

YOCTO-CFA: A PROGRAM ANALYZER THAT YOU CAN UNDERSTAND

by Leandro Facchinetti

A dissertation submitted to Johns Hopkins University in conformity with the requirements for the degree of Doctor of Philosophy

Baltimore, Maryland August 2020

2020-06-23T17:35:29.206Z

Table of Contents

1 De	veloping an Analyzer	1
1.1 T	The Analyzed Language: Yocto-JavaScript	1
1.1.1	Values in Yocto-JavaScript	2
1.1.2	Operations in Yocto-JavaScript	3
1.1.3	The Computational Power of Yocto-JavaScript	5
1.1.4	A Formal Grammar for Yocto-JavaScript	7
1.2 T	The Analyzer Language: TypeScript	7
1.3 S	tep 0: Substitution-Based Interpreter	7
1.3.1	Architecture	8
1.3.2	Data Structures to Represent Yocto-JavaScript Programs	10
1.3.3	An Expression That Already Is a Value	13
1.3.4	A Call Involving Immediate Functions	14
1.3.5	Substitution in Function Definitions	17
1.3.6	Name Mismatch	18
1.3.7	Name Reuse	19
1.3.8	Substitution in Function Calls	21
1.3.9	An Argument That Is Not Immediate	22
1.3.10	A Function That Is Not Immediate	24
1.3.11	Continuing to Run After a Function Call	25
1.3.12	A Reference to an Undefined Variable	25
1.3.13	The Entire Runner	26
1.3.14	An Operational Semantics for the Interpreter	27
1.3.15	S Parser	29
1 3 16	Generator	32

1.3.17	Programs That Do Not Terminate	33
1.4 S	tep 1: Environment-Based Interpreter	36
1.4.1	Avoiding Substitution by Introducing Environments and Closures	36
1.4.2	New Data Structures	38
1.4.3	Adding an Environment to the Runner	39
1.4.4	A Function Definition	40
1.4.5	A Function Call	41
1.4.6	Name Reuse	42
1.4.7	A Variable Reference	43
1.4.8	A Function Body Is Evaluated with the Environment in Its Closure	44
1.4.9	The Entire Runner	47
1.4.10	Operational Semantics	48
1.4.11	Generator	48
1.4.12	Programs That Do Not Terminate	50
1.5 S	tep 2: Store-Based Interpreter	52
1.5.1	Avoiding Nested Environments by Introducing a Store	53
1.5.2	New Data Structures	54
1.5.3	Adding a Store to the Runner	55
1.5.4	Adding a Value to the Store	55
1.5.5	Retrieving a Value from the Store	57
1.5.6	The Entire Runner	58
1.5.7	Operational Semantics	59
1.5.8	Programs That Do Not Terminate	60
1.6 S	tep 3: Finitely Many Addresses	61
1.6.1	The Entire Runner	61
Biblio	graphy	64

1 Developing an Analyzer

[](#developing-an-analyzer)

1.1 The Analyzed Language: Yocto-JavaScript

[](#the-analyzed-language-yocto-javascript)

Our first decision when developing a program analyzer is which language it should analyze. This decision is important, among other reasons, because it influences how difficult it is to develop the analyzer. In this dissertation we are interested in analysis techniques for higher-order functions, a feature that is present in most languages, so we have plenty of options from which to choose, including JavaScript, Java, Python, Ruby, and so forth.

From all these options, we would like to choose JavaScript because it is the most popular programming language [29, 11], but JavaScript has many features besides higher-order functions that would complicate our study. As a compromise, we analyze some parts of JavaScript, not the entire language. We select the JavaScript features that are related to higher-order functions to design our own artificial little language called *Yocto-JavaScript* (JavaScript \times 10⁻²⁴), which becomes the language over which our analyzer works. We design Yocto-JavaScript such that every Yocto-JavaScript program is also a JavaScript program, but the converse does not hold.

Advanced

On the surface the choice of analyzed language is important because it influences how difficult it is to develop the analyzer, but that choice has deeper

consequences as well: the analyzed language may also influence the analyzer's precision and running time. For example, there is an analysis technique called k-CFA [28] that may be slower when applied to a language with higher-order functions than when applied to a language with objects, because the algorithmic complexity of the former is exponential and of the latter is polynomial [18].

Technical Terms

• λ -Calculus [30 (§ 6)]: A mathematical theory to study higher-order functions and their applications. Yocto-JavaScript is a representation of the λ -calculus.

1.1.1 Values in Yocto-JavaScript [](#values-in-yocto-javascript)

JavaScript has many kinds of values:

From all these kinds of values, Yocto-JavaScript supports only one: Function. An Yocto-JavaScript function is written as parameter> => <body>, for example, x => x, in which the parameter> is called x and the <body> is a reference to the variable x (see § 1.1.2 for more on variable references). An Yocto-JavaScript function must have exactly one parameter. Because an Yocto-JavaScript function

is a value, it may be passed as argument in a function call or returned as the result of a function call (see § 1.1.2 for more on function calls).

Technical Terms

- Arrow Function Expressions [19]: The notation we use for writing functions.
- **Identity Function:** The function given as example, $x \Rightarrow x$.
- **High-Order Functions:** Functions that may act as values.

1.1.2 Operations in Yocto-JavaScript

[](#operations-in-yocto-javascript)

JavaScript has many kinds of operations on the values introduced in § 1.1.1:

Kind of JavaScript Operation	Example	Result
Access a character in a String	"Leandro"[2]	"a"
Add Numbers	29 + 1	30
Call a Function	<pre>parseInt("29")</pre>	29
:	:	•

From all these operations, Yocto-JavaScript supports only two: function calls and variable references. A function call is written as <function>(<argument>), for example, f(a), in which the <function> is a hypothetical function f and the <argument> is a hypothetical argument a. An Yocto-JavaScript function call must have exactly one argument (because an Yocto-JavaScript function must have exactly one parameter; see § 1.1.1). A variable reference is written as a bare identifier, for example, x.

The following is a complete Yocto-JavaScript program that exemplifies all the supported operations:

Example Yocto-JavaScript Program Result

$$(y \Rightarrow y)(x \Rightarrow x)$$
 $x \Rightarrow x$

This program is a function call in which the <function> is y => y and the <argument> is x => x. When an Yocto-JavaScript function is called, it returns the result of computing its <body>, and the <body> of y => y is a reference to the variable y, so y => y is a function that returns its argument unchanged and the result of the program above is x => x.

In general, all kinds of Yocto-JavaScript expressions (function definitions, function calls, and variable references) may appear in the $\langle body \rangle$ of a function definition, or as the $\langle function \rangle$ or $\langle argument \rangle$ of a call. For example, in the program (f(a))(b) the function call f(a) appears as the $\langle function \rangle$ of a call.

We use parentheses to resolve ambiguities on where function definitions start and end, and in which order operations are computed. For example, given hypothetical functions f, g, and h, in (f(g))(h) the call f(g) happens first and the result is a function that is called with h as argument, and in f(g(h)) the call g(h) happens first and the result is passed as argument in a call to f. If there are no parentheses in a sequence of expressions, then the following conventions apply:

Kind of Sequence	Reading Direction	Example	Equivalent to
Function Definitions	Right-to-Left	x => y => x	$x \Rightarrow (y \Rightarrow x)$
Function Calls	Left-to-Right	f (a)(b)	(f (a))(b)

Technical Terms

• **Precedence:** The order in which operations of different kinds are computed. Operations that are computed first have *higher precedence* and operations that are computed later have *lower precedence*.

• **Associativity:** The order in which a sequence of operations of the same kind is computed. Function definitions are *right-associative* and function calls are *left-associative*.

Advanced

1.1.3 The Computational Power of Yocto-JavaScript

[](#the-computational-power-of-yocto-javascript)

Yocto-JavaScript has only a few features, which makes it the ideal language for discussing the analysis of higher-order functions, but does it have enough features to support all kinds of computation? Perhaps surprisingly, the answer is positive: Yocto-JavaScript is equivalent to JavaScript (and Java, Python, Ruby, and so forth) in the sense that any program in any one of these languages may be translated into an equivalent program in any other language [30 (§ 6)].

As an example of how this translation could be done, consider a JavaScript function of two parameters: $(x, y) \Rightarrow x$. This function is not supported by Yocto-JavaScript because it does not have exactly one parameter (see § 1.1.1), but we may encode it as $x \Rightarrow y \Rightarrow x$, which is a function that receives the first parameter and returns another function that receives the second parameter. Similarly, we may encode a call with multiple arguments as a sequence of calls that passes one argument at a time; for example, f(a, b) may be encoded as f(a)(b).

Technical Terms

• **Computational Power:** The ability of expressing computations, for

- example, adding two numbers together, selecting a character from a string, and so forth.
- Turing Complete [30 (§ 7)]: The property of a language that may express any computation of which a computer is capable. Yocto-JavaScript, JavaScript, Java, Python, Ruby, and so forth are all Turing Complete.
- **Currying [30 (page 163)]:** The translation technique we used to encode functions with multiple parameters and calls with multiple arguments.

For our goal of exploring analysis techniques, we are concerned only with computational power, but it is worth noting that programmers would be more interested in other language properties: Does the language promote writing programs of higher quality? (It most probably does not [4].) Does the language improve productivity? Is the language appropriate for the domain of the problem? (For example, we would probably write an operating system in C and a web application in JavaScript, not the other way around.) Is the language more expressive than others? (Perhaps surprisingly, it is possible to make formal arguments about expressiveness instead of resorting to personal preference and anecdotal evidence [7].) Despite having the same computational power as other languages, Yocto-JavaScript fares badly in these other aspects: it is remarkably unproductive and inexpressive.

