Simulate ABW Z-call sigmoid and estimate signal's covariance matrix

In this code:

- 1. First, the Z-call sigmoid is simulated based on FX. Socheleau 2015 JASA paper.
- 2. then, the covariance matrix of the signal is evaluated as a first part of the SMF application

```
clearvars
close all
clc
addpath ../Functions
```

Choose if the output is saved or not

```
Save = 'On';
disp(['Save is: ' Save])
Save is: On
```

Sigmoid parameters

Here, for ABW call detection, the parametric model described in (Socheleau, 2015) is used. It is based on the complex form of an acoustic signal $s(n) = a(n)e^{j\varphi(n)}$, with a(n) the time-varying amplitude and $\varphi(n)$ the time-varying phase. From the definition of the instantaneous frequency and its parametric expression as a fuction of the (continuous) time

$$f(t) = f_c + \frac{1}{2\pi} \frac{d\varphi(t)}{dt} = f_c + L + \frac{U - L}{1 + e^{\alpha(t - M)}},$$

it is possible to derive the expression of the time-varying phase $\varphi(n)$, where n, denotes the discrete time, as

$$\varphi(n) = 2\pi \left(L \frac{n}{f_s} + \frac{U - L}{\alpha} \ln \left(\frac{1 + e^{-\alpha M}}{\frac{\alpha(n - M)}{f_s}} \right) \right) + \varphi_0,$$

where $f_c = 22.6$ Hz is the central frequency in the [15-30]Hz bandwidth, L and U are respectively linked to the lower and upper asymptotes of the Z-call, M represents the time shift and α the grow rate. The amplitude a(n), is set to vary in accordance with the energetic difference between unit A and C.

Definition of the different constants

```
fs = 100 ; % (Hz) sampling frequency

Tz = 20 ; % (s) duration of an ABW call
tz = 0:1/fs:Tz; % time axis
```

```
N = length(tz); % number of samples

fc = 22.6; % (Hz) Z-call center frequency
alpha = 1.8; % slope

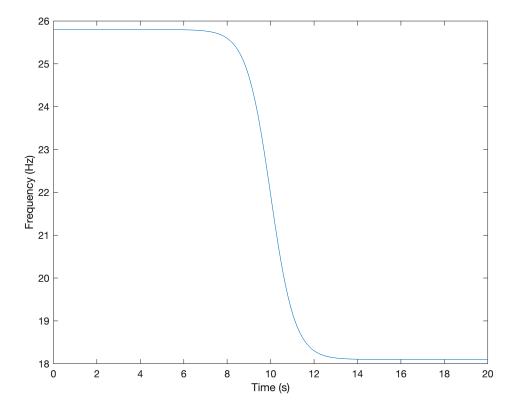
L = -4.5; % (Hz) Lower assymptote
U = 3.2; % (Hz) Upper asymptote
M = Tz/2; % (s) time at half of the slope
```

Instantaneous frequency

This section is not mandatory, it can just be used to visualize the result simulated call

```
f_whale = zeros(length(L),N);
for i = 1:length(L)
    f_whale(i,:) = fc + L(i) + ((U(i)-L(i))./(1+exp(alpha*(tz-M(i)))));
end

figure
plot(tz,f_whale)
xlabel('Time (s)')
ylabel('Frequency (Hz)')
```



Estimation of the time-varying phase

```
adj = fc - 8.5; % Compared to the Socheleau paper, the sigmoid has to be
% shifted in frequency to match the Z-call signal
```

```
L = L-adj; % Lower asymptote (Hz)
U = U-adj; % Upper asymptote (Hz)
% Phase calculation
n = 0:N-1; % Sample axis
phase_whale = 2*pi*(L*n/fs + ((U-L)/alpha) * ...
log((1+exp(-alpha*M))./(1+exp(alpha*(n/fs-M))));
phase_whale = phase_whale(end:-1:1); % Reverse in time to have it from high to low if
% Temporal signal
s_whale = exp(1j*phase_whale);
s_whale = real(s_whale/max(abs(s_whale)));
% Amplitude variation through time
amplitude = [ones(1,round(N/2)-1) ones(1,round(N/2))*0.95];
s_whale = amplitude.*s_whale;
s_whale = s_whale/max(abs(s_whale));
```

Covariance matrix estimation

```
[covs,vecs] = SMF_sig_preprocess(s_whale);
```

Save matrices

```
switch Save
    case 'On'
        save('../Offline_saved/s_whale.mat', 's_whale','covs','vecs')
        disp('Matrices saved in: Offline_saved/s_whale.mat')
    case 'Off'
        disp('Matrices not saved')
    otherwise warning('Uknown Save command - matrices not saved')
end
```

Matrices saved in: Offline_saved/s_whale.mat