

# **Blockchain technology and applications**

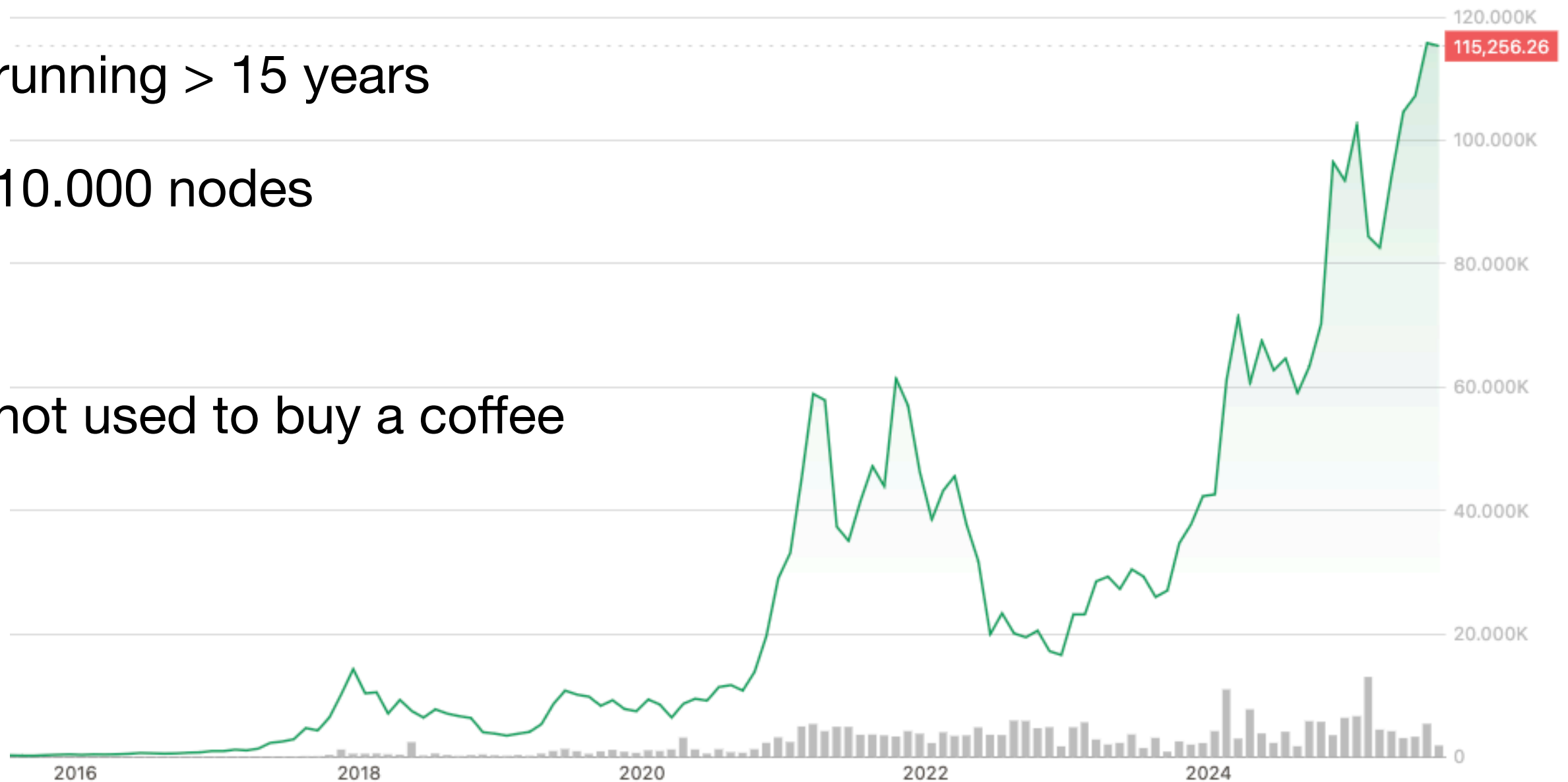
**Intro**

# Blockchain

## Motivation

### Bitcoin

- running > 15 years
- 10.000 nodes
- not used to buy a coffee



<https://www.coindesk.com/price/bitcoin>

# Blockchain and applications

Take a look at blockchain technology and applications

- What works
- What does not work

Learning goal: Know how and when to use it.