1.1.4 A Formal Grammar for Yocto-JavaScript

[](#a-formal-grammar-for-yocto-javascript)

The description of Yocto-JavaScript given in § 1.1.1-§ 1.1.2 is informal; the following is a grammar in *Backus–Naur Form* (BNF) [17, 1 (§ 4.2)] that formalizes it:

 $e ::= x \Rightarrow e \mid e(e) \mid x$ Expressions x ::= «A JavaScript Identifier» Variables

1.2 The Analyzer Language: TypeScript

[](#the-analyzer-language-typescript)

After choosing our analyzed language (Yocto-JavaScript; see § 1.1), we must decide in which language to develop the analyzer itself. Our analyzed language is based on JavaScript, so JavaScript is a natural first candidate for analyzer language as well. But JavaScript lacks a feature which we will need: the ability to express the *types* of data structures, functions, and so forth (see, for example, § 1.3.2), so we choose to implement our analyzer in a JavaScript extension with support for types called *TypeScript* [32, 31, 5].

1.3 Step 0: Substitution-Based Interpreter

[](#step-0-substitution-based-interpreter)

Having chosen the analyzed language (Yocto-JavaScript; see § 1.1) and the language in which to develop the analyzer itself (TypeScript; see § 1.2), we are ready to start developing the analyzer. This development happens in Steps: In Step 0 we

develop an interpreter and in each subsequent Step we modify the program from the previous Step in some way until it becomes an analyzer.

The interpreter in Step 0 executes Yocto-JavaScript programs and produces the same outputs that would be produced by a regular JavaScript interpreter. This is a good starting point for two reasons: first, this interpreter is the basis upon which we will build the analyzer; and second, the outputs of this interpreter are the ground truth against which we will validate the outputs of the analyzer.

1.3.1 Architecture [](#architecture)

Our interpreter is defined as a function called evaluate(), which receives an Yocto-JavaScript program represented as a string and returns the result of running it.

The following are two examples of how we will be able to use evaluate() by the end of Step 0 (the > represents the console, and by convention strings that represent Yocto-JavaScript programs are delimited by backticks (`) [24]):

```
> evaluate('x => x')
'x => x'
> evaluate('(y => y)(x => x)')
'x => x'
```

The implementation of evaluate() is separated into three parts called parse(), run(), and generate():



```
export function evaluate(input: string): string {
  return generate(run(parse(input)));
}
```

The parse() function prepares the input for interpretation, converting it from a string into more convenient data structures (see § 1.3.2 for more on these data structures). The run() function is responsible for the interpretation itself. The generate() function converts the outputs of run() into a human-readable format. In the following sections (§ 1.3.2–§ 1.3.14) we address the implementation of run(), deferring parse() to § 1.3.15 and generate() to § 1.3.16.

In later Steps the implementations of run() and generate() will change, but the implementations of evaluate() and parse() will remain the same, because the architecture and the data structures used to represent Yocto-JavaScript programs will remain the same.

Advanced

The evaluate() function is named after a native JavaScript function called eval() [21], which is similar to evaluate() but for JavaScript programs instead of Yocto-JavaScript. The parse() and generate() functions are named after the library functions used to implement them (see § 1.3.15 and § 1.3.16).

1.3.2 Data Structures to Represent Yocto-JavaScript Programs

[](#data-structures-to-represent-yocto-javascript-programs)

The evaluate() function receives an Yocto-JavaScript program represented as a string (see § 1.3.1), which is convenient for humans to write and read, but inconvenient for run() to manipulate directly, because run() is concerned with the *structure* rather than the *text* of the program: for run() it does not matter, for example, whether a function is written as x = x or x = x. So before run() starts interpreting the program, parse() transforms it from a string into more convenient data structures (see § 1.3.15 for parse()'s implementation).

The following are two examples of Yocto-JavaScript programs and the data structures used to represent them:

```
"name": "x"
  }
}
> parse('(y => y)(x => x)')
  "type": "CallExpression",
  "callee": {
    "type": "ArrowFunctionExpression",
    "params": [
      {
        "type": "Identifier",
        "name": "y"
      }
    ],
    "body": {
      "type": "Identifier",
      "name": "y"
    }
                                                         call
  },
  "arguments": [
    {
      "type":
"ArrowFunctionExpression",
      "params": [
        {
          "type": "Identifier",
          "name": "x"
        }
      ],
      "body": {
        "type": "Identifier",
        "name": "x"
      }
    }
  ]
}
```

We choose to represent Yocto-JavaScript programs with the data structures above because they match the data structures used by Babel [2], which is a library to manipulate JavaScript programs that we use to implement the parse() and

generate() functions (see § 1.3.15 and § 1.3.16).

In general, the data structures used to represent Yocto-JavaScript programs have the following types (written as TypeScript types adapted from the Babel types [3] to include only the features supported by Yocto-JavaScript):

```
type Expression = ArrowFunctionExpression | CallExpression | Identifier;
type ArrowFunctionExpression = {
   type: "ArrowFunctionExpression";
   params: [Identifier];
   body: Expression;
};
type CallExpression = {
   type: "CallExpression";
   callee: Expression;
   arguments: [Expression];
};
type Identifier = {
   type: "Identifier";
   name: string;
};
```

In later Steps almost everything about the interpreter will change, but the data structures used to represent Yocto-JavaScript programs will remain the same.

Technical Terms

- **Parsing [1 (§ 4)]:** The process of converting a program represented as a string into more convenient data structures.
- **Abstract Syntax Tree (AST) [1 (§ 4)]:** The data structures that represent a program.

Advanced

The data structures used to represent programs correspond to the Yocto-JavaScript grammar (see § 1.1.4); for example, Expression corresponds to

1.3.3 An Expression That Already Is a Value

[](#an-expression-that-already-is-a-value)

Example Program Current Output Expected Output $\times => \times$ $\times => \times$

Having defined the architecture (§ 1.3.1) and the data structures to represent Yocto-JavaScript programs (§ 1.3.2), we start developing the run() function. The development is driven by a series of example programs that highlight different aspects of the interpreter. In § 1.3.3–§ 1.3.12 we begin with these example programs and modify the implementation to achieve the expected output.

Consider the example program above. As mentioned in § 1.3.2, the run() function receives as parameter an Yocto-JavaScript program represented as an Expression. The run() function is then responsible for interpreting the program and producing a value. In Yocto-JavaScript, the only kind of value is a function (see § 1.1.1), so we start the implementation of run() with the following (we use throw as a placeholder for code that has not been written yet to prevent the TypeScript compiler from signaling type errors):

```
type Value = ArrowFunctionExpression;
function run(expression: Expression): Value {
  throw new Error("NOT IMPLEMENTED YET");
}
```

The first thing that run() has to do is determine which type of expression it is given:

```
function run(expression: Expression): Value {
  switch (expression.type) {
```

```
case "ArrowFunctionExpression":
    throw new Error("NOT IMPLEMENTED YET");
case "CallExpression":
    throw new Error("NOT IMPLEMENTED YET");
case "Identifier":
    throw new Error("NOT IMPLEMENTED YET");
}
```

In our current example, the expression already is a Value, so we return it unchanged:

```
// run()
case "ArrowFunctionExpression":
  return expression;
```

1.3.4 A Call Involving Immediate Functions

[](#a-call-involving-immediate-functions)

```
Example Program Current Output Expected Output (y \Rightarrow y)(x \Rightarrow x) NOT IMPLEMENTED YET x \Rightarrow x
```

Interpreting function calls is the main responsibility of our interpreter. There are several techniques to do this and in Step 0 we use one of the simplest: when the interpreter encounters a function call, it substitutes the variable references in the body of the called function with the argument. This is similar to how we reason about functions in mathematics; for example, given the function f(x) = x + 1, we begin to calculate f(29) by substituting the references to x in x + 1 with the argument 29: f(29) = 29 + 1. The implementation of this substitution technique starts in this section and will only be complete in § 1.3.8.

In the example program above, both the function that is called (y => y) and the argument (x => x) are immediate functions, as opposed to being the result of other operations, so for now we may restrict the interpreter to handle only this

case:

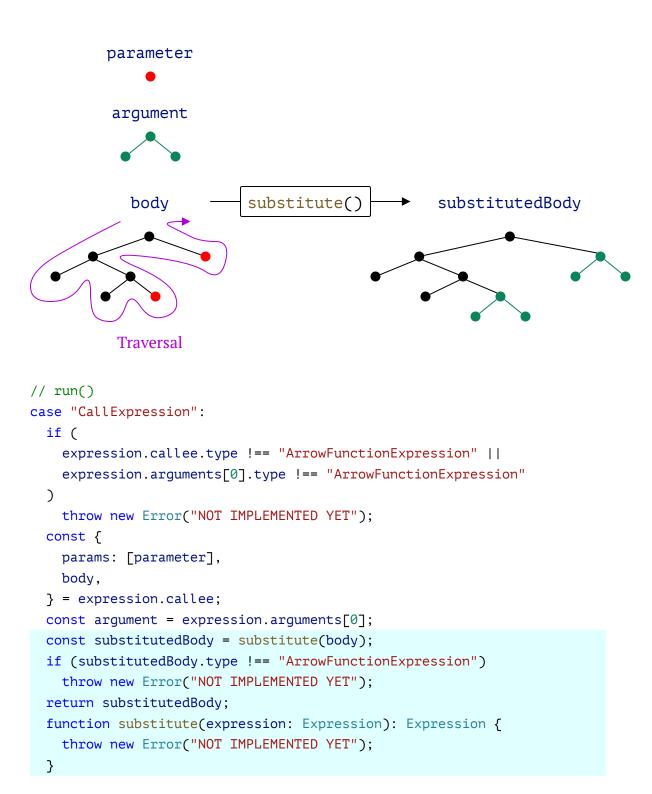
```
// run()
case "CallExpression":
   if (
      expression.callee.type !== "ArrowFunctionExpression" ||
      expression.arguments[0].type !== "ArrowFunctionExpression"
   )
      throw new Error("NOT IMPLEMENTED YET");
throw new Error("NOT IMPLEMENTED YET");
```

