## Blockchain 2

**PoW and Forks** 

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#### **Problem**

```
type Block struct { b_1 b_2 b_3 prev pointer data bytes prevhash hash } b_1 b_2 b_3 prev data: d_1 d_1 d_2 d_3 d_4 d_4
```

- $id_b = H(b.prevhash||b.data)$
- Blockchain identified by  $id_{b_3}$
- Changing  $d_1$  changes  $id_{b_3}$
- Removing  $b_2$  changes  $id_{b_3}$
- Adding  $b'_2$  changes  $id_{b_3}$

#### secured against changes

#### **Problems:**

- Can recreate complete chain
- Who adds blocks?

A proof of work allows to convince others that you did spend a certain amount of time/resources.

$$\pi \leftarrow f_{PoW}(\mathsf{data}, d)$$

bool 
$$\leftarrow verify(\mathsf{data}, \pi, d)$$

- d configurable difficulty
- $f_{PoW}$  is long running
- *verify* is fast

#### Use case:

Rate limit web API

#### **Verify:**

- compute  $hash = H(data||\pi)$
- check if first d bits of hash are 0

```
VERIFY(	ext{data}, \pi, d:) hash = H(	ext{data}||\pi) if first d bits of hash are 0 then return true return false
```

#### PoW:

repeatedly try different nonces (data)

#### Some math

**Lemma:** For two different nonces, the probability to find a solution is independent.

**Theorem:** If p is the probability to find a nonce, then the expected number of trials is  $\frac{1}{p}$ .

#### **Example:**

- d = 4
- Probability to find a proof on one trial is  $p = 2^{-4} = 1/16$
- Expected number of trials until success is 1/p = 16
- Probability to not find a proof in 32 trials  $(1-p)^{32}=0.127$

• 
$$d = 5$$
  $p = 2^{-5} = 1/32$   $1/p = 32$ 

#### **Verify:**

- compute  $hash = H(data||\pi)$
- check if first d bits of hash are 0

```
\begin{aligned} \text{VERIFY}(\textbf{data}, \pi, d:) \\ hash &= H(\textbf{data}||\pi) \\ \textbf{if first } d \text{ bits of } hash \text{ are } 0 \textbf{ then} \\ \textbf{return true} \\ \textbf{return false} \end{aligned}
```

- Changing difficulty gives double/half the expected trials
- Amount of work needed is very variable.

#### **Better version**

• Difficulty D is hexadecimal number

#### **Verify:**

- compute  $hash = H(data||\pi)$
- check if hash is smaller than D

```
egin{aligned} 	ext{VERIFY}(	ext{data},\pi,D:) \ hash &= H(	ext{data}||\pi) \ 	ext{if } hash &\leq D 	ext{ then} \ 	ext{return true} \ 	ext{return false} \end{aligned}
```

#### PoW:

repeatedly try different nonces

## Proof of work Difficulty adjustion example

#### **Example:**

- A computer computes a PoW every 15 seconds.
- How can we adapt difficulty to get 20 seconds?

#### In the blockchain

```
type Block struct { prev pointer data bytes prevhash hash nonce uint } b_1 b_2 b_3 b_4 b_5 b_6 b_7 b_8 b_8 b_8 b_9 b_9
```

- $id_b = H(b.prevhash||b.data||b.nonce)$
- to recreate chain, need to recompute all proof of work

Who computes PoW?

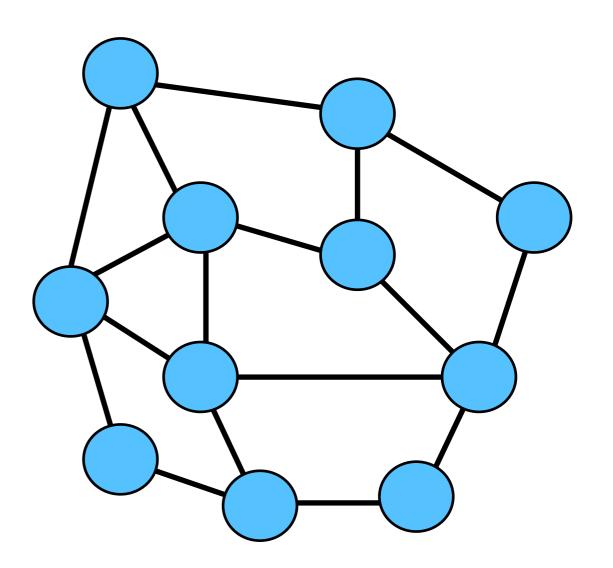
# PoW in peer to peer network

#### **Problem**

- Store blockchain on many nodes
- Unknown nodes, anyone can join
- Decide what is the next block

