

Real-Time Systems

Lecture Topic - Rate Monotonic Theory Advantages and Pitfalls

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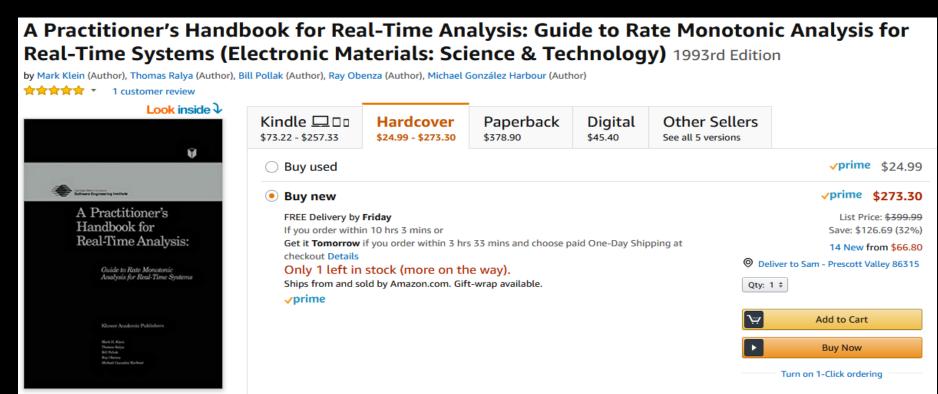
Electrical, Computer and Energy Engineering

Embedded Systems Engineering Program



Real-Time Systems Practitioner

- By completion of RT-Systems course, you should be a beginning RT practitioner
- IEEE RTSS, RTAS, RTCSA, IEEE Computer Society TCRTS
- Linux Foundation RT Linux, Zephyr, Carrier & Automotive Grade Linux
- Standards ARINC 653, RTCA DO-178 B & C



RMA is the state of Practice

- Technical Society and Committee Support
- 2. Industry
- 3. Standards
- 4. Linux Foundation
- 5. Software Engineering Institute
- 6. Publications, Textbook, and online education and training

Major Issue Summary – Assumptions and Constraints

- 1. Inexact RM LUB Solved with Worst Case Analysis
- 2. T=D Limitation Solved by DM and by RM Practitioner's Guide
- 3. Fails in cases where Dynamic Priorities succeed Trade-off for simpler failure mode and scheduler implementation
- 4. Does not include Secondary, Tertiary, ... etc. resource issues Mostly solved by priority inheritance or Priority ceiling (Course #2)
- 5. Does not encode importance of services solved to a degree by period transform
- 6. Supported best by Cyclic Executive or RTOS rather than general OS POSIX real-time extensions
- 7. Lack of broad understanding courses like this, textbooks, Practitioner's guide, Course #2 full derivation of RM LUB
- 8. WCET variability ARM R-Series Microprocessors
- 9. Accuracy, precision and deterministic timing limitations Use a co-processor (FPGA, ASIC, GP-GPU)
- 10. Does not scale well AMP with multi-core SoCs, and with SMP and VMs in research

RM Necessary and Sufficient Feasibility

- RM LUB is Only Sufficient (Order N)
- DM is Only Sufficient (Order N²)
- N&S Feasibility Tests (Order N³)
 - Lehoczky, Shah, Ding Theorem
 - Worst-Case Analysis
 - If S_i Can be Schedule over Longest T_i => Feasible
 - Best To Look over LCM of All T_i (Full Story)
 - N&S Test: Iterate Over Subsets of Si for Each Longest Ti for All Si
 - Encodes Process of Hand Drawing Timing
 - With Preemption According to RM Policy
 - Scheduling Point (N&S) Automates WC Analysis (hand)
 - Completion Test (N&S) Automates WC Analysis
- RM LUB Sufficient Test Will Never Incorrectly Pass an Infeasible Service Set
- But Will Fail Some Feasible Ones
- An N&S Test is Exact Will Not Pass Infeasible Sets Nor Will it Fail a Feasible Set

RM LUB is Sufficient

- if scenario passes, it is feasible,
- but if scenario fails LUB, it might still be feasible

RM Worst-Case Analysis is EXACT (Necessary and Sufficient)

Truth table				
S	N	$S \Rightarrow N$	$S \Leftarrow N$	$S \Leftrightarrow N$
Т	Т	Т	Т	Т
Т	F	F	Т	F
F	Т	Т	F	F
F	F	Т	Т	Т

The assertion that a statement is a "necessary and sufficient" condition of another means that the former statement is true if and only if the latter is true. That is, the two statements must be either simultaneously true or simultaneously false. [2][3][4] -Wikipedia

