

Fall 2020

## Strategic Interaction Over Time

- Last topic: Strategic interaction in static setting.
  - But in practice, many interactions occur dynamically over time.
- Dynamic games: Games where players play the game over and over, and move either repeatedly or sequentially.

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- A set of small navigation icons typically found in Beamer presentations, including symbols for back, forward, search, and other slide controls.

# Outline

- 1 Repeated Games
- 2 Sequential Games
- 3 Deterring Entry
- 4 Cost and Innovation Strategies
- 5 Disadvantages of Moving First
- 6 Behavioural Game Theory

# Repeated Games

- A repeated game is a game in which a static *constituent* game is repeated a finite and pre-specified number of times, or is repeated indefinitely.
- We still need to know:
  - Players
  - Rules
  - Information
  - Payoffs
- Key difference from a static game: How we think about actions and strategies.

# Repeated Games

- In a repeated game:
  - An action is a single move that a player makes at a specified time, such as choosing an output level or a price.
  - A strategy is a battle plan that specifies the *full set* of actions that a player will make throughout the game.
    - It may involve actions that are conditional on prior actions of other players, or on new information available at a given time.

# Repeated Games

- As an example, we will revisit game between American and United.
- Recall: The Nash equilibrium in the static game is both firms producing high (64k passengers) and making \$4.1 million.

# Repeated Games

		<b>American Airlines</b>	
		$q_A = 64$	$q_A = 48$
<b>United Airlines</b>	$q_U = 64$	4.1	3.8
	$q_U = 48$	5.1	4.6

*Note:* Quantities are in thousands of passengers per quarter; (rounded) profits are in millions of dollars per quarter.



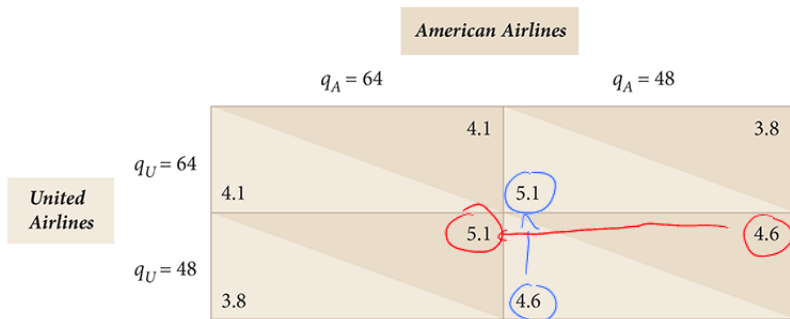
# Repeated Games

- Now assume that the same game gets repeated indefinitely.
  - Now firms must consider both current and future profits.
- With repetition, the outcome may be different than in the static game.
  - Depends on the strategies used by the firms.

# Repeated Games

- Suppose, for example, that American adopts the following strategy:
  - It cheap-talks United that it will produce the collusive or cooperative quantity of 48k in the first period.
  - But its subsequent decisions depend on United:
    - If United produces 48k in period  $t$ , American will produce 48k in period  $t + 1$ .
    - If United produces 64k in period  $t$ , American will produce 64k in period  $t + 1$ .
- What is United's best response to this strategy?

# Repeated Games



Note: Quantities are in thousands of passengers per quarter; (rounded) profits are in millions of dollars per quarter.

remember: gains to deviation for  
United or for American in the static  
game

# Repeated Games

Choice is now 4.6 forever vs 5.1 once and then 4.1 forever  
 NPV of 92 vs 83.2  
 NPV of 46 vs 42.4

		<b>American Airlines</b>	
		$q_A = 64$	$q_A = 48$
<b>United Airlines</b>	$q_U = 64$	4.1	3.8
	$q_U = 48$	3.8	4.6

Handwritten annotations on the table:  
 - The value 5.1 in the top-right cell is circled in blue.  
 - The value 5.1 in the bottom-left cell is circled in red.  
 - The value 4.6 in the bottom-right cell is circled in red.  
 - A red line connects the 5.1 in the bottom-left cell to the 4.6 in the bottom-right cell.  
 - Blue arrows point from the 5.1 in the top-right cell to the 5.1 in the bottom-left cell and to the 4.6 in the bottom-right cell.

