

CHI-SQUARE TEST ASSIGNMENT

1. SAMPLE SIZE OF 1600 CARDS HAVING 4 diff. shapes.

so assuming they are equally present in the deck. $= 1600/4 = 400$ cards.

| | Expected | Observed | $\chi^2 (O-E)^2/E$ |
|----------|----------|----------|------------------------|
| Spades | 400 | 404 | $16/400 = 1/25 = 0.04$ |
| Hearts | 400 | 420 | $400/400 = 1$ |
| Diamonds | 400 | 400 | 0 |
| Clubs | 400 | 376 | $576/400 = 1.44$ |
| | | | <u>2.48</u> |

[Degrees of freedom are how many bins we create or groups we create out of the data]

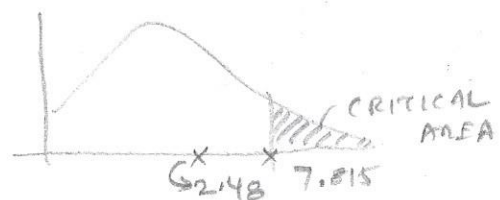
df = 4 for population
df = 4-1 for a sample size
= 3

lets assume CI for 95% CL
so lets get the critical value from the χ^2 table.

df: 3 and critical area 5% (0.05)

Probability of exceeding the critical value is 7.815.

so NULL HYPOTHESIS IS PROVED AS 2.48 is well within 7.815



NULL HYPOTHESIS: SUITS ARE EQUALLY LIKELY

ALTERNATIVE HYPOTH: HAVE DISCREPANCIES.

2. SAMPLE SIZE OF 1662 cards with 5 different types of cards. for a sample df = 5-1 = 4.

| | Expected | Observed | $\chi^2 (O-E)^2/E$ |
|----------|----------|----------|--------------------|
| SPADES | 400 | 404 | 0.04 |
| HEARTS | 400 | 420 | 1.0 |
| DIAMONDS | 400 | 400 | 0.0 |
| CLUBS | 400 | 356 | 4.84 |
| JOKERS | 62 | 82 | 6.45 |
| | | | <u>12.33</u> |

[Generally there are 2 cards for every JOKER 52 CARDS]

so for 1600 cards we can find

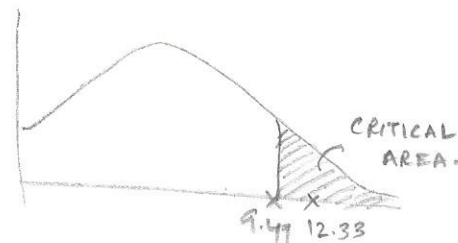
$$\frac{1600 \times 2}{52} = 62 \text{ (approx) Jokers}$$

Degrees of freedom = 5-1 = 4.

Assume critical region: 5% (0.05) Area = 9.49

NULL HYPOTHESIS IS REJECTED

ALTERNATE HYPOTHESIS IS TRUE: HAVE DISCREPANCIES-



CHI-SQUARE TEST

5. Alpha level $\alpha = 0.05$, confidence level = 95%.

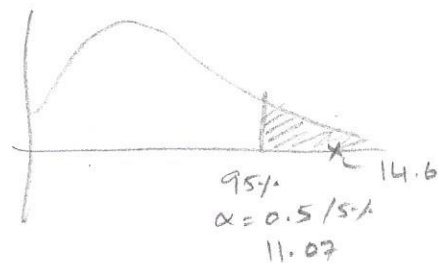
| Store | # Shoppers | Expected | χ^2 | | | |
|-------|------------|----------|-------------|---------------|------|------------|
| A | 262 | 220 | $220 - 262$ | $-42^2 / 220$ | 8.01 | Sum = 14.6 |
| B | 234 | 220 | $220 - 234$ | $-14^2 / 220$ | 0.89 | |
| C | 204 | 220 | $220 - 204$ | $16^2 / 220$ | 1.16 | |
| D | 190 | 220 | $220 - 190$ | $30^2 / 220$ | 4.09 | |
| E | 210 | 220 | $220 - 210$ | $10^2 / 220$ | 0.45 | |

[Observed: Users do not have a preference and so the expectation is they are equally distributed]

from the table we get $df = 5$, $\chi^2(0.05) = 11.07$

So it is under the tail so reject the NULL HYPOTHESIS.
and ACCEPT ALTERNATE HYPOTHESIS

Therefore there is no preference for shoppers.



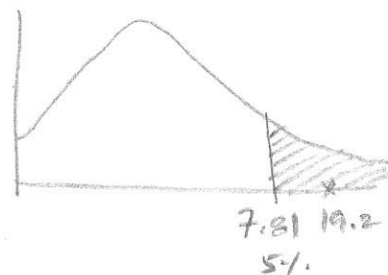
3. Tigris and cheetah cross. Results would be categorized as

| | Observed. | expected | χ^2 | |
|--------------------------|-----------|----------|------------------|-------------|
| 4 stripes only | 50 | 60 | $(50-60)^2 / 60$ | 1.66 |
| 3 spots only | 41 | 58 | $(41-58)^2 / 58$ | 4.98 |
| 9 both stripes and spots | 85 | 58 | $(85-58)^2 / 58$ | 12.56 |
| | | | | <u>19.2</u> |

Assumption: Let us consider the critical region of 5%
degrees of freedom $n = 3$ (whole population) and not sample.

NULL HYPOTHESIS: DID SHE GET PREDICTED OUTCOME

= FALSE \rightarrow It falls in the critical region



4.

| | COLOR | POD SHAPE | INFLATED | CONSTRICTED | |
|--------|-------------|-------------|----------|-------------|--|
| YELLOW | 556 (557.6) | 184 (182.4) | | 740 | |
| GREEN | 193 (191.4) | 61 (62.6) | | 254 | |
| | <u>749</u> | <u>245</u> | | <u>994</u> | |

$$\chi^2 = \frac{(556-557.6)^2}{557.6} + \frac{(184-182.4)^2}{182.4} + \frac{(193-191.4)^2}{191.4} + \frac{(61-62.6)^2}{62.6}$$

$$\chi^2 = 0.073 \text{ degree of freedom} = (r-1)(c-1) = (1 \times 1) = 1$$

From CHI-SQUARE TABLE $df = 1$ and 5% STATISTICAL SIGNIFICANCE = 3.84 / $0.073 < 3.84$

considering these categorical variables are independent [NULL HYPOTHESIS]

$$P(A \cap B) = P(A) \cdot P(B)$$

$$i.e. Y \cap Int = P(Ye) \cdot P(Int)$$

$$= \frac{240}{994} \cdot \frac{749}{994} = 0.561 \text{ per instance}$$

$$\text{for 994 instance} = 994 \times 0.561$$

$$\text{PROPORTION} = 557.6$$

SO NULL HYPOTHESIS IS TRUE
(INDEPENDENT)