# Explainable AI: Learning Arguments

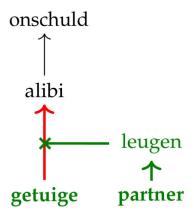
Jonas Bei, David Pomerenke, Sepideh Sharbaf, Lukas Schreiner Supervisors: Nico Roos & Pieter Collins



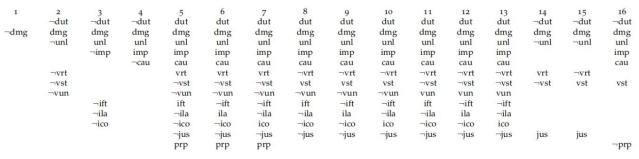
## Agenda

- Introduction
- Learning Arguments
- Discretization
- Experiments
- Future work
- Summary

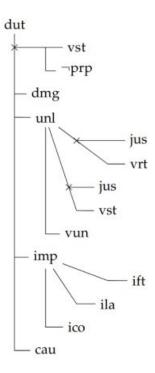
## Arguments



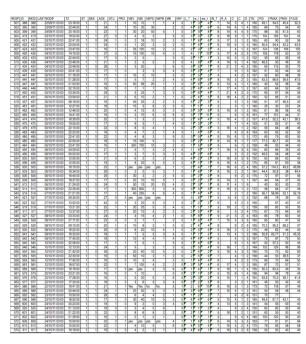
## Learning Arguments



 $1 > 2 > 3 > 4 > 5 \sim 6 \sim 7 \sim 8 \sim 9 \sim 10 \sim 11 \sim 12 \sim 13 > 14 \sim 15 \sim 16$ 

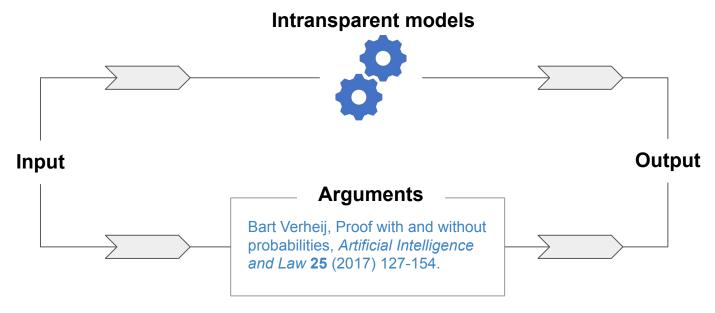


## Machine learning setting



- Prediction
- Categorization

## Explainable artificial intelligence



## Arguments in Verheij 2017

Coherent arguments:

Conclusion holds sometime when the premises hold.

• Presumptively valid arguments:

Conclusion holds in the most likely case where the premises hold.

Conclusive arguments:

Conclusion always holds when the premises hold.

## Research questions

- 1. Can we **reproduce** the examples from Verheij 2017 and Verheij 2020?
- 2. Can we **find an (efficient) algorithm** for learning arguments with this approach? How do we decide which arguments are relevant and which ones can be discarded?
- 3. Can we transfer the approach to a **general attribute-value classification** machine learning setting?
- 4. What **existing techniques** are there for learning arguments, and how do they relate to each other? What insights can we transfer to the implementation of the approach by Verheij 2017?
- 5. Can we show the (in)applicability of the approach on a real-world dataset?

  How does the approach compare with similar rule-based approaches in terms of
  (a) accuracy and (b) runtime on real world datasets?

  What can we infer about explainability by looking at the theories generated by the algorithms?

