

MH1403 Algorithms and Computing

Lab 4 Sorting and Divide-and-Conquer Algorithms

Submission Instructions:

1. This lab is 5% of the final grade of this course.
2. The submission deadline is 11:59PM, 19 April (Sunday).
3. You need to submit the codes of Task 1 and Task 2 through NTULearn.

Task 1. (2.5 marks) Write a Python function `insertionSort()` to sort a list (we assume that all the elements in the list are numerical values). The input to this function is a list to be sorted. You should not use the `sort()` function of Python in this task. Note that you do not print anything from the function `insertionSort`.

Create a list containing the elements $(5*i+2)\%37$ for i from 0 to 20. Call the function `insertionSort()` to sort this list, print the sorted list to the screen.

You write the code in the file `task1.py`

Task 2. (2.5 marks) Write a Python function `mergeSort()` to sort a list (we assume that all the elements in the list are numerical values). The input to this function is a list to be sorted. You should not use the `sort()` function of Python in this task. Note that you do not print anything from the function `mergeSort`.

Create a list containing the elements $(5*i+2)\%37$ for i from 0 to 20. Call the function `mergeSort()` to sort this list, print the sorted list to the screen.

You submit your code in the file `task2.py`

Task 3. (optional) When we learn the maximum subsequence problem in Lecture 1 (the last 7 slides of Lecture 1), we mentioned that the maximum subsequence problem can be solved using the divide-and-conquer algorithm with very low running time.

The divide-and-conquer algorithm on the maximum subsequence problem works as follows:

- Locate the middle element of the sequence. It divides the sequences into three parts: the left half, the right half, and the middle element.
- Find the sum of the maximum subsequence for the left half (in a recursive way)
- Find the sum of the maximum subsequence for the right half (in a recursive way)
- Find the sum of the maximum sequence that contains the middle element (how to solve this problem in an efficient way?)
- Return the maximum of the above three sums.

Write a python function `maximumSequence()` that computes the sum of the maximum sequence. The input to this function is a list.

Create a list A as `[4, -3, 5, -2, -1, 2, 6, -2]`. Call the function `maximumSequence()` to compute the sum of the maximum sequence of List A, print the sum to the screen.