

CURRENT ELECTRICITY

1. ELECTRIC CURRENT

“The flow of charge in a definite direction constitutes the electric current and the time rate of flow of charge through any cross-section of a conductor is the measure of current”. i.e.,

$$\text{Electric current, } I = \frac{\text{net charge flown}}{\text{time taken}} = \frac{q}{t} = \frac{dq}{dt}$$

1. Though the “electric current represents the direction of flow of positive charge”.
2. Yet it is treated as a scalar quantity.
3. Current follows, the laws of scalar addition and not the laws of vector addition.
4. Because the angle between the wires carrying currents does not affect the total current in the circuit.

2. CURRENT CARRIERS

(a) Current carriers in solid conductors :

1. In solid conductors like metals, the valence electrons of the atoms do not remain attached to individual atoms but are free to move throughout the volume of the conductor.
2. Under the effect of an external electric field, the valence electrons move in a definite direction causing electric current in the conductors.
3. Thus, valence electrons are the current carriers in solid conductors.

(b) Current carriers in liquids :

1. In an electrolyte like CuSO_4 , NaCl etc., there are positively and negatively charged ions (like Cu^{++} , SO_4^{-} , Na^+ , Cl^-).
2. These are forced to move in definite directions under the effect of an external electric field, causing electric current.
3. Thus, in liquids, the current carriers are positively and negatively charged ions.

(c) Current carriers in gases :

1. Ordinarily, the gases are insulators of electricity.
2. They can be ionized by applying a high potential difference at low pressure
3. Thus, positive ions and electrons are the current carriers in gases.

3. DRIFT VELOCITY

“If $\vec{u}_1, \vec{u}_2, \vec{u}_3, \dots, \vec{u}_n$ are random thermal velocities of n free electrons in the metal conductor, then the average thermal velocity of electrons is

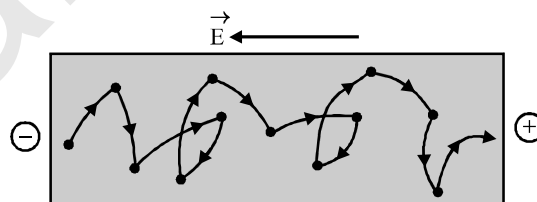
$$\frac{\vec{u}_1 + \vec{u}_2 + \vec{u}_3 + \dots + \vec{u}_n}{n} = \vec{0}$$

As a result, there will be no net flow of electrons of charge in one particular direction in a metal conductor, hence no current”.

“Drift velocity is defined as the average velocity with which the free electrons get drifted towards the positive end of the conductor under the influence of an external electric field applied”.

1. The drift velocity of electrons is of the order of 10^{-4} ms^{-1} .
2. If V is the potential difference applied across the ends of the conductor of length l , the magnitude of electric field set up is

$$E = \frac{\text{Potential difference}}{\text{length}} = \frac{V}{l}$$



3. Each free electrons in the conductor experience a force, $\vec{F} = -e\vec{E}$.
4. The acceleration of each electron is $\vec{a} = \frac{e\vec{E}}{m}$.
5. At any instant of time, the velocity acquired by electron having thermal velocity \vec{u}_1 will be

$$\vec{v}_1 = \vec{u}_1 + \vec{a}\tau_1$$

where τ_1 is the time elapsed since it has suffered its last collision with ion/atom of the conductor.

6. Similarly, the velocities acquired by other electrons in the conductor will be

$$\vec{v}_2 = \vec{u}_2 + \vec{a}\tau_2, \quad \vec{v}_3 = \vec{u}_3 + \vec{a}\tau_3, \dots, \quad \vec{v}_n = \vec{u}_n + \vec{a}\tau_n.$$

7. The average velocity of all the free electrons in the conductor under the effect of external electric field is the drift velocity \vec{v}_d of the free electrons.

$$\begin{aligned} \text{Thus, } \vec{v}_d &= \frac{\vec{v} + \vec{v}_2 + \dots + \vec{v}_n}{n} \\ &= \frac{(\vec{u}_1 + \vec{a}\tau_1) + (\vec{u}_2 + \vec{a}\tau_2) + \dots + (\vec{u}_n + \vec{a}\tau_n)}{n} \\ &= \left(\frac{\vec{u}_1 + \vec{u}_2 + \dots + \vec{u}_n}{n} \right) + \vec{a} \left(\frac{\tau_1 + \tau_2 + \dots + \tau_n}{n} \right) = 0 + \vec{a}\tau = \vec{a}\tau \end{aligned}$$

where, $\tau = \frac{\tau_1 + \tau_2 + \dots + \tau_n}{n}$ = average time that has elapsed

since each electron suffered its last collision with the ion/atom of conductor and is called average relaxation time.

8. Its value is the order of 10^{-14} second.

9. Putting the value of \vec{a} in the above relation, we have

$$\vec{v}_d = \frac{-e\vec{E}\tau}{m}$$

Average drift speed, $v_d = \frac{eE}{m}\tau$

The negative sign show that \vec{v}_d is opposite to the direction of \vec{E} .

3.1 Relaxation time (τ)

The time interval between two successive collisions of electrons with the positive ions in the metallic lattice is defined

as relaxation time $\tau = \frac{\text{mean free path}}{\text{r.m.s. velocity of electrons}} = \frac{\lambda}{v_{\text{rms}}}$. With

rise in temperature v_{rms} increases consequently τ decreases.

3.2 Mobility

Drift velocity per unit electric field is called mobility of electron *i.e.*

$$\mu = \frac{v_d}{E} \text{ It's unit is } \frac{\text{m}^2}{\text{volt} - \text{sec}}$$

- ✱ If cross-section is constant, $I \propto J$ *i.e.* for a given cross-sectional area, greater the current density, larger will be current.

- ✱ The drift velocity of electrons is small because of the frequent collisions suffered by electrons.
- ✱ The small value of drift velocity produces a large amount of electric current, due to the presence of extremely large number of free electrons in a conductor. The propagation of current is almost at the speed of light and involves electromagnetic process. It is due to this reason that the electric bulb glows immediately when switch is on.
- ✱ In the absence of electric field, the paths of electrons between successive collisions are straight line while in presence of electric field the paths are generally curved.

- ✱ Free electron density in a metal is given by $n = \frac{N_A \times d}{A}$ where N_A = Avogadro number, x = number of free electrons per atom, d = density of metal and A = Atomic weight of metal.