## Review of progress

Implementation

of Verheij's approach

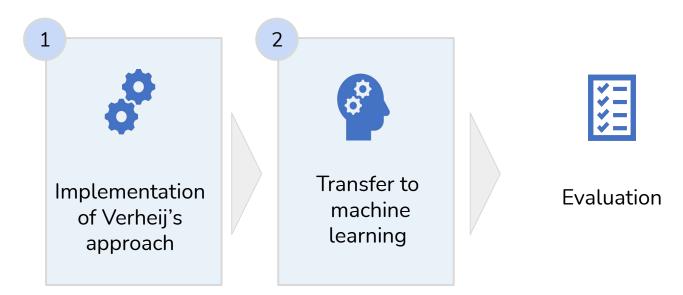


Transfer to machine learning

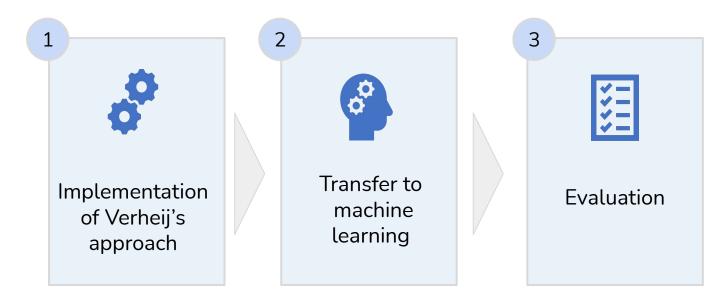


**Evaluation** 

## Review of progress



## Review of progress



- 1. Naive search
- 2. Pruned search
- 3. HeRO algorithm
- 4. Decision trees

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- 2. Pruned search
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Require categorical data

Require categorical data

- 1. Naive search
- 2. Pruned search
- 3. HeRO algorithm
- 4. Decision trees

Hyperparameter optimization

1. Enumerate all possible arguments:

 $\to \mathsf{C}$ 

 $a \rightarrow c$ 

 $\neg a \rightarrow c$ 

 $b \rightarrow c$ 

 $\neg b \rightarrow c$ 

a,  $b \rightarrow c$ 

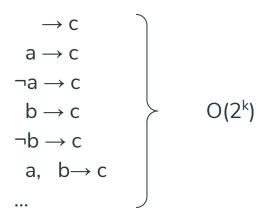
...

1. Enumerate all possible arguments:

$$\begin{array}{c} \rightarrow c \\ a \rightarrow c \\ \neg a \rightarrow c \\ b \rightarrow c \\ \neg b \rightarrow c \\ a, b \rightarrow c \\ ... \end{array}$$

2. Filtering irrelevant arguments

1. Enumerate all possible arguments:



2. Filtering irrelevant arguments

### Filtering irrelevant arguments

- Discard overly specific arguments
- Keep them if they are an exception
- Merge arguments with identical premises
- Eliminate arguments that do not affect the closure of arguments

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 $b \rightarrow c$   
 $a \rightarrow c$ 

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$$a \rightarrow b$$
  
 $b \rightarrow c$   
 $a \rightarrow c$   
 $a \rightarrow b$   
 $b \rightarrow c$   
 $a \rightarrow c$   
 $a \rightarrow c$   
 $a \wedge b \rightarrow \neg c$ 

```
case_model = CaseModel.fromStr([
          (3, 'inn, ¬gui, ¬evi'),
          (2, "¬inn, gui, evi, ¬evi'"),
          (1, "inn, ¬gui, evi, ¬evi'"),
          (0, "¬inn, gui, evi, evi'"),
])
```



```
evi ← ¬evi'
evi ∧ gui ← ¬inn
evi ∧ gui ∧ ¬inn ← evi'
evi ∧ ¬inn ← gui
inn ← ¬gui
inn ∧ ¬gui ← ¬evi
¬evi' ← evi ∧ inn
¬evi' ← evi ∧ ¬gui
¬gui ← inn
gui ∧ ¬evi' ∧ ¬inn ← evi
gui ∧ ¬inn ← evi ∧ ¬evi'
gui ∧ ¬inn ← ¬evi'
inn ∧ ¬evi ∧ ¬gui ←
¬evi' ← gui
¬evi' ← ¬inn
```

### **Observations:**

(A, B) coherent

 $\Rightarrow$ 

(S, B) coherent for all  $S \subseteq A$ 

(A, B) conclusive

 $\Rightarrow$ 

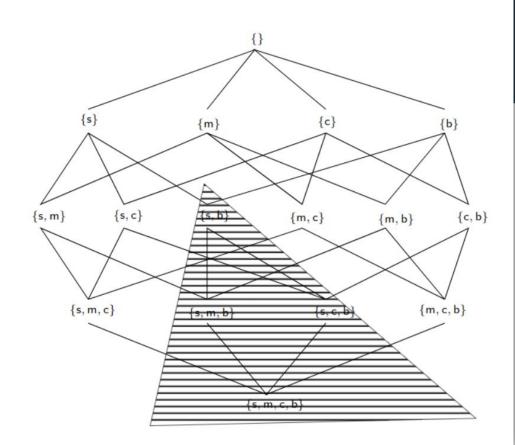
(S, B) conclusive for all  $S \supseteq A$ where (S, B) is coherent

