Show all work and make sure to give exact answers. Good luck, and enjoy your weekend!

For all problems let \mathcal{R} be the region bound by $y = x^2$ and y = x.

1. (5 points) Find the area of \mathcal{R} .

2. (5 points) Find the volume of the solid obtained by revolving \mathcal{R} around y = -1.

3. (5 points) Find the volume of the solid obtained by revolving \mathcal{R} around the y-axis.

4. (5 points) Let \mathcal{R} be the base of a solid. Cross-sections perpendicular to the x-axis are squares. Find the the volume of this solid.