1. Mobility of charge carrier (μ), responsible for current is defined as the magnitude of drift velocity of charge per unit electric field applied, *i.e.*,

$$\mu = \frac{\text{drift velocity}}{\text{electric field}} = \frac{v_d}{E} = \frac{qE\tau/m}{E} = \frac{q\tau}{m}$$

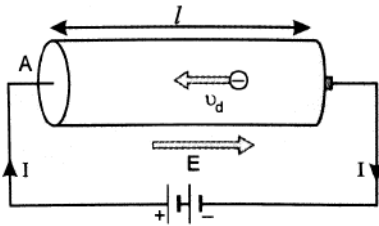
2. Mobility of electron, $\mu_e = \frac{e\tau_e}{m_e}$
3. The total current in the conducting material is the sum of the currents due to positive current carriers and negative current carriers.

$$v_d = \mu_e E$$

4. SI unit of mobility is $\text{m}^2\text{S}^{-1}\text{V}^{-1}$ or $\text{ms}^{-1}\text{N}^{-1}\text{C}$

3.3 Relation between current and Drift Velocity

1. Consider a conductor (say a copper wire) of length l and of uniform area of cross-section
 \therefore Volume of the conductor = Al .
2. If n is the number density of electrons, *i.e.*, the number of free electrons per unit volume of the conductor, then total number of free electrons in the conductor = Aln .
3. Then total charge on all the free electrons in the conductor,
 $q = Alne$
4. The electric field set up across the conductor is given by $E = V/l$ (in magnitude)
5. Due to this field, the free electrons present in the conductor will begin to move with a drift velocity v_d towards the left hand side as shown in figure



6. Time taken by the free electrons to cross the conductors,
 $t = l/v_d$

$$\text{Hence, current, } dI = \frac{q}{t} = \frac{A \ell n e}{t = \frac{\ell}{v_d}}$$

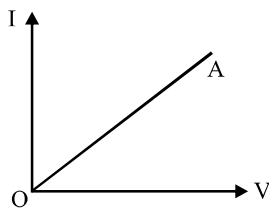
or $I = A n e v_d$

7. Putting the value of $v_d \left(= \frac{e E \tau}{m} \right)$, we have

$$I = \frac{A n e^2 \tau E}{m}$$

4. OHM'S LAW

Ohm's law states that the current (I) flowing through a conductor is directly proportional to the potential difference (V) across the ends of the conductor."



i.e., $I \propto V$ or $V \propto I$ or $V = RI$

or $\frac{V}{I} = R = \text{constant}$

4.1 Deduction of Ohm's law

We know that $v_d = \frac{e E \tau}{m}$

But $E = V/l \therefore v_d = \frac{e V \tau}{m l}$

Also, $I = A n e v_d$

$$\therefore I = A n e \left(\frac{e V \tau}{m l} \right) = \left(\frac{A n e^2 \tau}{m l} \right) V$$

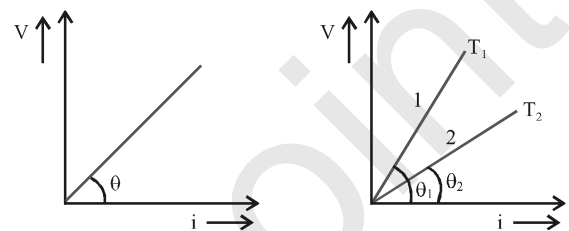
$$\text{or } \frac{V}{I} = \frac{m l}{A n e^2 \tau} = R = \text{a constant for a given conductor for a}$$

given value of n, l and at a given temperature. It is known as the electrical resistance of the conductor.

Thus, $V = RI$

this is Ohm's law.

- (1) Ohm's law is not a universal law, the substances, which obey ohm's law are known as ohmic substance.
- (2) Graph between V and i for a metallic conductor is a straight line as shown. At different temperatures V - i curves are different.



(A) Slope of the line

(B) Here $\tan \theta_1 > \tan \theta_2$

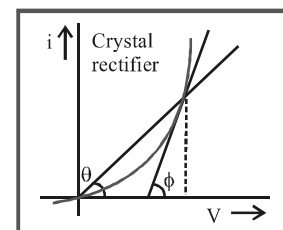
$$= \tan \theta = \frac{V}{i} = R$$

So, $R_1 > R_2$ i.e., $T_1 > T_2$

- (3) The device or substances which don't obey ohm's law e.g. gases, crystal rectifiers, thermoionic valve, transistors etc. are known as non-ohmic or non-linear conductors. For these V - i curve is not linear.

$$\text{Static resistance } R_{st} = \frac{V}{i} = \frac{1}{\tan \theta}$$

$$\text{Dynamic resistance } R_{dyn} = \frac{\Delta V}{\Delta I} = \frac{1}{\tan \phi}$$



5. ELECTRICAL RESISTANCE

"The electrical resistance of a conductor is the obstruction posed by the conductor to the flow of electric current through it".

1. i.e., $R = V/I$

2. The SI unit of electrical resistance is ohm or $\frac{\text{volt}}{\text{amp}}$.

3. Dimensions of electric resistance

$$= \frac{\text{Pot. diff.}}{\text{current}} = \frac{\text{work done/charge}}{\text{current}}$$

$$= \frac{ML^2T^{-2} / AT}{A} = [M^1 L^2 T^{-3} A^{-2}]$$

5.1 Electrical, Resistivity or Specific Resistance

“The resistance of a conductor depends upon the following factors :

- Length (l) :** The resistance (R) of a conductor is directly proportional to its length (l), i.e., $R \propto l$
- Area of cross-section (A) :** The resistance (R) of a conductor is inversely proportional to the area of cross-section (A), of the conductor, i.e., $R \propto 1/A$
- The resistance of conductor also depends upon the **nature of material** and temperature of the conductor.

From above ; $R \propto \frac{l}{A}$ or $R = \frac{\rho l}{A}$.”

5.2 Resistivity (ρ)

- Where ρ is constant of proportionality and is known as specific resistance or electrical resistivity of the material of the conductor
- Specific resistance** (or electrical resistivity) of the material of a conductor is defined as the resistance of a unit length with unit areas of cross section of the material of the conductor.

(i) Unit and dimension : It's S.I. unit is *ohm × m* and dimension is $[ML^3T^{-3}A^{-2}]$

(ii) It's formula : $\rho = \frac{m}{ne^2\tau}$

(iii) Resistivity is the intrinsic property of the substance. It is independent of shape and size of the body (i.e. l and A).

(iv) For different substances their resistivity is also different e.g. ρ_{silver} = minimum = $1.6 \times 10^{-8} \Omega\text{-m}$ and $\rho_{\text{fused quartz}}$ = maximum $\approx 10^{16} \Omega\text{-m}$

$$\rho_{\text{insulator}} > \rho_{\text{alloy}} > \rho_{\text{semi-conductor}} > \rho_{\text{conductor}}$$

(Maximum for fused quartz) (Minimum for silver)

(v) Resistivity depends on the temperature. For metals $\rho_t = \rho_0(1 + \alpha\Delta t)$ i.e. resistivity increases with temperature.

- Resistivity increases with impurity and mechanical stress.
- Magnetic field increases the resistivity of all metals except iron, cobalt and nickel.
- Resistivity of certain substances like selenium, cadmium, sulphides is inversely proportional to intensity of light falling upon them.

3. We have, $R = \frac{V}{I} = \frac{m\ell}{Ane^2\tau} = \frac{m}{ne^2\tau} \times \frac{\ell}{A}$

comparing the above relation with the relation, $R = \rho \frac{\ell}{A}$.

4. We have, the resistivity of the material of a conductor,

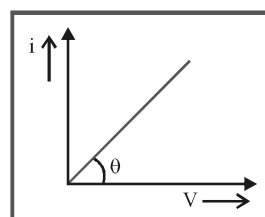
$$\rho = \frac{m}{ne^2\tau}$$

5.3 Conductivity

Reciprocal of resistivity is called conductivity (σ) i.e. $\sigma = \frac{1}{\rho}$ with unit *mho/m* and dimensions $[M^{-1}L^{-3}T^3A^2]$.

