



BUEC 311: Business Economics, Organization and Management

Problem Set #5

Consumer Preferences

October 22, 2021

1. Suppose that Jim is contemplating whether to spend the money to buy a promotional ski card for this upcoming season. His utility function for skiing and all other goods is given by $U = x \cdot s + x$, such that his marginal utility for skiing is given by $U_s = x$ and his marginal utility for other consumption is $U_x = s + 1$. Assume that he has \$500 of disposable income to allocate across these goods, and that the price of a daily lift ticket is \$100. Use a price of \$1 for the indexed other goods (i.e. the budget constraint has intercept at $x=500$ and $s=5$.)
 - a) With no promotional discount, and assuming he can only ski full days, how many days should Jim ski this year?
 - b) Now assume that a promotional card costs \$50 but offers half price lift tickets? Should Jim buy the card?
 - c) How many days will he ski once he has purchased the card?
 - d) Now, let's ask a different question. Jim is contemplating a change of job that will give him more disposable income but will mean he is near to a more expensive ski hill. If lift ticket prices are more expensive (\$150 per ticket) and the job offers him \$100 more in disposable income, will Jim end up better off, indifferent or worse off. Assume he can only ski full days.
 - e) If Jim can ski half days for \$75 per ticket, will he be indifferent, better off or worse off with the new job and \$600 in disposable income?
 - f) If Jim can ski half days, but at a higher price of \$100 per ticket, will he be indifferent, better off or worse off with the new job and \$600 in disposable income?

$$U = x \cdot s + x \quad Y = 500 = P_s s + x$$

$$\frac{\partial U}{\partial s} = x \quad \frac{\partial U}{\partial x} = s + 1$$

a) Two conditions

$$\frac{MU_s}{P_s} = \frac{MU_x}{P_x} \quad Y = P_s s + x$$

$$Y = 500, P_s = 100 \quad Y = P_s s + P_s (s+1)$$

$$\frac{x}{P_s} = s+1 \quad \uparrow = P_s (2s+1)$$

$$x = P_s (s+1)$$

$$500 = 100s + 100(s+1)$$

$$= 200s + 100$$

$$400 = 200s$$

$$s = 2, x = 300$$

$$U = 2 \cdot 300 + 300 = 900$$

$$b) 450 = 50s + 50(s+1)$$

$$= 100s + 50$$

$$400 = 100s$$

$$s = 4, x = 250$$

$$U = x \cdot s + x$$

$$\Rightarrow 4 \cdot 250 + 250$$

$$= 1250 \text{ w card}$$

\therefore yes to card.

$$d) 600 = 150s + 150(s+1)$$

$$600 = 300s + 150$$

$$450 = 300s$$

$$s = 1.5 \quad \begin{matrix} s=1 \\ U=450+450 \end{matrix}$$

$$x = 375 \quad \begin{matrix} s=2 \\ U=2 \cdot 300(2) + 300 \end{matrix}$$

$$e) U = 1.5(375) + 375 = 937.5$$

$$f) U = 350(1.5) + 350 = 875$$