

CS61C: Learn 6 great ideas in computer architecture to enable high performance programming via parallelism, not just learn C Abstraction (Layers of Representation/Interpretation) Moore's Law Principle of Locality/Memory Hierarchy Parallelism Performance Measurement and

6. Dependability via Redundancy

CS61C L02 Number

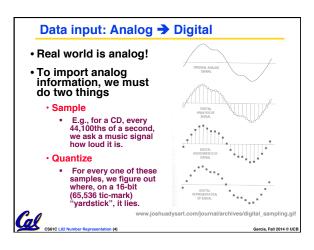
CS61C L02 Number Representation (2)

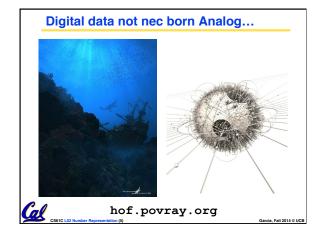
Improvement

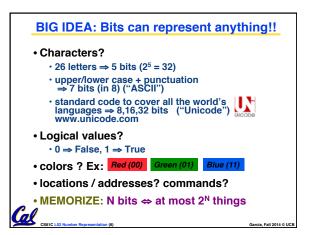
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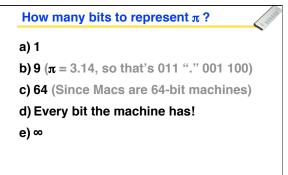


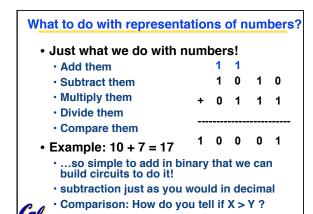
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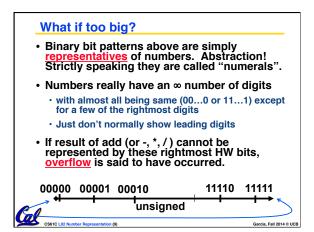


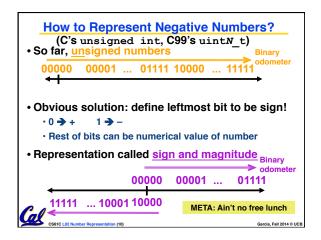








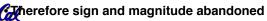


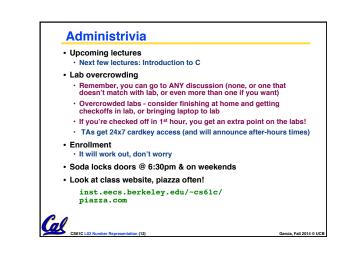


Shortcomings of sign and magnitude? • Arithmetic circuit complicated • Special steps depending whether signs are the same or not • Also, two zeros • 0x00000000 = +0_{ten} • 0x80000000 = -0_{ten}

• What would two 0s mean for programming?

- Also, incrementing "binary odometer", sometimes increases values, and
- sometimes increases values, and sometimes decreases!





Great DeCal courses I supervise

- UCBUGG (3 units, P/NP)
 - · UC Berkeley Undergraduate Graphics Group
 - · TuTh 7-9pm in 200 Sutardja Dai
 - · Learn to create a short 3D animation
 - No prereqs (but they might have too many students, so admission not guaranteed)
 - · http://ucbugg.berkeley.edu
- MS-DOS X (2 units, P/NP)
 - Macintosh Software Developers for OS X
 - · MoWe 8-10pm in 200 Sutardja Dai
 - · Learn to program iOS devices!
 - No prereqs (other than interest)
 - · http://msdosx.berkeley.edu



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Another try: complement the bits

- $7_{10} = 00111_2 7_{10} = 11000_2$ • Example:
- Called One's Complement
- Note: positive numbers have leading 0s, negative numbers have leadings 1s.Binary

00000 00001 ... 01111 10000 ... 11110 11111

- What is -00000 ? Answer: 11111
- How many positive numbers in N bits?

How many negative numbers?

Shortcomings of One's complement?

- Arithmetic still a somewhat complicated.
- Still two zeros
 - $0x00000000 = +0_{ten}$
 - 0xFFFFFFF = -0_{ten}
- Although used for a while on some computer products, one's complement was eventually abandoned because another solution was better.