5.4 Conductance

Reciprocal of resistance is known as conductance. $C = \frac{1}{R}$ It's unit is $\frac{1}{\Omega}$ or Ω^{-1} or “Siemen”.

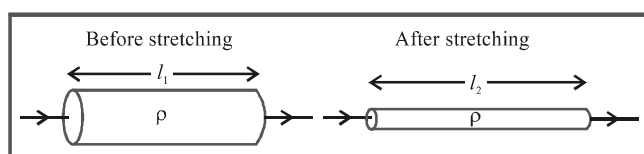


5.5 Stretching of Wire

If a conducting wire stretches, it's length increases, area of cross-section decreases so resistance increases but volume remain constant.

Suppose for a conducting wire before stretching it's length = l_1 , area of cross-section = A_1 , radius = r_1 , diameter = d_1 , and

resistance = $R_1 = \rho \frac{l_1}{A_1}$



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Volume remains constant i.e., $A_1 l_1 = A_2 l_2$

After stretching length = l_2 , area of cross-section = A_2 ,

radius = r_2 , diameter = d_2 and resistance = $R_2 = \rho \frac{l_2}{A_2}$

Ratio of resistances before and after stretching

$$\frac{R_1}{R_2} = \frac{l_1}{l_2} \times \frac{A_2}{A_1} = \left(\frac{l_1}{l_2}\right)^2 = \left(\frac{A_2}{A_1}\right)^2 = \left(\frac{r_2}{r_1}\right)^4 = \left(\frac{d_2}{d_1}\right)^4$$

(1) If length is given then $R \propto l^2 \Rightarrow \frac{R_1}{R_2} = \left(\frac{l_1}{l_2}\right)^2$

(2) If radius is given then $R \propto \frac{1}{r^4} \Rightarrow \frac{R_1}{R_2} = \left(\frac{r_2}{r_1}\right)^4$

6. CURRENT DENSITY, CONDUCTANCE AND ELECTRICAL CONDUCTIVITY

6.1 Relation between J, σ and E

We know, $I = n A e v_d = n A e \left(\frac{eE}{m} \tau\right) = \frac{n A e^2 \tau E}{m}$

or $\frac{I}{A} = \frac{n e^2 \tau E}{m}$ or $J = \frac{1}{\rho} E$

$\therefore \boxed{J = \sigma E}$

1. **Insulators** : These are those materials whose electrical conductivity is either very very small or nil.

Insulators do not conduct charges. When a small potential difference is applied across the two ends of an insulator, the current through the insulator is zero.

Examples of insulators are glass, rubber, wood etc.

Variation of R , ρ with T

2. **Conductors** : These are those materials whose electrical conductivity is very high

Conductors conduct charges very easily. When a small potential difference is applied across the two ends of a conductor, a strong current flows through the conductor. For super-conductor, the value of electrical conductivity is infinite and electrical resistivity is zero.

Examples of conductors are all metals like copper, silver, aluminium, tungsten etc.

3. **Semiconductors** : These are those material whose electrical conductivity lies inbetween that of insulators and conductors.

Semiconductors can conduct charges but not so easily as is in case of conductors. When a small potential difference is applied across the ends of a semiconductor, a weak current flows through semiconductor due to motion of electrons and holes.

Examples of semiconductors are germanium, silicon etc.

The value of electrical resistance R increases with rise of temperature.

$$\alpha = \frac{R_t - R_0}{R_0 \times t} = \frac{\text{increase in resistance}}{\text{original resistance} \times \text{rise of temp.}}$$

Thus, temperature coefficient of resistance is defined as the increase in resistance per unit original resistance per degree celsius or kelvin rise of temperature.

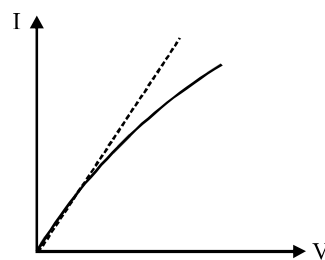
1. **For metals** like silver, copper, etc., the value of α is positive, therefore, resistance of a metal increases with rise in temperature. The unit of α is K^{-1} or $^{\circ}C^{-1}$.
2. **For insulators and semiconductors α is negative**, therefore, the resistance decreases with rise in temperature.

6.2 Non-Ohmic Devices

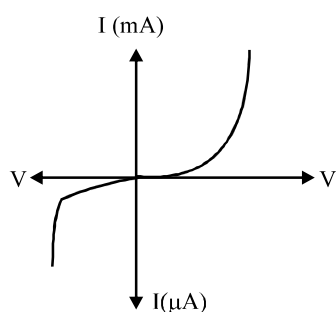
Those devices which do not obey Ohm's law are called non-ohmic devices. For example, vacuum tubes, semiconductor diode, liquid electrolyte, transistor etc.

For all **non-ohmic devices** (where there will be failure of Ohm's law), V - I graph has one or more of the following characteristics :

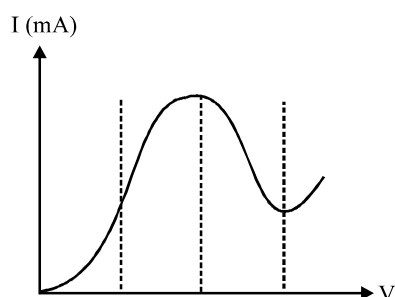
- (a) The relation between V and I is **non-linear**, figure



- (b) The relation between V and I depends on the sign of V . It means, if I is the current for a certain value of V , then reversing the direction of V , keeping its magnitude fixed, does not produce a current of same magnitude I , in the opposite direction, figure.



- (c) The relation between V and I is not unique, i.e., there is more than one value of V for the same current I , figure.



7. COLOUR CODE FOR CARBON RESISTORS

The colour code for carbon resistance is given in the following table.

Colour code of carbon resistors

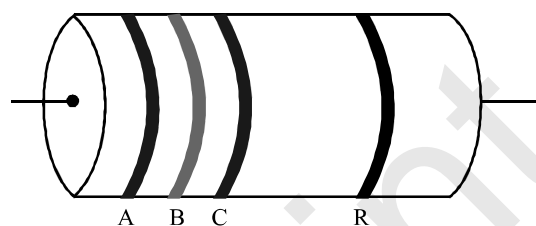
Colour	Letter as an Aid to memory	No.	Multplier	Colour	Tolerance
Black	B	0	10^0	Gold	5%
Brown	B	1	10^1	Silver	10%
Red	R	2	10^2	No colour	20%
Orange	O	3	10^3		
Yellow	Y	4	10^4		
Green		5	10^5		
Blue	B	6	10^6		
Violet	V	7	10^7		
Grey		8	10^8		
White	W	9	10^9		
Gold			10^{-1}		
Silver			10^{-2}		

To remember the value of colour coding used for carbon resistor, the following sentences are found to be of great help (where bold letters stand for colours).

B B ROY Green, Britain Very Good Wife **Gold Silver**.

Way of finding the resistance of carbon resistor from its colour coding.

In the system of colour coding, Strips of different colours are given on the body of the resistor, figure. The colours on strips are noted from left to right.

