

Cr terio de Sassenfeld: $S_1 = \frac{1}{|a_{11}|} (|a_{12}| + |a_{13}| + |a_{14}| + \dots + |a_{1n}|),$
 $S_2 = \frac{1}{|a_{22}|} (|a_{21}|S_1 + |a_{23}| + |a_{24}| + \dots + |a_{2n}|), \quad S_3 = \frac{1}{|a_{33}|} (|a_{31}|S_1 + |a_{32}|S_2 + |a_{34}| + \dots + |a_{3n}|), \dots$
 $\dots \quad S_n = \frac{1}{|a_{nn}|} (|a_{n1}|S_1 + |a_{n2}|S_2 + \dots + |a_{nn-1}|S_{n-1})$

M todo de Newton para sistemas: $x_{i+1} = x_i - \left[\frac{f_y g_y - g_y f_y}{|J|} \right]_i, \quad y_{i+1} = y_i - \left[\frac{g f_x - f g_x}{|J|} \right]_i$
 $|J| = (f_x g_y - f_y g_x)_i$

Interpola  o polinomial (Lagrange): $p_n(x) = y_0 L_0(x) + y_1 L_1(x) + \dots + y_n L_n(x)$
 $L_k(x) = \frac{(x - x_0)(x - x_1) \dots (x - x_{k-1})(x - x_{k+1}) \dots (x - x_n)}{(x_k - x_0)(x_k - x_1) \dots (x_k - x_{k-1})(x_k - x_{k+1}) \dots (x_k - x_n)}$

Interpola  o polinomial (Newton - diferen as divididas):
 $p_n(x) = d_0 + d_1(x - x_0) + d_2(x - x_0)(x - x_1) + \dots + d_n(x - x_0)(x - x_1) \dots (x - x_{n-1})$ onde
 $d_k = f[x_k, x_{k-1}, \dots, x_0]$
 $f[x_i] = f(x_i), \quad f[x_{i+1}, x_i] = \frac{f(x_{i+1}) - f(x_i)}{x_{i+1} - x_i}, \quad f[x_{i+2}, x_{i+1}, x_i] = \frac{f[x_{i+2}, x_{i+1}] - f[x_{i+1}, x_i]}{x_{i+2} - x_i}$

Interpola  o polinomial (Newton - diferen as simples):
 $p_n(x) = y_0 + \frac{x - x_0}{h} \Delta y_0 + \frac{(x - x_0)(x - x_1)}{2! h^2} \Delta^2 y_0 + \dots + \frac{(x - x_0)(x - x_1) \dots (x - x_{n-1})}{n! h^n} \Delta^n y_0$
 $\Delta y_i = y_{i+1} - y_i, \quad \Delta^2 y_i = \Delta y_{i+1} - \Delta y_i = y_{i+2} - 2y_{i+1} + y_i, \quad \Delta^k y_i = \Delta^{k-1} y_{i+1} - \Delta^{k-1} y_i$

Estimativas de erro para o polin mio interpolador:

$$|E_n(x)| \leq |(x - x_0)(x - x_1)(x - x_2) \dots (x - x_n)| \max_{x \in I} \frac{|f^{(n+1)}(x)|}{(n+1)!},$$

$$|E_n(x)| \approx |(x - x_0)(x - x_1) \dots (x - x_n)| |f[x_{n+1}, x_n, \dots, x_0]|,$$

$$|E_n(x)| \approx |(x - x_0)(x - x_1) \dots (x - x_n)| \left| \frac{\Delta^{n+1} y_0}{(n+1)! h^{n+1}} \right|$$

Spline C bica

$$S_i(x) = f(x_i) + (x - x_i)(c_i + (x - x_i)(b_i - (x - x_i)a_i))$$

$$z_{i-1} + 4z_i + z_{i+1} = \frac{6}{h^2}(y_{i+1} - 2y_i + y_{i-1}), \text{ para } i = 1, 2, \dots, n-1 \text{ e } z_0 = z_n = 0$$

$$a_i = \frac{1}{6h}(z_{i+1} - z_i)$$

$$b_i = \frac{z_i}{2}$$

$$c_i = -\frac{h}{6}z_{i+1} - \frac{h}{3}z_i + \frac{y_{i+1} - y_i}{h}$$

M nimos quadrados: $g(x) = \sum_{k=0}^m a_k g_k(x)$

Ajustamento a um polin mio de grau p :

$$\begin{bmatrix} n+1 & \sum_{i=0}^n x_i & \dots & \sum_{i=0}^n x_i^p \\ \sum_{i=0}^n x_i & \sum_{i=0}^n x_i^2 & \dots & \sum_{i=0}^n x_i^{p+1} \\ \vdots & \vdots & & \vdots \\ \vdots & \vdots & & \vdots \\ \sum_{i=0}^n x_i^p & \sum_{i=0}^n x_i^{p+1} & \dots & \sum_{i=0}^n x_i^{2p} \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ \vdots \\ a_p \end{bmatrix} = \begin{bmatrix} \sum_{i=0}^n y_i \\ \sum_{i=0}^n x_i y_i \\ \vdots \\ \vdots \\ \sum_{i=0}^n x_i^p y_i \end{bmatrix}$$