tkz-euclide examples

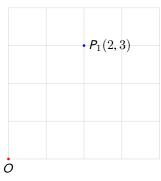
This lowly sand that your trample underfoot, if you throw it in a furnace and let it melt and seethe, will become a sparkling crystal; and thanks to such as this a Galileo or Newton will discover the stars.

Victor Hugo, Les Misérables

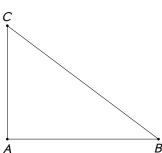
1 Points

1.1 Fixed Points

1.1.1 Cartesian Coordinates: (x, y)

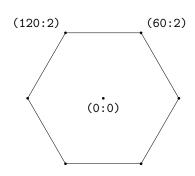


```
\begin{tikzpicture}
  \tkzInit[xmax=4,ymax=4]
  \tkzGrid[color=gray!30]
  \tkzDefPoint(0,0){0}
  \tkzDrawPoint[red](0)
  \tkzDefPoint(2,3){P1}
  \tkzDrawPoint[blue](P1)
  \tkzLabelPoint[right](P1){$P_1(2,3)$}
  \tkzLabelPoints[below](0)
  \end{tikzpicture}
```



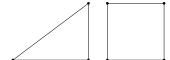
\begin{tikzpicture}
 \tkzDefPoint(0,0){A}
 \tkzDefPoint(4,0){B}
 \tkzDefPoint(0,3){C}
 \tkzDrawPolygon(A,B,C)
 \tkzDrawPoints(A,B,C)
 \tkzLabelPoints[below](A,B)
 \tkzLabelPoints[above](C)

1.1.2 Polar Coordinates: (degree:radius)



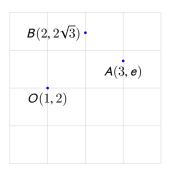
```
\begin{tikzpicture}
  \tkzDefPoint(0:0){0}
  \tkzDefPoint(60:2){A_1} \tkzDefPoint(120:2){A_2}
  \tkzDefPoint(180:2){A_3} \tkzDefPoint(240:2){A_4}
  \tkzDefPoint(300:2){A_5} \tkzDefPoint(360:2){A_6}
  \tkzDrawPolygon(A_1,A_...,A_6)
  \tkzDrawPoints(A_1,A_...,A_6,0)
  \tkzLabelPoint[above right](A_1){\texttt{(60:2)}}
  \tkzLabelPoint[above left](A_2){\texttt{(120:2)}}
  \tkzLabelPoint[below](0){\texttt{(0:0)}}
}
```

1.1.3 Multiple Points: \tkzDefPoints



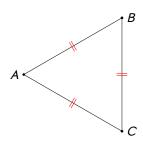
\begin{tikzpicture}[scale=1]
 \tkzDefPoints{0/0/A,2/0/B,2/1.5/C}
 \tkzDrawPolygon(A,B,C)
 \tkzDrawPoints(A,B,C)
 \tkzDefPoints{2.5/0/A,4/0/B,4/1.5/C,2.5/1.5/D}
 \tkzDrawPolygon(A,...,D)
 \tkzDrawPoints(A,B,C,D)
 \end{tikzpicture}

1.2 Calculations: xfp



\begin{tikzpicture}
 \tkzInit[xmax=4,ymax=4] \tkzGrid[color=gray!30]
 \tkzDefPoint(-1+2,sqrt(4)){0}
 \tkzDefPoint({3*ln(exp(1))},{exp(1)}){A}
 \tkzDefPoint({4*sin(pi/6)},{4*cos(pi/6)}){B}
 \tkzDrawPoints[color=blue](0,B,A)
 \tkzLabelPoint[below](0){\$0(1,2)\$}
 \tkzLabelPoint[below](A){\$A(3,e)\$}
 \tkzLabelPoint[left](B){\$B(2,2\sqrt{3})\$}
 \end{tikzpicture}

1.3 Point Relative to Another: \tkzDefShiftPoint

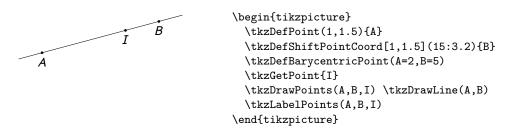


\begin{tikzpicture}[scale=1]
 \tkzDefPoint(2,3){A}
 \tkzDefShiftPoint[A](30:3){B}
 \tkzDefShiftPoint[A]({3/2*sqrt(3)},-1.5){C}
 \tkzDrawPolygon(A,B,C)
 \tkzDrawPoints(A,B,C)
 \tkzLabelPoints[right](B,C)
 \tkzLabelPoints[left](A)
 \tkzMarkSegments[mark=||,color=red](A,B,A,C,B,C)
 \end{tikzpicture}

