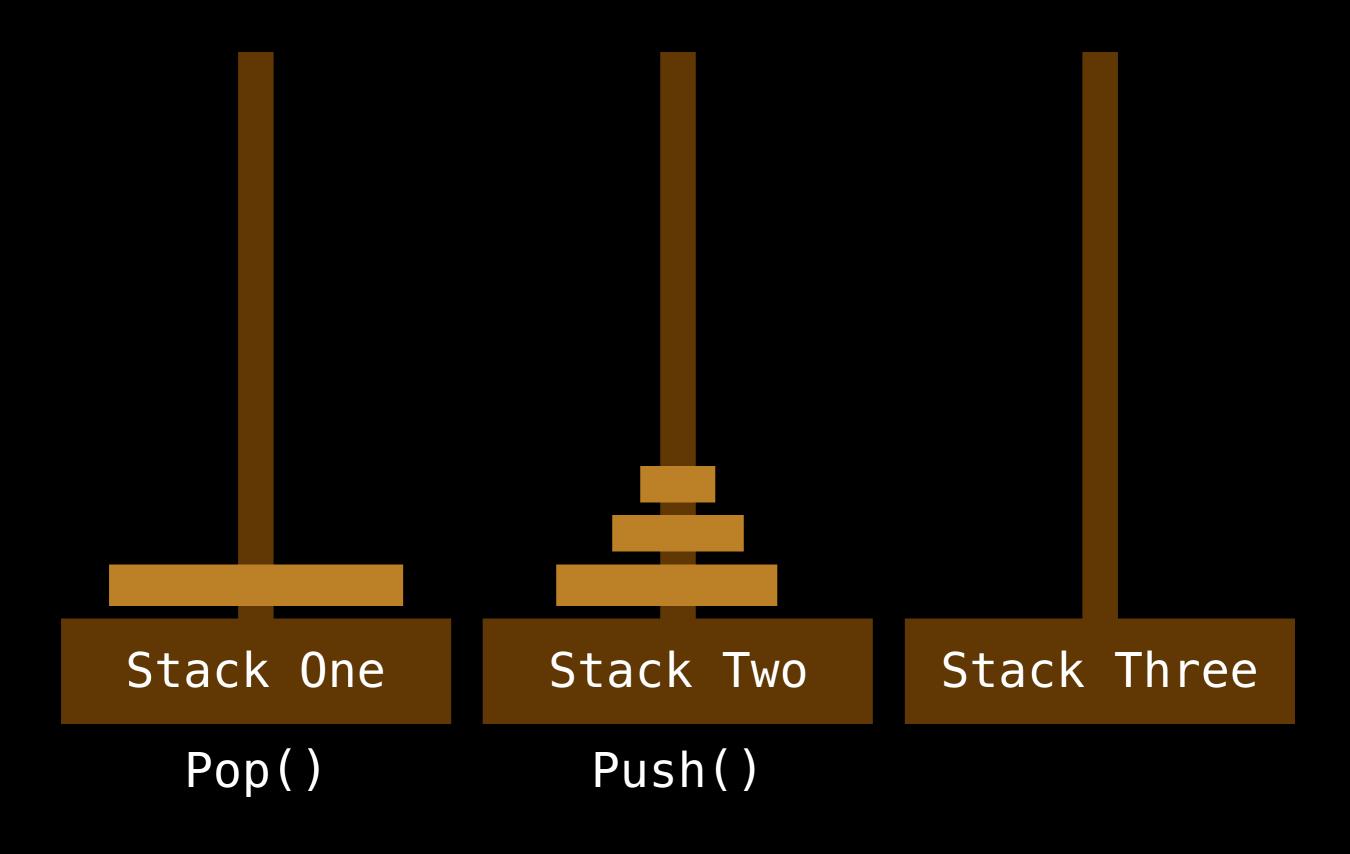


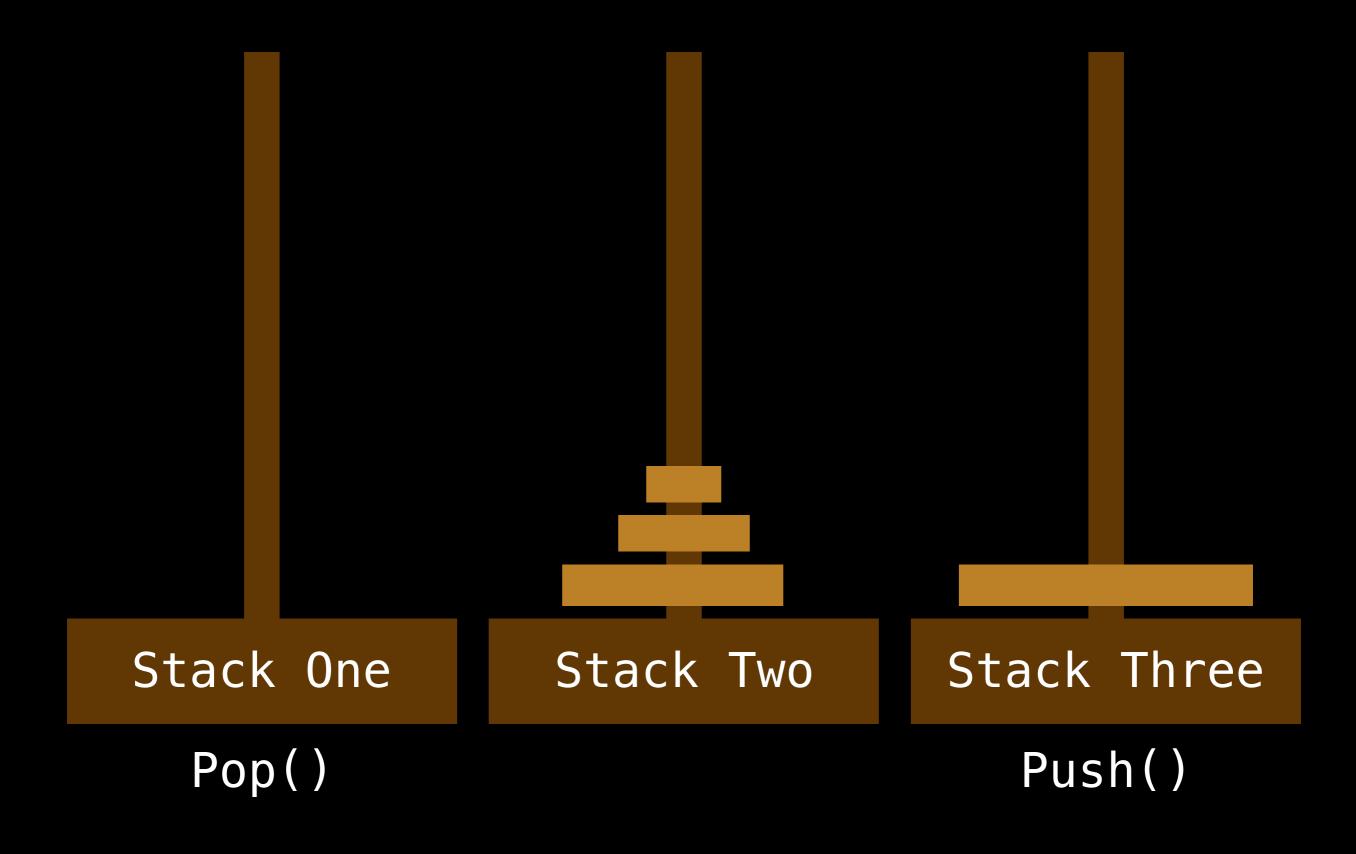


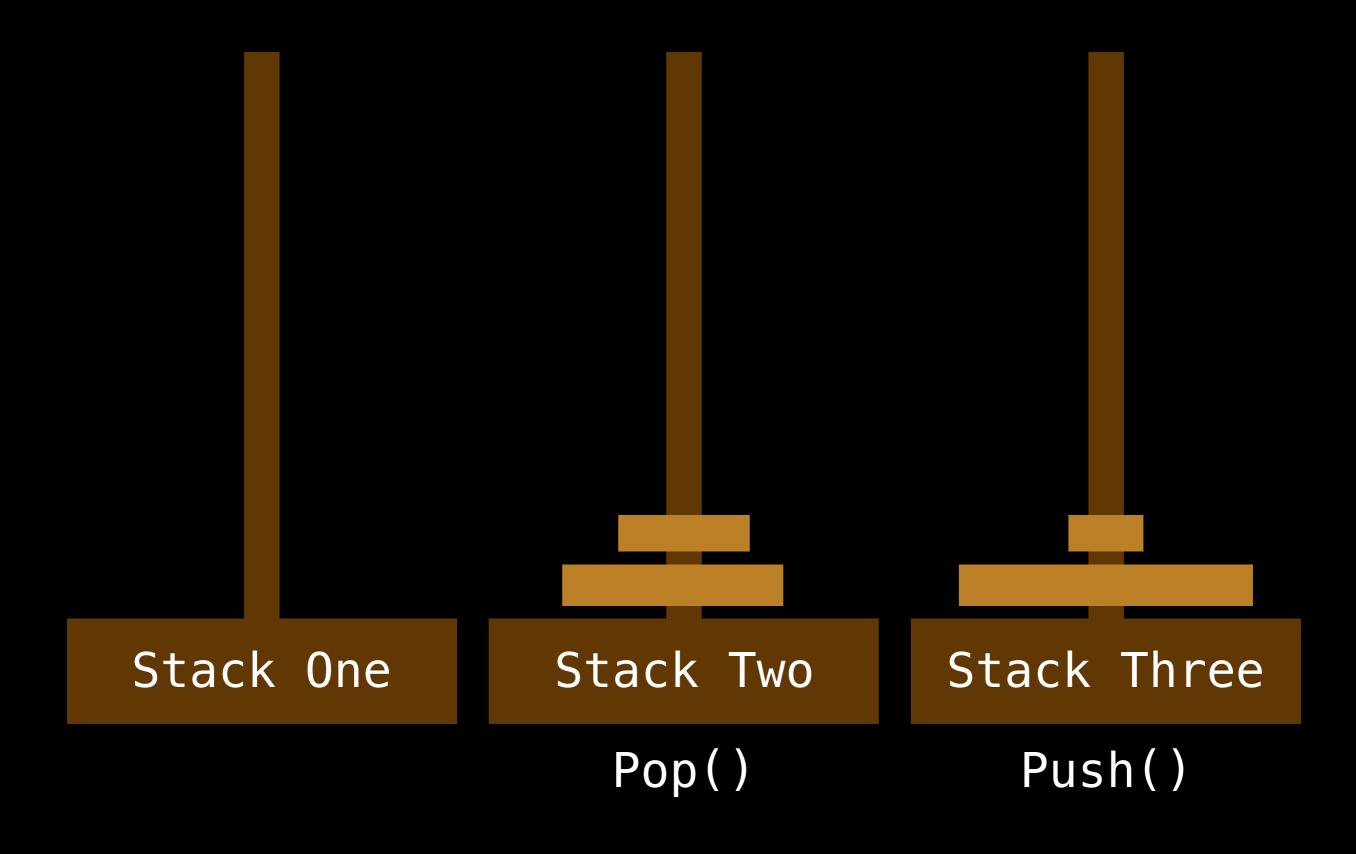