Note: Quantities are in thousands of passengers per quarter; (rounded) profits are in millions of dollars per quarter.

remember: gains to deviation for  
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# Repeated Games

- The equilibrium of the repeated game between American and United is an example of a collusive outcome.
- In most modern economies, explicit collusion is illegal.
  - However, antitrust and competition laws typically do not strictly prohibit choosing the cooperative (or cartel) quantity or price as long as no explicit agreement is reached.
  - Firms may be able to engage in implicit collusion or tacit collusion using trigger, tit-for-tat, or other similar strategies, as long as firms do not explicitly communicate with each other.
    - Tacit collusion lowers society's total surplus just as explicit collusion does.

# Repeated Games

- Sustaining the cooperative outcome requires that players believe the game will repeat for ever.
- if there is a known end to the game, and players have complete foresight, the cooperation can be impossible to maintain.



- To see this, suppose that American and United know that they will play the game a finite number of times ( $T$ ).
- Suppose both firms use the trigger strategy that sustained collusion when the game was infinitely repeated.
- Now, the trigger strategy does not lead to a Nash Equilibrium.
- Why not?

# Repeated Games

		<b>American Airlines</b>	
		$q_A = 64$	$q_A = 48$
<b>United Airlines</b>	$q_U = 64$	4.1	3.8
	$q_U = 48$	5.1	4.6

*Note:* Quantities are in thousands of passengers per quarter; (rounded) profits are in millions of dollars per quarter.

# Repeated Games

- When the game is repeated a finite number of times, the only Nash Equilibrium is for both firms to produce a high level of output in all periods.
  - There is no cooperation again.

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- So far, we've maximized strategic interactions where players make simultaneous decisions.
- But in many interactions, players alternate moves.
- We can model this type of strategic interaction as a sequential game.

## Stackelberg Oligopoly

- As an example, we will again revisit the interaction between American and United, but we will now assume that the firms move sequentially in two stages:
  - First, American (the leader) chooses its output level.
  - Second, United (the follower) chooses its output level.
- This is an example of a Stackelberg oligopoly.
  - Stackelberg oligopoly involves one leader and one or more followers.

# Stackelberg Oligopoly

		American Airlines		
		$q_A = 96$	$q_A = 64$	$q_A = 48$
United Airlines	$q_U = 96$	0 0	2.0 3.1	2.3 4.6
	$q_U = 64$	3.1 2.0	4.1 4.1	3.8 5.1
	$q_U = 48$	4.6 2.3	5.1 3.8	4.6 4.6

Note: Quantities are in thousands of passengers per quarter; (rounded) profits are in millions of dollars per quarter.

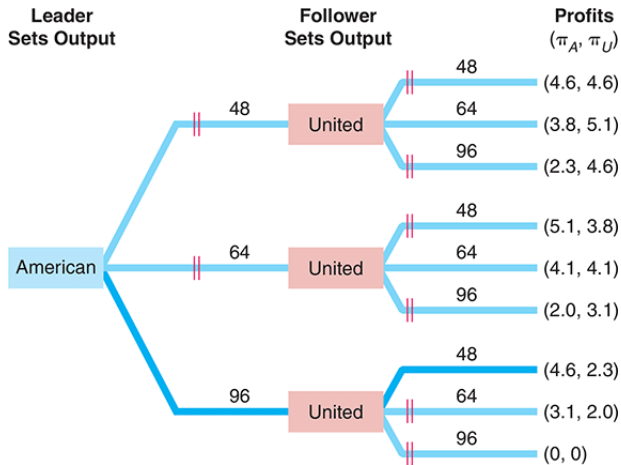
Figure: Payoffs in the Stackelberg game

# Decision trees

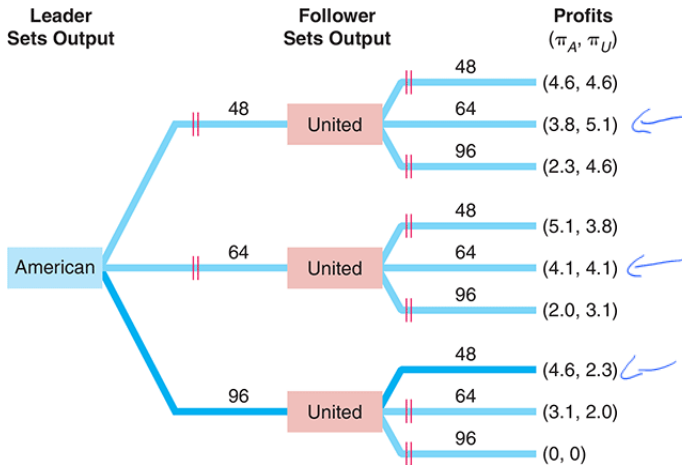
- Key issue with the payoff matrix:
  - It does not show the sequential nature of the game.
- We can better illustrate the game using an extensive form diagram.
  - Also known as a game tree, or a decision tree.
  - The extensive form is a branched diagram that shows the players, the sequence of moves, the actions players can take at each move, the information that each player has about previous moves, and the payoff function over all possible strategy combinations.