Next, we unpack the called function (using something called *destructuring assign-ment* [20]) and the argument:

```
// run()
case "CallExpression":
    if (
        expression.callee.type !== "ArrowFunctionExpression" ||
        expression.arguments[0].type !== "ArrowFunctionExpression"
    )
        throw new Error("NOT IMPLEMENTED YET");

const {
    params: [parameter],
    body,
    } = expression.callee;
    const argument = expression.arguments[0];
    throw new Error("NOT IMPLEMENTED YET");
```

Finally, we setup an auxiliary function called substitute() that implements
the traversal of the body looking for references to parameter and substituting
them with the argument (for now the result of substitution is restricted to be an
ArrowFunctionExpression):

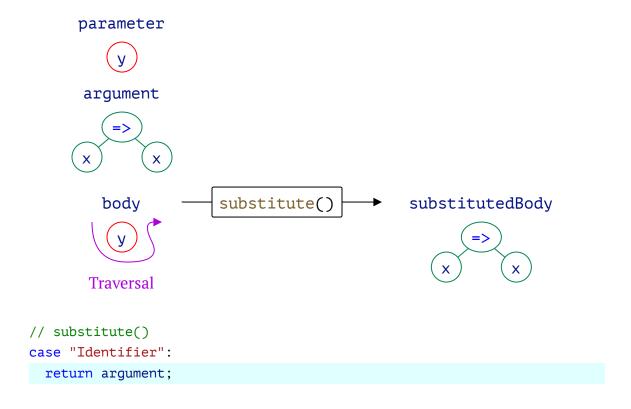


Similar to run() itself, substitute() starts by determining which type of expression is passed to it:

```
function substitute(expression: Expression): Expression {
```

```
switch (expression.type) {
   case "ArrowFunctionExpression":
      throw new Error("NOT IMPLEMENTED YET");
   case "CallExpression":
      throw new Error("NOT IMPLEMENTED YET");
   case "Identifier":
      throw new Error("NOT IMPLEMENTED YET");
}
```

In our current example the expression is y, which is an Identifier that must be substituted with the argument (x => x):

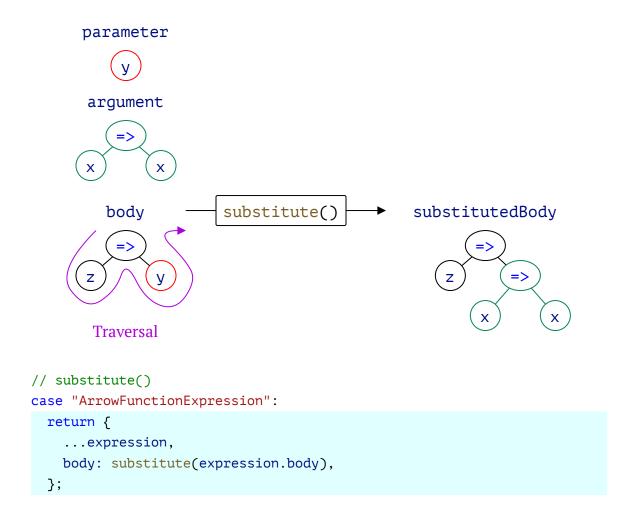


1.3.5 Substitution in Function Definitions

[](#substitution-in-function-definitions)

```
Example Program Current Output Expected Output (y \Rightarrow z \Rightarrow y)(x \Rightarrow x) NOT IMPLEMENTED YET z \Rightarrow x \Rightarrow x
```

When substitute() (see § 1.3.4) starts traversing the body of the example above, the expression is an ArrowFunctionExpression (z => y), and we want substitution to proceed deeper to find and substitute y, so we call substitute() recursively (we use a feature called *spread syntax* [23] to build an expression based on the existing one with a new body):

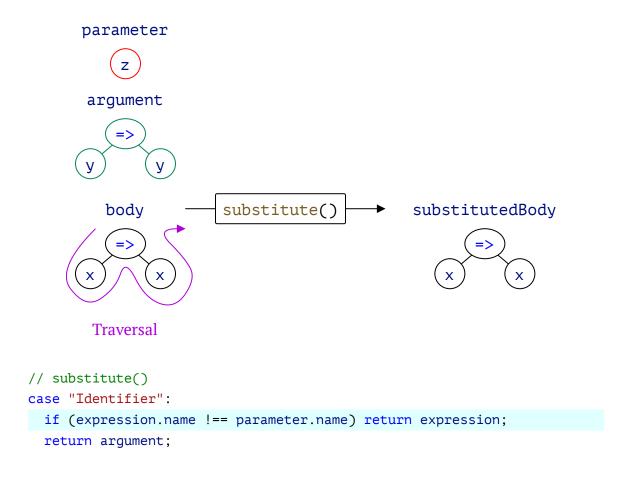


1.3.6 Name Mismatch [](#name-mismatch)

```
Example Program Current Output Expected Output (z \Rightarrow x \Rightarrow x)(y \Rightarrow y) \times x \Rightarrow (y \Rightarrow y) \times x \Rightarrow x
```

The implementation of substitute() introduced in § 1.3.4 always substitutes

variable references, regardless of whether they refer to the parameter. For example, in the program above substitute() is substituting the x even though the parameter is z. To fix this, we check whether the variable reference matches the parameter, and if it does not then we prevent the substitution by retuning the variable reference unchanged:



1.3.7 Name Reuse [7(#name-reuse)]

Example Program Current Output Expected Output
$$(x \Rightarrow x \Rightarrow x)(y \Rightarrow y) \times x \Rightarrow (y \Rightarrow y) \times x \Rightarrow x$$

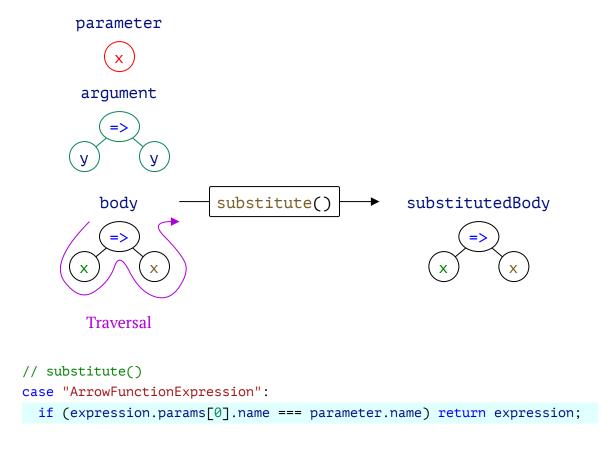
In the program above, \times could refer to either \times or \times :

If x Refers to Then the Output of Example Program Is

Option 1
$$\times$$
 \times => $(y \Rightarrow y)$
Option 2 \times \times => \times

Currently substitute() is implementing Option 1, but this leads to an issue: we are unable to reason about $\times => \times$ independently; we must know where it appears and whether a variable called \times is already defined there.

We avoid this issue by modifying substitute() to implement Option 2, which is also the choice of JavaScript and every other popular programming language. We change substitute()'s behavior when encountering a function definition so that if the parameter of the function definition matches the parameter that substitute() is looking for, then substitute() returns the function unchanged, preventing further substitution (there is no recursive call to substitute() in this case):



```
return {
    ...expression,
    body: substitute(expression.body),
};
```

Technical Terms

- Local Reasoning: The ability to reason about a function without having to know the context under which it is defined. Option 1 defeats local reasoning and Option 2 enables it.
- **Shadowing:** The behavior exhibited by Option 2: \times is *shadowed* by \times because there is no way to refer to \times from the body of the inner function.

1.3.8 Substitution in Function Calls

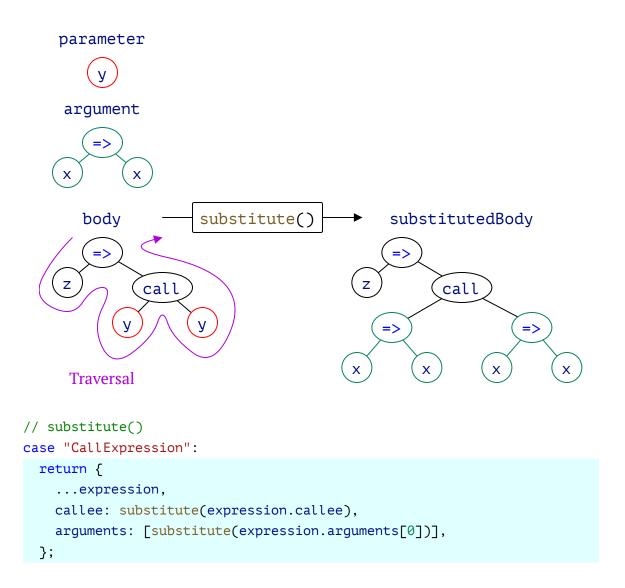
[](#substitution-in-function-calls)

```
Example Program (y \Rightarrow z \Rightarrow y(y))(x \Rightarrow x)

Current Output NOT IMPLEMENTED YET

Expected Output z \Rightarrow (x \Rightarrow x)(x \Rightarrow x)
```

This case is analogous to § 1.3.5 for function calls. The substitute() function must continue traversing the function call recursively:



This concludes the implementation of substitute().

1.3.9 An Argument That Is Not Immediate

[](#an-argument-that-is-not-immediate)

```
Example Program (a => z => a)((y => y)(x => x))

Current Output NOT IMPLEMENTED YET

Expected Output z => x => x
```

The arguments in the example programs from § 1.3.3-§ 1.3.8 are ArrowFunctionExpressions, but in general an argument may be any kind

of Expression; for example, in the program above the argument is a CallExpression((y => y)(x => x)). We address the general case by calling run() recursively on the argument to evaluate it to a Value:

```
// run()
case "CallExpression":
  if (expression.callee.type !== "ArrowFunctionExpression")
   throw new Error("NOT IMPLEMENTED YET");
 const {
   params: [parameter],
   body,
  } = expression.callee;
 const argument = run(expression.arguments[0]);
 const substitutedBody = substitute(body);
 if (substitutedBody.type !== "ArrowFunctionExpression")
   throw new Error("NOT IMPLEMENTED YET");
  return substitutedBody;
  function substitute(expression: Expression): Expression {
    // ...
  }
```

Technical Terms

• **Big-Step Interpreter [12]:** An interpreter using the technique of calling run() recursively to evaluate the argument.