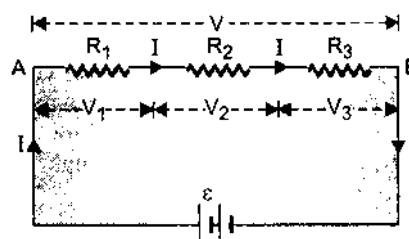


- Colour of the first strip A from the end indicates the first significant figure of resistance in ohm.
- Colour of the second strip B indicate the second significant figure of resistance in ohm.
- The colour of the third strip C indicates the multiplier, i.e., the number of zeros that will follow after the two significant figure.
- The colour of fourth strip R indicates the tolerance limit of the resistance value of percentage accuracy of resistance.

8. COMBINATION OF RESISTORS

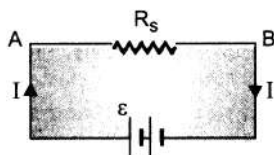
8.1 Resistances in Series

Resistors are said to be connected in series, if the same current is flowing through each resistor when some potential difference is applied across the combination.



- Let V be the potential difference applied across A and B using the battery ϵ . In series combination, the same current (say I) will be passing through each resistance.
- Let V_1 , V_2 , V_3 be the potential difference across R_1 , R_2 and R_3 respectively. According to Ohm's law
 $V_1 = IR_1$, $V_2 = IR_2$, $V_3 = IR_3$
- Here, $V = V_1 + V_2 + V_3 = IR_1 + IR_2 + IR_3 = I(R_1 + R_2 + R_3)$

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4. If R_s is the equivalent resistance of the given series combination of resistances, figure, then the potential difference across A and B is,

$$V = IR_s.$$

We have

$$IR_s = I(R_1 + R_2 + R_3)$$

or $\boxed{R_s = R_1 + R_2 + R_3}$

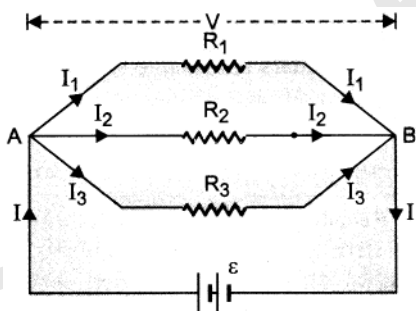
Memory note

In a series resistance circuit, it should be noted that :

- the current is same in every resistor.
- the current in the circuit is independent of the relative positions of the various resistors in the series.
- the voltage across any resistor is directly proportional to the resistance of the resistor.
- the total resistance of the circuit is equal to the sum of the individual resistances, plus the internal resistance of a cell if any.
- The total resistance in the series circuit is obviously more than the greatest resistance in the circuit.

8.2 Resistances in Parallel

Any number of resistors are said to be connected in parallel if potential difference across each of them is the same and is equal to the applied potential difference.



- Let V be the potential difference applied across A and B with the help of a battery ϵ .
- Let I be the main current in the circuit from battery. I divides itself into three unequal parts because the resistances of these

branches are different and I_1, I_2, I_3 be the current through the resistances R_1, R_2 and R_3 respectively. Then,

$$I = I_1 + I_2 + I_3$$

3. Here, potential difference across each resistor is V , therefore

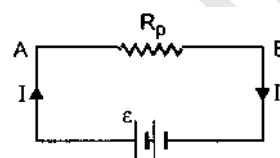
$$V = I_1 R_1 = I_2 R_2 = I_3 R_3$$

or $I_1 = \frac{V}{R_1}, I_2 = \frac{V}{R_2}, I_3 = \frac{V}{R_3}$

Putting values, we get

$$I = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

4. If R_p is the equivalent resistance of the given parallel combination of resistance, figure, then



$$V = IR_p \text{ or } I = V/R_p$$

we have

$$\frac{V}{R_p} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3} \text{ or } \boxed{\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

Thus, the reciprocal of equivalent resistance of a number of resistor connected in parallel is equal to the sum of the reciprocals of the individual resistances.

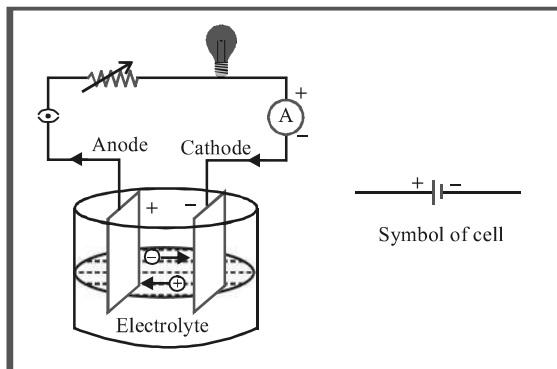
Memory note

In a parallel resistance circuit, it should be noted that :

- the potential difference across each resistor is the same and is equal to the applied potential difference.
- the current through each resistor is inversely proportional to the resistance of that resistor.
- total current through the parallel combination is the sum of the individual currents through the various resistors.
- The reciprocal of the total resistance of the parallel combination is equal to the sum of the reciprocals of the individual resistances.
- The total resistances are connected in series, the current through each resistance is same. When the resistance are in parallel, the pot-diff. across each resistance is the same and not the current.

9. CELL

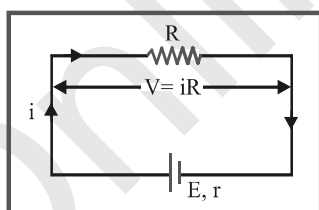
The device which converts chemical energy into electrical energy is known as electric cell. Cell is a source of constant emf but not constant current.



- (1) **Emf of cell (E)** : The potential difference across the terminals of a cell when it is not supplying any current is called its emf.
- (2) **Potential difference (V)** : The voltage across the terminals of a cell when it is supplying current to external resistance is called potential difference or terminal voltage. Potential difference is equal to the product of current and resistance of that given part i.e. $V = iR$.
- (3) **Internal resistance (r)** : In case of a cell the opposition of electrolyte to the flow of current through it is called internal resistance of the cell. The internal resistance of a cell depends on the distance between electrodes ($r \propto d$), area of electrodes [$r \propto (1/A)$] and nature, concentration ($r \propto C$) and temperature of electrolyte [$r \propto (1/\text{temp.})$].
A cell is said to be ideal, if it has zero internal resistance.

9.1 Cell in Various Positions

- (1) **Closed circuit** : Cell supplies a constant current in the circuit.



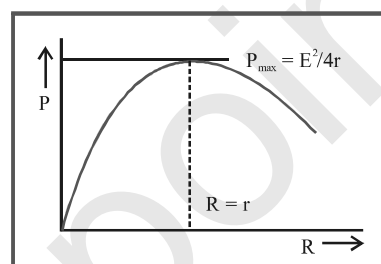
- (i) Current given by the cell $i = \frac{E}{R + r}$
- (ii) Potential difference across the resistance $V = iR$

- (iii) Potential drop inside the cell $= ir$
- (iv) Equation of cell $E = V + ir$ ($E > V$)
- (v) Internal resistance of the cell $r = \left(\frac{E}{V} - 1 \right) \cdot R$
- (vi) Power dissipated in external resistance (load)

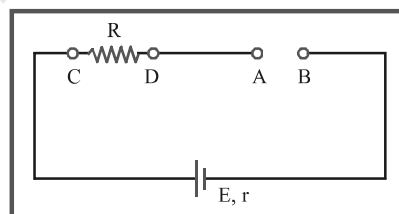
$$P = Vi = i^2 R = \frac{V^2}{R} = \left(\frac{E}{R + r} \right)^2 \cdot R$$

Power delivered will be maximum when $R = r$ so $P_{\max} = \frac{E^2}{4r}$.