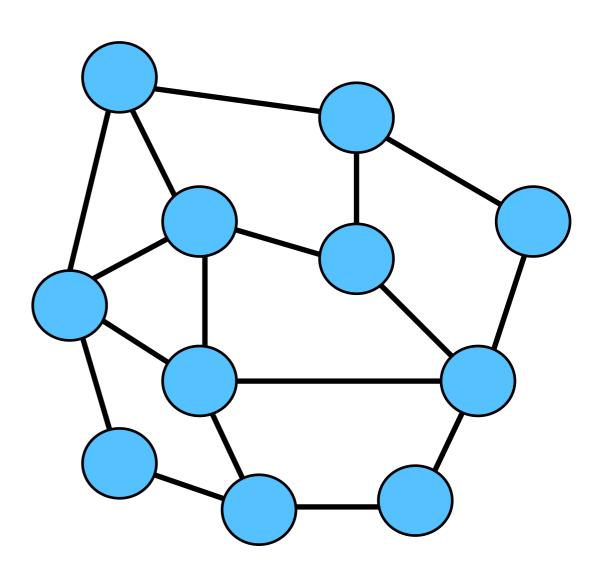
#### **Problems:**

- No list of all ids exists
- New ids/nodes can be added easily



#### A Peer to Peer network

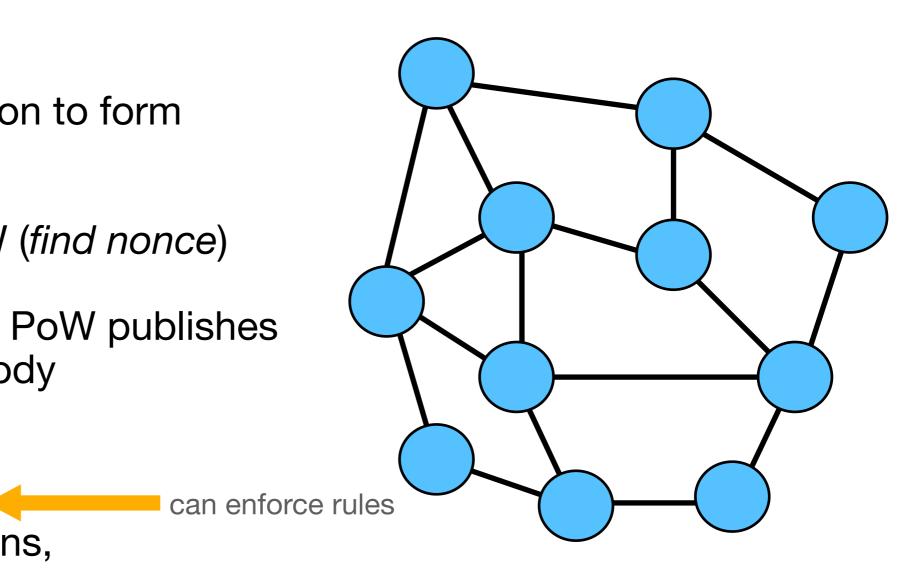
- several independent nodes
- nodes are well connected
- every node stores the blockchain
- transactions is broadcast to all nodes



#### **Proof of work workflow**

#### Every node does:

- collect transaction to form block data
- try to solve PoW (find nonce)
- the first to solve PoW publishes block to everybody
- all check PoW, validate Block, apply transactions, continue



#### **Properties**

#### Censorhip resistance

One node cannot prevent a transaction to be put in a block.

#### **Fault tolerance**

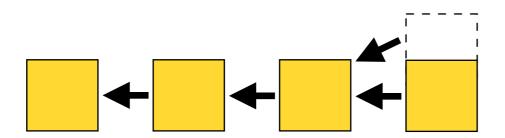
Individual nodes may fail.

#### Rate control

- Difficulty of PoW determines how fast blocks are created.
- Maximum on data size gives rate limit on transactions.

#### **Proof of work workflow**

Moving to a new block, a node has the same chances to find a PoW.



## Difficulty adjustment

Number of nodes in the system may change, need to adjust difficulty.

Idea: Include a timestamp in every block.

Need to validate timestamp on new block!

