

2.6 Long Run Industry Equilibrium - Practice Problems

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The supply of bicycle rentals in a small town is given by:

$$q_S = 10p - 200$$

1. Find the inverse supply function.

Solve the supply function for p :

$$\begin{array}{ll} q_S = 10p - 200 & \text{The supply function} \\ q_S - 10p = -200 & \text{Subtracting } 10p \\ -10p = -200 - q_S & \text{Subtracting } q_S \\ p = 20 + \frac{1}{10}q_S & \text{Dividing by } -10 \end{array}$$

2. What is the price elasticity of supply at a price of \$25.00?

First we use the supply function and find q_S when $p = 25$:

$$\begin{array}{ll} q_S = 10p - 200 & \text{The supply function} \\ q_S = 10(25) - 200 & \text{Plugging in } 25 \\ q_S = 250 - 200 & \text{Multiplying} \\ q_S = 50 & \text{Subtracting} \end{array}$$

Now we know the price, quantity, and slope, so we can use the elasticity formula.

$$\begin{array}{ll} \epsilon_S = \frac{1}{\text{slope}} \times \frac{p}{q_S} & \text{The formula for elasticity} \\ \epsilon_S = \frac{1}{\frac{1}{10}} \times \frac{25}{50} & \text{Plugging in} \\ \epsilon_S = 10 \times 0.5 & \text{Simplifying} \\ \epsilon_S = 5 & \text{Multiplying} \end{array}$$

This is relatively elastic.

3. What is the price elasticity of supply at a price of \$50.00?

First we use the supply function and find q_S when $p = 50$:

$$q_S = 10p - 200 \quad \text{The supply function}$$

$$q_S = 10(50) - 200 \quad \text{Plugging in 25}$$

$$q_S = 500 - 200 \quad \text{Multiplying}$$

$$q_S = 300 \quad \text{Subtracting}$$

Now we know the price, quantity, and slope, so we can use the elasticity formula.

$$\epsilon_S = \frac{1}{\text{slope}} \times \frac{p}{q_S} \quad \text{The formula for elasticity}$$

$$\epsilon_S = \frac{1}{\frac{1}{10}} \times \frac{50}{300} \quad \text{Plugging in}$$

$$\epsilon_S = 10 \times \frac{50}{300} \quad \text{Simplifying}$$

$$\epsilon_S = 1.667 \quad \text{Multiplying}$$

This is also relatively elastic, but less elastic than at the lower price.