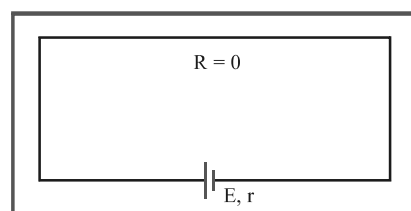
This statement in generalised form is called “*maximum power transfer theorem*”.



- (vii) When the cell is being charged i.e. current is given to the cell then $E = V - ir$ and $E < V$.
- (2) **Open circuit** : When no current is taken from the cell it is said to be in open circuit.



- (i) Current through the circuit $i = 0$
- (ii) Potential difference between A and B, $V_{AB} = E$
- (iii) Potential difference between C and D, $V_{CD} = 0$
- (3) **Short circuit** : If two terminals of cell are joined together by a thick conducting wire

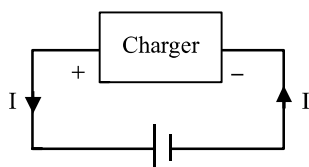


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- (i) Maximum current (called short circuit current) flows momentarily $i_{sc} = \frac{E}{r}$
- (ii) Potential difference $V = 0$

Memory note

- It is important to note that during charging of a cell, the positive electrode of the cell is connected to positive terminal of battery charger and negative electrodes of the cell is connected to negative terminal of battery charger. In this process, current flows from positive electrode to negative electrode through the cell. Refer figure



$$\therefore V = \varepsilon + Ir$$

Hence, the terminal potential difference becomes greater than the emf of the cell.

- The difference of emf and terminal voltage is called lost voltage as it is not indicated by a voltmeter. It is equal to Ir .

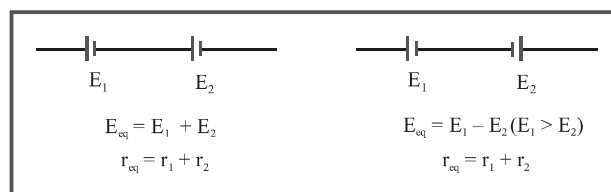
9.2 Distinction between E.M.F. and Potential Difference

E.M.F. of a Cell	Potential Difference
1. The emf of a cell is the maximum potential difference between the two electrodes of a cell when the cell is in the open circuit.	1. The potential difference between the two points is the difference of potential between those two points in a closed circuit.
2. It is independent of the resistance of the circuit and depends upon the nature of electrodes and the nature of electrolyte of the cell.	2. It depends upon the resistance between the two points of the circuit and current flowing through the circuit.
3. The term emf is used for the source of electric current.	3. The potential difference is measured between any two points of the electric circuit.
4. It is a cause.	4. It is an effect.

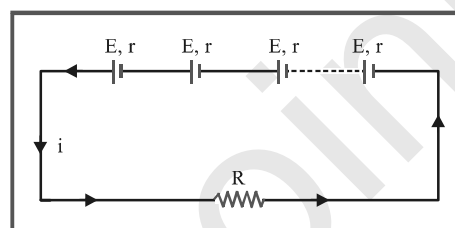
9.3 Grouping of Cells

In series grouping of cell's their emf's are additive or subtractive while their internal resistances are always additive. If dissimilar

plates of cells are connected together their emf's are added to each other while if their similar plates are connected together their emf's are subtractive.

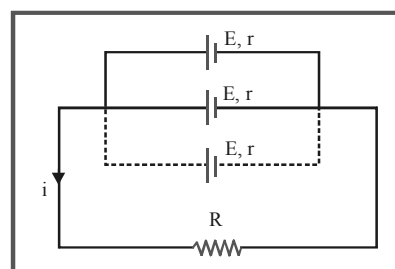


- (1) **Series grouping** : In series grouping anode of one cell is connected to cathode of other cell and so on. If n identical cells are connected in series



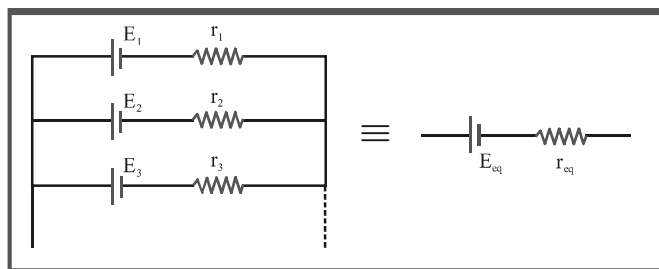
- Equivalent emf of the combination $E_{eq} = nE$
- Equivalent internal resistance $r_{eq} = nr$
- Main current = Current from each cell $i = \frac{nE}{R + nr}$
- Potential difference across external resistance $V = iR$
- Potential difference across each cell $V' = \frac{V}{n}$
- Power dissipated in the external circuit $= \left(\frac{nE}{R + nr} \right)^2 \cdot R$
- Condition for maximum power $R = nr$ and $P_{max} = n \left(\frac{E^2}{4r} \right)$
- This type of combination is used when $nr \ll R$.

- (2) **Parallel grouping** : In parallel grouping all anodes are connected at one point and all cathode are connected together at other point. If n identical cells are connected in parallel



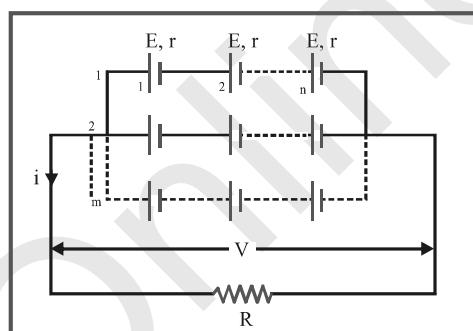
- (i) Equivalent emf $E_{eq} = E$
- (ii) Equivalent internal resistance $R_{eq} = r/n$
- (iii) Main current $i = \frac{E}{R + r/n}$
- (iv) Potential difference across external resistance = p.d. across each cell $V = iR$
- (v) Current from each cell $i' = \frac{i}{n}$
- (vi) Power dissipated in the circuit $P = \left(\frac{E}{R + r/n} \right)^2 \cdot R$
- (vii) Condition for max. power is $R = r/n$ and $P_{max} = n \left(\frac{E^2}{4r} \right)$
- (viii) This type of combination is used when $nr \gg R$

Generalized Parallel Battery



$$E_{eq} = \frac{\frac{E_1}{r_1} + \frac{E_2}{r_2} + \dots + \frac{E_n}{r_n}}{\frac{1}{r_1} + \frac{1}{r_2} + \dots + \frac{1}{r_n}} \quad \text{and} \quad \frac{1}{r_{eq}} = \frac{1}{r_1} + \frac{1}{r_2} + \dots + \frac{1}{r_n}$$

- (3) **Mixed Grouping :** If n identical cell's are connected in a row and such m row's are connected in parallel as shown.