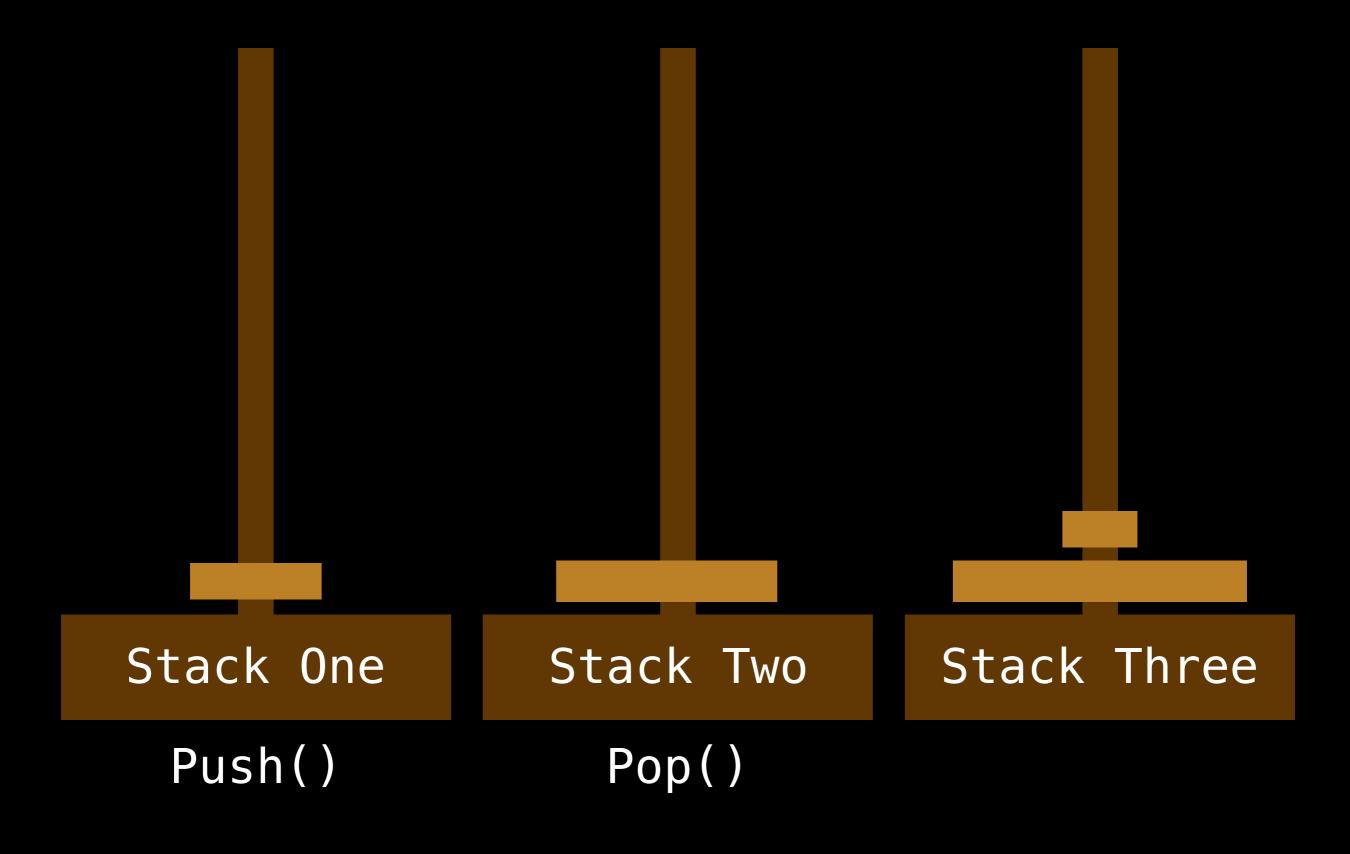


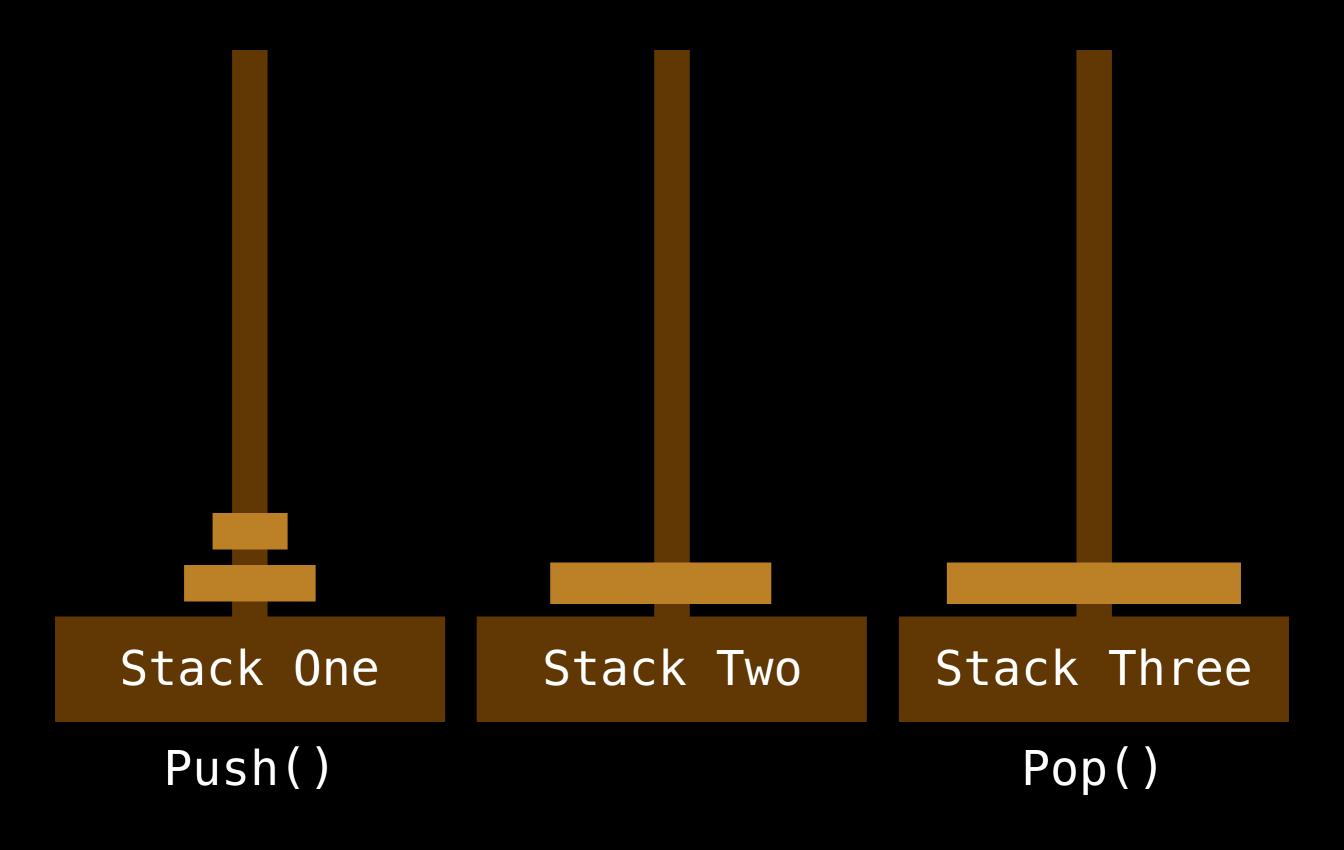