Advanced

The notion that the argument is interpreted to produce a value as soon as the function call is encountered characterizes Yocto-JavaScript as a *call-by-value* language [25]. JavaScript and most other popular programming languages are call-by-value as well, but there is one notable exception, Haskell, which is a *call-by-need* language. In a call-by-need language the argument is interpreted only if it is *needed*, for example, if it is used in the function position of another call (see § 1.3.10), or if it is the result of the program (see

§ 1.3.11). In a call-by-need language the result of the program above would be $z \Rightarrow ((y \Rightarrow y)(x \Rightarrow x))$, and the call $(y \Rightarrow y)(x \Rightarrow x)$ would not be computed, because it is not needed. Besides call-by-value and call-by-need, there is yet another policy for when to interpret arguments: *call-by-name*. The policy of call-by-name is similar to call-by-need, except that an argument that is used multiple times could be computed multiple times in a call-by-name language, and it is guaranteed to be computed at most once in a call-by-need language.

1.3.10 A Function That Is Not Immediate

[](#a-function-that-is-not-immediate)

```
Example Program ((z => z)(y => y))(x => x)

Current Output NOT IMPLEMENTED YET

Expected Output x => x
```

This is the dual of § 1.3.9 for the called function, and the solution is the same: to call run() recursively:

```
// run()
case "CallExpression":
    const {
        params: [parameter],
        body,
    } = run(expression.callee);
    const argument = run(expression.arguments[0]);
    const substitutedBody = substitute(body);
    if (substitutedBody.type !== "ArrowFunctionExpression")
        throw new Error("NOT IMPLEMENTED YET");
    return substitutedBody;
    function substitute(expression: Expression): Expression {
        // ...
    }
}
```

1.3.11 Continuing to Run After a Function Call

[](#continuing-to-run-after-a-function-call)

```
Example Program (z => (y => y)(z))(x => x)

Current Output NOT IMPLEMENTED YET

Expected Output x => x
```

This is similar to § 1.3.9 and § 1.3.10: the result of substitution may be not an immediate function but another call, in which case more computation is required. We solve this with yet another recursive call to run():

```
// run()
case "CallExpression":
   const {
    params: [parameter],
    body,
   } = run(expression.callee);
   const argument = run(expression.arguments[0]);
   return run(substitute(body));
   function substitute(expression: Expression): Expression {
        // ...
   }
```

1.3.12 A Reference to an Undefined Variable

[](#a-reference-to-an-undefined-variable)

```
Example Program (y => u)(x => x)
Current Output NOT IMPLEMENTED YET
Expected Output Reference to undefined variable: u
```

The only case in which run() may encounter a variable reference directly is if the referenced variable is undefined, otherwise substitute() would have already substituted it (see § 1.3.4–§ 1.3.11). In this case, we throw an exception:

```
// run()
```

```
case "Identifier":
  throw new Error(`Reference to undefined variable:
  ${expression.name}`);
```

Example Program Current Output Expected Output

```
y \Rightarrow u y \Rightarrow u y \Rightarrow u
```

If the reference to an undefined variable occurs in the body of a function that is not called, then we do not reach the case addressed in this section and an exception is not thrown. This is consistent with JavaScript's behavior.

1.3.13 The Entire Runner [](#the-entire-runner)

The implementation of the run() function is complete:

```
type Value = ArrowFunctionExpression;
 2
 3
    function run(expression: Expression): Value {
 4
      switch (expression.type) {
 5
        case "ArrowFunctionExpression":
 6
          return expression;
 7
        case "CallExpression":
 8
          const {
 9
            params: [parameter],
10
            body,
11
          } = run(expression.callee);
12
          const argument = run(expression.arguments[0]);
13
          return run(substitute(body));
          function substitute(expression: Expression): Expression {
15
            switch (expression.type) {
16
              case "ArrowFunctionExpression":
17
                if (expression.params[0].name === parameter.name)
    return expression;
18
                return {
19
                  ...expression,
20
                  body: substitute(expression.body),
21
                };
              case "CallExpression":
22
```

```
23
                return {
24
                   ...expression,
25
                  callee: substitute(expression.callee),
26
                   arguments: [substitute(expression.arguments[0])],
27
                };
28
              case "Identifier":
29
                if (expression.name !== parameter.name) return
    expression;
30
                return argument;
31
            }
32
        case "Identifier":
33
          throw new Error(`Reference to undefined variable:
34
    ${expression.name}`);
35
      }
36
   }
```

Advanced

1.3.14 An Operational Semantics for the Interpreter

[](#an-operational-semantics-for-the-interpreter)

What we accomplished in § 1.3.3–§ 1.3.13 is more than defining an interpreter for Yocto-JavaScript; we also defined formally the *meaning* of Yocto-JavaScript programs: an Yocto-JavaScript program means what the interpreter produces for it. The definition of the meaning of programs in a language is something called the *semantics* of the language, and there are several techniques to specify semantics; the technique we have been using so far is known as a *definitional interpreter* [27].

A definitional interpreter has some advantages over other techniques for specifying semantics: it is executable and it is easier to understand for most programmers. But a definitional interpreter also has one disadvantage: to understand the meaning of an Yocto-JavaScript program we have

to understand an interpreter written in TypeScript, which is a big language with many complex features. To address this, there are other techniques for defining semantics that do not depend on other programming languages, and in this section we introduce one of them: *operational semantics* [12, 8, 10].

First, we extend the grammar from § 1.1.4 with the notion of values that is equivalent to the type Value (see § 1.3.13, line 1):

$$v := x \Rightarrow e$$
 Values

Next, we define a *relation* $e \Rightarrow v$ using *inference rules* that are equivalent to the behavior of run() (see § 1.3.13, lines 3–36):

Value
$$\overline{v \Rightarrow v}$$

Function Call
$$egin{array}{cccc} e_f \Rightarrow (x_p \implies e_b) & e_a \Rightarrow v_a & e_b[x_p ackslash v_a] \Rightarrow v \\ & e_f(e_a) \Rightarrow v \end{array}$$

Finally, we define a *metafunction* $e[x \setminus v] = e$ that is equivalent to the behavior of substitute() (see § 1.3.13, lines 14–32):

$$\begin{array}{rcl} (x \Rightarrow e) [x_p \backslash v_a] &=& x \Rightarrow (e[x_p \backslash v_a]) & \text{if } x \neq x_p \\ (x_p \Rightarrow e) [x_p \backslash v_a] &=& x_p \Rightarrow e \\ (e_f(e_a)) [x_p \backslash v_a] &=& (e_f[x_p \backslash v_a](e_a[x_p \backslash v_a])) \\ & x[x_p \backslash v_a] &=& x & \text{if } x \neq x_p \\ x_p[x_p \backslash v_a] &=& v_a \end{array}$$

1.3.15 Parser [7(#parser)

The parser is responsible for converting a string representing an Yocto-JavaScript program into data structures that are more convenient for the runner to manipulate (see § 1.3.1 for a high-level view of the architecture and § 1.3.2 for the definition of the data structures). We choose data structures that are compatible with Babel [2], which is a library to manipulate JavaScript programs that we reuse to implement the Yocto-JavaScript parser and the generator (see § 1.3.16).

Our strategy to implement the Yocto-JavaScript parser is to delegate most of the work to Babel and check that the program is using only features supported by Yocto-JavaScript. The following is the full implementation of the parser:

```
function parse(input: string): Expression {
 1
      const expression = babelParser.parseExpression(input);
 3
      babelTypes.traverse(expression, (node) => {
        switch (node.type) {
 4
 5
          case "ArrowFunctionExpression":
 6
            if (node.params.length !== 1)
 7
              throw new Error(
 8
                "Unsupported Yocto-JavaScript feature:
    ArrowFunctionExpression with multiple parameters"
 9
10
            if (node.params[0].type !== "Identifier")
11
              throw new Error(
12
                "Unsupported Yocto-JavaScript feature:
    ArrowFunctionExpression param that isn't Identifier"
13
              );
14
            break;
15
          case "CallExpression":
16
            if (node.arguments.length !== 1)
17
              throw new Error(
18
                "Unsupported Yocto-JavaScript feature: CallExpression
    with multiple arguments"
19
              );
20
            break;
21
          case "Identifier":
```

```
break;
default:
throw new Error(`Unsupported Yocto-JavaScript feature:
    ${node.type}`);
}

// Property of the strong of
```

- Line 1: The parser is defined as a function called parse(), which receives the string called input representing a program and returns an Expression (see § 1.3.2).
- Line 2: Call babelParser.parseExpression(), which parses the input as a JavaScript program and produces a data structure following the Babel types [3]. The babelParser.parseExpression() function signals problems if there is a syntax error (for example, the missing function body in the program x =>) or if the input is not a simple JavaScript expression, and therefore is not supported by Yocto-JavaScript (for example, x => x; y => y, which is a sequence of two expressions, and const f = x => x, which is a variable declaration).
- Line 3: Extract the single Expression from within the Program returned by esprima.parseScript(). The as <something> forms sidestep the Type-Script type checker and assert that the expression is of the correct type. This is safe to do because of checkFeatures().
- Line 5: The checkFeatures() function, which is passed to esprima.parseScript() is called with every fragment of data structure used to represent the program. These fragments are called *nodes*, because

the data structure as a whole forms a *tree*, also known as the *Abstract Syntax Tree* (AST) of the program (see § 1.3.2). The checkFeatures() does not return anything (void); its purpose is only to throw an exception in case the program uses a feature that is not supported by Yocto-JavaScript.

