

Use the Matlab `linprog` function to solve the multi-period planning problem with the following data.

Cash needed:

| Year               | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
|--------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Cash (in \$1,000s) | 11 | 14 | 16 | 17 | 19 | 22 | 24 | 25 | 27 | 28 | 29 | 31 | 32 | 34 | 37 | 38 |

Annual interest rate of guaranteed savings account = 7%

Securities available:

| Security | Current Cost | Yearly Return | Years to Maturity | Principal Repayment at Maturity |
|----------|--------------|---------------|-------------------|---------------------------------|
| 1        | \$975        | \$65          | 12                | \$1,000                         |
| 2        | \$975        | \$70          | 13                | \$1,000                         |
| 3        | \$985        | \$60          | 4                 | \$1,000                         |

Give the the minimum amount of the lump sum needed (in \$1,000s).

Let  $S_i$  be the amount invested in savings account at year  $i$ , 7%

Let  $B_1$  be the face value invested in security 3

Let  $B_2$  be the face value invested in security 1

Let  $B_3$  be the face value invested in security 2

Min =  $L$

Time Period 0:  $L - 0.985*B_1 - 0.975*B_2 - 0.975*B_3 - S_0 = 11$

Time Period 1:  $0.06*B_1 + 0.065*B_2 + 0.07*B_3 + 1.07*S_0 - S_1 = 14$

Time Period 2:  $0.06*B_1 + 0.065*B_2 + 0.07*B_3 + 1.07*S_1 - S_2 = 16$

Time Period 3:  $0.06*B_1 + 0.065*B_2 + 0.07*B_3 + 1.07*S_2 - S_3 = 17$

Time Period 4:  $1.06*B_1 + 0.065*B_2 + 0.07*B_3 + 1.07*S_3 - S_4 = 19$

Time Period 5:  $+ 0.065*B_2 + 0.07*B_3 + 1.07*S_4 - S_5 = 22$

Time Period 6:  $+ 0.065*B_2 + 0.07*B_3 + 1.07*S_5 - S_6 = 24$

Time Period 7:  $0.065*B_2 + 0.07*B_3 + 1.07*S_6 - S_7 = 25$

Time Period 8:  $0.065*B_2 + 0.07*B_3 + 1.07*S_7 - S_8 = 27$

Time Period 9:  $0.065*B_2 + 0.07*B_3 + 1.07*S_8 - S_9 = 28$

Time Period 10:  $0.065*B_2 + 0.07*B_3 + 1.07*S_9 - S_{10} = 29$

Time Period 11:  $0.065*B_2 + 0.07*B_3 + 1.07*S_{10} - S_{11} = 31$

Time Period 12:  $1.065*B_2 + 0.07*B_3 + 1.07*S_{11} - S_{12} = 32$

Time Period 13:  $0.065*B_3 + 0.07*B_3 + 1.07*S_{12} - S_{13} = 34$

Time Period 14:  $1.07*S_{13} - S_{14} = 37$

Time Period 15:  $1.07*S_{14} - S_{15} = 38$

Hence, problem statement is, find minimal value of L, subject to the constraints as shown above.

We want to minimize L

#MatLab Code

```
f = [1; 0;0;0;0;0;0;0;0;0;0;0;0;0;0;0;0;0;0;0];
A = [1 -0.985 -0.975 -0.975 -1 0 0 0 0 0 0 0 0 0 0 0
0 0 0 0 0 0
0 0 0.06 0.065 0.070 1.07 -1 0 0 0 0 0 0 0 0 0
0 0 0 0 0 0
0 0 0.06 0.065 0.070 0 1.07 -1 0 0 0 0 0 0 0
0 0 0 0 0 0
0 0 0.06 0.065 0.070 0 0 1.07 -1 0 0 0 0 0 0
0 0 0 0 0 0
0 1.06 0.065 0.070 0 0 0 1.07 -1 0 0 0 0 0 0
0 0 0 0 0 0
0 0.00 0.065 0.070 0 0 0 0 1.07 -1 0 0 0 0 0
0 0 0 0 0 0
0 0.00 0.065 0.070 0 0 0 0 0 1.07 -1 0 0 0 0
0 0 0 0 0 0
0 0 0.065 0.070 0 0 0 0 0 0 1.07 -1 0 0 0
0 0 0 0 0 0
0 0 0.065 0.070 0 0 0 0 0 0 0 1.07 -1 0
0 0 0 0 0 0
0 0 0.065 0.070 0 0 0 0 0 0 0 0 1.07
-1 0 0 0 0 0
0 0 0.065 0.070 0 0 0 0 0 0 0 0 0 0
1.07 -1 0 0 0 0
0 0 1.065 0.070 0 0 0 0 0 0 0 0 0 0
0 1.07 -1 0 0 0
0 0 0 1.070 0 0 0 0 0 0 0 0 0 0
0 0 1.07 -1 0 0
0 0 0 0 0.00 0 0 0 0 0 0 0 0 0
0 0 0 1.07 -1 0
0 0 0 0 0 0 0 0 0 0 0 0 0 0
0 0 0 0 1.07 -1 ];
```

```
B = [11 ; 14; 16; 17; 19; 22; 24; 25;27;28;29;31;32;34;37;38];
lb = zeros(20,1);

[x, fval, exitflag, output, lambda]= linprog(f, [], [], A,B, lb);
disp(lambda)
```

Ans: 228.1538