

DZ11-Marcec-Lea.R

Lea

2022-01-13

```
data(iris)
str(iris)
```

```
## 'data.frame':    150 obs. of  5 variables:
##  $ Sepal.Length: num  5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...
##  $ Sepal.Width : num  3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...
##  $ Petal.Length: num  1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...
##  $ Petal.Width : num  0.2 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...
##  $ Species      : Factor w/ 3 levels "setosa","versicolor",...: 1 1 1 1 1 1 1 1 1 1
##  1 ...
```

```
# priprema podataka
df <- iris
df
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
## 1	5.1	3.5	1.4	0.2	setosa
## 2	4.9	3.0	1.4	0.2	setosa
## 3	4.7	3.2	1.3	0.2	setosa
## 4	4.6	3.1	1.5	0.2	setosa
## 5	5.0	3.6	1.4	0.2	setosa
## 6	5.4	3.9	1.7	0.4	setosa
## 7	4.6	3.4	1.4	0.3	setosa
## 8	5.0	3.4	1.5	0.2	setosa
## 9	4.4	2.9	1.4	0.2	setosa
## 10	4.9	3.1	1.5	0.1	setosa
## 11	5.4	3.7	1.5	0.2	setosa
## 12	4.8	3.4	1.6	0.2	setosa
## 13	4.8	3.0	1.4	0.1	setosa
## 14	4.3	3.0	1.1	0.1	setosa
## 15	5.8	4.0	1.2	0.2	setosa
## 16	5.7	4.4	1.5	0.4	setosa
## 17	5.4	3.9	1.3	0.4	setosa
## 18	5.1	3.5	1.4	0.3	setosa
## 19	5.7	3.8	1.7	0.3	setosa
## 20	5.1	3.8	1.5	0.3	setosa
## 21	5.4	3.4	1.7	0.2	setosa
## 22	5.1	3.7	1.5	0.4	setosa
## 23	4.6	3.6	1.0	0.2	setosa
## 24	5.1	3.3	1.7	0.5	setosa
## 25	4.8	3.4	1.9	0.2	setosa
## 26	5.0	3.0	1.6	0.2	setosa
## 27	5.0	3.4	1.6	0.4	setosa
## 28	5.2	3.5	1.5	0.2	setosa
## 29	5.2	3.4	1.4	0.2	setosa
## 30	4.7	3.2	1.6	0.2	setosa
## 31	4.8	3.1	1.6	0.2	setosa

## 32	5.4	3.4	1.5	0.4	setosa
## 33	5.2	4.1	1.5	0.1	setosa
## 34	5.5	4.2	1.4	0.2	setosa
## 35	4.9	3.1	1.5	0.2	setosa
## 36	5.0	3.2	1.2	0.2	setosa
## 37	5.5	3.5	1.3	0.2	setosa
## 38	4.9	3.6	1.4	0.1	setosa
## 39	4.4	3.0	1.3	0.2	setosa
## 40	5.1	3.4	1.5	0.2	setosa
## 41	5.0	3.5	1.3	0.3	setosa
## 42	4.5	2.3	1.3	0.3	setosa
## 43	4.4	3.2	1.3	0.2	setosa
## 44	5.0	3.5	1.6	0.6	setosa
## 45	5.1	3.8	1.9	0.4	setosa
## 46	4.8	3.0	1.4	0.3	setosa
## 47	5.1	3.8	1.6	0.2	setosa
## 48	4.6	3.2	1.4	0.2	setosa
## 49	5.3	3.7	1.5	0.2	setosa
## 50	5.0	3.3	1.4	0.2	setosa
## 51	7.0	3.2	4.7	1.4	versicolor
## 52	6.4	3.2	4.5	1.5	versicolor
## 53	6.9	3.1	4.9	1.5	versicolor
## 54	5.5	2.3	4.0	1.3	versicolor
## 55	6.5	2.8	4.6	1.5	versicolor
## 56	5.7	2.8	4.5	1.3	versicolor
## 57	6.3	3.3	4.7	1.6	versicolor
## 58	4.9	2.4	3.3	1.0	versicolor
## 59	6.6	2.9	4.6	1.3	versicolor
## 60	5.2	2.7	3.9	1.4	versicolor
## 61	5.0	2.0	3.5	1.0	versicolor
## 62	5.9	3.0	4.2	1.5	versicolor
## 63	6.0	2.2	4.0	1.0	versicolor
## 64	6.1	2.9	4.7	1.4	versicolor
## 65	5.6	2.9	3.6	1.3	versicolor
## 66	6.7	3.1	4.4	1.4	versicolor