- Lines 6, 7, 13, 15, 17, 23, 25: Similar to run() and substitute() (see § 1.3.13), checkFeatures() starts by determining which type of estree. Node it is given.
- Lines 8-11: Check that the Program contains a single statement. This prevents programs such as x => x; y => y.
- Lines 13, 15: ExpressionStatements and ArrowFunctionExpressions are supported in Yocto-JavaScript unconditionally. We could check that the ArrowFunctionExpression includes only one parameter and that this parameter is a variable (as opposed to being a pattern such as [x, y], for example), but this would be redundant because Esprima already calls checkFeatures() with other unsupported nodes that subsume these cases. For example, given the program (x, y) => x, which is a function of multiple parameters, Esprima calls checkFeatures() with a node of type SequenceExpression. Similarly, given the program ([x, y]) => x, which is a function in which the parameter is a pattern, Esprima calls checkFeatures() with a node of type ArrayExpression.
- **Lines 18–21:** Check that the CallExpression contains a single argument. This prevents programs such as **f**(a, b).
- Line 23: Identifiers are supported in Yocto-JavaScript unconditionally.

An Identifier may be an expression or the parameter of an ArrowFunctionExpression.

Line 26: All other types of estree. Node are not supported by Yocto-JavaScript. This includes programs such as 29 (estree.Literal) and const
 f = x => x (estree.VariableDeclarator).

In later Steps almost everything about the interpreter will change, but the parser will remain the same.

1.3.16 Generator [](#generator)

The generator transforms a Value produced by run() into a human-readable format (see § 1.3.1 for a high-level view of the architecture). Similar to what happened in the parser (see § 1.3.15), we may implement the generator by reusing existing tools from the JavaScript ecosystem, because we are representing Yocto-JavaScript programs and values with data structures that follow the ESTree specification. In particular, we use a library called Escodegen [??] to generate a string representation of an ESTree data structure, and a library called Prettier [26] to format that string. The following is the full implementation of the generator:

```
function generate(value: Value): string {
2
     return prettier
3
       .format(escodegen.generate(value), {
4
         parser: "babel",
5
         semi: false,
6
         arrowParens: "avoid",
7
       })
       .trim();
8
9 }
```

\begin{description} \item [Line 4:]

Prettier needs to parse and regenerate the string representing the value, in an architecture similar to that of the interpreter (see § 1.3.1), and it may use different parsers. We choose Babel [2], which is the default parser for JavaScript (Prettier also supports formatting other languages, for example, TypeScript and Markdown).

\item [Line 5:]

Instruct Prettier not to produce semicolons at the end of the line, for example, $x \Rightarrow y$ instead of $x \Rightarrow y$;

\item [Line 6:]

Instruct Prettier not to wrap parameters in parentheses, for example, \times => y instead of (x) => y.

\item [Line 8:]

Remove the newline at the end of the output produced by Prettier. \end{description}

1.3.17 Programs That Do Not Terminate

[](#programs-that-do-not-terminate)

\begin{center} \begin{tabular}{ll} \textbf{Example Program} & (f => f(f))(f
=> f(f)) \\textbf{Current Output} & DOES NOT TERMINATE \\textbf{Expected Output} & DOES NOT TERMINATE \\end{tabular} \end{center}

Technical Terms

This example program is also known as the Ω -combinator. The function \mathbf{f} => $\mathbf{f}(\mathbf{f})$ that is part of this program is also known as the U-combinator ($\Omega = (U)(U)$).

Yocto-JavaScript may express any program that a computer may run (see §\ref{The Computational Power of Yocto-JavaScript}), including some programs that do not terminate. For example, consider the program above, which is the shortest non-terminating program in Yocto-JavaScript. The following is a trace of the first call to run():

 $\begin{center} \begin{tabular}{rrcl} \textbf{Line} & \multicolumn{1}{l}{(see $ 1.3.13)} & & \ 3 & \mbox{expression} & = & (f => f(f))(f => f(f)) \ 9 \\ & \mbox{parameter} & = & f \ 10 & \mbox{body} & = & f(f) \ 12 & \mbox{argument} & = & f \\ => f(f) \ 13 & \mbox{substitute(body)} & = & (f => f(f))(f => f(f)) \ \mbox{end{tabular} \end{center}}$

The result of substitution is the same as the initial expression, so when it is passed as argument to the recursive call to run() in line 13, it causes run() to go into an infinite loop.

 $\begin{center} \begin{tabular}{ll} \textbf{Example Program} & (f => (f(f))(f(f)))(f => (f(f))(f(f))) \textbf{Current Output} & DOES \\ NOT TERMINATE \textbf{Expected Output} & DOES NOT TERMINATE \end{tabular} \end{center}$

There are also programs for which interpretation does not terminate that never produce the same expression twice. For example, consider the program above, which is a variation of the first program in which every variable reference to f has been replaced with f(f). The following is a trace of the first call to run():

 $\begin{center} \begin{tabular}{rrcl} \textbf{Line} & \multicolumn{1}{l}{(see § 1.3.13)} & \& \mbox{ where } F = f => (f(f))(f(f)) \ 3 & \mbox{ expression } \& = \& F(F) \ 9 & \mbox{ parameter } \& = \& f \ 10 & \mbox{ body } \& = \& (f(f))(f(f)) \ 12 & \mbox{ argument } \& = \& F \ 13 & \mbox{ substitute(body) } \& = \& (F(F))(F(F)) \ \mbox{ end{tabular}}$

\end{center}

The result of substitution ((F(F))(F(F))) is an expression that contains the initial expression (the first F(F)) in addition to some extra work (the second F(F)), so when it is passed as argument to the recursive call to run() in line 13, it causes run() to go into an infinite loop. Unlike what happened in the first example, when interpreting this program the expressions that are passed to run() never repeat themselves:

Non-termination is what we expect from an interpreter, but not from an analyzer, and as the second example demonstrates, preventing non-termination is not as simple as checking whether run() is being called with the same expression multiple times. As we move forward from an interpreter to an analyzer in the next Steps one of the main issues we address is termination: even if it takes a long time, an analyzer must eventually finish its work regardless of the program it is given.

Advanced

Detecting non-termination in an interpreter without losing any information about the original program is a problem that cannot be solved, regardless of the sophistication of the detector and the computational power available to it. The problem, which is known as the *halting problem*, is said to be *uncomputable* [30 (§ 8)], and is a direct consequence of the Turing completeness of Yocto-JavaScript (see § \ref{The Computational Power of Yocto-JavaScript}). In our analyzer we will guarantee termination by allowing some information

to be lost.

1.4 Step 1: Environment-Based Interpreter

[](#step-1-environment-based-interpreter)

The interpreter in Step 0 may not terminate for some programs, and preventing non-termination is one of the main issues we must address when developing an analyzer (see § \ref{Step 0: Programs That Do Not Terminate}). The source of non-termination in Step 0 is substitution, which may produce infinitely many new expressions and cause the interpreter to loop forever. In Step 1, we modify the interpreter so that it does not perform substitution, and as a consequence it considers only the finitely many expressions found in the input program. The interpreter in Step 1 may still not terminate, but that is due to other sources of non-termination that will be addressed in subsequent Steps.

1.4.1 Avoiding Substitution by Introducing Environments and Closures

[](#avoiding-substitution-by-introducing-environments-and-closures)

When the interpreter from Step 0 encounters a function call, it produces a new expression by traversing the body of the called function and substituting the references to the parameter with the argument, for example:

 $\begin{center} \begin{tabular}{ll} \text{Example Program} (see § 1.3.5) & (x => z => x)(y => y) \textbf{Step 0 Output} & z => (y => y) \textbf{tabular} \end{center} \label{eq:center}$

The issue with this strategy is that the expression $z \Rightarrow (y \Rightarrow y)$ does not

exist in the original program, and as mentioned in § \ref{Step 0: Programs That Do Not Terminate}, there is a possibility that the interpreter tries to produce infinitely many of these new expressions and loops forever. In Step 1 we want to avoid producing new expressions, so that the interpreter has to consider only the finitely many expressions found in the original program. We accomplish this by interpreting function calls with a different strategy: instead of performing substitution, we maintain a map from variables to the values with which they would have been substituted, for example:

Technical Terms

A map from variables to the values with which they would have been replaced (for example, [jsx `` \mapsto \langle `` js(y => y) , [] \rangle]) is something called an *environment*. A function along with an environment (for example, \langle js(z => x) ``, [`` jsx \mapsto \langle js(y => y), []\rangle]\rangle) is something called a *closure* [13].

In Step 1 we have a different notion of *value*: while in Step 0 the interpreter produced a *function*, now it produces a *closure*. It is possible to use the closure produced in Step 1 to recreate the function that would have been produced in Step 0 by substituting the variable references in the function body with the corresponding values from the environment found in the closure. We may do this to check

that the outputs of the interpreters are equivalent, but in Step 1 we do not perform substitution in the regular course of interpretation; we add more mappings to the environment and look up variable references in the environment.

Alternative Argument

Another way to reason about an environment-based interpreter is that it is a substitution-based interpreter in which substitutions are delayed until they are needed.

1.4.2 New Data Structures [](#new-data-structures)

The following are the data structures used to represent environments and closures:

```
type Value = Closure;
type Closure = {
  function: ArrowFunctionExpression;
  environment: Environment;
};
type Environment = MapDeepEqual<Identifier["name"], Value>;
```

Implementation Details

The MapDeepEqual data structure is provided by a JavaScript package developed by the author called Collections Deep Equal [6]. A MapDeepEqual is similar to a Map, except that the keys are compared by value, not by reference, for example:

```
> new Map([[{ age: 29 }, "Leandro"]]).get({ age: 29 });
undefined
> new MapDeepEqual([[{ age: 29 }, "Leandro"]]).get({ age: 29 });
"Leandro"
```

The occurrences of { age: 29} are objects with the same key and value, but they are not the same object.