At regular intervals, check average block delay, adjust difficulty.

#### Rewards

Each transaction pays fees

For every new block a block reward is payd out/created

- A block includes pk of the node that receives the reward. Coinbase transaction
- Each nodes has a differnt block and needs a different nonce.

#### **Interesting:**

- Block rewards make the system run, even without transactions.
- Fees ensure nodes do actually include transactions.

#### **Fees**

Each transaction pays fees

Each block may contain at most 1MB of transactions.

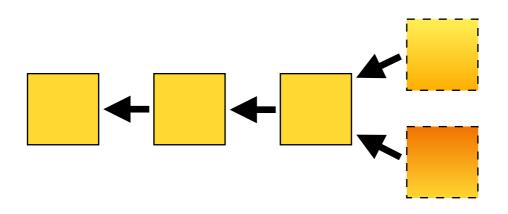
Include transactions which pay most fee per byte.

#### **Interesting:**

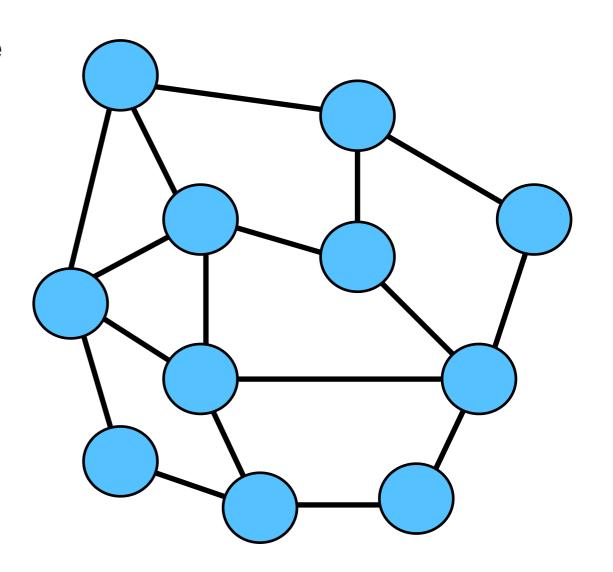
- Transaction with large fee included before transaction with small fee.
- Fee independent from transaction value.

# Forks and longest chain rule

A fork is if multiple blocks have the same predecessor



• Why: Two blocks found "concurrently"



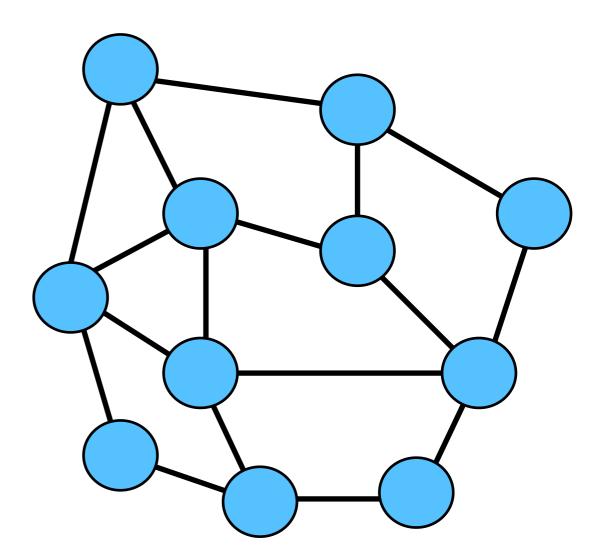
#### **Proof of work workflow**

#### Every node does:

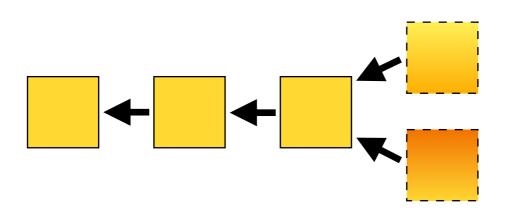
- collect transaction to form block data
- try to solve PoW (find nonce)
- the first to solve PoW publishes block to everybody