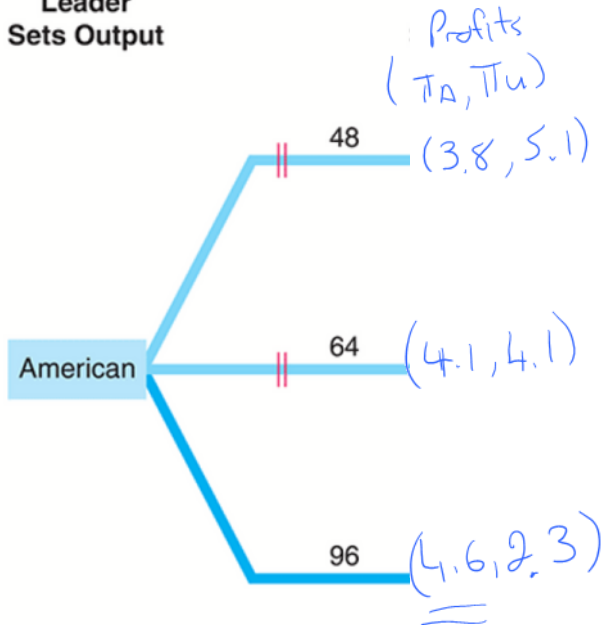
# Stackelberg Game Tree



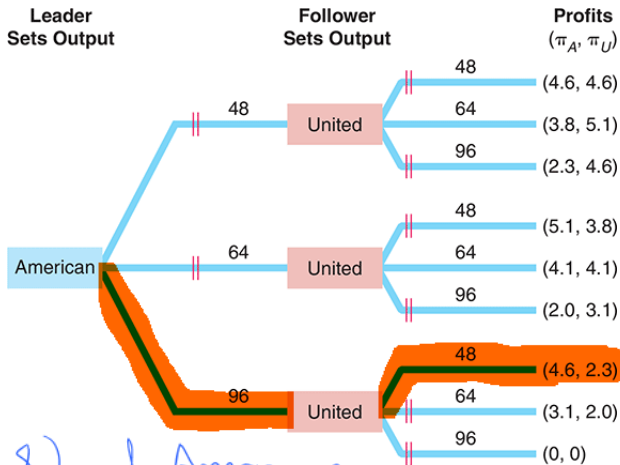
# Stackelberg Game Tree



Leader  
Sets Output



# Stackelberg Game Tree



SPNE is (96, 48) and American earns 4.6m to United's 2.3m

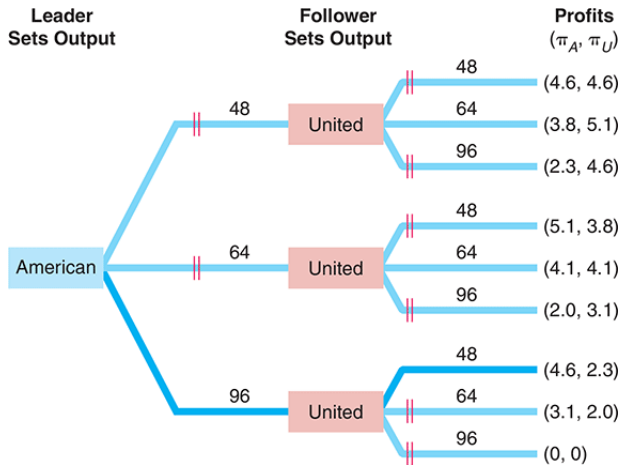
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# Subgame Perfection



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- Entry Deterrence
- Sports - a golf or tennis match
- Limit pricing
- Innovation and R&D
- Bargaining