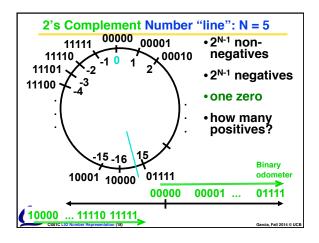


Standard Negative # Representation

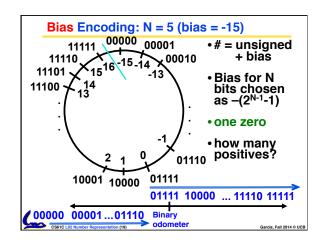
- Problem is the negative mappings "overlap" with the positive ones (the two 0s). Want to shift the negative mappings left by one.
 - · Solution! For negative numbers, complement, then
- As with sign and magnitude, & one's compl. leading 0s ⇒ positive, leading 1s ⇒ negative
 - .000000...xxx is ≥ 0, 111111...xxx is < 0
 - · except 1...1111 is -1, not -0 (as in sign & mag.)
- This representation is Two's Complement
 - This makes the hardware simple!

(C's int, aka a "signed integer") (Also C's short, long long, ..., C99's intN_t)

Two's Complement Formula



Can represent positive and negative numbers in terms of the bit value times a power of 2: $d_{31} \times (-(2^{31})) + d_{30} \times 2^{30} + ... + d_2 \times 2^2 + d_1 \times 2^1 + d_0 \times 2^0$ Example: 1101_{two} in a nibble? $= 1x-(2^3) + 1x2^2 + 0x2^1 + 1x2^0$ $= -2^3 + 2^2 + 0 + 2^0$ Example: -3 to +3 to -3 (again, in a nibble): = -8 + 4 + 0 + 1= -8 + 5: 1101 : 0010 two : 0011 two : 1100 two : 1101 two



How best to represent -12.75?

- a) 2s Complement (but shift binary pt)
- b) Bias (but shift binary pt)
- c) Combination of 2 encodings
- d) Combination of 3 encodings
- e) We can't

Shifting binary point means "divide number by some power of 2. E.g., $11_{10} = 1011.0_2$ so $(11/4)_{10} = 2.75_{10} = 10.110_2$

CS61C L02 Number Rep

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And in summary... We represent "things" in

META: We often make design decisions to make HW simple

- We represent "things" in computers as particular bit patterns: N bits \Rightarrow 2N things
- These 5 integer encodings have different benefits; 1s complement and sign/mag have most problems.
- unsigned (C99's uintN_t):

00000 00001 ... 01111 10000 ... 11111

• 2's complement (C99's intN_t) universal, learn!

00000 00001 ... 01111

Overflow: numbers ∞; computers finite,errors!

META: Ain't no free lunch

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REFERENCE: Which base do we use?

- Decimal: great for humans, especially when doing arithmetic
- Hex: if human looking at long strings of binary numbers, its much easier to convert to hex and look 4 bits/symbol
 - · Terrible for arithmetic on paper
- Binary: what computers use;
 you will learn how computers do +, -, *, /
 - To a computer, numbers always binary
 - · Regardless of how number is written:
 - $\cdot 32_{\text{ten}} == 32_{10} == 0 \times 20 == 100000_2 == 0 \text{b} 100000$
 - Use subscripts "ten", "hex", "two" in book, slides when might be confusing

er Representation (22) Garcia, Fall 20

Two's Complement for N=32

- One zero; 1st bit called sign bit
- 1 "extra" negative:no positive 2,147,483,648_{ten}

CS61C L02 Number Representation (23)

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Two's comp. shortcut: Sign extension

- Convert 2's complement number rep. using n bits to more than n bits
- Simply replicate the most significant bit (sign bit) of smaller to fill new bits
 - · 2's comp. positive number has infinite 0s
 - · 2's comp. negative number has infinite 1s
 - Binary representation hides leading bits;
 sign extension restores some of them
 - 16-bit -4_{ten} to 32-bit:

1111 1111 1111 1100_{two}

1111 1111 1111 1111 1111 1111 1111 1111 1100_{two}

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