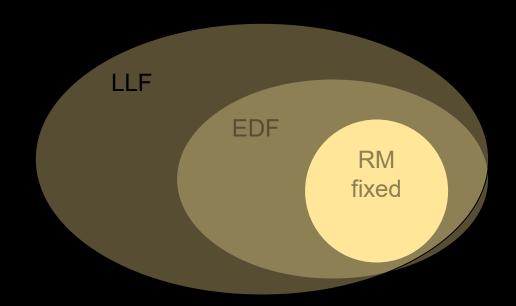
RM compared to Dynamic Priority EDF and LLF

Generally Higher Overhead than Fixed Priority

- EDF Update priorities based on TTD (Time-To-Deadline) on every Ready Queue change
- LLF Update priorities based on Laxity (TTD Time-to-Complete)
- Both Encode Urgency, so they have Distinct Advantage
- Failure Mode on Over-runs harder to DEBUG (less deterministic)
- Can Schedule More Cases (especially EDF compared to RM)
- Harmonic Cases, U=100% for all 3
- RM and EDF Most Common
- LLF Hard to Implement
- LLF and EDF often Same

Buttazzo, Giorgio C. "Rate monotonic vs. EDF: judgment day." *Real-Time Systems* 29.1 (2005): 5-26.

Brun, Adrien, Chunhui Guo, and Shangping Ren. "A Note on the EDF Preemption Behavior in "Rate Monotonic Versus EDF: Judgment Day"." *IEEE Embedded Systems Letters* 7.3 (2015): 89-91.

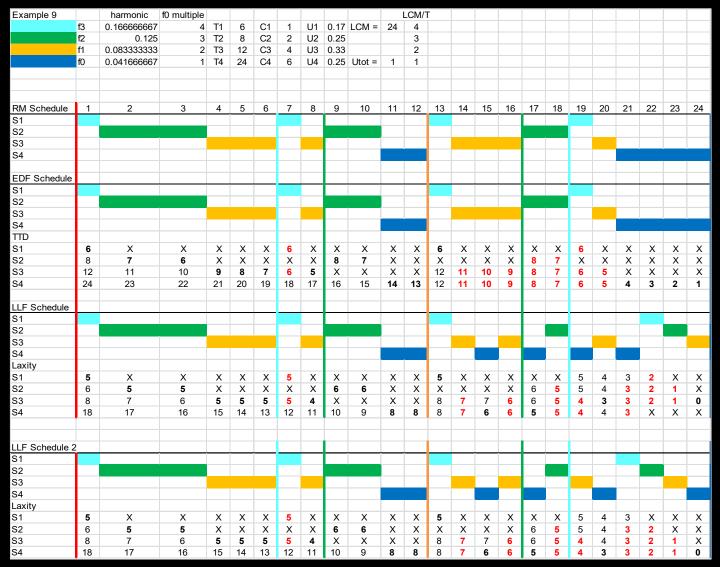


Deadline Driven Scheduling (Liu & Layland) is EDF

- 1) Course #2 in RTES series covers EDF and LLF
- 2) RMA and Fixed Priority are a standard of practice
- 3) Open area of debate and research for HRT
- 4) Accepted for SRT

Timing Diagrams - sched-example-9

- EDF and LLF have Priority TIES
- For EDF/LLF, More than ONE valid schedule (Course #2)
- RM most often used for HRT
- EDF for SRT
- RM failure mode is simpler
 - Highest frequency succeeds
 - Lowest frequency fails
 - Services higher priority than over-run unaffected



Application of RM Theory

Policy to Assign Priorities in RTOS or SCHED_FIFO for Service Set

Feasibility Test (On-Line, Off-Line, By Mode)

- Off-Line for Fixed Set of Services
 - Transition from Off-Line Boot to On-Line RT Services
 - Service Set Can't Change No Dynamic Admission
- On-Line Admission of Services
 - Feasibility Test Must be Run On-Line to Re-Test Feasibility of New Services
 Before They Go On-Line
 - Feasibility Test Itself is a Service that Must Be Admitted by Off-Line Test

Most RT Systems Have Static Services Sets

Or, Modes with Different Service Sets

- E.g. Space Telescope in Observing Mode, Ready Mode, Safe Mode
- Can Apply RM Feasibility Testing to Each Mode

RM Theory Pessimism

Pessimistic Assumptions Require Resource Margin for Safety

C = WCET

- Longest Path for Code
- Path is Executed Least Efficiently
- WCET Is Worse than 3-Sigma Deviation (Rarely Happens)

T = Worst Case Inter-arrival Rate (Period Transform Required)

Importance Encoding Requires Period Transform
Critical Instant - Assumes that Service Requests May All Come At Once
RM LUB not EXACT

- RM LUB is Based Upon Service Periods That Are Not Necessarily Harmonic, So Partial Interference can be Over-Accounted for
- Feasible Service Sets May Be Rejected, Although Unsafe Will Never Be Admitted
- Can Use Alternative Scheduling Point or Completion Test RM N&S Feasibility Tests

Pitfalls Applying RM Theory

Audsley, Neil, and Alan Burns. "Real-time system scheduling." (1990).

