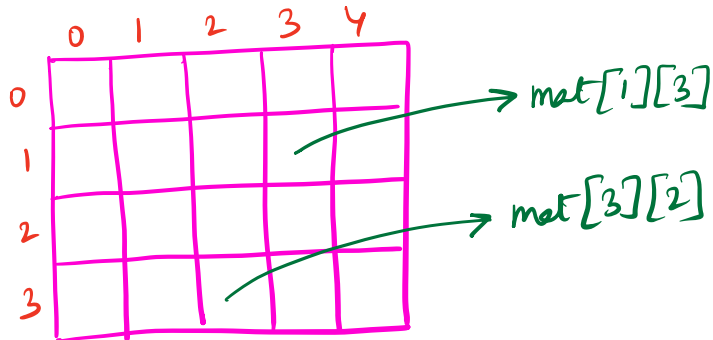


There are no big problems, there are
just a lot of little problems.

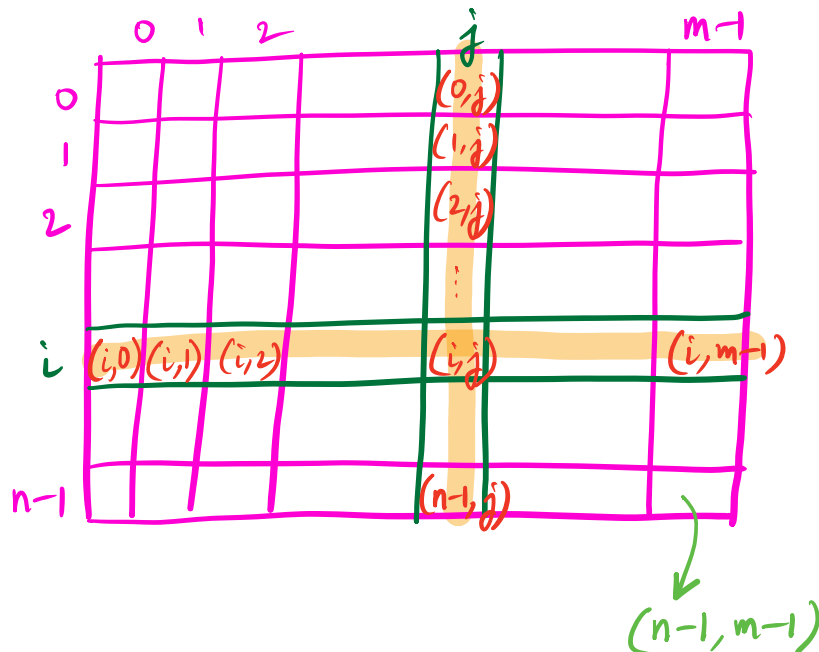
— Henry Ford

2-D Matrix Basics

`int mat[][] = new int [4][5]`
↑ rows
↓ columns



`int mat[n][m]`



Obs:-

- 1) If we iterate in a row, (L→R), the col. no. changes from 0 to m-1
- 2) If we iterate in a column, (T→B), the row no. changes from 0 to n-1

Q1) Given $mat[n][m]$, print row wise sum

Output

	0	1	2	3	
0	4	3	1	2	→ 10
1	8	7	2	9	→ 26
2	2	6	5	14	→ 27

T.C. → $O(n*m)$
S.C. → $O(1)$

We can't do better.

```
void row_sum(int mat[][]) {  
    int n = mat.length;  
    int m = mat[0].length;  
    // visit every row  
    for (i = 0; i < n; i++) {  
        int sum = 0;  
        // find sum for ith row  
        for (j = 0; j < m; j++) {  
            sum += mat[i][j];  
        }  
        print(sum)  
    }  
}
```

