

SupervisedLearning: DSVII End to End Data Science Course -Batch 7

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## **Central Limit Theroem Assignment**

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- 1. An officer in the army needs 35 men for a mission. He wants these soldiers to be smart enough to understand the details the mission so the average IQ score of the 35 men must be greater than 98 pt. It is known that average IQ of a soldier is 96 with a standard deviation of 16 points. If the officer is given a random sample of 35 soldiers for the mission, what is the probability that he will get what he wants.
- 2. Engineers must consider the breadths of male heads when designing motorcycle helmets. Men have head breadths that are normally distributed with a mean of 6.0 inch and a standard deviation of 1.0 inch.
- a. If one male is randomly selected, find the probability that his head breadth is less than 6.2 inch.
- b. Find the probability that 100 randomly selected men have a mean head breadth that is less than 6.2 in.
- c. A Production Manager for Safeguard Helmet Company plans an initial run of 100 helmets. Seeing the result from part(b), the manager reasons that all helmets should be made for men with head breadths less than 6.2 in., because they would fit all but a few men. What is wrong with that reasoning?
- 3. The lengths of pregnancies are normally distributed with a mean of 268 days and a standard deviation of 15 days. If 25 women are randomly selected, find the probability that their lengths of pregnancy have a mean that is less than 260 days. If 25 women are put on a special diet just before they become pregnant and they end up having a mean length of pregnancy of less than 260 days, does it appear that the diet has an effect on the length of pregnancy?

- 4. The weights of adult males are normally distributed with a mean of 172 pounds and a standard deviation of 29 pounds. Based on this info, solve the following problems:-
- a. What is the probability that one randomly selected adult male will weigh more than 190 pounds?
- b. What is the probability that 25 randomly selected adult males will have a mean weight of more than 190 pounds?
- c. An elevator at a men's fitness center has a sign that the maximum allowable weight is 4750 pounds. If 25 randomly selected men cram into the elevator, what is the probability it will be over the maximum allowable weight?
- 5. The amount of impurity in a batch of a chemical product is a random variable with a mean value 4.0 g and a standard deviation of 1.5 g. If 50 batched are independently prepared, what is the (approx) probability that the average amount of impurity in these 50 batches is between 3.5g and 3.8g?
- 6. You draw a random sample of size n = 64 from a population with mean  $\mu$  = 50 and standard deviation  $\sigma$  = 16. From this, you compute the sample mean, X $^-$ .
- a. What are the expectation and standard deviation of  $X^{-}$ ?
- b. Approximately what is the probability that the sample mean is above 54?
- c. Do you need any additional assumptions for part (b) to be true?
- 7. Suppose the age a student graduates from Salem State is Normally distributed. If the mean age is 23.1 years and the standard deviation is 3.1 years, what is the probability that 6 randomly selected students had a mean age at graduation that was greater than 27?
- 8. While checking receipts at Reds, it was determined that the average amount spent on food per table was \$21.50 with a standard deviation of \$2.22. If we can assume that the amount of money spent was Normally distributed, what is the probability that the average of 8 checks is between \$20 and \$23?
- 9. Suppose the grades in a finite mathematics class are Normally distributed with a mean of 75 and a standard deviation of 5.
- a. What is the probability that a randomly selected student had a grade of at least 83?

- b. What is the probability that the average grade for 5 randomly selected students was at least 83?
- 10. The average age of major league baseball players is 28.3 years and has a standard deviation of 2.3 years. If we can assume that ages are Normally distributed, what is the probability that the average age of 10 randomly selected Red Sox players is less than 27 years?

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