Klein, Mark, et al. A practitioner's handbook for real-time analysis: guide to rate monotonic analysis for real-time systems. Springer Science & Business Media, 2012.

Problem: Period is not Constant

- Service Releases have Period Jitter, are Sporadic, or A-periodic
- Possible Solution: Period Transform
 - Assume Service Period Based on Worst Case Inter-arrival Rate (Highest Known Frequency of Requests)
 - When Frequency is Lower than Worst Case, Margin Available for Slack Stealers
 - May not Handle Truly A-periodic Services (Worst Case Frequency Unknown)

Problem: C is not Deterministic

- Service Execution has Jitter due to Processor Architecture and Data Driven Algorithms
- Possible Solution: WCET
 - Assume Worst Case Execution Time
 - Longest Path Possible for Algorithms
 - Worst Efficiency Possible Executing that Path (e.g. all cache accesses miss)

Pitfalls Applying RM Theory

Problem: RM Policy Does Not Encode Importance

- The Longest Period Service May not Be the Service We Want to Fail in an Overload Situation
- Possible Solution: Period Transform
 - Assume High Importance Service with Long Period has a Shorter Period than it Actually Does to Artificially Increase Priority
 - Increases System CPU Resource Margin
 - Overload Failures Result in Less Important Services Missing Deadlines

Problem: Deadline Not Equal Period (Longer – overlapping duplicates, Shorter – output time)

- Deadline may be Less than Period when Response I/O Latency is Accounted for (e.g. if Service Response is Transported on a Network)
- Deadline may be Greater than Period if Service Release Processing is Allowed to Overlap (e.g. 2 or more service requests within T)
- **Possible Solution**: Deadline Monotonic Policy and Feasibility Test

Deadline Monotonic Theory

DM Policy: Higher Priority Given to Services with Shorter Deadlines

DM Sufficient Feasibility:
$$\forall i: 1 \le i \le n: \frac{C_i}{D_i} + \frac{I_i}{D_i} \le 1.0$$

For All Services from 1 to n, if the Deadline Interval is Long Enough To Contain The Service Execution Time Interval Plus All Interfering Execution Time Intervals, Then the Service is Feasible - If all Services are Feasible, Then the System is Feasible.

$$I_{i} = \sum_{j=1}^{i-1} \left[\frac{D_{i}}{T_{j}} \right] C_{j}$$

$$Worst Case Number of Releases S_{j} Over Deadline Interval for S_{i}$$



Worst Case Number of Releases of

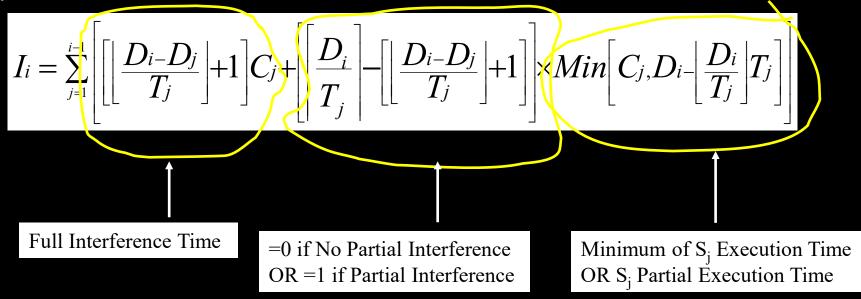
Interference to Service S_i is due to Preemption By All Higher Priority Services S₁ to S_{i-1} and the total Interference Time is the Number of Releases of Si Over The Deadline Interval Di for S_i Multiplied by S_i Execution Time C_i Summed for All S_i which Have Greater Priority Than S_i.