1.4.3 Adding an Environment to the Runner

```
[](#adding-an-environment-to-the-runner)
```

The runner needs to maintain an environment, so we modify the implementation of run() from § 1.3.13 to introduce an auxiliary function called step() that receives an environment as an extra parameter:

```
function run(expression: Expression): Value {
 2
      return step(expression, new MapDeepEqual());
      function step(expression: Expression, environment: Environment):
   Value {
 4
        switch (expression.type) {
          case "ArrowFunctionExpression":
            return expression;
 7
          case "CallExpression":
 8
            const {
 9
              params: [parameter],
10
              body,
            } = step(expression.callee, environment);
11
12
            const argument = step(expression.arguments[0], environment);
13
            return step(substitute(body), environment);
            function substitute(expression: Expression): Expression {
              switch (expression.type) {
16
                case "ArrowFunctionExpression":
17
                  if (expression.params[0].name === parameter.name)
18
                    return expression;
19
                  return {
20
                    ...expression,
21
                    body: substitute(expression.body),
22
                  };
23
                case "CallExpression":
24
                  return {
25
                    ...expression,
```

```
26
                    callee: substitute(expression.callee),
27
                    arguments: [substitute(expression.arguments[0])],
28
                  };
29
                case "Identifier":
30
                  if (expression.name !== parameter.name) return
    expression;
31
                  return argument;
32
              }
33
            }
          case "Identifier":
            throw new Error(`Reference to undefined variable:
    ${expression.name}`);
36
        }
37
      }
38 }
```

\begin{description} \item [Line 3:]

We define the step() auxiliary function that receives an environment as an extra parameter.

```
\item [Line 2:]
```

The environment starts empty.

\item [Lines 11–13:]

The recursive calls to run() are changed to recursive calls to step() and the environment is propagated. \end{description}

The listing above does not compile yet because we are not producing closures. In the following sections we fix this by considering how to manage the environment for each type of expression.

1.4.4 A Function Definition [](#a-function-definition)

```
gle`\\end{tabular}\end{center}
```

When the interpreter encounters a function definition, it captures the current environment in a closure:

```
// step()
case "ArrowFunctionExpression":
  return { function: expression, environment };
```

1.4.5 A Function Call [](#a-function-call)

```
\begin{center} \begin{array}{l} \text{Example Program} & (x => z => x)(y => y) \\ \text{Current Output} & - \text{Example Program} & (x => z => x)(y => y) \\ \text{Example Program} & (x => z => z => x)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z => z)(y => y) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z)(y => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z) \\ \text{Example Program} & (x => z => z)
```

First, we remove substitute(), which is the goal of Step 1:

```
// step()
case "CallExpression":
  const {
    params: [parameter],
    body,
  } = step(expression.callee, environment);
  const argument = step(expression.arguments[0], environment);
  return step(body, environment);
```

Next, we fix the pattern that matches the result of the interpretation of the called function to take in account the closure:

```
// step()
case "CallExpression":
  const {
    function: {
       params: [parameter],
       body,
    },
```

```
environment: functionEnvironment,
} = step(expression.callee, environment);
const argument = step(expression.arguments[0], environment);
return step(body, environment);
```

Finally, we modify the recursive call to step() that interprets the function body so that it receives a new augmented environment including a mapping from the parameter (for example, \times) to the argument (for example, \langle js(y => y), [] \rangle'):

```
1 // step()
    case "CallExpression":
 3
      const {
 4
        function: {
 5
          params: [parameter],
 6
          body,
 7
        },
        environment: functionEnvironment,
      } = step(expression.callee, environment);
10
      const argument = step(expression.arguments[0], environment);
11
      return step(
12
        body,
13
        new MapDeepEqual(environment).set(parameter.name, argument)
14
      );
```

1.4.6 Name Reuse [](#name-reuse-1)

```
\begin{center} \begin{array}{l} \text{Lextbf} & (x => x => z \\ => x)(a => a)(y => y) \\ \text{Current Output} & (js(z => x) ``, [ `` jsx \mapsto \langle js(y => y) ``, [] \rangle] \\ \text{Lextbf} & `` math \langle (z => x), [x \mapsto \langle (y => y), [] \rangle] \\ \text{Langle} & `` \math \langle (z => x), [x \mapsto \langle (y => y), [] \rangle] \\ \text{Langle} & `` \math \langle (z => x), [x \mapsto \mapst
```

If a name is reused (for example, x in the example program above), then the second time it is encountered by step() it is overwritten in the environment

(see the call to set() in line 13 of § \ref{A Function Call}, which overwrites an existing map key). This causes the variable reference to x to refer to the second (inner) x, which is the expected behavior (it is what we called Option 2 in § \ref{Step 0: Name Reuse}).

1.4.7 A Variable Reference [](#a-variable-reference)

 $\begin{center} \begin{array}{l} \text{Lextbf} & \text{Example Program} & (y => y)(x => x) \\ \text{Lextbf} & - \text{Expected Output} & \langle js(y => y) \\ \text{Lextbf} & \text{Expected Output} & \langle js(y => y) \\ \text{Lextbf} & \text{Example Program} & \text{Lextbf} & \text{Expected Output} \\ \text{Lextbf} & \text{Lextbf} & \text{Expected Output} & \text{Lextbf} & \text{Expected Output} \\ \text{Lextbf} & \text{$

When we encounter a variable reference, we look it up in the current environment:

1.4.8 A Function Body Is Evaluated with the Environment in Its Closure

[](#a-function-body-is-evaluated-with-the-environment-in-its-closure)

This example program shows the difference between the current environment with which an expression is evaluated and the environment that comes from a closure. The following is a trace of the first call to step(), when a closure is created:

And the following is a trace of the recursive call to step() in which that closure is called:

 expression.arguments[0] & = & x \ \rowcolor[rgb]{.88,1,1} & environment & = & [jsx `` \mapsto \langle `` js(a => a) , [\cdots] \rangle, \cdots] \9 & tsstep(``\cdots `` ts) & = & math\langle `` js(z => x) , [js x\mapsto \langlejs(y => y) , [] \rangle] \rangle \5 & ts `parameter `& = &` js` z \rowcolor[rgb]{.88,1,1} 6 & ts `body `& = &` js` x \rowcolor[rgb]{.88,1,1} 8 & ts `functionEnvironment `& = &` math` [js x\mapsto \langlejs(y => y) , [] \rangle] \multicolumn{4}{c}{Paused before line 10}\\end{tabular} \end{center}

At this point, there are two expressions left to evaluate: the argument (expression.arguments[0]; line 10), and the body of the called function (body; lines 11–14). Both of these expressions have the same code (x), and our current implementation looks up this variable both times on the current environment, which produces the same value: $\langle js(a => a), \lceil cdots \rceil \rceil$

But this leads to an issue: we may not reason about $z \Rightarrow x$ by looking only at where it is defined; we must also examine all the places in which it may be called. This is the same issue we had to solve when considering name reuse in Step 0 (see $\$ \ref{Step 0: Name Reuse}). We would like, instead, for each x to refer to the value that existed in the environment where the closure is *created*, not where it is *called*:

\begin{center} \includegraphics[page = 8]{images.pdf} \end{center}

To implement this, we change the recursive call to step() that evaluates the function body so that it uses the environment coming from the closure (functionEnvironment) instead of the current environment (environment):

```
// step()
case "CallExpression":
  const {
    function: {
```

```
params: [parameter],
  body,
},
environment: functionEnvironment,
} = step(expression.callee, environment);
const argument = step(expression.arguments[0], environment);
return step(
  body,
  new MapDeepEqual(functionEnvironment).set(parameter.name, argument)
);
```

Technical Terms

The principle of being able to reason about a function only by looking at its definition is something called *local reasoning* (see § \ref{Step 0: Name Reuse}). The treatment given to the environment before this section is something called *dynamic scoping*, because the *scope* of a variable (where a variable is defined) is *dynamic*, depending on where the function is called. The treatment given to the environment in this section is something called *static scoping* or *lexical scoping*, because the scope of a variable is determined before we start interpreting the program.

Advanced

There are languages that implement dynamic scoping. In some cases dynamic scoping is the only option, for example, in the original implementation of LISP [16], though that was later considered a mistake [15]. In some cases dynamic scoping is the default, but there is an option to use static scoping, for example, in Emacs Lisp [14 (§ 12.10)]. In some cases dynamic scoping is an extra feature to be used sparingly, for example, in Racket's parameterize [9 (§ 4.13)].

1.4.9 The Entire Runner [7](#the-entire-runner-1)

We completed the changes necessary to transform the run() function from the substitution-based interpreter in Step 0 into an environment-based interpreter:

```
1
   type Value = Closure;
 2
 3
   type Closure = {
     function: ArrowFunctionExpression;
 5
      environment: Environment;
 6
   };
   type Environment = MapDeepEqual<Identifier["name"], Value>;
9
    function run(expression: Expression): Value {
      return step(expression, new MapDeepEqual());
11
12
      function step(expression: Expression, environment: Environment):
    Value {
13
        switch (expression.type) {
14
          case "ArrowFunctionExpression":
15
            return { function: expression, environment };
          case "CallExpression":
16
17
            const {
18
              function: {
19
                params: [parameter],
20
                body,
21
              },
22
              environment: functionEnvironment,
23
            } = step(expression.callee, environment);
24
            const argument = step(expression.arguments[0], environment);
25
            return step(
26
              body,
27
              new MapDeepEqual(functionEnvironment).set(parameter.name,
    argument)
28
            );
29
          case "Identifier":
30
            const value = environment.get(expression.name);
31
            if (value === undefined)
32
              throw new Error(
33
                `Reference to undefined variable: ${expression.name}`
```

```
34          );
35          return value;
36     }
37     }
38  }
```

Advanced

1.4.10 Operational Semantics [](#operational-semantics)

We adapt the operational semantics from § 1.3.14 to the interpreter defined in Step 1. First, we change the notion of values:

```
\begin{center} \begin{tabular}{rcll} v \& = \& \ js( ``x `` js => e js) \\ ``, \rho \rangle `` \& Values / Closures \\ `` math\rho & = & math`\{x \mapsto v, \cdots\} `` & Environments \end{tabular} \end{center} \\ We then define the relation $\rho \vdash e \Rightarrow v$ to be equivalent to the new im-
```

We then define the relation $\rho \vdash e \Rightarrow v$ to be equivalent to the new implementation of run():

 $\label{lem:langle (x =>e_b), \rho_f \rangle (x =>e_b), \rho_f \rangle \rho \vdash e_a \Rightarrow v_a \rho_f \cup {x \mapsto v_a} \vdash e_b \Rightarrow v \} {\rho \vdash e_f(e_a) \Rightarrow v}$

\inferrule { } {\rho \vdash x \Rightarrow \rho(x)} \end{mathpar}

1.4.11 Generator [](#generator-1)

We modify the generator from § 1.3.16 to support closures. For example, the following is the representation of the closure from § \ref{A Function Call}:

The following is the modified implementation of generate():

```
function generate(value: any): string {
2
      return JSON.stringify(
 3
        value,
4
        (key, value) => {
5
          if (value.type !== undefined)
 6
            return prettier
 7
              .format(escodegen.generate(value), {
                parser: "babel",
 9
                semi: false,
                arrowParens: "avoid",
10
11
              })
12
              .trim();
13
          return value;
14
        },
15
        2
16
      );
17
   }
```

\begin{description} \item [Line 1:]

Change the input type from Value to any, because this implementation of strinfigy() supports any data structure, including the data structures we will

define in later Steps.