### **Observations:**

(A, B) coherent

 $\Rightarrow$ 

(S, B) coherent for all  $S \subseteq A$ 



```
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             , age
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                           ,1 ,296 ,15.3
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                                             .396.9 .9.14 .21.6
      ,7.185 ,61.1 ,4.9671 ,2 ,242 ,17.8
                                             ,392.83 ,4.03 ,34.7
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                                             ,390.5 ,15.71 ,21.7
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       5.57 98.1 3.7979
                                .307 21
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niign_rau <- niign_istat \ niign_meuv \ niign_ptratio \ niign_tax

niigh_tax <- high_b \ high_ptratio \ nigh_rad \ nhigh_lstat \ nhigh_medv

niigh_tax <- high_b \ high_ptratio \ n-high_lstat \ n-high_medv

niigh_tax <- high_b \ high_ptratio \ n-high_lstat \ n-high_medv \ n-high_rad

niigh_tax <- high_lstat \ high_medv \ n-high_ptratio \ n-high_b \ n-high_ptratio

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```

#### Parameters:

- maximum size of premises
- maximum depth of exceptions

## An algorithm for the induction of defeasible logic theories from databases

## HeRO algorithm 🚜



Incremental approach

- Information gain
- Maximum information gain

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#### Abstract

Defeasible logic is a non-monotonic logic with applications in rule-based domains such as law. To ease the development and improve the accuracy of expert systems based on defeasible logic, it is desirable to automatically induce a theory of the logic from a training set of precedent data. Empirical evidence suggests that minimal theories that describe the training set tend to be more faithful representations of reality. We show via transformation from the hitting set problem that this global minimization problem is intractable, belonging to the class of NP optimisation problems. Given the inherent difficulty of finding the optimal solution, we instead use heuristics and demonstrate that a best-first, greedy, branch and bound algorithm can be used to find good theories in short time. This approach displays significant improvements in both accuracy and theory size as compared to recent work in the area that post-processed the output of an Apriori association rule-mining algorithm, with comparable execution times.