another block found before end of propagation

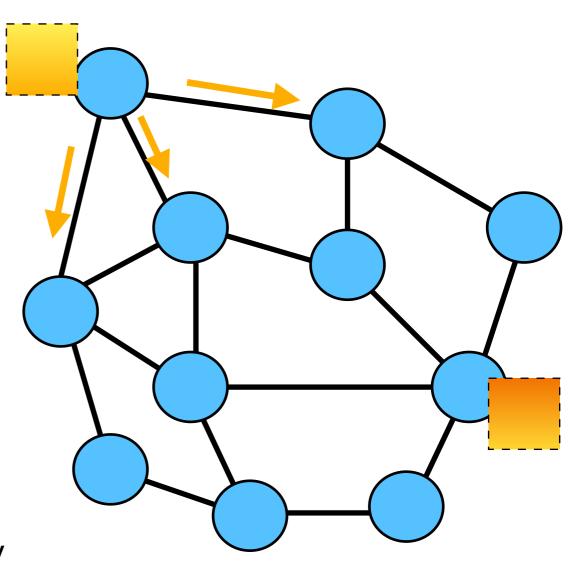
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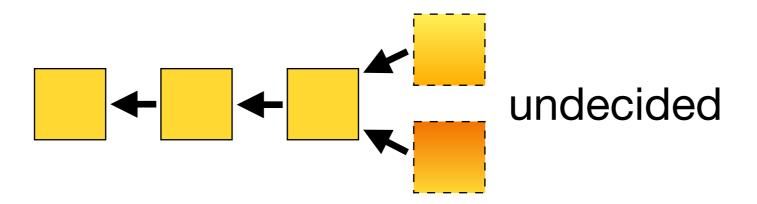


- Why: Two blocks found "concurrently"
- Bitcoin 2013: avg. 12.6sec block delivery [Decker, Wattenhofer]



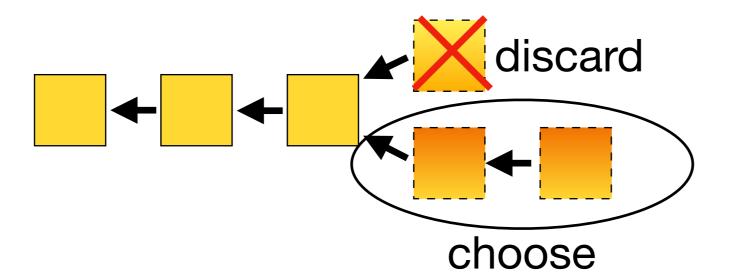
#### Longest chain rule

• If a fork exists, all nodes should adopt the longest chain.



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#### **Problems:**

- Blocks & Transactions in smaller chain are discarded
  - Miners loose reward
  - Some transactions may be only in one fork
  - Two conflicting transactions may be included in different forks (double spend)