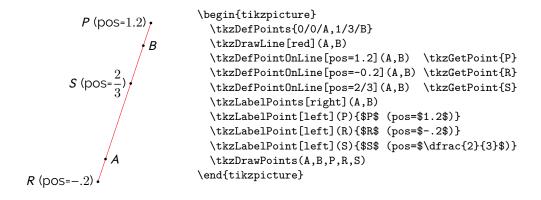
1.4 Midpoint: \tkzDefMidPoint



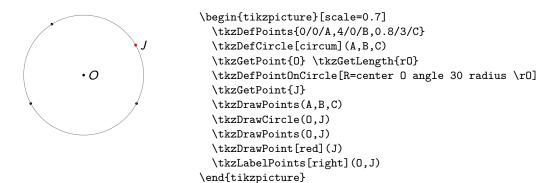
1.5 Barycenter: \tkzDefBarycentricPoint



1.6 Point on a Line: \tkzDefPointOnLine

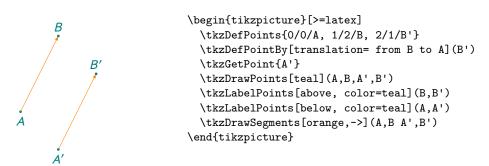


1.7 Point on a Circle: \tkzDefPointOnCircle

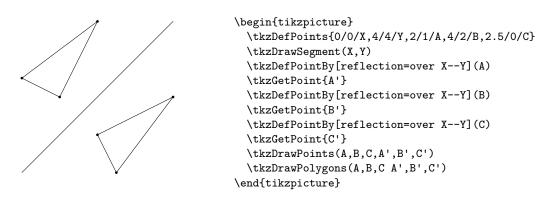


1.8 Transformations: \tkzDefPointBy

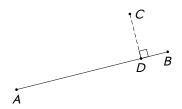
1.8.1 Translation



1.8.2 Reflection

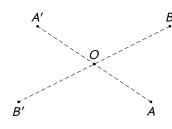


1.8.3 Projection



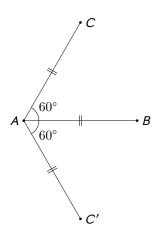
```
\begin{tikzpicture}
  \tkzDefPoints{0/0/A,4/1/B,3/2/C}
  \tkzDrawSegment(A,B)
  \tkzDefPointBy[projection=onto A--B](C)
  \tkzGetPoint{D}
  \tkzDrawPoints(A,B,C,D)
  \tkzDrawSegment[densely dashed](C,D)
  \tkzMarkRightAngle[size=.2](B,D,C)
  \tkzLabelPoints(A,B,D)
  \tkzLabelPoints[right](C)
\end{tikzpicture}
```

1.8.4 Symmetry



```
\begin{tikzpicture}[scale=1]
  \tkzDefPoint(0,0){0}
  \tkzDefPoint(1.5,-1){A}
  \tkzDefPoint(2,1){B}
  \tkzDefPointsBy[symmetry=center 0](B,A){}
  \tkzDrawSegments[densely dashed](A,A' B,B')
  \tkzDrawPoints(A,B,0,A',B')
  \tkzLabelPoints[below](A,B')
  \tkzLabelPoints[above](A',0,B)
  \end{tikzpicture}
```

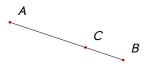
1.8.5 Rotation and Rotation in Rad



```
\begin{tikzpicture}
  \tkzDefPoint["$A$" left](0,0){A}
  \tkzDefPoint["$B$" right](3,0){B}
  \tkzDefPointBy[rotation=center A angle 60](B)
  \tkzGetPoint{C}
  \tkzDefPointBy[rotation in rad=center A angle -
pi/3](B)
  \tkzGetPoint{C'}
  \tkzLabelPoints[right](C,C')
  \tkzDrawPoints(A,B,C,C')
  \tkzDrawSegments(A,B A,C A,C')
  \tkzMarkAngles[mark=none, size=0.4cm](B,A,C C',A,B)
  \tkzLabelAngles[pos=0.75](B,A,C C',A,B){$60\degree$}
  \tkzMarkSegments[mark=||](A,B A,C A,C')
  \end{tikzpicture}
```

