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Basics of Neural Network Programming

Vectorizing Logistic Regression

在正向传播中使用向量化

Vectorizing Logistic Regression

$$\begin{aligned} \Rightarrow \underline{z^{(1)}} &= \underline{w^T x^{(1)}} + b \\ \Rightarrow \underline{a^{(1)}} &= \sigma(z^{(1)}) \end{aligned}$$

$$\begin{aligned} \underline{z^{(2)}} &= \underline{w^T x^{(2)}} + b \\ \underline{a^{(2)}} &= \sigma(z^{(2)}) \end{aligned}$$

$$\begin{aligned} \underline{z^{(3)}} &= \underline{w^T x^{(3)}} + b \\ \underline{a^{(3)}} &= \sigma(z^{(3)}) \end{aligned}$$

$$\underline{X} = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \\ | & | & & | \\ | & | & & | \end{bmatrix}$$

\uparrow

$$\frac{(n_x, m)}{\mathbb{R}^{n_x \times m}}$$

$$\underline{w}^T \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \end{bmatrix}$$

$$\underline{Z} = \begin{bmatrix} \underline{z^{(1)}} & \underline{z^{(2)}} & \dots & \underline{z^{(m)}} \end{bmatrix} = \underline{w^T X} + \underbrace{[b \ b \ \dots \ b]}_{1 \times m} = \begin{bmatrix} \underline{w^T x^{(1)}} + b \end{bmatrix} \begin{bmatrix} \underline{w^T x^{(2)}} + b \end{bmatrix} \dots \begin{bmatrix} \underline{w^T x^{(m)}} + b \end{bmatrix}$$

\uparrow $1 \times m$

$$\Rightarrow \underline{Z} = \text{np.dot}(\underline{w.T}, X) + \underline{b}$$

$\mathbb{R}^{(1,1)}$ \mathbb{R}

$$\underline{A} = \begin{bmatrix} \underline{a^{(1)}} & \underline{a^{(2)}} & \dots & \underline{a^{(m)}} \end{bmatrix} = \sigma(\underline{Z})$$