#### Math: How likely is a fork

 $p_{sec}$  probability a block is found in one second

 $\delta$  average time to get a block from the network

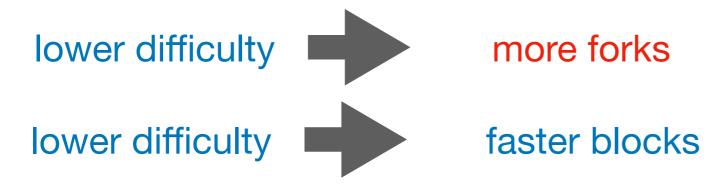
#### **Theorem:**

$$P[fork] = 1 - (1 - p_{sec})^{\delta}$$

#### Reparametrization

Fork probability depends on

- Network delay time to propagate a block
- PoW difficulty

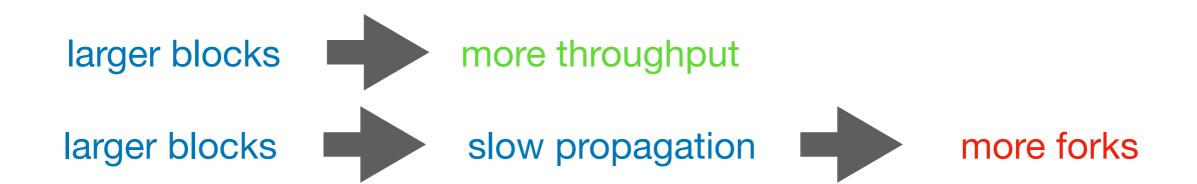




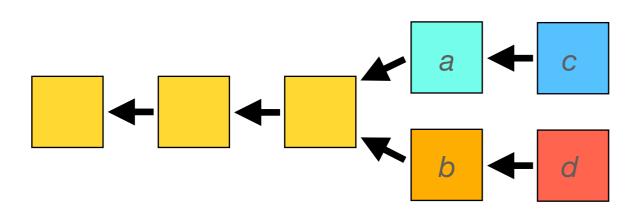
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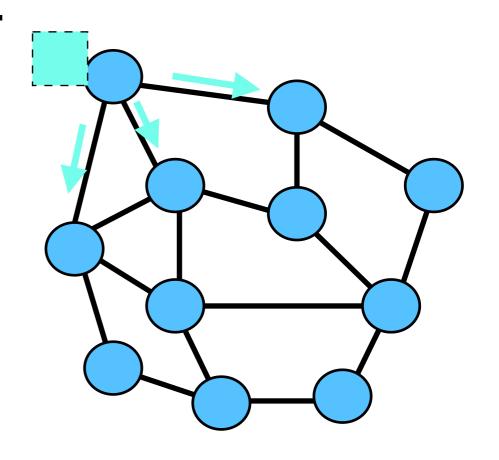
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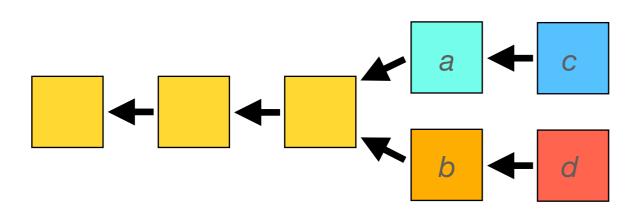


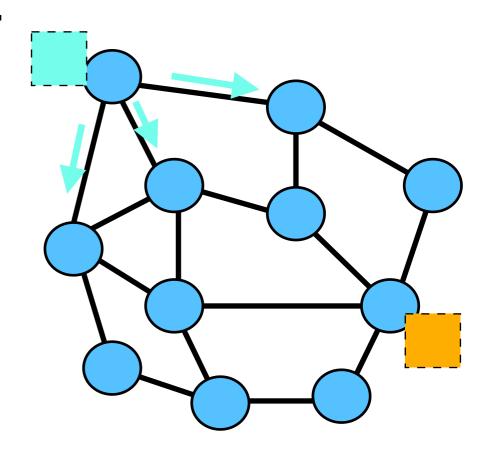
- Multiple forks may arrise after each other.
- E.g. b found while a was propagated,
  - d found while c was propagated.



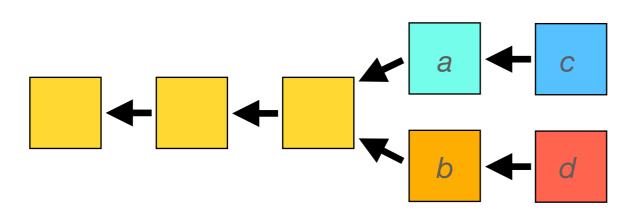


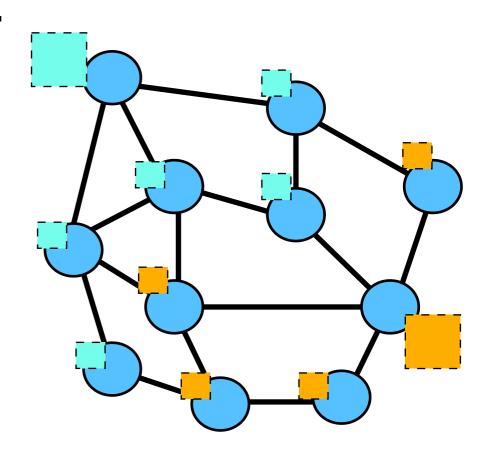
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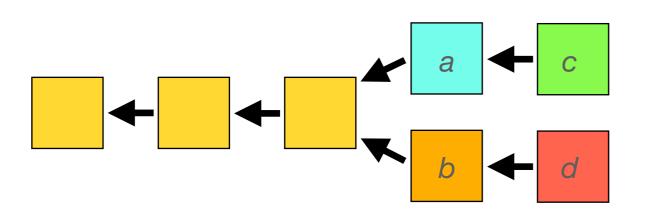