\item [Line 2:]

Call JSON. stringify() [22], which traverses any data structure and converts it into a string.

\item [Line 4:]

Provide a replacer that is responsible for converting data structures that represent Yocto-JavaScript programs into strings.

\item [Line 5:]

Check whether a data structure represents an Yocto-JavaScript program by checking the existence of a field called type (see § 1.3.2), in which case we use the previous implementation of generate() (see § 1.3.16) to produce a string.

\item [Line 15:]

Format the output with indentation of two spaces. \end{description}

This implementation of generate() supports not only closures but any data structure (because of JSON.stringify()), so it will remain the same in the following Steps.

1.4.12 Programs That Do Not Terminate

[](#programs-that-do-not-terminate-1)

The programs that do not terminate in Step 0 (see § \ref{Step 0: Programs That Do Not Terminate}) do not terminate in Step 1 either, because the interpreters are equivalent except for the technique used to interpret function calls, but the sources of non-termination are different. In Step 0 substitution may produce infinitely many expressions, including expressions that do not occur in the original program. In Step 1 the interpreter considers only the finitely many expressions that occur in the original program, but it may produce infinitely many environ-

ments.

This difference is significant because there are programs that produce infinitely many different expressions in Step 0, but produce the same expression and environment repeatedly in Step 1, and in these cases we could detect non-termination by checking whether the runner is in a loop with the same arguments, for example:

 $\label{thm:local_local$

But this strategy is insufficient to guarantee termination, because there are programs that do not terminate which produce infinitely many different environments, for example:

```
, [jsc `` \mapsto \langle `` jsC , [jsc `` \mapsto \langle
`` js(y => y) , [] \rangle, \cdots] \rangle, \cdots] \rangle,
\cdots] \rangle \( \langle \lang
```

The interpreter in Step 1 may produce infinitely many different environments because environments may be nested. That is the issue that we address in Step 2.

Technical Terms

The nesting of environments in Step 1 characterizes them as something called *recursive data structures*: data structures that may contain themselves. The data structures used to represented Yocto-JavaScript programs are recursive as well (see § 1.3.2).

1.5 Step 2: Store-Based Interpreter

[](#step-2-store-based-interpreter)

The source of non-termination in Step 1 is the nesting of the environments (see § \ref{Step 1: Programs That Do Not Terminate}). In Step 2, we address this issue by introducing a layer of indirection between a name in the environment and its

corresponding value. The interpreter in Step 2 may still not terminate, but that is due to other sources of non-termination that will be addressed in subsequent Steps.

1.5.1 Avoiding Nested Environments by Introducing a Store

[](#avoiding-nested-environments-by-introducing-a-store)

In Step 1 a closure contains an environment mapping names to other closures, which in turn contain their own environments mapping to yet more closures. In Step 2, we remove this circularity by introducing a layer of indirection: an environment maps names to *addresses*, which may be used to lookup values in a *store*, for example:

Each closure continues to include its own environment, because it needs to look up variable references from where the closure was created (see § \ref{A Function Body Is Evaluated with the Environment in Its Closure}), but there is only one store for the entire interpreter, and we avoid ambiguities by allocating different addresses, for example:

 $\label{thm:linear} $\left(See \S \left(A Function Body Is Evaluated with the Environment in Its Closure \right) & \multicolumn{1}{c}{\left(Step 1} \right) & \multicolumn{1}{c}{\left(Step 2} \right) & \multicolumn{1}{c$

The runner must return the store along with the value, for the variable references to be looked up, for example:

Advanced

The technique used in Step 2 is related to the run-time environments that are the target of traditional compilers for languages such as C [1 (§ 7)]: an environment corresponds to some of the data stored in an activation frame on the call stack, and the store corresponds to the heap.

1.5.2 New Data Structures [](#new-data-structures-1)

The following are the data structures used to represent environments, stores, and addresses:

```
type Environment = MapDeepEqual<Identifier["name"], Address>;
type Store = MapDeepEqual<Address, Value>;
```

```
type Address = number;
```

1.5.3 Adding a Store to the Runner

```
[](#adding-a-store-to-the-runner)
```

We modify the implementation of run() from § \ref{Step 1: The Entire Runner} to introduce a store:

```
function run(expression: Expression): { value: Value; store: Store }
{
  const store: Store = new MapDeepEqual();
  return { value: step(expression, new MapDeepEqual()), store };
  function step(expression: Expression, environment: Environment):
  Value {
    // ...
}
```

\begin{description} \item [Lines 1 and 3:]

The store is returned because it is necessary to look up variable references in the value.

```
\item [Lines 2 and 4:]
```

The store is unique for the whole interpreter, unlike environments which are different for each closure, so we create only one store that is always available to step() instead of adding it as an extra parameter. \end{description}

1.5.4 Adding a Value to the Store [](#adding-a-value-to-the-store)

\end{tabular} \end{center}

In Step 1, when we encounter a function call we extend the functionEnvironment with a mapping from the parameter.name to the argument (see § \ref{A Function Call}, \ref{A Function Body Is Evaluated with the Environment in Its Closure}). In Step 2, we introduce the store as a layer of indirection:

```
// step()
   case "CallExpression": {
3
     const {
4
        function: {
          params: [parameter],
 6
          body,
 7
        },
8
        environment: functionEnvironment,
9
      } = step(expression.callee, environment);
10
      const argument = step(expression.arguments[0], environment);
11
     const address = store.size;
12
     store.set(address, argument);
13
     return step(
14
        body,
15
        new MapDeepEqual(functionEnvironment).set(parameter.name,
    address)
16
     );
17
   }
```

\begin{description} \item [Line 11:]

Allocate an address. We use the store.size as the address because as the store grows this number changes, so it is guaranteed to be unique throughout the interpretation of a program.

```
\item [Line 15:]
```

Extend the functionEnvironment with a mapping from the parameter.name to the address.

```
\item [Line 12:]
```

Extend the store with a mapping from the address to the argument. This is mutating the unique store that is available to the entire step() function, not creating a new store in the same way that extending an environment creates a new environment (see line 15). \end{description}

1.5.5 Retrieving a Value from the Store

```
[](#retrieving-a-value-from-the-store)
```

```
\begin{center} \begin{tabular}{ll} \textbf{Example Program} & (y => y)(x => x) \textbf{Current Output} & - \textbf{Expected Output} & value = \langle js(y => y) ``, [] \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \textbf{Expected Output} & `` tsstore = math[ `` js0 \mapsto \maps
```

In Step 1 we retrieved values directly from the environment (see § \ref{A Variable Reference}), but in Step 2 we have to go through the store:

\begin{description} \item [Line 3:]

Retrieve the address from the environment.

\item [Line 8:]

Retrieve the value from the store at the given address found in the environment. The address is guaranteed to be in the store because we extend the store and the environment together (see § \ref{Adding a Value to the

Store]), so we use ! to indicate that get() may not return undefined. \end{description}

1.5.6 The Entire Runner [](#the-entire-runner-2)

We completed the changes necessary to remove the circularity between closures and environments:

```
1 type Environment = MapDeepEqual<Identifier["name"], Address>;
 2
   type Store = MapDeepEqual<Address, Value>;
 3
 4
 5
   type Address = number;
 6
 7
   function run(expression: Expression): { value: Value; store: Store
    } {
      const store: Store = new MapDeepEqual();
      return { value: step(expression, new MapDeepEqual()), store };
10
      function step(expression: Expression, environment: Environment):
   Value {
11
        switch (expression.type) {
12
          case "ArrowFunctionExpression": {
13
            return { function: expression, environment };
          }
          case "CallExpression": {
15
16
            const {
17
              function: {
                params: [parameter],
18
19
                body,
20
              },
21
              environment: functionEnvironment,
22
            } = step(expression.callee, environment);
23
            const argument = step(expression.arguments[0], environment);
24
            const address = store.size;
25
            store.set(address, argument);
26
            return step(
              body,
27
28
              new MapDeepEqual(functionEnvironment).set(parameter.name,
```

```
address)
29
            );
30
31
          case "Identifier": {
32
            const address = environment.get(expression.name);
33
            if (address === undefined)
34
              throw new Error(
                 `Reference to undefined variable: ${expression.name}`
35
36
              );
37
            return store.get(address)!;
39
        }
40
      }
41
   }
```

Advanced

1.5.7 Operational Semantics [](#operational-semantics-1)

We adapt the operational semantics from § \ref{Step 2: Operational Semantics} to the interpreter defined in Step 2. First, we change the notion of environments:

 $\begin{center} \begin{tabular}{rcll} \rho \& = \& \ \{x \mapsto A, \cdots\} \& \ Environments \setminus \sigma \& = \& \ \{A \mapsto v, \cdots\} \& \ Stores \setminus A \& = \& \ \mathbb{N} \& \ Addresses \setminus end{tabular} \end{center}$