Keywords: Defeasible Logic, Machine Learning, Association Rules

#### 1 Introduction

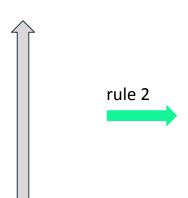
Expert and decision support systems are slowly making inroads into the legal community, but unfortunately they currently appear to be limited in terms of either the difficulty of their construction or their inability to justify their reasoning processes to the user. Existing systems could be roughly classified into two broad categories: expert systems that are constructed by manual encoding of knowledge (Zeleznikow & Hunter 1994), and classification tools that are automatically trained from precedent data using machine learning or data mining techniques (Zeleznikow & Stranieri 1997, Brüninghaus & Ashlev 1999). Unsurprisingly, the expense involved in employing human experts and the difficulty that experts have in expressing the reasoning behind their "intuition" can eliminate the option of building expert systems in spite expert systems, but facilitating construction via automatic induction.

Recent work in the field of non-monotonic logics suggests the suitability of the formalism as an underlying model for such reasoning, that turns out (as we will show) to be conducive to automatic induction. Non-monotonic logics, such as defeasible logic. were originally developed to simplify reasoning with incomplete information (Ginsberg 1993). In contrast to monotonic logics whereby a conclusion of a theory remains valid irrespective of how many assertions are added to the theory, non-monotonic logics can reach tentative conclusions that may be overridden (and replaced with a contrary conclusion) in light of additional information. Defeasible logic is one of many non-monotonic logics in use, but is particularly desirable for use in information systems because it matches the non-monotonicity of legal reasoning and is computationally efficient without sacrificing too much expressiveness. The extension of a defeasible logic theory has been shown to be computable in linear time (Antoniou, Billington, Governatori & Maher 2001. Maher 2001), as opposed to the NP-hardness or even undecidability of most non-monotonic and monotonic logics (Prakken 1997, Ginsberg 1993). While some expressiveness is sacrificed in using defeasible logic over first order logic, it still remains quite suited to legal domains. Antoniou et al (1999) have demonstrated the extremely high correspondence between regulatory documents and their equivalent expression as defeasible logic theories, in some cases the correspondence is almost 1-1 between sentences in legal documents and logical rules.