Know when not to use it.

But: No investment tips

# Blockchain and applications

Where can many people, jointly store an important document?

- e.g. Will
- e.g. Ownership list
- Can changes be made?

# **Blockchain 1**

## **Hashlist and Merkle trees**

# Blockchain datastructure

# What is a blockchain

A blockchain is an append only log  
secured against changed.

Typically a blockchain

- is stored on different nodes

Idea: Log all interactions

- Log enables anyone to reproduce/recreate state.

# Cryptographic hash function

Idea

$$H(x) = y$$



# Cryptographic hash function

## Idea

$$H(x) = y$$

- $x$  string or byte array
- $y$  fixed size byte array

**looks random:** hashing something new gives a random value

**is deterministic:** hashing something twice gives the same value

# Cryptographic hash function

## Properties

```
<script src="https://code.jquery.com/jquery-3.3.1.slim.min.js"
integrity="sha384-q8i/X+965DzO0rT7abK41JStQIAqVgRVzpbzo5smXKp4YfRvH+8abtTE1Pi6jizo">
</script>
```

### Properties:

- **Pre-image resistance:**  
given  $y$  cannot find  $x$  s.t.  $H(x) = y$
- **Weak collision resistance:**  
given  $x$  cannot find  $x'$  s.t.  $H(x) = H(x')$
- **Strong collision resistance:**  
cannot find  $x$  and  $x'$  s.t.  $H(x) = H(x')$

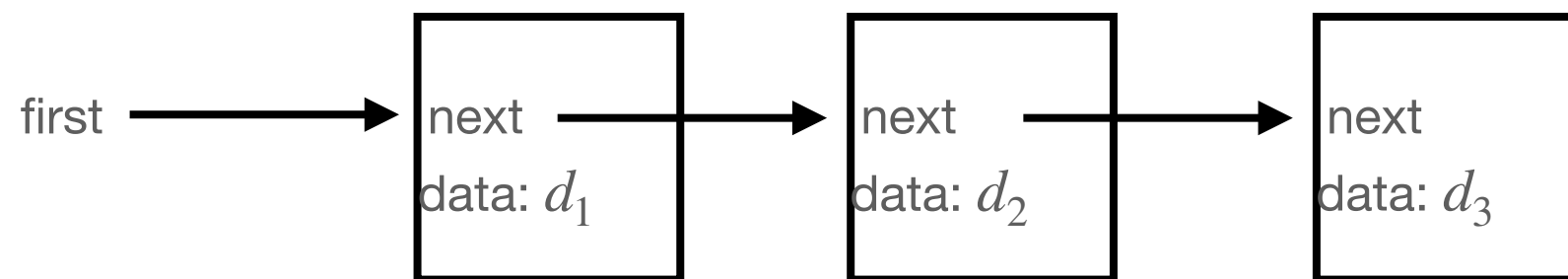
Use cases examples:

- Password hashes
- HTML5 integrity attribute

# Hash chain

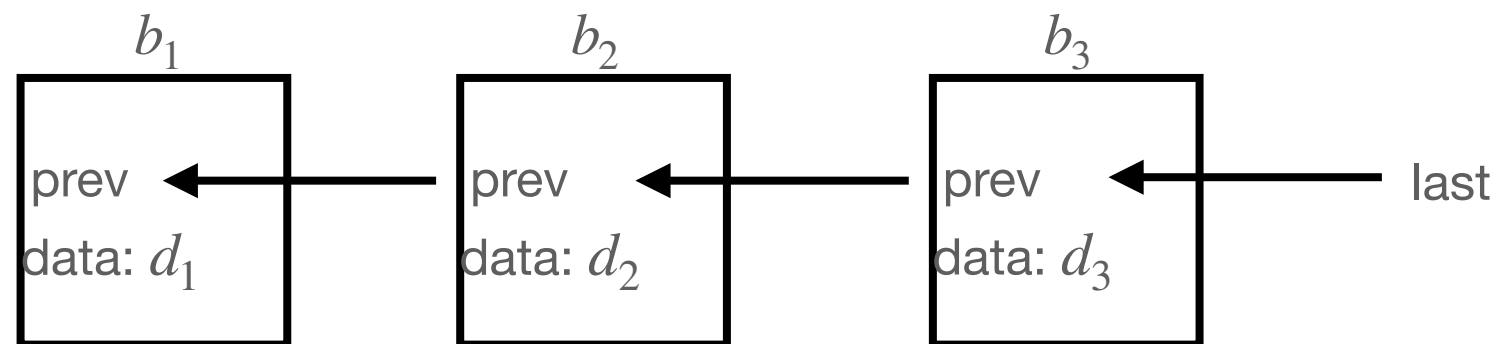
# Hash chain

## Linked list



```
type Node struct {  
    next pointer  
    data bytes  
}
```

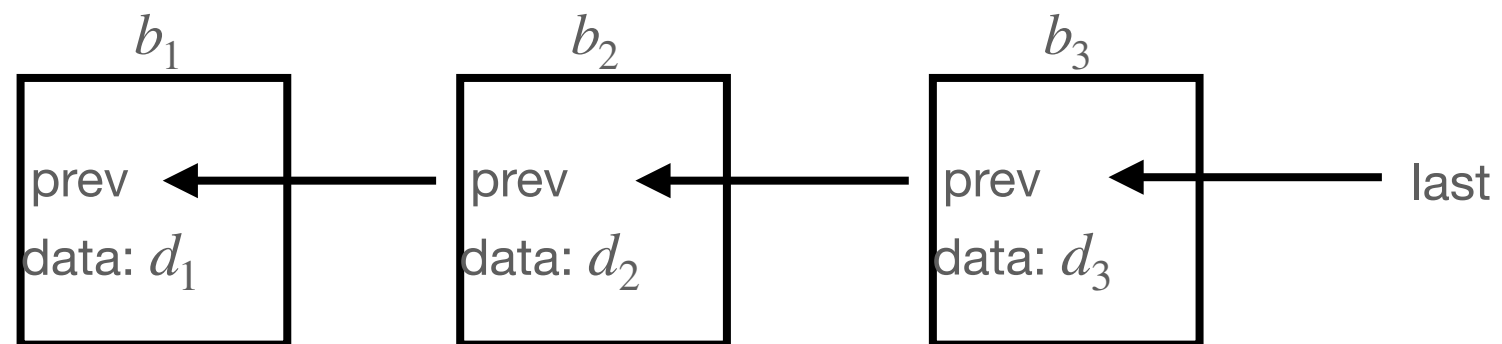
# Hash chain



```
type Block struct {  
    prev pointer  
    data bytes  
    prevhash hash  
}
```

- Can hash a block by concatenating fields.
- Blockhash gives id:  
 $id_b = H(b.\text{prevhash} || b.\text{data})$
- $b_2.\text{prevhash} = id_{b_1}$