We then define the relation $ho,\sigma \vdash e \Rightarrow \langle v,\sigma \rangle$ to be equivalent to the new implementation of run():

 $\label{langle (x =>e) Rightar-row langle (x =>e), \\ \label{langle (x =>e), rho rangle, sigma rangle}$

 $\label{thm:condition} $$\inf\{ \rho_{\alpha, \sigma} \cdot e_f \cdot e_f \cdot e_f \cdot e_b , \rho_{\alpha, \sigma} \cdot e_a \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_f \cdot e_f \cdot e_f \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_f \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\} . $$ inferrule $$\} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\} . $$ inferrule $$\} . $$ inferrule $$\} . $$ inferrule $$\} . $$ inferrule $$\{ \rho_{\alpha, \sigma} \cdot e_b \cdot e_b \cdot e_b \cdot e_b \} . $$ inferrule $$\} . $$ inferrule $$\} . $$ inferru$

1.5.8 Programs That Do Not Terminate

[](#programs-that-do-not-terminate-2)

The programs that do not terminate in Step 1 (see § \ref{Step 1: Programs That Do Not Terminate}) do not terminate in Step 2 either, because the interpreters are equivalent except for the treatment of environments, but the sources of non-termination are different. In both cases the issue is that the interpreter may create infinitely many environments, but in Step 1 the environments are nested, and in Step 2 they contain different addresses, for example:

 $\label{thm:local_local$

```
[ `` jsc \mapsto \langle jsC ``, [ `` jsc \mapsto \langle js(y
=> y) ``, [] \rangle, \cdots] \rangle, \cdots] \rangle,
\cdots] \rangle, \cdots] \rangle `` \\ \multicolumn{1}{c}{\`
math\vdots } \\ \multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\textbf{Step 2}} \\
\multicolumn{1}{c}{\text{mapsto `` jsc `` \mapsto \\
\mapsto \langle f(f)(C), [c \mapsto 2, \cdots] \rangle } \\
\multicolumn{1}{c}{\text{mapsto } \\
\multicolumn{1}{c}{\text{mapsto } \\
\mapsto \langle \cdots] \rangle \\
\mapsto \langle \cdots] \rangle, jsc \cdots] \rangle, jsc \\
\mapsto \langle \cdots] \rangle, jsc \cdots] \rangle, jsc \\
\mapsto \langle \cdots] \rangle, \cdots] \rangle, jsc \cdots] \rangle, jsc \\
\mapsto \langle, \cdots] \rangle, jsc \cdots] \rangle, jsc \\
\mapsto \langle, \cdots] \rangle, jsc \cdots] \rangle, jsc \\
\mapsto \langle, \cdots] \rangle, jsc \cdots] \rangle, jsc \\\
\mapsto \langle, \cdots] \rangle, jsc \cdots] \rangle, jsc \\\
\mapsto \langle, \cdots] \rangle, jsc \cdots] \rangle, jsc \\\
\mapsto \langle, \cdots] \rangle, jsc \cdots \rangle, jsc \cdots \rangle, jsc \cdots
```

We address this issue in Step 3.

1.6 Step 3: Finitely Many Addresses

[](#step-3-finitely-many-addresses)

1.6.1 The Entire Runner [7(#the-entire-runner-3)

We completed the changes necessary to produce only finitely many addresses:

```
type Value = SetDeepEqual < Closure >;

type Address = Identifier;

function run(expression: Expression): { value: Value; store: Store
```

```
} {
 6
      const store: Store = new MapDeepEqual();
      return { value: step(expression, new MapDeepEqual()), store };
      function step(expression: Expression, environment: Environment):
    Value {
 9
        switch (expression.type) {
          case "ArrowFunctionExpression": {
10
11
            return new SetDeepEqual([{ function: expression,
    environment }]);
12
          }
13
          case "CallExpression": {
14
            const value: Value = new SetDeepEqual();
15
            for (const {
16
              function: {
17
                params: [parameter],
18
                body,
19
              },
20
              environment: functionEnvironment,
21
            } of step(expression.callee, environment)) {
22
              const argument = step(expression.arguments[0],
    environment);
23
              const address = parameter;
24
              store.merge(new MapDeepEqual([[address, argument]]));
25
              value.merge(
26
                step(
27
                  body,
28
                  new
    MapDeepEqual(functionEnvironment).set(parameter.name, address)
29
                )
30
              );
31
            }
32
            return value;
33
          }
34
          case "Identifier": {
            const address = environment.get(expression.name);
35
36
            if (address === undefined)
37
              throw new Error(
38
                `Reference to undefined variable: ${expression.name}`
39
              );
40
            return store.get(address)!;
41
          }
```

```
42 }
43 }
```

Bibliography

- 1. Alfred Aho, Monica Lam, Ravi Sethi, and Jeffrey Ullman. *Compilers: Principles, Techniques, and Tools*. Addison-Wesley. 2006.
- 2. *Babel*. https://babeljs.io. Accessed 2020-04-06.
- 3. Babel Types. https://git.io/JfZF8. Accessed 2020-05-06.
- 4. Emery Berger, Celeste Hollenbeck, Petr Maj, Olga Vitek, and Jan Vitek.

 On the Impact of Programming Languages on Code Quality: A Reproduction Study. ACM Transactions on Programming Languages and Systems. 2019. https://doi.org/10.1145/3340571.
- 5. Gavin Bierman, Martín Abadi, and Mads Torgersen. *Understanding Type-Script*. European Conference on Object-Oriented Programming (ECOOP). 2014.
- 6. **Leandro Facchinetti**. *Collections Deep Equal*. https://github.com/leafac/collections-deep-equal. Accessed 2020-04-01.
- 7. Matthias Felleisen. *On the Expressive Power of Programming Languages*. Science of Computer Programming. 1991. https://doi.org/10.1016/0167-6423(91)90036-W.
- 8. Matthias Felleisen, Robert Bruce Findler, and Matthew Flatt. *Semantics Engineering with PLT Redex*. The MIT Press. 2009.
- 9. Matthew Flatt, Robert Bruce Findler, and PLT. *The Racket Guide*. https://docs.racket-lang.org/guide/. Accessed 2020-04-13.
- 10. Mike Grant, Zachary Palmer, and Scott Smith. *Principles of Programming Languages*. 2020.
- 11. JetBrains. The State of Developer Ecosystem 2019.

 https://www.jetbrains.com/lp/devecosystem-2019/.Ac-

- cessed 2020-01-14.
- 12. Gilles Kahn. *Natural Semantics*. Annual Symposium on Theoretical Aspects of Computer Science. 1987.
- 13. Peter Landin. *The Mechanical Evaluation of Expressions*. The Computer Journal. 1964.
- 14. Bil Lewis, Dan LaLiberte, and Richard Stallman. *GNU Emacs Lisp Reference Manual*. 2015.
- 15. John McCarthy. *History of LISP*. History of Programming Languages. 1978. https://doi.org/10.1145/800025.1198360.
- 16. John McCarthy. *Recursive Functions of Symbolic Expressions and Their Computation by Machine, Part I.* Communications of the ACM. 1960. https://doi.org/10.1145/367177.367199.
- 17. Matthew Might. *The Language of Languages*.

 http://matt.might.net/articles/grammars-bnf-ebnf/. Accessed 2020-01-17.
- 18. Matthew Might, Yannis Smaragdakis, and David Van Horn. *Resolving and Exploiting the k-CFA Paradox: Illuminating Functional vs Object-Oriented Program Analysis*. Programming Language Design and Implementation (PLDI). 2010. https://doi.org/10.1145/1806596.1806631.
- 19. Mozilla. *Arrow Function Expressions*.

https://developer.mozilla.org/en-US/docs/Web/
JavaScript/Reference/Functions/Arrow_functions. Accessed
2020-01-16.

20. Mozilla. Destructuring Assignment.

https://developer.mozilla.org/en-US/docs/Web/ JavaScript/Reference/Operators/

- Destructuring assignment. Accessed 2020-01-27.
- 21. Mozilla.eval().https://developer.mozilla.org/en-US/docs/Web/JavaScript/Reference/Global_Objects/eval.Accessed 2020-02-13.
- 22. Mozilla. JSON.stringify(). https://developer.mozilla.org/
 en-US/docs/Web/JavaScript/Reference/Global_Objects/
 JSON/stringify. Accessed 2020-04-13.
- 23. Mozilla. Spread Syntax. https://developer.mozilla.org/en-US/docs/Web/JavaScript/Reference/Operators/Spread_syntax. Accessed 2020-02-03.
- 24. Mozilla. *Template Literals*. https://developer.mozilla.org/en-US/docs/Web/JavaScript/Reference/Template_literals. Accessed 2020-02-03.
- 25. Gordon Plotkin. *Call-By-Name, Call-By-Value and the* λ -*Calculus*. Theoretical Computer Science. 1975. https://doi.org/10.1016/0304-3975(75)90017-1.
- 26. Prettier. https://prettier.io. Accessed 2020-02-18.
- 27. John Reynolds. *Definitional Interpreters for Higher-Order Programming Languages*. Proceedings of the ACM Annual Conference. 1972. https://doi.org/10.1145/800194.805852.
- 28. Olin Shivers. *Control-Flow Analysis of Higher-Order Languages*. PhD Dissertation, Carnegie Mellon University. 1991.
- 29. Stack Overflow. *Developer Survey Results 2019*. https://insights.stackoverflow.com/survey/2019. Accessed 2020-01-14.
- 30. Tom Stuart. Understanding Computation: From Simple Machines to Impos-

sible Programs. O'Reilly Media. 2013.

31. Basarat Ali Syed. *TypeScript Deep Dive*.

https://basarat.gitbook.io/typescript/.Accessed 2020-01-17.

32. TypeScript Documentation. https://www.typescriptlang.org/docs. Accessed 2020-01-17.