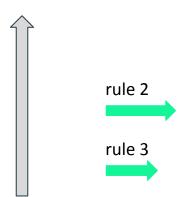
#### 2 Defeasible Logic

In this section we will present a formal explanation of defeasible logic. Because we are focusing our attention to a specific application of defeasible logic, for simplicity our terminology slightly devi-

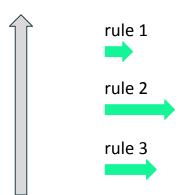






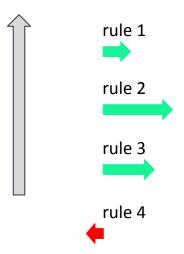




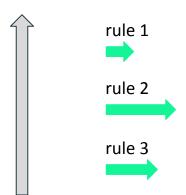


# HeRO algorithm 🚜





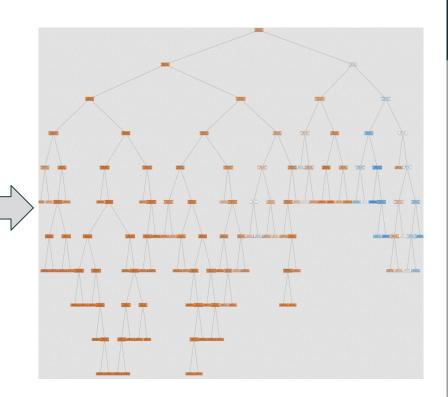


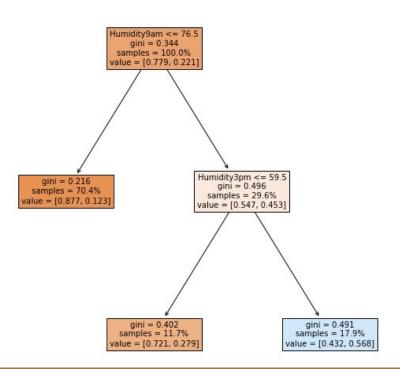


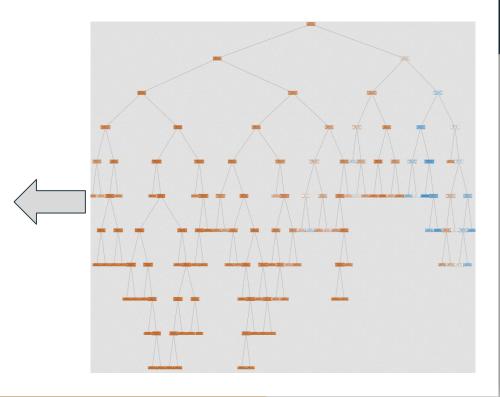
- Efficient on large data sets
- Entropy-based discretization
- Small number of arguments thanks to pruning
- No exceptions

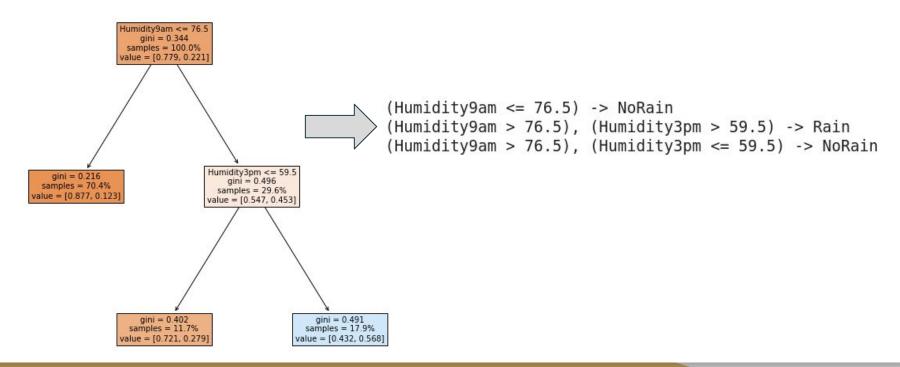
	MinTemp	MaxTemp	Evaporation	Sunshine	WindGustSpeed	WindSpeed9am	WindSpeed3pm	Humidity
6049	17.9	35.2	12.0	12.3	48.0	6.0	20.0	2
6050	18.4	28.9	14.8	13.0	37.0	19.0	19.0	3
5555								
6052	19.4	37.6	10.8	10.6	46.0	30.0	15.0	4
6053	21.9	38.4	11.4	12.2	31.0	6.0	6.0	3
6054	24.2	41.0	11.2	8.4	35.0	17.0	13.0	1
142298	19.3	33.4	6.0	11.0	35.0	9.0	20.0	6
142299	21.2	32.6	7.6	8.6	37.0	13.0	11.0	5
142300	20.7	32.8	5.6	11.0	33.0	17.0	11.0	4
142301	19.5	31.8	6.2	10.6	26.0	9.0	17.0	6
142302	20.2	31.7	5.6	10.7	30.0	15.0	7.0	7

56420 rows × 92 columns



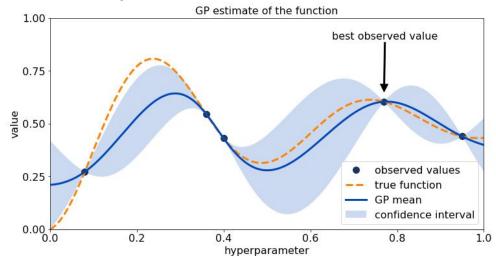


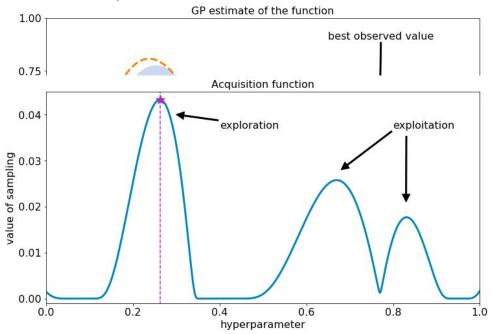


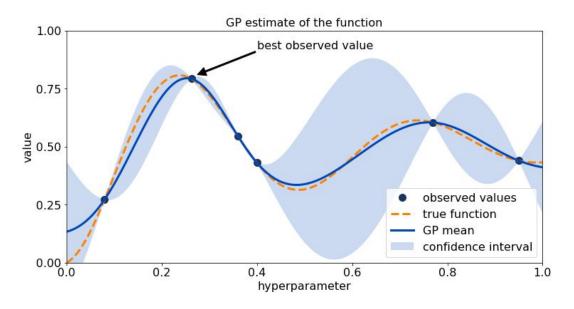




- Sampled points are used to estimate the objective function (prior)
- Points are sampled using an acquisition function and the prior is updated
  - Acquisition function balances exploration & exploitation via uncertainty in the prior
- Prior is updated
- After a given number of iterations, use a numerical method to find the estimated optimum



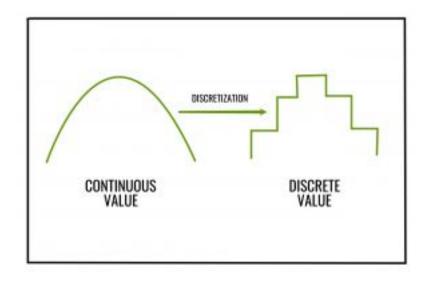


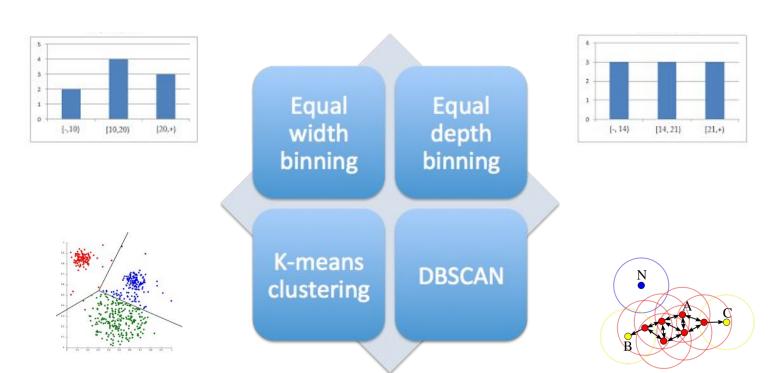


## Discretization Algorithms

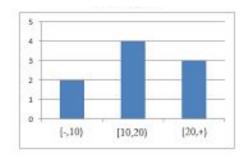
## Techniques used

With the exception of decision trees, the rule-mining algorithms cannot be trained on continuous data. Therefore, in order to apply the rule-mining algorithms to datasets, we must rely on data discretization techniques to preprocess the data before mining the rules.



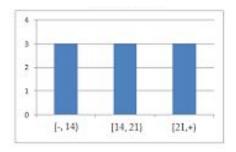


## **Equal Width Binning**



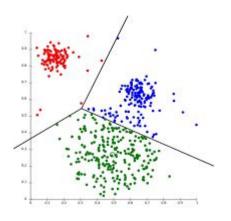