## 67	5.6	3.0	4.5	1.5	versicolor
## 68	5.8	2.7	4.1	1.0	versicolor
## 69	6.2	2.2	4.5	1.5	versicolor
## 70	5.6	2.5	3.9	1.1	versicolor
## 71	5.9	3.2	4.8	1.8	versicolor
## 72	6.1	2.8	4.0	1.3	versicolor
## 73	6.3	2.5	4.9	1.5	versicolor
## 74	6.1	2.8	4.7	1.2	versicolor
## 75	6.4	2.9	4.3	1.3	versicolor
## 76	6.6	3.0	4.4	1.4	versicolor
## 77	6.8	2.8	4.8	1.4	versicolor
## 78	6.7	3.0	5.0	1.7	versicolor
## 79	6.0	2.9	4.5	1.5	versicolor
## 80	5.7	2.6	3.5	1.0	versicolor
## 81	5.5	2.4	3.8	1.1	versicolor
## 82	5.5	2.4	3.7	1.0	versicolor
## 83	5.8	2.7	3.9	1.2	versicolor
## 84	6.0	2.7	5.1	1.6	versicolor
## 85	5.4	3.0	4.5	1.5	versicolor
## 86	6.0	3.4	4.5	1.6	versicolor
## 87	6.7	3.1	4.7	1.5	versicolor
## 88	6.3	2.3	4.4	1.3	versicolor

## 89	5.6	3.0	4.1	1.3	versicolor
## 90	5.5	2.5	4.0	1.3	versicolor
## 91	5.5	2.6	4.4	1.2	versicolor
## 92	6.1	3.0	4.6	1.4	versicolor
## 93	5.8	2.6	4.0	1.2	versicolor
## 94	5.0	2.3	3.3	1.0	versicolor
## 95	5.6	2.7	4.2	1.3	versicolor
## 96	5.7	3.0	4.2	1.2	versicolor
## 97	5.7	2.9	4.2	1.3	versicolor
## 98	6.2	2.9	4.3	1.3	versicolor
## 99	5.1	2.5	3.0	1.1	versicolor
## 100	5.7	2.8	4.1	1.3	versicolor
## 101	6.3	3.3	6.0	2.5	virginica
## 102	5.8	2.7	5.1	1.9	virginica
## 103	7.1	3.0	5.9	2.1	virginica
## 104	6.3	2.9	5.6	1.8	virginica
## 105	6.5	3.0	5.8	2.2	virginica
## 106	7.6	3.0	6.6	2.1	virginica
## 107	4.9	2.5	4.5	1.7	virginica
## 108	7.3	2.9	6.3	1.8	virginica
## 109	6.7	2.5	5.8	1.8	virginica
## 110	7.2	3.6	6.1	2.5	virginica
## 111	6.5	3.2	5.1	2.0	virginica
## 112	6.4	2.7	5.3	1.9	virginica
## 113	6.8	3.0	5.5	2.1	virginica
## 114	5.7	2.5	5.0	2.0	virginica
## 115	5.8	2.8	5.1	2.4	virginica
## 116	6.4	3.2	5.3	2.3	virginica
## 117	6.5	3.0	5.5	1.8	virginica
## 118	7.7	3.8	6.7	2.2	virginica
## 119	7.7	2.6	6.9	2.3	virginica
## 120	6.0	2.2	5.0	1.5	virginica
## 121	6.9	3.2	5.7	2.3	virginica
## 122	5.6	2.8	4.9	2.0	virginica
## 123	7.7	2.8	6.7	2.0	virginica
## 124	6.3	2.7	4.9	1.8	virginica
## 125	6.7	3.3	5.7	2.1	virginica
## 126	7.2	3.2	6.0	1.8	virginica
## 127	6.2	2.8	4.8	1.8	virginica
## 128	6.1	3.0	4.9	1.8	virginica
## 129	6.4	2.8	5.6	2.1	virginica
## 130	7.2	3.0	5.8	1.6	virginica
## 131	7.4	2.8	6.1	1.9	virginica
## 132	7.9	3.8	6.4	2.0	virginica
## 133	6.4	2.8	5.6	2.2	virginica
## 134	6.3	2.8	5.1	1.5	virginica
## 135	6.1	2.6	5.6	1.4	virginica
## 136	7.7	3.0	6.1	2.3	virginica
## 137	6.3	3.4	5.6	2.4	virginica
## 138	6.4	3.1	5.5	1.8	virginica
## 139	6.0	3.0	4.8	1.8	virginica
## 140	6.9	3.1	5.4	2.1	virginica
## 141	6.7	3.1	5.6	2.4	virginica
## 142	6.9	3.1	5.1	2.3	virginica
## 143	5.8	2.7	5.1	1.9	virginica
## 144	6.8	3.2	5.9	2.3	virginica
## 145	6.7	3.3	5.7	2.5	virginica