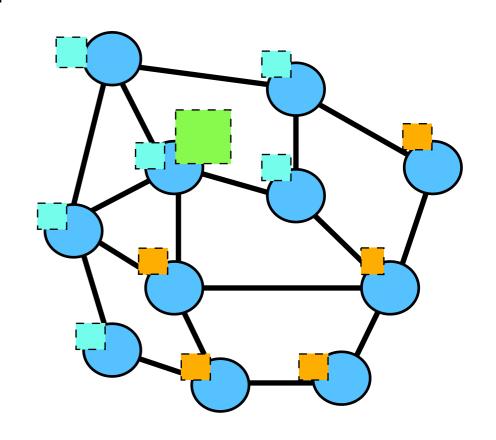
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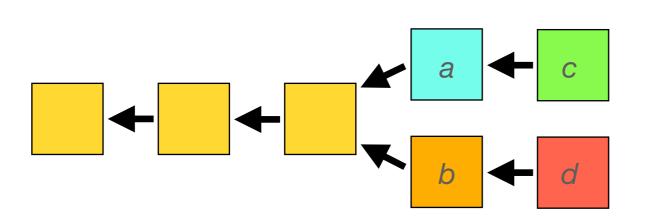
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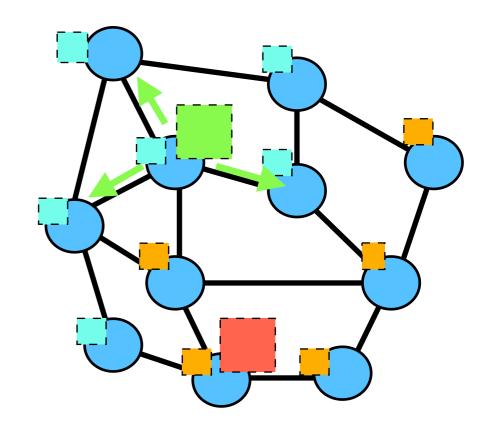


#### Multiple forks

- Multiple forks may arrise after each other.
- E.g. b found while a was propagated,
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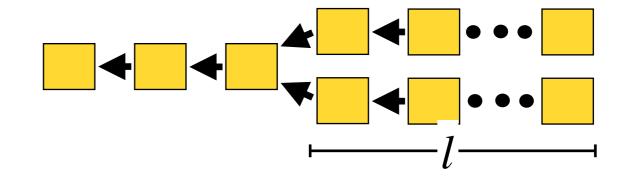
 Probability for second for smaller than the first.



## **Forks**Multiple forks

- Multiple forks may arrise after each other.
- Probability for second for smaller than the first.
- ullet Probability for l forks decreases exponentially

•  $P[l \times \text{fork}] \leq P[\text{fork}]^l$ 



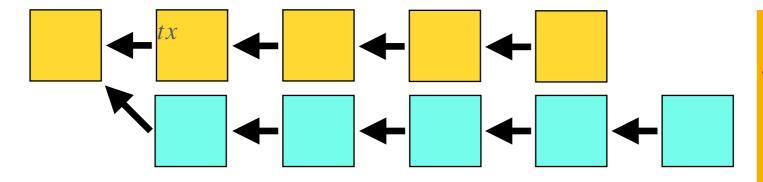
Wait for l blocks to consider a transaction confirmed.

### Attacks

### Attacks 51% attack

- Assume the attacker has  $\alpha > 50\,\%$  of the hashing power.
  - Attacker can grow a private chain faster than the public chain.

A private chain is a fork with blocks not propagated through the network.



#### Attacker can:

- Double spend
- Get all the reward

### **Attacks**

### **Stubborn mining:**

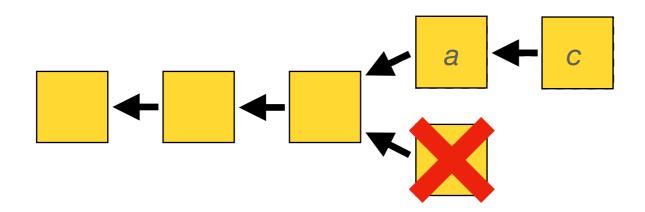
Attacker does not follow longest chain rule.

### Selfish mining:

• Attacker keeps blocks secret.