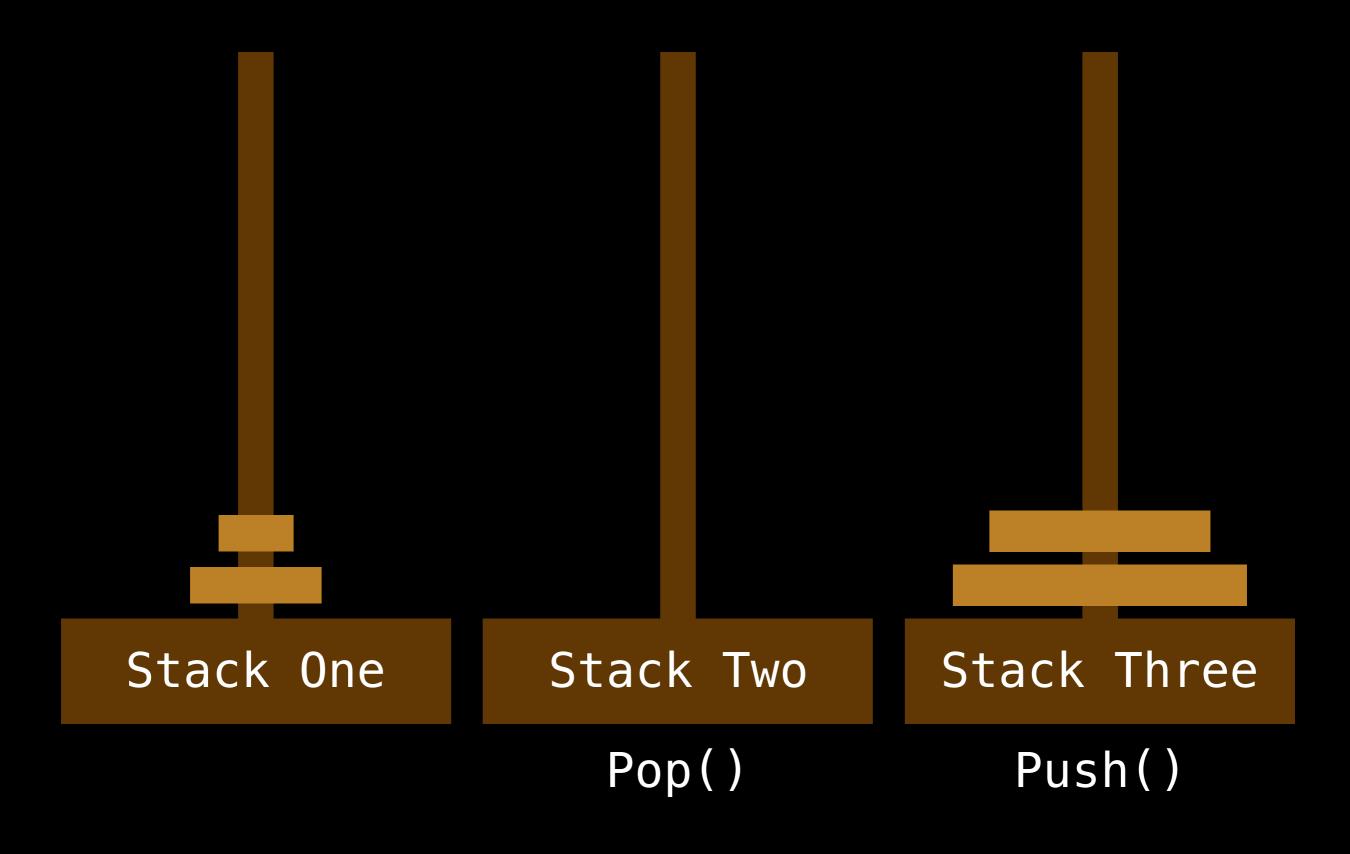


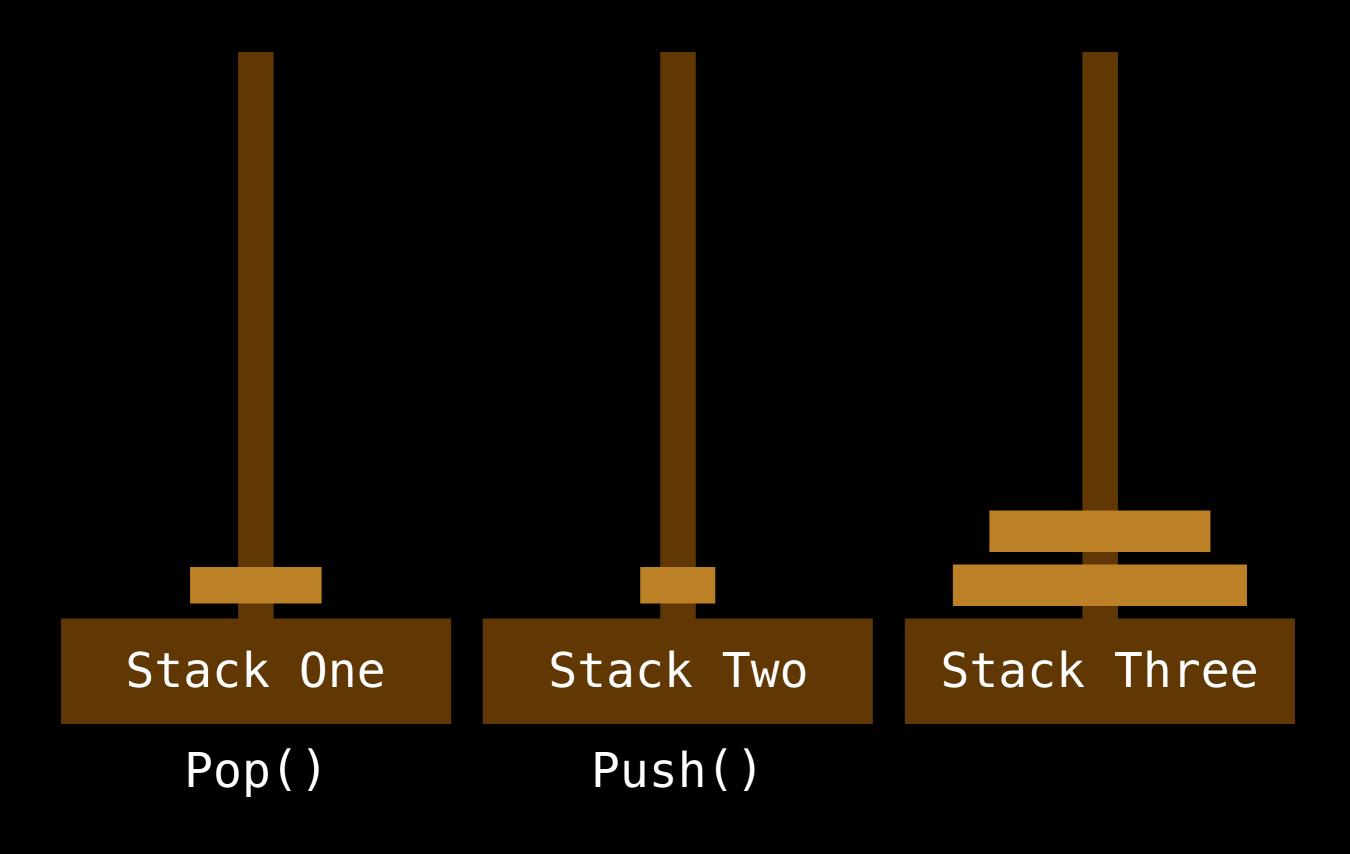


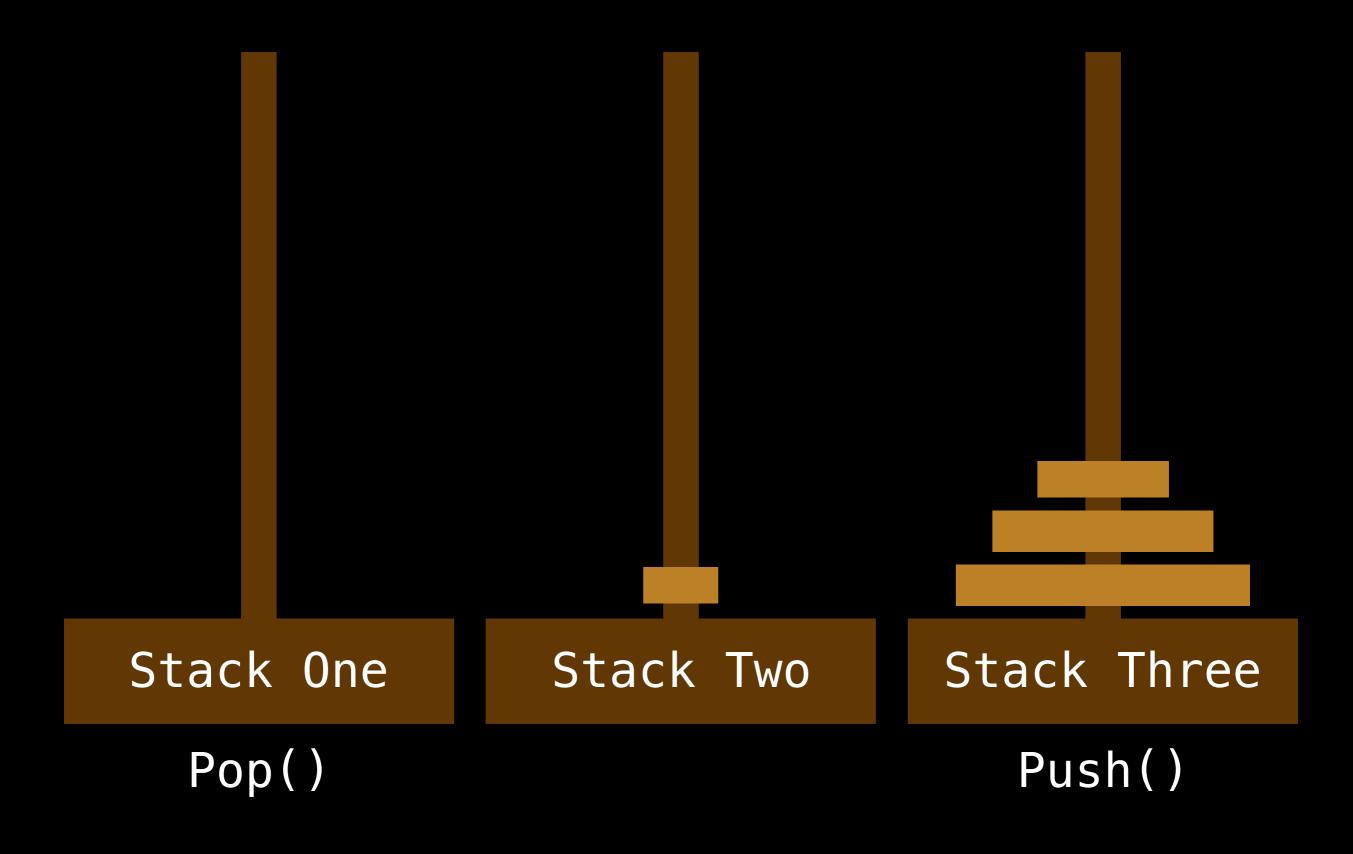