- (i) Equivalent emf of the combination $E_{eq} = nE$
- (ii) Equivalent internal resistance of the combination $r_{eq} = \frac{nr}{m}$

- (iii) Main current flowing through the load

$$i = \frac{nE}{R + \frac{nr}{m}} = \frac{mnE}{mR + nr}$$

- (iv) Potential difference across load $V = iR$
- (v) Potential difference across each cell $V' = \frac{V}{n}$
- (vi) Current from each cell $i' = \frac{i}{n}$
- (vii) Condition for maximum power $R = \frac{nr}{m}$ and $P_{max} = (mn) \frac{E^2}{4r}$
- (viii) Total number of cell $= mn$

Memory note

Note that (i) If the two cells connected in parallel are of the same emf ϵ and same internal resistance r , then

$$\epsilon_{eq} = \frac{\epsilon r + \epsilon r}{r + r} = \epsilon$$

$$\frac{1}{r_{eq}} = \frac{1}{r} + \frac{1}{r} = \frac{2}{r} \quad \text{or} \quad r_{eq} = \frac{r}{2}$$

- (ii) If n identical cells are connected in parallel, then the equivalent emf of all the cells is equal to the emf of one cell.

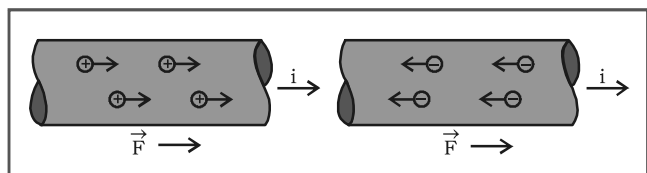
$$\frac{1}{r_{eq}} = \frac{1}{r} + \frac{1}{r} + \dots + n \text{ terms} = \frac{n}{r} \quad \text{or} \quad r_{eq} = r/n$$

10. ELECTRIC CURRENT

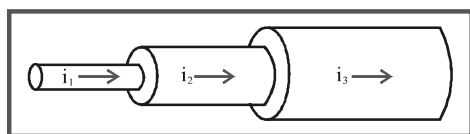
- (1) The time rate of flow of charge through any cross-section is called current. $i = \lim_{\Delta t \rightarrow 0} \frac{\Delta Q}{\Delta t} = \frac{dQ}{dt}$. If flow is uniform then $i = \frac{Q}{t}$. Current is a scalar quantity. It's S.I. unit is ampere (A) and C.G.S. unit is emu and is called biot (Bi), or ab ampere. $1A = (1/10) \text{ Bi (ab amp.)}$
- (2) Ampere of current means the flow of 6.25×10^{18} electrons/sec through any cross-section of the conductor.
- (3) The conventional direction of current is taken to be the direction of flow of positive charge, i.e. field and is

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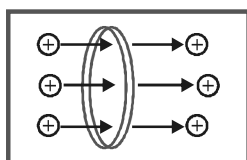
opposite to the direction of flow of negative charge as shown below.



- (4) The net charge in a current carrying conductor is zero.
- (5) For a given conductor current does not change with change in cross-sectional area. In the following figure $i_1 = i_2 = i_3$



- (6) **Current due to translatory motion of charge :** If n particle each having a charge q , pass through a given area in time t then

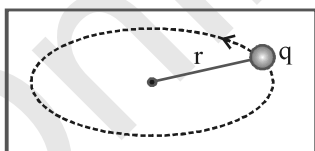


If n particles each having a charge q pass per second per unit area, the current associated with cross-sectional area A is $i = nqA$

If there are n particle per unit volume each having a charge q and moving with velocity v , the current thorough, cross section A is $i = nqvA$

- (7) **Current due to rotatory motion of charge :** If a point charge q is moving in a circle of radius r with speed v (frequency ν , angular speed ω and time period T) then

$$\text{corresponding current } i = qv = \frac{q}{T} = \frac{qv}{2\pi r} = \frac{q\omega}{2\pi}$$



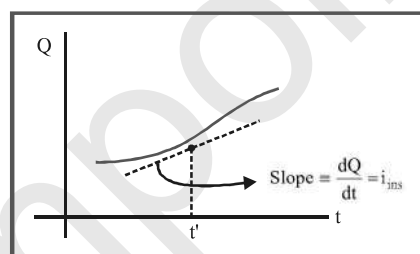
- (8) **Current carriers :** The charged particles whose flow in a definite direction constitutes the electric current are called current carriers. In different situation current carriers are different.

- (i) **Solids :** In solid conductors like metals current carriers are free electrons.
- (ii) **Liquids :** In liquids current carriers are positive and negative ions.
- (iii) **Gases :** In gases current carriers are positive ions and free electrons.
- (iv) **Semi conductor :** In semi conductors current carriers are holes and free electrons.
- (v) The amount of charge flowing through a crosssection of a conductor from $t = t_1$ to $t = t_2$ is given by :

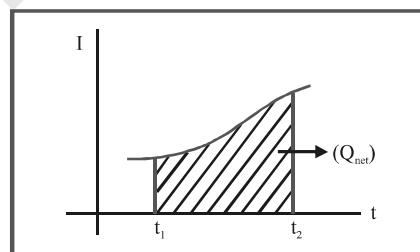
$$q = \int_{t_1}^{t_2} I dt$$

From Graphs

- (i) Slope of Q vs t graph gives instantaneous current.



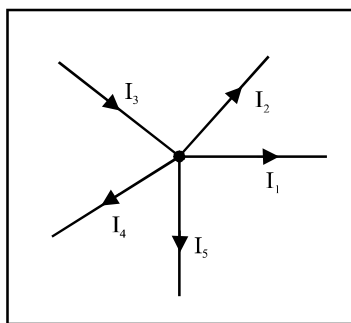
- (ii) Area under the I vs t graph gives net charge flown.



11. KIRCHHOFF'S LAW

11.1 Kirchhoff's first law or Kirchhoff's junction law or Kirchhoff's current law.

- the algebraic sum of the currents meeting at a junction in a closed electric circuit is zero, i.e., $\sum I = 0$
- Consider a junction O in the electrical circuit at which the five conductors are meeting. Let I_1, I_2, I_3, I_4 and I_5 be the currents in these conductors in directions, shown in figure,



3. Let us adopt the following sign convention : the current flowing in a conductor towards the junction is taken as positive and the current flowing away from the junction is taken as negative.
4. According to Kirchhoff's first law, at junction O
 $(-I_1) + (-I_2) + I_3 + (-I_4) + I_5 = 0$
 or $-I_1 - I_2 + I_3 - I_4 + I_5 = 0$
 or $\Sigma I = 0$
 or $I_3 + I_5 = I_1 + I_2 + I_4$
5. i.e., total current flowing towards the junction is equal to total current flowing out of the junction.
6. Current cannot be stored at a junction. It means, no point/junction in a circuit can act as a source or sink of charge.
7. **Kirchhoff's first law supports law of conservation of charge.**

11.2 Kirchhoff's Second law or Kirchhoff's loop law or Kirchhoff's voltage law.

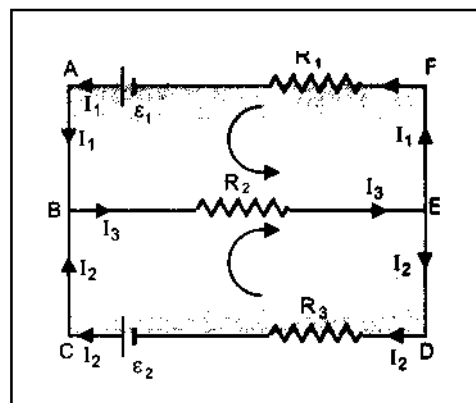
The algebraic sum of changes in potential around any closed path of electric circuit (or closed loop) involving resistors and cells in the loop is zero, i.e., $\Sigma \Delta V = 0$.