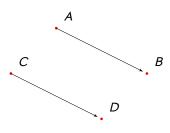
1.9 Defining Points Using a Vector: \tkzDefPointWith

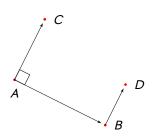
1.9.1 Linear



\begin{tikzpicture}
 \tkzDefPoint(1,3){A}
 \tkzDefPoint(4,2){B}
 \tkzDefPointWith[linear,K=2/3](A,B)
 \tkzGetPoint{C}
 \tkzDrawPoints[color=red](A,B,C)
 \tkzDrawSegment(A,B)
 \tkzLabelPoints[above right=3pt](A,B,C)
\end{tikzpicture}

1.9.2 Colinear

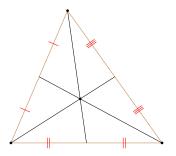




```
\begin{tikzpicture}[scale=1.2,
    vect/.style={->,shorten >=3pt,>=latex'}]
  \tkzDefPoint(2,3){A}
  \tkzDefPoint(4,2){B}
  \tkzDefPoint(1,2){C}
  \tkzDefPointWith[colinear=at C](A,B)
  \tkzGetPoint{D}
  \tkzDrawPoints[color=red](A,B,C,D)
  \tkzLabelPoints[above right=3pt](A,B,C,D)
  \tkzDrawSegments[vect](A,B C,D)
\end{tikzpicture}
\begin{tikzpicture}[scale=1.2,
    vect/.style={->,shorten >=3pt,>=latex'}]
  \tkzDefPoints{2/3/A, 4/2/B}
  \tkzDefPointWith[orthogonal,K=2/3](A,B)
  \tkzGetPoint{C}
  \tkzDefPointWith[orthogonal,normed,K=-1](B,A)
  \tkzGetPoint{D}
  \tkzDrawPoints[color=red](A,B,C,D)
  \tkzLabelPoints[right=3pt](B,C,D)
  \tkzLabelPoints[below=3pt](A)
  \tkzDrawSegments[vect](A,B A,C B,D)
  \tkzMarkRightAngle(B,A,C)
\end{tikzpicture}
```

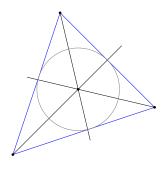
1.10 Triangle Centers: \tkzDefTriangleCenter

1.10.1 Centroid



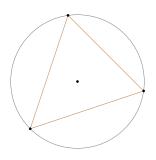
```
\begin{tikzpicture}
  \tkzDefPoints{0/0/A,4/0/B,1.5/3.5/C}
  \tkzDrawPolygon[color=brown](A,B,C)
  \tkzDefTriangleCenter[centroid](A,B,C) \tkzGetPoint{D}
  \tkzDrawPoints(A,B,C,D)
  \tkzDefMidPoint(A,B) \tkzGetPoint{E}
  \tkzDefMidPoint(B,C) \tkzGetPoint{F}
  \tkzDefMidPoint(C,A) \tkzGetPoint{G}
  \tkzDrawSegments(C,E A,F B,G)
  \tkzMarkSegments[mark=|,color=red](C,G A,G)
  \tkzMarkSegments[mark=||,color=red](A,E B,E)
  \tkzMarkSegments[mark=||,color=red](B,F C,F)
  \end{tikzpicture}
```

1.10.2 Incenter



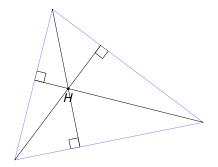
\begin{tikzpicture}[scale=1.25]
 \tkzDefPoints{0/1/A,3/2/B,1/4/C}
 \tkzDefTriangleCenter[in](A,B,C) \tkzGetPoint{I}
 \tkzDefPointBy[projection=onto A--C](I)
 \tkzGetPoint{Ib}
 \tkzDrawPolygon[color=blue](A,B,C)
 \tkzDrawPoints(A,B,C,I)
 \tkzDrawLines[add = 0 and 2/3](A,I B,I C,I)
 \tkzDrawCircle(I,Ib)
 \end{tikzpicture}

1.10.3 Circumcenter



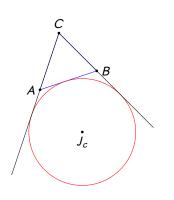
\begin{tikzpicture}
 \tkzDefPoints{0/1/A,3/2/B,1/4/C}
 \tkzDefTriangleCenter[circum](A,B,C) \tkzGetPoint{G}
 \tkzDrawPolygon[color=brown](A,B,C)
 \tkzDrawCircle(G,A)
 \tkzDrawPoints(A,B,C,G)
 \end{tikzpicture}

