

BE - Discussion #2, 2020-09-11

Nice to see you again!

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* please unmute, show video,
and fully participate

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Announcements

- make sure you have all three exams and all quizzes listed in the syllabus on your calendar
 - first exam is 3 weeks from today!
- if you have questions, please check to see if your question has been answered on the discussion forum, and if it hasn't then post it! (Do not email Prof. Attaway)
- TA Open Hours:
 - Sunday 4-10 pm
 - Tuesday 6-10 pm
 - Thursday 4-10 pm {Devin's OH 6-8 pm Thursday}
- Practice quiz this afternoon ... please take like a real quiz!!!
 - it will release on Gradescope at 4:40 pm, due by 4:55 pm
 - quizzes will only be accepted via gradescope, not email
 - download quiz, fill it out, scan it, upload as a PDF.
 - pdf must be correct number of pages
 - time yourself so that you're ready for week
 - will also be open for a couple days to get extra practice with uploading
- Classes next week:
 - in-person will be an option by invitation only
 - class will be conducted the same, so fully via zoom with breakout rooms like we have been doing
 - you can only come to the room if you received an invite

Review of Material

- vectors and matrices
- matrix operations and functions
- logical indexing vs. using find()
- anything else?

Vectors + Matrices

$$1:0.5:3 \rightarrow 1 \quad 1.5 \quad 2 \quad 2.5 \quad 3$$

$$\text{linspace}(1, 3, 5) \rightarrow 1 \quad 1.5 \quad 2 \quad 2.5 \quad 3$$

↑
of elements

spacing for linspace formula:
 $(x_2 - x_1) / (n - 1)$

$$\text{linspace}(x_1, x_2, n)$$

ex. $\text{linspace}(9, 5, 3)$

$$\hookrightarrow (5 - 9) / (3 - 1) \rightarrow (-4) / (2) \rightarrow -2$$

$$\Rightarrow 9 \quad 7 \quad 5$$

Matrix (Array) Multiplication

$$A = \begin{bmatrix} 1 & 4 \\ 3 & 2 \end{bmatrix}$$

2×2

$$B = \begin{bmatrix} 2 & 1 & 3 \\ 1 & 5 & 6 \\ 3 & 6 & 0 \end{bmatrix}$$

3×3

$$C = \begin{bmatrix} 3 & 2 & 5 \\ 4 & 1 & 2 \end{bmatrix}$$

2×3

ex. $3 * A$

$$\begin{bmatrix} 3 & 12 \\ 9 & 6 \end{bmatrix}$$

ex. $A * B$

2×2 3×3

↑
dimensions don't match

INVALID

ex. $A * C$

$$\begin{bmatrix} 1 & 4 \\ 3 & 2 \end{bmatrix} \begin{bmatrix} 3 & 2 & 5 \\ 4 & 1 & 2 \end{bmatrix}$$

2×2 2×3
↑
dimensions match!

$$\begin{bmatrix} 1 \cdot 3 + 4 \cdot 4 & 1 \cdot 2 + 4 \cdot 1 & 1 \cdot 5 + 4 \cdot 2 \\ 3 \cdot 3 + 2 \cdot 4 & 3 \cdot 2 + 2 \cdot 1 & 3 \cdot 5 + 2 \cdot 2 \end{bmatrix}$$

$$\begin{bmatrix} 19 & 6 & 13 \\ 17 & 8 & 19 \end{bmatrix} \leftarrow \text{final answer, VALID}$$

↑ 2×3 matrix (outer dimensions)

$$D = \begin{bmatrix} 2 & 4 \\ 6 & 8 \end{bmatrix}_{2 \times 2} \quad E = \begin{bmatrix} 0 & 1 \\ 2 & 3 \end{bmatrix}_{2 \times 2}$$

$2 \cdot 0 + 4 \cdot 2$ $2 \cdot 1 + 4 \cdot 3$
 $6 \cdot 0 + 8 \cdot 2$ $6 \cdot 1 + 8 \cdot 3$

$D * E$... VALID, you'll get a 2×2 matrix $\Rightarrow \begin{bmatrix} 8 & 14 \\ 16 & 30 \end{bmatrix}$

$D .* E$... MSO VALID

$$\begin{bmatrix} \underline{2} & \underline{4} \\ \underline{6} & \underline{8} \end{bmatrix} \begin{bmatrix} \underline{0} & \underline{1} \\ \underline{2} & \underline{3} \end{bmatrix} \Rightarrow \begin{bmatrix} 0 & 4 \\ 12 & 24 \end{bmatrix} \quad \begin{array}{l} \text{element-by-} \\ \text{element operation} \end{array}$$

Changing Elements in an Array

$\gg v = 1:5$

$\gg v =$

1 2 3 4 5

$\gg v(2:5) = 7:9$

$\gg v =$

1 7 8 9 5

$\gg \text{mat} = [2:4, 5:7]$

$\gg \text{mat} =$

2 3 4

5 6 7

$\gg \text{mat}(1, :) =$

$\gg \text{mat} =$

1 1 1

5 6 7

rand() vs. randi()

$\text{rand()} * 5 + 5$ will generate random real numbers from 5 to 10

\uparrow generate \uparrow multiply that * by 5 \uparrow will then add 5 to $5 * 5$
 # from 0 to 1

isequal vs. ==

$\gg \text{vec1} = 1:3; \quad \Rightarrow \quad 1 \quad 2 \quad 3$

$\gg \text{vec2} = [1 \ 0 \ 3]; \quad \Rightarrow \quad 1 \quad 0 \quad 3$

$\gg \text{isequal}(\text{vec1}, \text{vec2})$

$\gg \text{ans} =$

0

← single logical value ... these aren't identical vectors

$\gg \text{vec1} == \text{vec2}$

$\gg \text{ans} =$

1 0 1

← element-by-element logical values

Logical Indexing vs. Using find()

```
>> vect = randi([-5, 10], 1, 6)
```

```
>> vect =
```

-5 8 9 5 7 6

```
>> vect(vect > 0)
```

```
>> ans =
```

8 9 5 7 6

← gives the actual elements > 0

```
>> find(vect > 0)
```

```
>> ans =
```

2 3 4 5 6

← find() returns the indices

veca =

2

4

6

8

(4 x 1)

vecb =

3 6 9 12

(1 x 4)

EXTRA STUFF

vecb * veca

$$\begin{bmatrix} 3 & 6 & 9 & 12 \end{bmatrix} \begin{bmatrix} 2 \\ 4 \\ 6 \\ 8 \end{bmatrix}$$

veca .* vecb NOT VALID

veca' .* vecb VALID

veca .* 3 is valid

veca * 3 is also valid

(MATLAB knows it's scalar mult.)