- This algorithm is a comparatively simple binning technique.
- Assuming each cluster, same diameter, each of bins have size max-min/K.
- To discretize, values are assigned to the respective bin they fall into.

## **Equal Depth Binning**



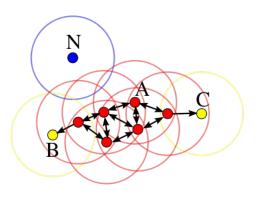
- Equal-depth or equal-frequency binning is another simple discretization approach.
- Each bin approximately holds the same number of instances.
- This is done by sorting the values of the feature.

### k-means



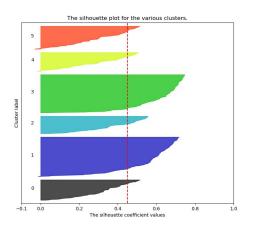
- K-Means is based on the idea of centroids, which are points in the centre of the cluster.
- K centroids are initialized randomly, and the instances are assigned to the cluster whose centroid is closest.
- The algorithm converges when the movement of centroids is below a certain threshold.
- Quite fast, sensitive to outliers

### **DBSCAN**



- DBSCAN considers clusters to be regions of high density.
- For each instance, the algorithm counts the number of instances within a distance  $\varepsilon$ , also called the instance's  $\varepsilon$ -neighbourhood.
- The neighbours of this core instance are considered to be in the same cluster, where some neighbours may also be core instances themselves.
- A cluster consists of a multitude of core instances.

## Cluster Optimization: Silhouette score



- The silhouette score has been utilized to provide a metric for accuracy of clusters in this project.
- This score computes the mean silhouette coefficient of all samples.

#### silhouette\_score=b-a/max(a,b)

 Clusters are optimized by exhaustive search this project, i.e., every combination of parameters is tested using the silhouette score, before returning the parameters resulting in the highest score.

## Set Up

- 1 Discretize the Data
  - Equal Width
  - Equal Depth
  - k-Means
  - DBSCAN

- 2 Learning Arguments
  - Pruned Search
  - Decision Trees
  - HeRO Algorithm

- 3 Make Predictions
  - Test Set
  - Training Set

- 4 Evaluate
  - Accuracy
  - F1 Score

- Hyperparamter
  - Algorithm Type
  - No. Bins (optional)

- Search Depth
- Max Premises

## **Evaluation Pruned Search**

n=198	Acc	F1	No	o. bins	Depth	Runtime	Max premises
Acc	1,000	)					
F1	0,940	) 1,	000				
No. bins	-0,008	3 0,	057	1,000	)		
Depth	0,000	0,	000	0,000	1,000		
Runtime	-0,173	-0,	001	0,170	0,035	1,000	)
Max premises	0,000	0,	000			0,207	1,000

 Depth and Premise constraint do not affect precision

 Algorithms with higher accuracy have lower the runtime