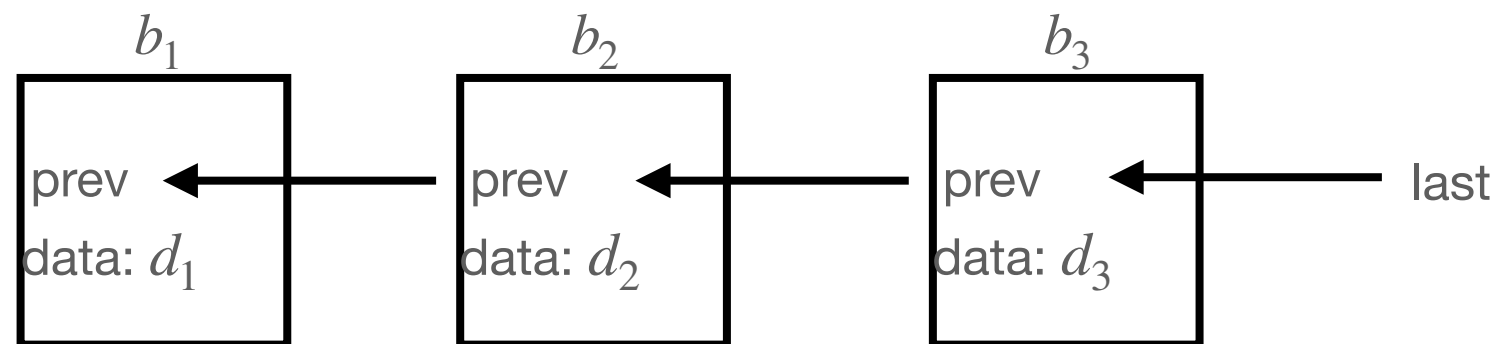
# Hash chain



- $id_b = H(b.\text{prevhash} || b.\text{data})$
- Blockchain identified by  $id_{b_3}$
- Changing  $d_1$  changes  $id_{b_3}$
- Removing  $b_2$  changes  $id_{b_3}$
- Adding  $b'_2$  changes  $id_{b_3}$

secured against changes

# Hash chain



```
type Block struct {  
    prev pointer  
    data bytes  
    datahash hash  
    prevhash hash  
    timestamp  
}
```

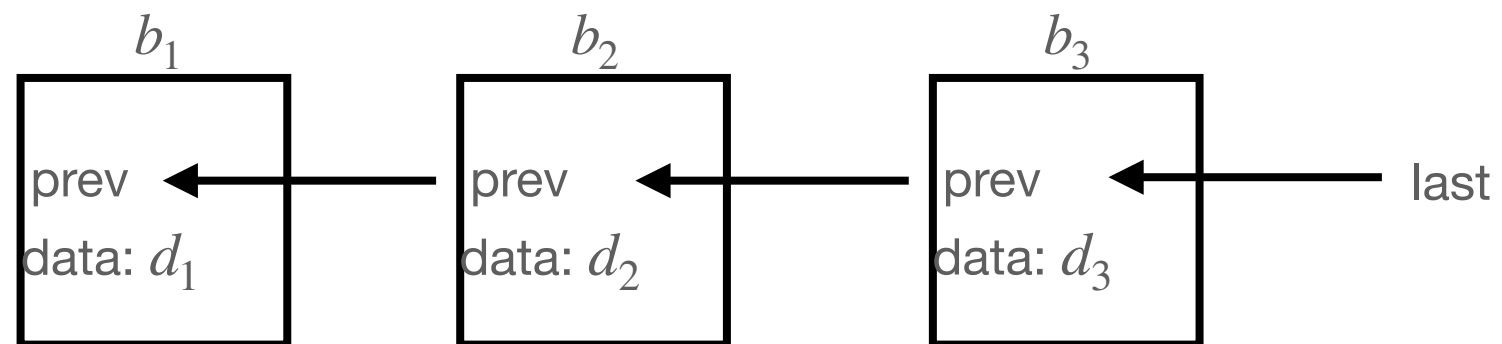
Reduce size:

- $id_b = H(b.\text{prevhash} || b.\text{datahash})$
- $b.\text{datahash} = H(b.\text{data})$

- easy to store
- can proof that data is included

# Hash chain

## Example: Linked timestamping



Trusted source collects data and publishes a new block, e.g. on newspaper.





# Hash chain

## Digital Signatures and trusted publishers

$$pk, sk \leftarrow \text{setup}(\kappa)$$

$$\sigma \leftarrow \text{sign}(sk, msg)$$

$$bool \leftarrow \text{verify}(\sigma, msg, pk)$$

Ideas:

- Require a trusted party to sign every new block
- Require  $m$  out of  $n$  trusted parties to sign a block

Permissioned blockchains!

# Merkle trees

# Merkle trees

## Problem

```
type Block struct {  
    prev pointer  
    data bytes  
    datahash hash  
    prevhash hash  
    timestamp  
}
```

Idea:

- put multiple data items into one block

- Is my item in the block?