DM Improved Feasibility Test – Still Not EXACT

DM Sufficient Feasibility Pessimistic

- Assumes that All Releases of S_i Over D_i Fully Interfere with S_i
- Last Release of S_i Over D_i May Only Partially Interfere with S_i

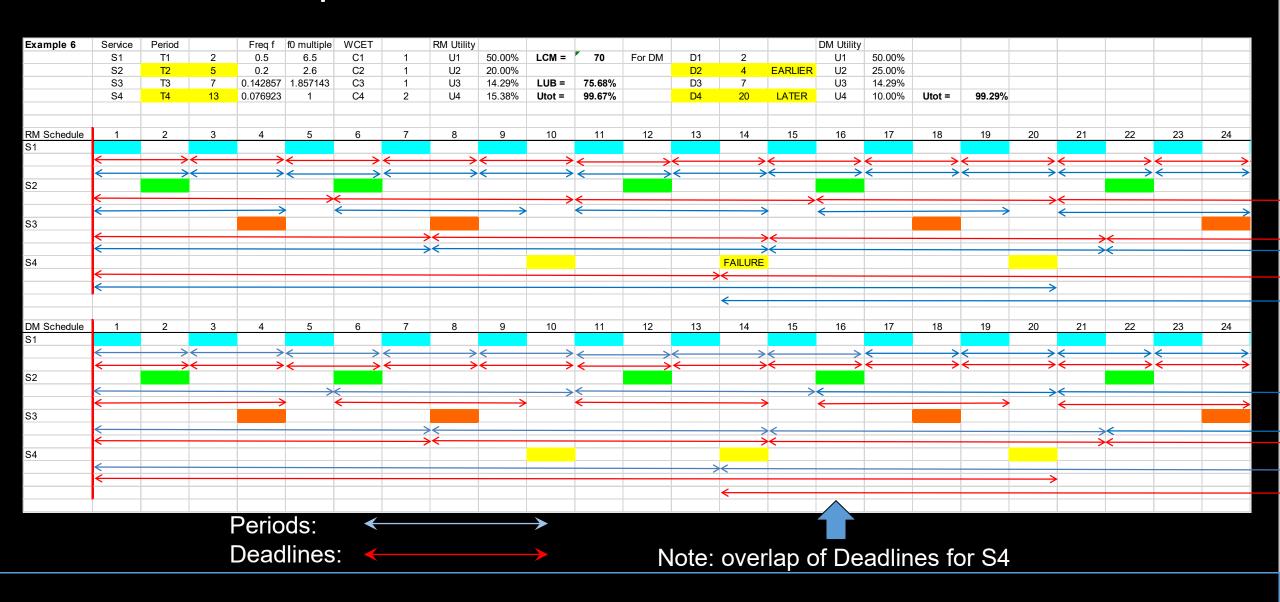
Improved Interference Estimation:



Still Not N&S Feasibility Test

- Over-Accounts for Partial Interferences (They Don't All Just Sum)
- Some Partial Interferences Over-lap in Time and Preempt Each Other

Example #6 - DM Ok, RM Fails, but DM is RM



Rate Monotonic or EDF?

Liu & Layland Rate Monotonic - Fixed Priority Policy

- Feasibility Test Sufficient RM LUB
- Most Hard RT Systems Have Static Services Sets

$$U = \sum_{i=1}^{m} (Ci/Ti) \le m(2^{\frac{1}{m}} - 1), U \lim m \to \infty = \ln(2) \approx 0.69$$

EDF (Deadline Driven) – Dynamic Priority Policy

Feasibility Test Based on Hyper-Period (Product of All Periods)

$$\forall tasks \in 1...m, T_{hyperperiod} = 0...(T_1T_2...T_{m-1}T_m)$$

$$(T_1T_2...T_{m-1}T_m) = \frac{(T_1T_2...T_{m-1}T_m)}{T_1}C_1 + ... + \frac{(T_1T_2...T_{m-1}T_m)}{T_m}C_m$$

$$\therefore \sum_{i=1}^m (Ci/Ti) \le 1$$

RMA LUB for quick analysis

RM Worst Case analysis for EXACT feasibility

EDF has feasibility tests, but can be inefficient at runtime

Sáez, Sergio, Joan Vila, and Alfons Crespo. "Using exact feasibility tests for allocating real-time tasks in multiprocessor systems." *Proceeding. 10th EUROMICRO Workshop on Real-Time Systems (Cat. No. 98EX168)*. IEEE, 1998.

Albers, Karsten, and Frank Slomka. "Efficient feasibility analysis for real-time systems with EDF scheduling." *Design, Automation and Test in Europe*. IEEE, 2005.

Singh, Jagbeer. "An algorithm to reduce the time complexity of earliest deadline first scheduling algorithm in real-time system." *arXiv preprint arXiv:1101.0056* (2010).

Notes on Dynamic Admission

- Off-Line for Fixed Set of Services
 - Transition from Off-Line to On-Line RT Services
 - Service Set Can't Change No Dynamic Admission
- On-Line Admission of Services
 - Feasibility Test Must be Run On-Line to Re-Test Feasibility of New Services Before They Go On-Line
 - Feasibility Test Itself is a Service that Must Be Admitted by Off-Line Test or Run on Dedicated Hardware

SMP Load-balancing – Migration of services essentially requires dynamic admission