### **Evaluation Decision Trees and HeRO**

#### **Decision Trees**

- Very high accuracy and F1 score for all discretization techniques
- Reasonable runtime in comparison
- Work as well with undiscretized input data

#### HeRO

- Performance strongly depends on the discretization technique.
   Accuracy varies from 0.5 to 0.97
- Very high variations in runtime.
   Some configurations were 30x
   times slower
- Still has potential for improvements

## Discussion

#### **Evaluation**

- Accuracy does not draw a complete picture because of explainability also matters
- Number of bins has a tremendous impact on the difficulty of the problem (e.g. no. bins=1)

Future Work: Measure explainability of the algorithm

#### **Runtime**

- Runtime increases exponentially in search and discretization algorithms
- Experiments were run on reduced data sets
- Needs improvement before becoming applicable

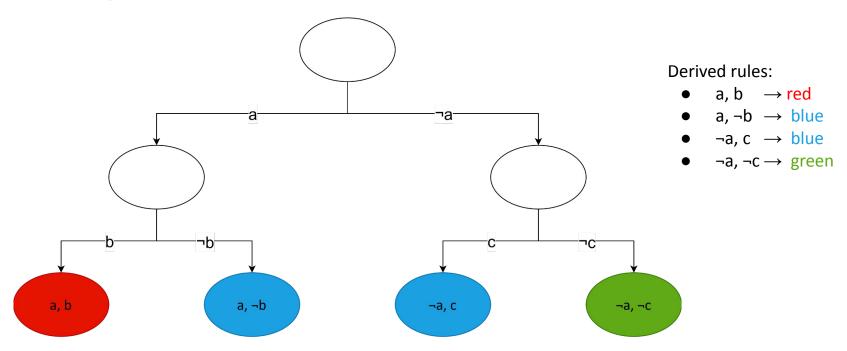
Future Work: Measure explainability of the algorithm

## Future Work

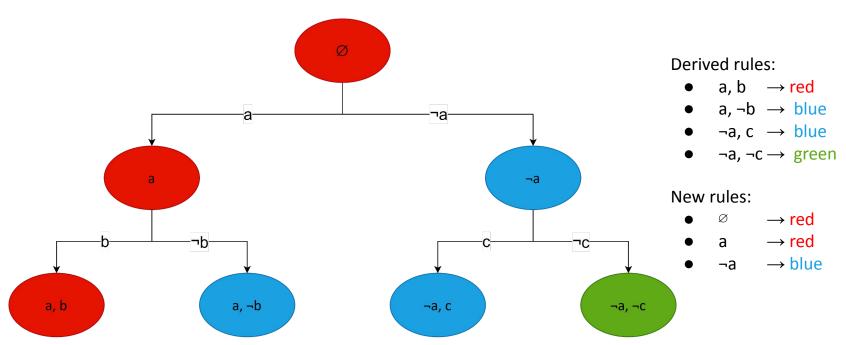
### Future Work

- Arguments with Exceptions for Decision Tree Rule-Mining
  - Derive arguments with exceptions from decision trees
  - Form arguments with exceptions, which allows prediction on incomplete data
- Optimizing Discretization
  - Choosing the columns to be discretized by selecting columns containing numerical values

## Arguments with exceptions from decision trees



## Arguments with exceptions from decision trees



# Arguments with exceptions from decision trees: Some rules imply others!

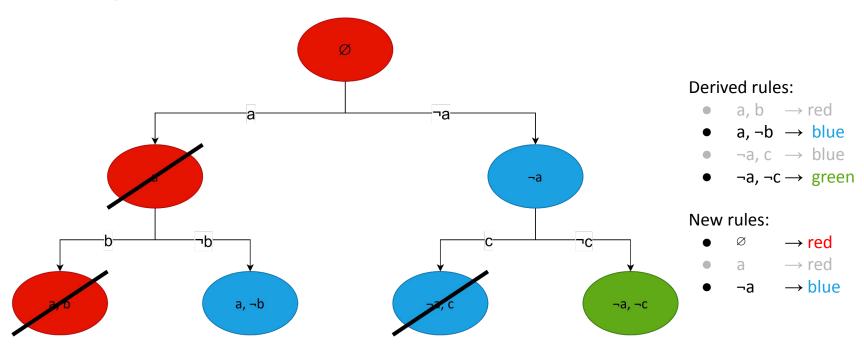
```
\varnothing \to \text{red} implies a, b \to \text{red} \neg a \to \text{blue} implies \neg a, c \to \text{blue}
```

If rule a implies rule b:

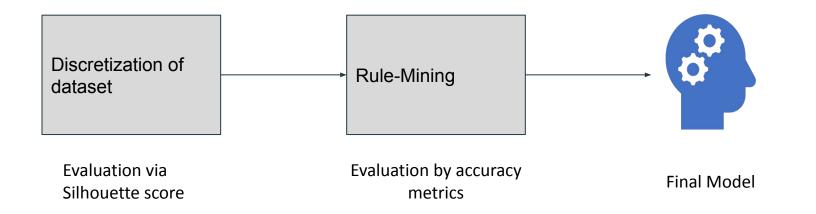
- The premises of rules a are a subset of the premises of rule b
- The conclusions of rule a and b are the same

Since these cases are covered by the less specific rules, we can prune rules that are implied.

## Arguments with exceptions from decision trees



# Merging discretization and rule-mining into one classifier



# Merging discretization and rule-mining into one classifier

Discretization +
Rule-Mining

Optimization of all parameters

- Parameters are combined from both techniques
- Can entail techniques used

Final Model

## Possible problem with the merge

- Target feature is not taken into account for discretization
- Instead, discretization will aim to maximize clustering metrics by design