# Merkle trees

## Ideas

Data items:  $D_1, D_2, D_3, D_4, \dots$

- $\text{datahash} = h$

Data as a hash

- $h = H(D_1 || D_2 || D_3 || \dots)$

Data as a list of hashes

- $h = H(H(D_1) || H(D_2) || H(D_3) || \dots)$

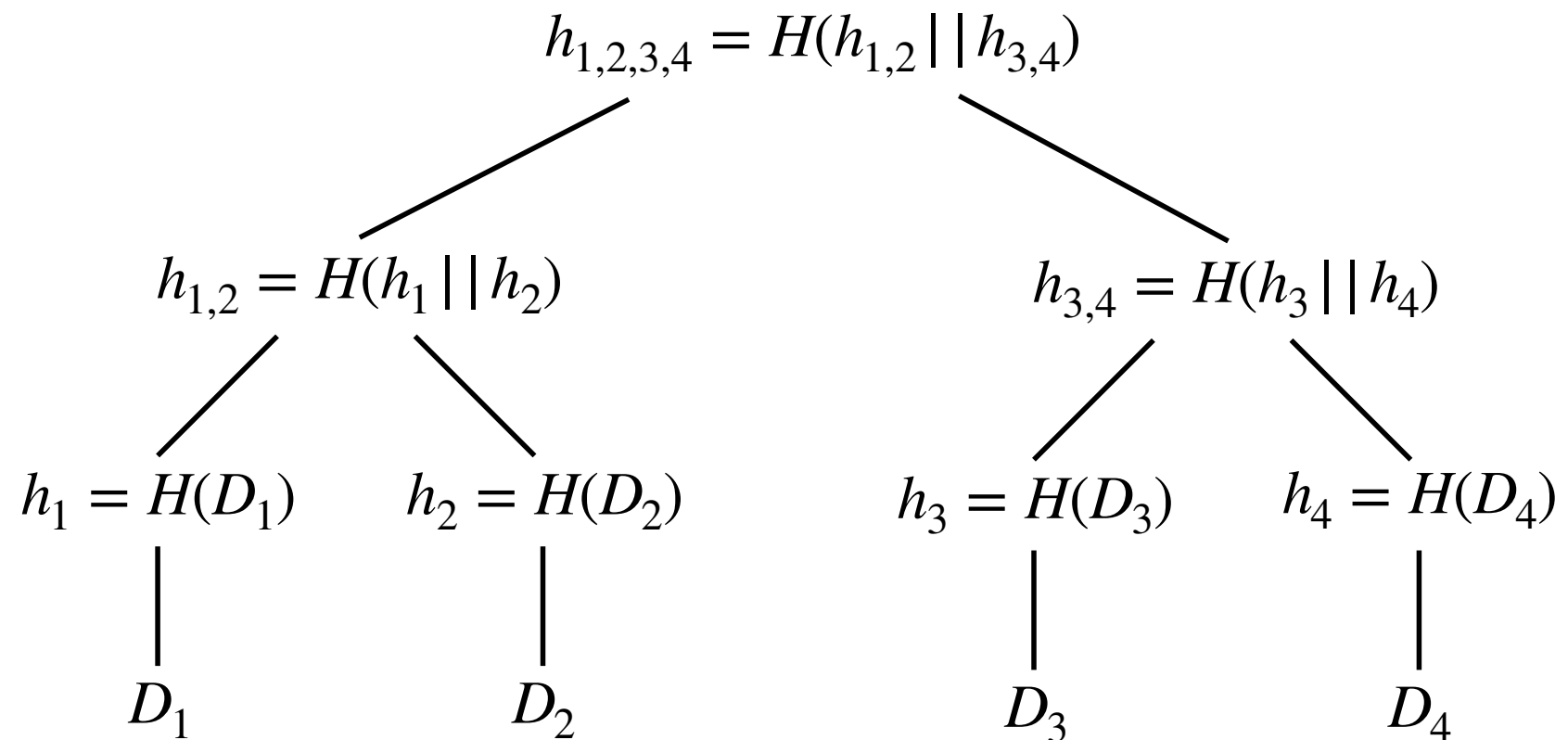
```
type Block struct {  
    prev pointer  
    data bytes  
    datahash hash  
    prevhash hash  
    timestamp  
}
```