```
## 146      6.7      3.0      5.2      2.3 virginica
## 147      6.3      2.5      5.0      1.9 virginica
## 148      6.5      3.0      5.2      2.0 virginica
## 149      6.2      3.4      5.4      2.3 virginica
## 150      5.9      3.0      5.1      1.8 virginica
```

```
str(df)
```

```
## 'data.frame':    150 obs. of  5 variables:
## $ Sepal.Length: num  5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...
## $ Sepal.Width : num  3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...
## $ Petal.Length: num  1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...
## $ Petal.Width : num  0.2 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...
## $ Species      : Factor w/ 3 levels "setosa","versicolor",...: 1 1 1 1 1 1 1 1 1 1
1 ...
```

```
df$Species <- factor(df$Species, levels = c("setosa", "versicolor", "virginica"),
  labels = c("Setosa", "Versicolor", "Virginica"))
```

```
# slucajan odabir skupa za učenje i skupa za testiranje
```

```
set.seed(1234)
```

```
train <- sample(nrow(df), 0.7*nrow(df))
```

```
# skup za učenje
```

```
df.train <- df[train,]
```

```
# skup za testiranje
```

```
df.validate <- df[-train,]
```

```
# tablica frekvencija - originalan skup podataka
```

```
table(df$Species)
```

```
##
##      Setosa Versicolor  Virginica
##      50          50          50
```

```
# tablica frekvenvija - skup za učenje
```

```
table(df.train$Species)
```

```
##
##      Setosa Versicolor  Virginica
##      39          29          37
```

```
# tablica frekvencija - skup za testiranje
```

```
table(df.validate$Species)
```

```
##
##      Setosa Versicolor  Virginica
##      11          21          13
```

```
# LOGISTICKA REGRESIJA
# varijabla Species je zavisna varijabla, a varijable Sepal.Length, Sepal.Width, P
etal.Length, Petal.Width su prediktori
fit.logit <- glm(Species~., data = df.train, family=binomial())
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
# analiza modela
summary(fit.logit)
```