Q2) Given $mat[n][m]$, print column wise sum

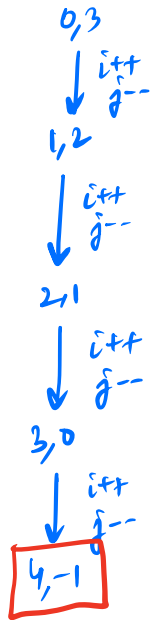
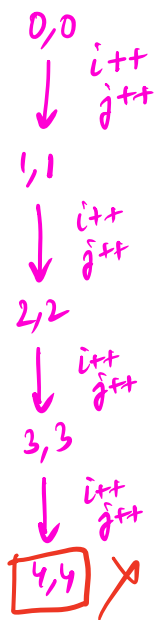
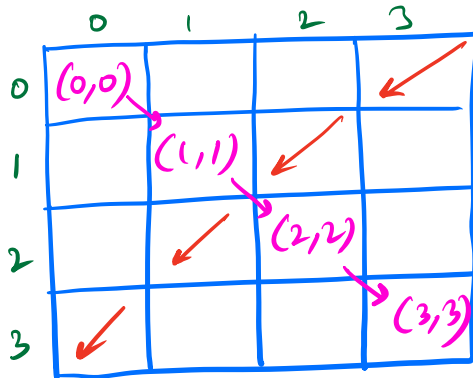
	0	1	2	3	
0	4	3	1	2	
1	8	7	2	9	
2	2	6	5	14	
	↓	↓	↓	↓	
	14	16	8	25	

H/W Todo.

Q3) Given square matrix $mat[n][n]$, print two diagonals

1) Top left to Bottom right

2) Top right to Bottom Left



```
i=0, j=0;
while (i < n && j < n) {
    print(mat[i][j]);
```

```
    i++;
    j++;
}
```

```
i=0, j=n-1;
while (i < n && j >= 0) {
    print(mat[i][j]);
```

```
    i++;
    j--;
}
```

Q4) Given a $mat[n][m]$, print all diagonals going from R \rightarrow L, starting from 0th row, 0th column.

	0	1	2	3	4
0					
1					
2					
3					

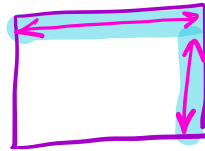
```

i = ?, j = ?
while (i < n & j >= 0) {
    print(mat[i][j]);
    i++;
    j--;
}

```

starting points

$(0,0)$ $(1,4)$
 $(0,1)$ $(2,4)$
 $(0,2)$ $(3,4)$
 $(0,3)$
 $(0,4)$



$(0,j)$ for every
 $j \in [0, m-1]$

$(i, m-1)$ for every
 $i \in [1, n-1]$

\rightarrow First print all diagonals starting at 0th row
 $(0,0) \rightarrow (0,1) \rightarrow (0,2) \rightarrow \dots \rightarrow (0,m-1)$

\rightarrow Print all the diagonals starting at $(m-1)$ th column.

```

void printAllDiagonals(int mat[], n, m) {
    for(int c=0; c<m; c++) {
        int i=0, j=c;
        while(i<n && j>=0) {
            print(mat[i][j]);
            i++;
            j--;
        }
    }
}

```

$O(nm)$ $\leq n$ times

```

    for(int r=1; r<n; r++) {
        int i=r, j=m-1;
        while(i<n && j>=0) {
            print(mat[i][j]);
            i++;
            j--;
        }
    }
}

```

$O(nm)$ $\leq m$ times

$O(nm)$ T.C.

$O(1)$ S.C.

[Break till 11:00 PM]

Q5) Given a matrix $mat[N][N]$, convert it to its transpose.
[O(1) space]

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

A



	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

A^T

$$A[i][j] = A^T[j][i]$$

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

swap (i, j) with (j, i)

```

for (i=0; i<n; i++) {
    for (j=0; j<i; j++) {
        int temp = mat[i][j];
        mat[i][j] = mat[j][i];
        mat[j][i] = temp;
    }
}

```

	0	1	2
0	1	4	3
1	2	5	6
2	7	8	9

$(0,1) \leftrightarrow (1,0)$
 $(1,0) \leftrightarrow (0,1)$

no net change.

Q.6) Given a matrix $mat[n][n]$, rotate it 90° clockwise.

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

90° clockwise
rotation

	0	1	2	3	4
0	21	16	11	6	1
1	22	17	12	7	2
2	23	18	13	8	3
3	24	19	14	9	4
4	25	20	15	10	5

Transpose

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

Reverse
each
row!

	0	1	2	3	4
0	21	16	11	6	1
1	22	17	12	7	2
2	23	18	13	8	3
3	24	19	14	9	4
4	25	20	15	10	5

Matrix $\xrightarrow{\text{Transpose}}$ $\xrightarrow{\text{Reverse every row}}$ 90° clockwise rotated matrix

Todo :- Code

Doubts

