

Proof: By Induction

For $n = 1$, left side is 2, and right side is $4 - 2 = 2$, so the identity is valid for $n = 1$.

Assume the identity holds for n . Then:

Let left side be $L(n)$.

$$\begin{aligned} L(n) &= 2 + 2^1 + \dots + 2^{n+1} \\ &= 2^{n+1} - 2 + 2^{n+1} \text{ (By Induction hypothesis)} \\ &= 2^{n+2} - 2 \end{aligned}$$

which is the identity for $n + 1$. The proof is complete.