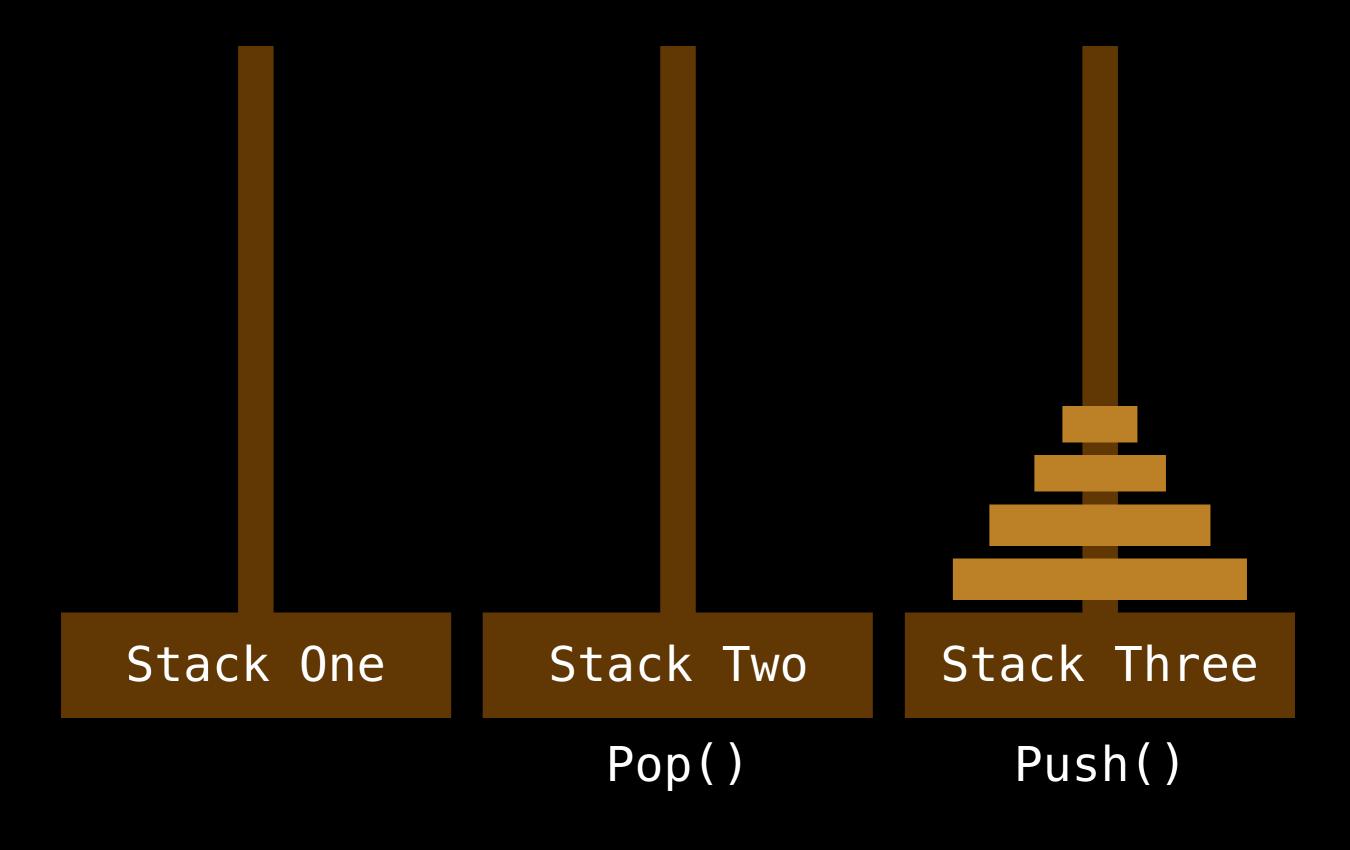


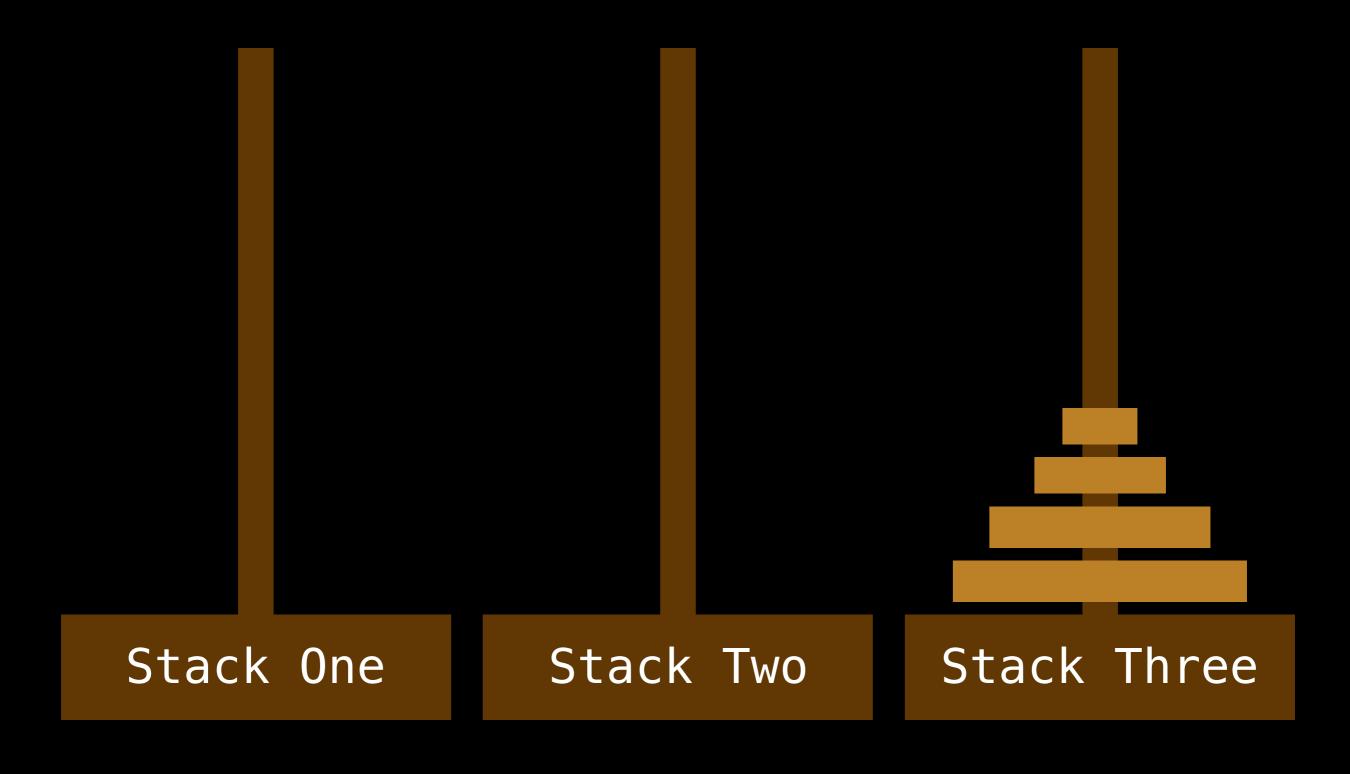