# Merkle trees

## Design

Data items:  $D_1, D_2, D_3, D_4, \dots$

- datahash =  $h$

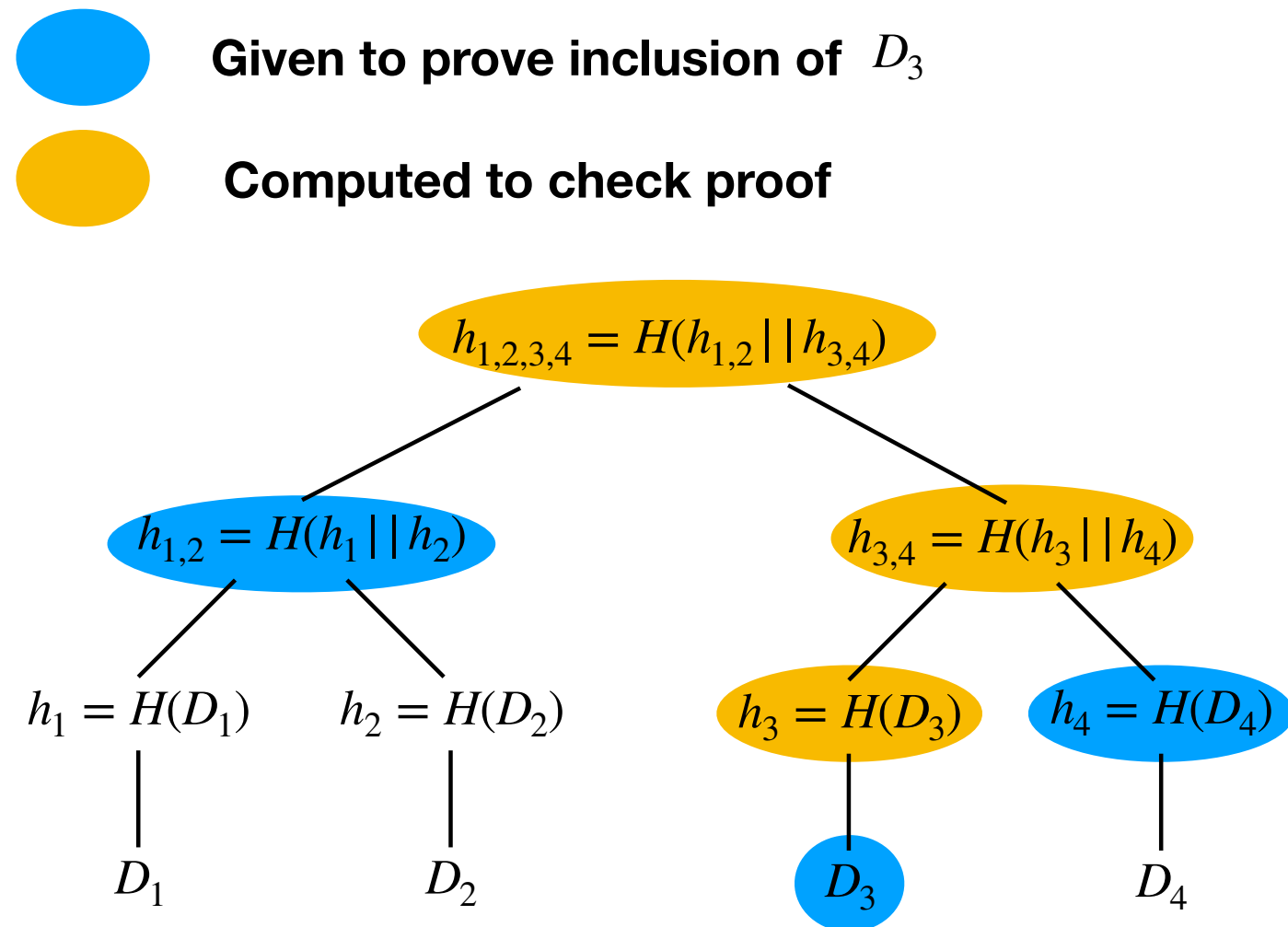


# Merkle trees

## Proofs

Data items:  $D_1, D_2, D_3, D_4, \dots$

- datahash =  $h$



# Merkle trees

## Proofs

Data items:  $D_1, D_2, D_3, D_4, \dots$

- datahash =  $h$

What if we have only 5 data items?

- Duplicate  $D_5$
- Add default element