```
##
## Call:
## glm(formula = Species ~ ., family = binomial(), data = df.train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.124e-05 -2.110e-08  2.110e-08  2.110e-08  2.105e-05
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    -10.934  351258.549      0      1
## Sepal.Length     -3.339   92833.858      0      1
## Sepal.Width     -11.549   64471.626      0      1
## Petal.Length     22.570   80185.641      0      1
## Petal.Width       3.230  163837.188      0      1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 1.3854e+02  on 104  degrees of freedom
## Residual deviance: 1.8975e-09  on 100  degrees of freedom
## AIC: 10
##
## Number of Fisher Scoring iterations: 25
```

```
# testiranje modela sa novim podacima
prob <- predict(fit.logit, df.validate, type = "response")

logit.pred <- factor(prob >.5, levels = c(FALSE, TRUE), labels = c("LAZ", "ISTINA")
))

# predikcija modela i stvarni rezultat
logit.perf <- table(df.validate$Species, logit.pred, dnn = c("Stvarni rezultat",
"Predikcija"))
# tablicni prikaz rezultata
logit.perf
```

```
##              Predikcija
## Stvarni rezultat LAZ ISTINA
##      Setosa      11      0
```

```
##      Versicolor    0      21
##      Virginica     0      13
```

```
# Stepwise logisticka regresija - uklanjanje prediktora koji nisu statisticki znacajni
fit.reducedlogit <- step(fit.logit)
```

```
## Start:  AIC=10
## Species ~ Sepal.Length + Sepal.Width + Petal.Length + Petal.Width
```

```
## Warning: glm.fit: algorithm did not converge

## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
##           Df    Deviance AIC
## - Petal.Width  1 1.9170e-09   8
## - Sepal.Length  1 1.9432e-09   8
## - Sepal.Width   1 2.5184e-09   8
## - Petal.Length  1 2.9548e-09   8
## <none>          1.8975e-09  10
```

```
## Warning: glm.fit: algorithm did not converge

## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
##
## Step:  AIC=8
## Species ~ Sepal.Length + Sepal.Width + Petal.Length
```

```
## Warning: glm.fit: algorithm did not converge

## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
##           Df   Deviance AIC
## - Sepal.Length 1 1.9435e-09  6
## - Sepal.Width  1 2.6657e-09  6
## - Petal.Length 1 1.0303e-08  6
## <none>          1.9170e-09  8
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
##
## Step:  AIC=6
## Species ~ Sepal.Width + Petal.Length
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
##           Df Deviance    AIC
## - Sepal.Width  1     0.000  4.000
## <none>          0.000  6.000
## - Petal.Length 1    95.637 99.637
```

```
## Warning: glm.fit: algorithm did not converge
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
##
## Step:  AIC=4
## Species ~ Petal.Length
##
##           Df Deviance    AIC
## <none>          0.00    4.00
## - Petal.Length 1   138.54 140.54
```

```
summary(fit.reducedlogit)
```

```
##
## Call:
## glm(formula = Species ~ Petal.Length, family = binomial(), data = df.train)
##
## Deviance Residuals:
```

```
##           Min           1Q           Median           3Q           Max
## -3.680e-05 -2.100e-08  2.100e-08  2.100e-08  4.269e-05
##
## Coefficients:
##           Estimate Std. Error z value Pr(>|z|)
## (Intercept)    -78.02   60970.43  -0.001    0.999
## Petal.Length    29.95   21853.16   0.001    0.999
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 1.3854e+02  on 104  degrees of freedom
## Residual deviance: 3.1968e-09  on 103  degrees of freedom
## AIC: 4
##
## Number of Fisher Scoring iterations: 25
```

```
prob.reducetlogit <- predict(fit.reducedlogit, df.validate, type = "response")
pred.reducetlogit <- factor(prob.reducetlogit >.5, levels = c(FALSE, TRUE), labels
= c("LAZ", "ISTINA"))
perf.reducedlogit <- table(df.validate$Species, pred.reducetlogit, dnn = c("Stvarni
i rezultat", "Predikcija"))
perf.reducedlogit
```

```
##           Predikcija
## Stvarni rezultat LAZ ISTINA
##      Setosa      11      0
##      Versicolor  0      21
##      Virginica   0      13
```