HW7-Notes

March 2020

$$p(y \mid x; \theta) = h_{\theta}(x)^{y}(1 - h_{\theta}(x))^{1-y}$$

$$y = 1 \Rightarrow p(y = 1 \mid x; \theta) = h_{\theta}(x)^{1}(1 - h_{\theta}(x))^{0}$$

$$y = 0 \Rightarrow p(y = 0 \mid x; \theta) = 1 - h_{\theta}(x)$$

$$L(\theta) = p(y = 0 \mid x; \theta) = \prod_{i} p(y^{i} \mid x^{i}; \theta) = \prod_{i} h_{\theta}(x^{i})^{y^{i}}(1 - h_{\theta}(x^{i}))^{1-y^{i}})$$
It is much easier to maximize the log likelihood.
$$l(\theta) = \log L(\theta) = \sum_{i} [y^{i} \log h_{\theta}(x^{i}) + (1 - y^{i}) \log(1 - h_{\theta}(x^{i}))]$$
How to maximize it? Use (stochastic) gradient descent.
$$\theta := \theta \bigoplus \alpha \nabla_{\theta} l(\theta)$$

$$\bigoplus: \text{along with the gradient direction.}$$

$$\frac{\partial}{\partial \theta_{i}} l(\theta) = \sum_{i=1}^{n} (y^{i} - h_{\theta}(x^{i})) x_{j}^{i}$$