In a closed loop, the algebraic sum of the emfs and algebraic sum of the products of current and resistance in the various arms of the loop is zero, i.e., $\Sigma \varepsilon + \Sigma IR = 0$.

Kirchhoff's second law supports the law of conservation of energy, i.e., the net change in the energy of a charge, after the charge completes a closed path must be zero.

Kirchhoff's second law follows from the fact that the electrostatic force is a conservative force and work done by it in any closed path is zero.

Consider a closed electrical circuit as shown in figure. containing two cells of emfs. ε_1 and ε_2 and three resistors of resistances R_1 , R_2 and R_3 .



We adopt the following sign convention :

Traverse a closed path of a circuit once completely in clockwise or anticlockwise direction.


Difference between Kirchhoff's I and II laws

First Law	Second Law
1. This law supports the law of conservation of charge.	1. This law supports the law of conservation of energy.
2. According to this law $\Sigma I = 0$.	2. According to this law $\Sigma \varepsilon = \Sigma IR$
3. This law can be used in open and closed circuits.	3. This law can be used in closed circuit only.

12. EXPERIMENTS

12.1 Galvanometer

It is an instrument used to detect small current passing through it by showing deflection. Galvanometers are of different types *e.g.* moving coil galvanometer, moving magnet galvanometer, hot wire galvanometer. In dc circuit usually moving coil galvanometer are used.

- (i) **It's symbol :** ; where G is the total internal resistance of the galvanometer.
- (ii) **Full scale deflection current :** The current required for full scale deflection in a galvanometer is called full scale deflection current and is represented by i_g .
- (iii) **Shunt :** The small resistance connected in parallel to galvanometer coil, in order to control current flowing through the galvanometer is known as shunt.

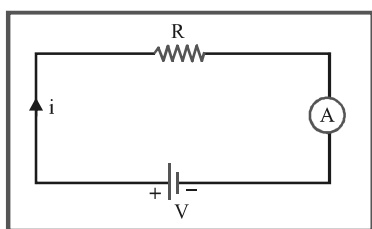
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Table : Merits and demerits of shunt

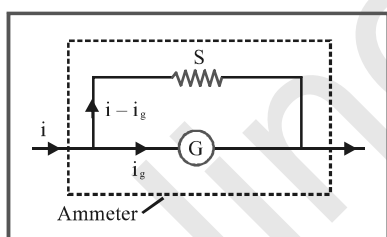
Merits of shunt	Demerits of shunt
To protect the galvanometer coil from burning . It can be used to convert any galvanometer into ammeter of desired range.	Shunt resistance decreases the sensitivity of galvanometer.

12.2 Ammeter

It is a device used to measure current and is always connected in series with the 'element' through which current is to be measured.



- The reading of an ammeter is always lesser than actual current in the circuit.
- Smaller the resistance of an ammeter more accurate will be its reading. An ammeter is said to be ideal if its resistance r is zero.
- Conversion of galvanometer into ammeter :** A galvanometer may be converted into an ammeter by connecting a low resistance (called shunt S) in parallel to the galvanometer G as shown in figure.



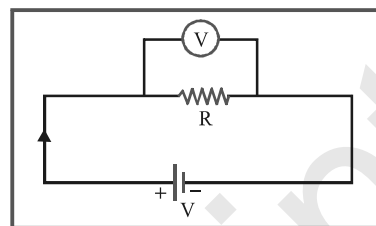
- Equivalent resistance of the combination $= \frac{GS}{G+S}$
- G and S are parallel to each other hence both will have equal potential difference i.e. $i_g G = (i - i_g) S$; which gives

$$\text{Required shunt } S = \frac{i_g}{(i - i_g)} G$$

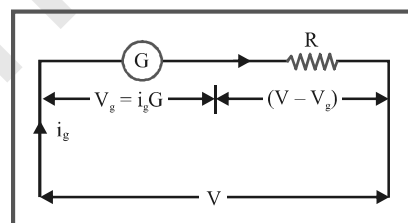
- To pass n th part of main current (i.e. $i_g = \frac{i}{n}$) through the galvanometer, required shunt $S = \frac{G}{(n-1)}$.

12.3 Voltmeter

It is a device used to measure potential difference and is always put in parallel with the 'circuit element' across which potential difference is to be measured.



- The reading of a voltmeter is always lesser than true value.
- Greater the resistance of voltmeter, more accurate will be its reading. A voltmeter is said to be ideal if its resistance is infinite, i.e., it draws no current from the circuit element for its operation.
- Conversion of galvanometer into voltmeter :** A galvanometer may be converted into a voltmeter by connecting a large resistance R in series with the galvanometer as shown in the figure.



- Equivalent resistance of the combination $= G + R$
- According to ohm's law Maximum reading of V which can be taken $V = i_g (G + R)$; which gives

$$\text{Required series resistance } R = \frac{V}{i_g} - G = \left(\frac{V}{V_g} - 1 \right) G$$

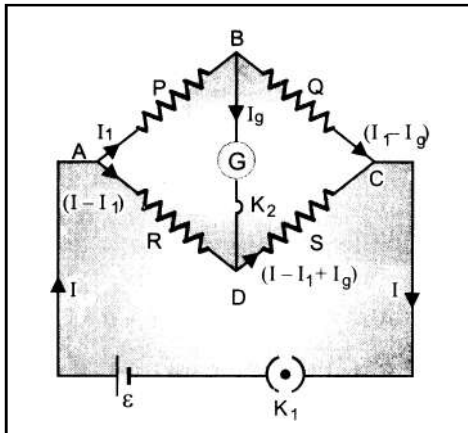
- If n^{th} part of applied voltage appeared across galvanometer (i.e. $V_g = \frac{V}{n}$) then required series resistance $R = (n - 1) G$.

12.4 Wheatstone Bridge Principle

Wheatstone Bridge Principle states that if four resistances P , Q , R and S are arranged to form a bridge as shown in figure, if galvanometer shows no deflection, the bridge is balanced.

In that case

$$\frac{P}{Q} = \frac{R}{S}$$



Proof :

Let I be the total current given out by the cell. On reaching the point A, it is divided into two parts :

1. I_1 is flowing through P
2. $(I - I_1)$ through R.

At B, the current I_1 is divided into two parts, I_g through the galvanometer G and $(I_1 - I_g)$ through Q.

A current $(I - I_1 + I_g)$ through S.

Applying Kirchhoff's Second Law to the closed circuit ABDA, we get

$$I_1 P + I_g G - (I - I_1) R = 0 \quad \dots(1)$$

where G is the resistance of galvanometer.

Again applying Kirchhoff's Second Law to the closed circuit BCDB, we get

$$(I_1 - I_g) Q - (I - I_1 + I_g) S - I_g G = 0 \quad \dots(2)$$

The value of R is adjusted such that the galvanometer shows no deflection, i.e., $I_g = 0$. Now, the bridge is balanced. Putting $I_g = 0$ in (1) and (2) we have

$$I_1 P - (I - I_1) R = 0 \text{ or } I_1 P = (I - I_1) R \quad \dots(3)$$

$$\text{and } I_1 Q - (I - I_1) S = 0 \text{ or } I_1 Q = (I - I_1) S \quad \dots(4)$$

$$\text{Dividing (3) by (4), we get } \frac{P}{Q} = \frac{R}{S}$$

Note that in Wheatstone bridge circuit, arms AB and BC having resistances P and Q form ratio arm. The arm AD, having a resistance R , is a known variable resistance arm and arm DC, having a resistance S is unknown resistance arm.