Stack Operations

William Fiset

<u>Instructions</u>

Push(4)

Push(2)

Push(5)

Push (13)

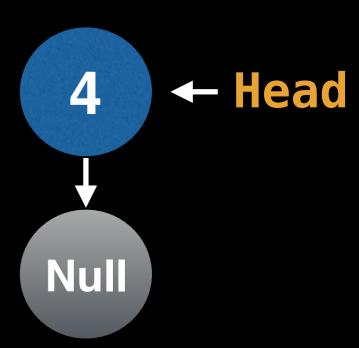
Instructions

```
Push(4)
Push(2)
Push(5)
Push(13)
```



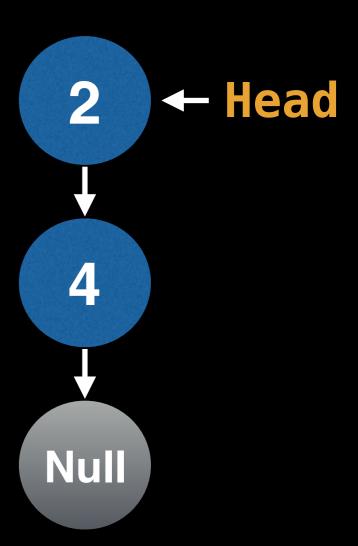
Instructions

Push(4)
Push(2)
Push(5)
Push(13)



Instructions

Push(4)
Push(2)
Push(5)
Push(13)