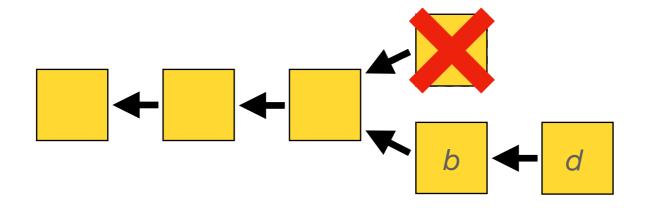
### Case 1, successfull attack:

- 1. attacker finds block a, keeps it secret
- 2. attacker finds block c, keeps it secret
- 3. other nodes find block b and propagate it
- 4. attacker propagates blocks a and c



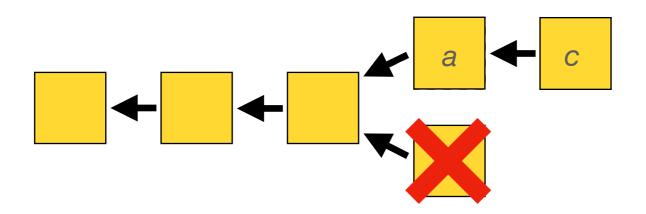
### Case 2, unsuccessfull attack:

- 1. attacker finds block a, keeps it secret
- 2. other nodes find block b and propagate it
- 3. attacker propagates block a
- 4. other nodes find block d extending b



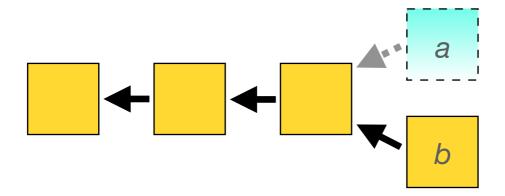
Case 3, kind of successfull attack:

- 1. attacker finds block a, keeps it secret
- 2. other nodes find block b and propagate it
- 3. attacker propagates block a
- 4. some node finds block c extending a



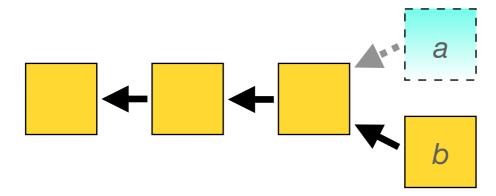
### To get Case 3 instead of Case 2 attacker needs to

- detect new blocks fast
- propagate its block faster



# **Attacks**Selfish mining - take away

- Attacker does not get more blocks, but others get less.
- Good control of network makes attack work better.



#### Algorithm 6 Selfish mining

```
Idea: Mine secretly, without immediately publishing newly found blocks Let l_p be length of the public chain

Let l_s be length of the secret chain

if a new block b_p is published, i.e. l_p has increased by 1 then

if l_p > l_s then

Start mining on b_p

else if l_p = l_s then

Publish secretly mined block b_s

Mine on b_s and immediately publish new block

else if l_p = l_s - 1 then

Push all secretly mined blocks
```

 $\alpha$  the attackers hashing power, and  $\gamma$  be the attackers network power.

Selfish mining is profitable, if

$$\alpha > 0.33$$

$$\alpha > 0.25$$
 and  $\gamma > 0.5$ 

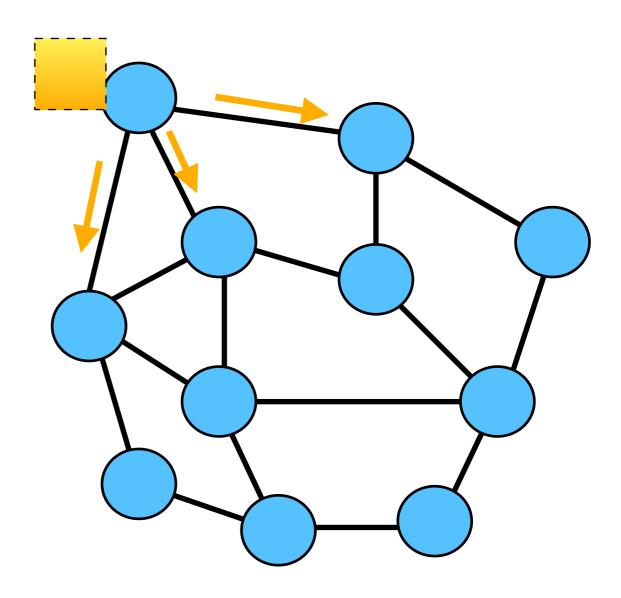
$$\alpha > 0$$
 and  $\gamma = 1$ 

# **Attacks**Delivery denial

#### **Broadcast block:**

- Broadcast inventory message including block hash
- Receiving new inventory, request block
- Send block

Block is only send from one neighbor



# **Attacks**Delivery denial

#### **Broadcast block:**

- Broadcast inventory
- Request block
- Send block

#### **Attack**

- Broadcast inventory
- Do not send out blocks
   Victims wait for timeout.

### **Bitcoin**Downsides

Throughput at most 7tx per second

Confirmation latency approx 1h

Enormous energy consumption

