

SM2-21st Computer Lab 4

Iterative Instructions and Applications on Numerical Algorithm and Pseudo Stochastic Process

15 Sept 2017 Friday 6:45pm
(Dinner outside LT27 at 6pm)

Unzip the **Lab4.zip** sent to you by email attachment. Please prepare for your programs in advance of the lab session.

Question 1:

The value of π can be 3.14159265. Use an iterative instruction in your C program to compute the value of the following series up to a tolerance of 10^{-8} .

$$2 - \frac{2\pi^2}{2!} + \frac{2\pi^4}{4!} - \dots + 2(-1)^n \frac{\pi^{2n}}{(2n)!}, \text{ where } n \geq 0.$$

Question 2:

The Maclaurin series of the sine function is given as follows:

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \frac{x^9}{9!} - \dots = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k+1)!} x^{2k+1}$$

Use an iterative instruction in your C program to compute the value of $\sin(135^\circ)$ up to a tolerance of 10^{-8} .

Question 3:

Refer to the lecture notes on numerical algorithm for Newton-Raphson's method. A variation for Newton-Raphson's method is the Secant's method based on two initial points and the new sliding gradient G defined as follows:

$$G(x_n) = \frac{f(x_n) - f(x_{n-1})}{x_n - x_{n-1}} \quad \text{where} \quad x_{n+1} = x_n - \frac{f(x_n)}{G(x_n)}$$

It is clear that if x_{n-1} is close to x_n , $G(x_n) \approx f'(x_n)$. Thus Secant's method can converge to Newton-Raphson's method.

- Write another C program named as **secant.c** which uses the Secant's Method to estimate the root of $f(x) = e^{2x} - x - 6$ with two initial points $x_0 = 0.25$ and $x_1 = 1.2$.
- Again, use your secant.c to estimate the value of $\sqrt[5]{37}$.
- Again, use your secant.c to estimate a solution for the equation $\cos(x) = x^3$. You can use the cosine function $\cos(x)$ in Visual C++ where x is in radian.

Same as the Newton-Raphson's Method, please take note that Secant's Method does not guarantee the convergence to the solution.

Question 4:

Write a complete C program to generate 20 random numbers which are uniformly distributed from -2.55 to 3.76.

Question 5:

Write a complete C program that uses random numbers to approximate the value of the finite integral $\int_2^5 x^2 dx$, i.e., the program will approximate the value of the area enclosed by $y = x^2$, $x = 2$, $x = 5$ and $y = 0$.

Question 6:

A biased dice has the probability distribution as shown in the following table.

Face	1	2	3	4	5	6
Probability	0.2	0.2	0.05	0.05	0.3	0.2

In every game you place a bet of \$2. If the number surfaced on the dice is 6, you win and the return will be \$4. If the surfaced number is 5, you win and the return will be \$3. If the surfaced number is 3 or 4, you get back your \$2. If the surfaced number is 1 or 2, you get back nothing. You play this game 50 times. Write a C program named as **advantage.c** which uses random numbers to estimate your total return. If the regulatory requirement for the house advantage is not more than 6%, your program should check and print on the screen whether this game has met the requirement of regulation. {House Advantage = [(Bet - Expected Return)/Bet] x 100% }

Please take note that the random numbers generated by computer is pseudo. The whole execution of your C program is not real stochastic. It is actually a pseudo stochastic process.

The lab time is only two hours. Please prepare for your programs in advance.

- A/Prof Tay