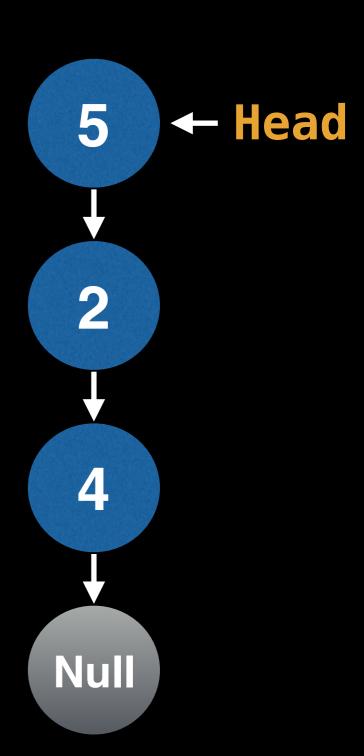
Instructions

Push(4)

Push(2)

Push(5)

Push (13)

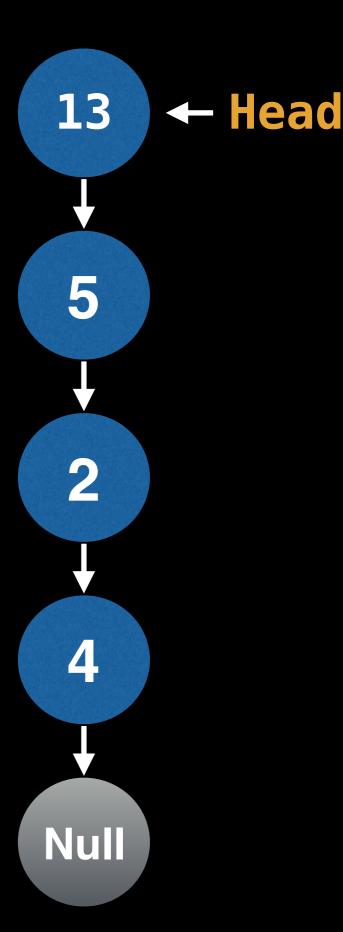


<u>Instructions</u>

Push(4) Push(2)

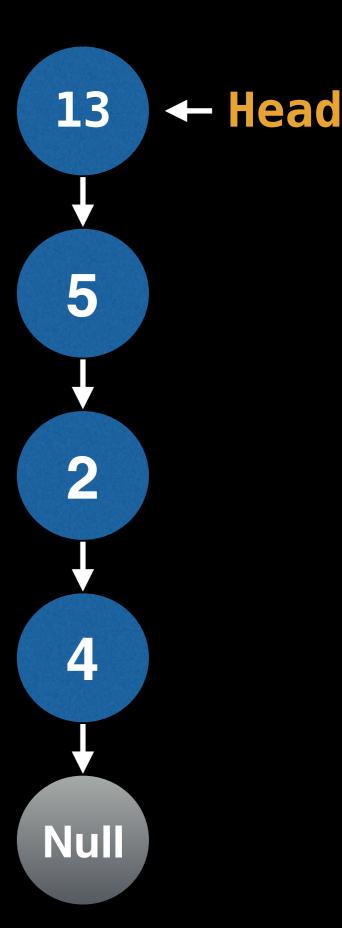
Push(5)

Push(13)



Instructions

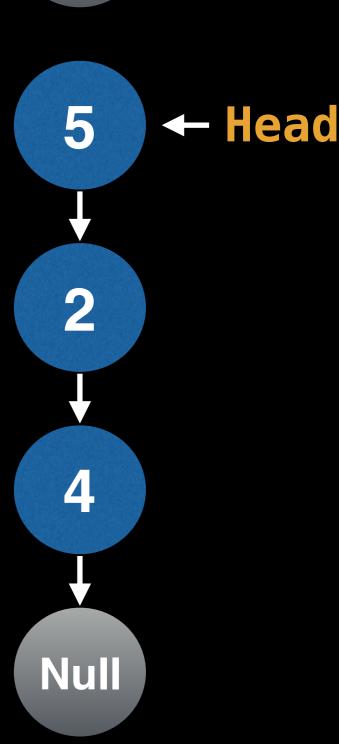
```
Pop()
Pop()
Pop()
```





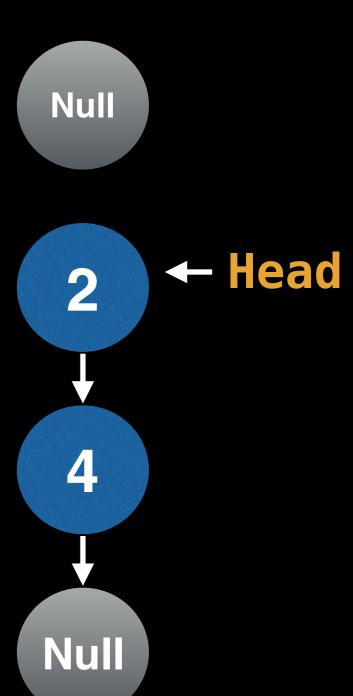
Instructions

Pop()
Pop()
Pop()
Pop()



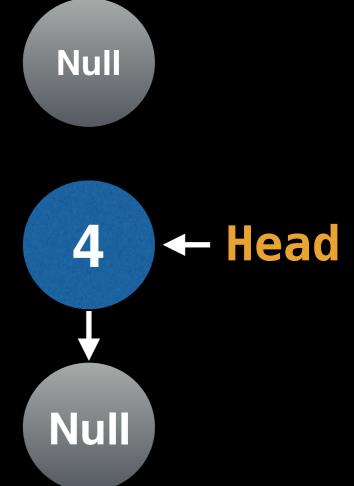
Instructions

Pop()
Pop()
Pop()
Pop()



Instructions

```
Pop()
Pop()
Pop()
Pop()
```



Instructions

Pop()
Pop()
Pop()
Pop()

Null



<u>Instructions</u>

```
Pop()
Pop()
Pop()
```

