

Proof:

By the definition of limit, given

Then

$$(\forall \epsilon > 0)(\exists n \in \mathcal{Z})(m \geq n) |a_n - L| < \epsilon$$

Since $M \geq 0$

So

$$(\forall M\epsilon > 0)(\exists n \in \mathcal{Z})(m \geq n) |Ma_n - ML| < M\epsilon$$

By the definition of limit, this proves the result.