- (i) **Balanced bridge :** The bridge is said to be balanced when deflection in galvanometer is zero i.e. no current flows

through the galvanometer or in other words $V_B = V_D$. In the

balanced condition $\frac{P}{Q} = \frac{R}{S}$, on mutually changing the

position of cell and galvanometer this condition will not change.

- (ii) **Unbalanced bridge :** If the bridge is not balanced current will flow from D to B if $V_D > V_B$ i.e. $(V_A - V_D) < (V_A - V_B)$ which gives $PS > RQ$.
- (iii) **Applications of wheatstone bridge :** Meter bridge, post office box and Carey Foster bridge are instruments based on the principle of wheatstone bridge and are used to measure unknown resistance.

12.5 Slide Wire Bridge or Meter Bridge

A slide wire bridge is a practical form of Wheatstone bridge.

It consists of a wire AC of constantan or manganin of 1 metre length and of uniform area of cross-section.

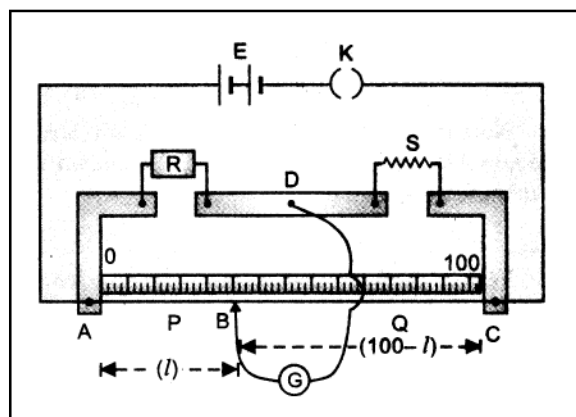
A meter scale is also fitted on the wooden board parallel to the length of the wire.

Copper strip fitted on the wooden board in order to provide two gaps in strips.

Across one gap, a resistance box R and in another gap the unknown resistance S are connected.

The positive pole of the battery E is connected to terminal A and the negative pole of the battery to terminal C through one way key K .

The circuit is now exactly the same as that of the Wheatstone bridge figure.



Adjust the position of jockey on the wire (say at B) where on pressing, galvanometer shows no deflection.

Note the length AB ($= l$ say) to the wire. Find the length BC ($= 100 - l$) of the wire.

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According to Wheatstone bridge principle

$$\frac{P}{Q} = \frac{R}{S}$$

If r is the resistance per cm length of wire, then

P = resistance of the length l of the wire $AB = lr$

Q = resistance of the length $(100-l)$ of the wire $BC = (100-l)r$.

$$\therefore \frac{\ell r}{(100-\ell)r} = \frac{R}{S} \text{ or } S = \left(\frac{100-\ell}{\ell} \right) \times R$$

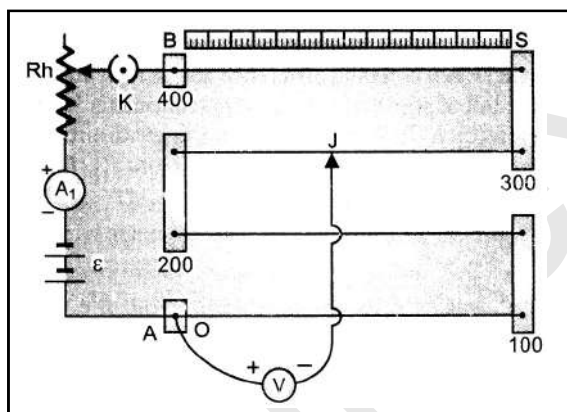
Knowing l and R , we can calculate S .

12.6 Potentiometer and its principle of working

Potentiometer is an apparatus used for measuring the emf of a cells or potential difference between two points in an electrical circuit accurately.

A potentiometer consists of a long uniform wire generally made of manganin or constantan, stretched on a wooden board.

Its ends are connected to the binding screws A and B. A meter scale is fixed on the board parallel to the length of the wire. The potentiometer is provided with a jockey J with the help of which, the contact can be made at any point on the wire, figure. A battery ε (called driving cell), connected across A and B sends the current through the wire which is kept constant by using a rheostat Rh.



Principle : The working of a potentiometer is based on the fact that the fall of potential across any portion of the wire is directly proportional to the length of that portion provided the wire is of uniform area of cross-section and a constant current is flowing through it.

Suppose A and ρ are respectively the area of cross-section and specific resistance of the material of the wire.

Let V be the potential difference across the portion of the wire of length l whose resistance is R .

If I is the current flowing through the wire, then from Ohm's law; $V = IR$; As, $R = \rho l/A$

$$\therefore V = I\rho \frac{\ell}{A} = K\ell, \quad \left(\text{where } K = \frac{I\rho}{A} \right)$$

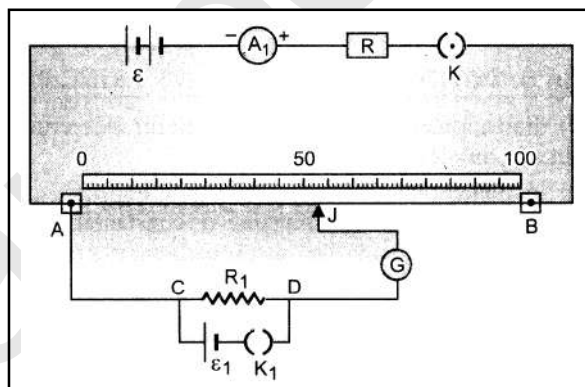
$$\text{or } V \propto l \quad (\text{if } I \text{ and } A \text{ are constant})$$

i.e., potential difference across any portion of potentiometer wire is directly proportional to length of the wire of that portion.

Here, $V/l = K$ is called potential gradient, i.e., the fall of potential per unit length of wire.

12.7 Determination of Potential Difference using Potentiometer

A battery of emf ε is connected between the end terminals A and B of potentiometer wire with ammeter A_1 , resistance box R and key K in series. This circuit is called an auxiliary circuit. The ends of resistance R_1 are connected to terminals A and Jockey J through galvanometer G . A cell ε_1 and key K_1 are connected across R_1 as shown in figure.



Working and Theory : Close key K and take out suitable resistance R from resistance box so that the fall of potential across the potentiometer wire is greater than the potential difference to be measured.

It can be checked by pressing, firstly the jockey J on potentiometer wire near end A and later on near end B, the deflections in galvanometer are in opposite directions.

Close key K_1 . The current flows through R_1 . A potential difference is developed across R_1 . Adjust the position of jockey on potentiometer wire where if pressed, the galvanometer shows no deflection. Let it be when jockey is at J . Note the length $AJ (= l)$ of potentiometer wire. This would happen when potential difference across R_1 is equal to the fall of potential across the potentiometer wire of length l . If K is the potential gradient of potentiometer wire, then potential difference across R_1 , i.e.,

$$V = Kl$$

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