- Improvement may be negligible

## Conclusion

## **Project Conclusion**

- 1. Examples from Verheij are implemented and replicated
- 2. Four different algorithms for learning arguments have been investigated:
  - Naive Search
  - Pruned Search
  - HerO
  - Decision Tree
- 3. The approach has been transferred to an attribute-value dataset:
  - Equal-Width Binning
  - Equal-Depth Binning
  - K-Means Clustering
  - DBSCAN Clustering

## **Project Conclusion**

- 4. We have given a survey over existing techniques for mining rules and arguments. We have applied ideas from logical learning and from the Apriori algorithm. We have implemented the HeRO algorithm. We also sketched an algorithm that allows learning arguments from decision trees
- 5. Applicability of the algorithms has been shown by experimentation

Thank you! Questions?

Bart Verheij. 'Proof with and without Probabilities'. Artificial Intelligence and Law 25, no. 1 (2017): 127–54.

Bart Verheij. 'Arguments for Good Artificial Intelligence'. Inaugural lecture. Groningen: University of Groningen, 2018.

Benjamin Johnston and Guido Governatori. 'An Algorithm for the Induction of Defeasible Logic Theories from Databases'. In *Proceedings of the 14th Australasian Database Conference-Volume 17*, 75–83, 2003.

## Appendix

# What specific algorithms are used in Bayesian Optimization?

- To create the prior: Kriging/Gaussian process regression
- For the acquisition function: Probabilistically, one of the following functions are chosen:
  - Lower confidence bound
  - Negative expected improvement
  - Negative probability of improvement
- An unknown numerical approach is used to find the optimum of the prior (not in documentation)

	Verheij 2017	Naive search	Pruned search	HeRO
	inn ↔	inn ∧ ¬gui ↔	inn ∧ ¬gui ↔	inn ∧ ¬gui ∧evi ↔
1 ∣ inn, ¬gui	¬gui ← inn		¬gui ← inn	
0 ¬inn, gui, evi			gui ← ¬inn	
o   min, gui, evi			evi ∧ gui ← ¬inn	
(a) Case model			evi ∧ ¬inn ← gui	
	gui ← evi		gui ∧ ¬inn ← evi	gui ∧ ¬inn ← evi

(b) Learned arguments

Figure 5.1: Learning arguments in case model 1 from Verheij (2017): Presumption of innocence.

2	a	b	C	y
1	a	b	¬с	¬у
0	a	¬b	¬с	У

Manual	Naive search	Pruned search	HeRO
y ←~	y <b>←</b> ~	y <b>←</b> ~	y <b>←</b> ~
		y ← c	
$\neg y \leftrightarrow \neg c$		¬y - ~ ¬c	99
		$\neg y \leftarrow b \land \neg c$	$\neg y \leftrightarrow b \land \neg c$
		¬y ← a ∧ ¬c	
y ← ¬b		y ← ¬b	

(b) Learned arguments

Figure 5.2: Learning arguments in case model 1 from Verheij (2017): Presumption of innocence.