

Assignment #8 posted, due in 1 week!

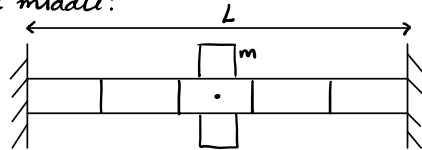
Vibrations-lecture 24  
Thur., 2021-04-22

Assignment #7 overview

- no zero nat. freq. because no rigid body movement
- went over solution
- MATLAB has `findpeaks()`! → to find "valleys" do one over the function

Assignment #8 Notes:

- beam fixed at both ends
- mass in the middle!



$l$  = length of 1 element



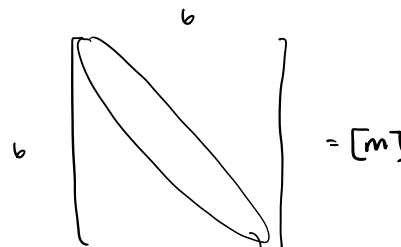
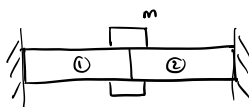
— non uniformity so can't use analytic approach... need FEM!

for a beam element, have 4 DOF:



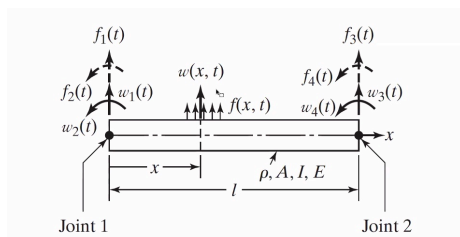
simple 2-element system (don't do two on the assignment!)

$6 \times 6$  matrix



mass will need to be added somewhere along diagonal?

MATLAB codes



← need to keep this numbering system in order to use the MATLAB codes: as in  $w_1(t)$  is up @ point 1 and  $w_2(t)$  is rotation at point 2

← why is mass matrix not diagonal?

- positive semi-definite ( $T = \frac{1}{2} \dot{x}^T [m] \dot{x} \geq 0$ )
- positive semi-definite for  $[k]$ , too ( $U = \frac{1}{2} x^T [k] x \geq 0$ )

if all eigenvalues  $\geq 0$ , then  $[k]$  and/or  $[m]$  are positive semi-definite

matlab scripts have matrices for  $m, k$  already typed in

→  $p = \#$  of elements

⊗ beam\_matrices.m

• each node has 2 DOF

• next part blows up the scalars to vectors  $r, x$ , such as  $\rho$

↳  $l$  will be sent in as a vector

• loop over elements, fill in  $[m]$  and  $[k]$

↳ then go through the connectivity

•  $M, K$  come out as if beam is free-free (in mid air)

↳ need to add the fixed-fixed in post processing

↳ also add the pin, mass, whatever in post-processing

beam\_matrices\_test.m

• still beam

• 200 elements, 1m long

• nodal locations, use  $x = \text{linspace}(0, L, Q)$  ↖ # of nodes

• length of elements =  $\text{diff}(x)$

• natural frequencies on diagonal of  $D$ , after square-rooting them, after  $[V, D] = \text{eig}()$

• Ch. 8:

$$\beta_1 l = 4.730041$$

$$\beta_2 l = 7.853205$$

$$\beta_3 l = 10.995605$$

$$\beta_4 l = 14.137165$$

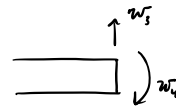
• higher # elements, longer it takes MATLAB to run

$$Q = \# \text{ nodes} = p + 1$$

$$N = \# \text{ DOF} = 2Q$$

$$M(N-1, N-1) = M(N-1, N-1) + \Delta m$$

if adding to



$w$

$\theta$

$w$

$\theta$

$\vdots$

$w$

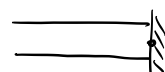
$\theta$

only add mass to xlatational, not rotational DOF

↳ bc treating like a pt. mass

• the natural frequencies will need to be real, not imaginary

⊗ when make something stiffer, natural frequencies go up



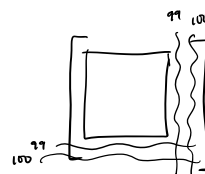
$$x = \left\{ \begin{matrix} \vdots \\ w \\ \theta \end{matrix} \right\}$$

$$w = 0$$

$$\frac{dw}{dx} = \theta = 0$$



the last node has these DOF



⇒ ZERO OUT ROW + COLUMN OF  $K + M$  FOR THAT DOF