1.10.4 Orthocenter



\begin{tikzpicture}
 \tkzDefPoint(0,0){A}
 \tkzDefPoint(5,1){B}
 \tkzDefPoint(1,4){C}
 \tkzClipPolygon(A,B,C)
 \tkzDefTriangleCenter[ortho](B,C,A) \tkzGetPoint{H}
 \tkzDefSpcTriangle[orthic,name=H](A,B,C){a,b,c}
 \tkzDrawPolygon[color=blue](A,B,C)
 \tkzDrawPoints(A,B,C,H)
 \tkzDrawLines[add=0 and 1](A,Ha B,Hb C,Hc)
 \tkzLabelPoint(H){\$H\$}
 \tkzAutoLabelPoints[center=H](A,B,C)
 \tkzMarkRightAngles(A,Ha,B B,Hb,C C,Hc,A)
 \end{tikzpicture}

1.10.5 Excenter

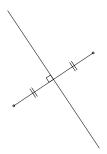


\begin{tikzpicture}[scale=0.5]
 \tkzDefPoints{0/1/A,3/2/B,1/4/C}
 \tkzDefTriangleCenter[ex](B,C,A) \tkzGetPoint{J_c}
 \tkzDefPointBy[projection=onto A--B](J_c)
 \tkzGetPoint{TC}
 \tkzDrawPolygon[color=blue](A,B,C)
 \tkzDrawPoints(A,B,C,J_c)
 \tkzDrawCircle[red](J_c,Tc)
 \tkzDrawLines[add=1.5 and 0](A,C B,C)
 \tkzLabelPoints[left](A)
 \tkzLabelPoints[right](B)
 \tkzLabelPoints[above](C)
 \tkzLabelPoints(J_c)
 \end{tikzpicture}

2 Lines

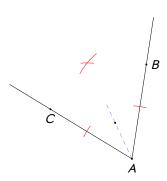
2.1 Definition: \tkzDefLine

2.1.1 Mediator



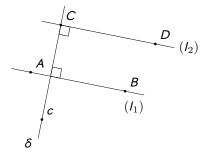
\begin{tikzpicture}[scale=0.7]
 \tkzSetUpPoint[size=1.5pt]
 \tkzDefPoints{-2/0/A,1/2/B}
 \tkzDefLine[mediator](A,B)
 \tkzGetPoints{C}{D}
 \tkzInterLL(C,D)(A,B)
 \tkzDrawPoints(A,B)
 \tkzDrawSegments(A,B C,D)
 \tkzMarkRightAngle[size=.2](A,I,C)
 \tkzMarkSegments[mark=||](A,I B,I)
\end{tikzpicture}

2.1.2 Bisector



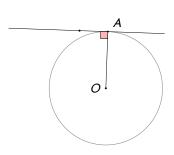
\begin{tikzpicture} [rotate=25,scale=.7]
 \tkzDefPoints{0/0/C, 2/-3/A, 4/0/B}
 \tkzDefLine[bisector,K=.5](B,A,C)
 \tkzGetPoint{a}
 \tkzDrawLines[add= 0 and .5](A,B A,C)
 \tkzShowLine[bisector,gap=4,size=2,color=red](B,A,C)
 \tkzDrawLines[blue!50,dashed,add= 0 and .5](A,a)
 \tkzLabelPoints[below](A,C)
 \tkzLabelPoints[right](B)
 \tkzDrawPoints[size=1.5pt](A,B,C,a)
 \end{tikzpicture}

2.1.3 Orthogonal And Parallel



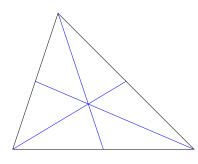
```
\begin{tikzpicture}
 \text{tkzDefPoints}\{-1.5/-0.25/A,1/-0.75/B,-0.7/1/C\}
 \tkzDrawLine(A,B)
 \tkzDefLine[orthogonal=through C](B,A)
 \tkzGetPoint{c}
                    \tkzDrawLine(C,c)
 \tkzInterLL(A,B)(C,c)
                          \tkzGetPoint{I}
 \tkzDefLine[parallel=through C](A,B)
 \tkzGetPoint{D}
                    \tkzDrawLine(C,D)
 \tkzDrawPoints(A,B,C,c,D)
 \tkzLabelPoints[above right](A,B,C,c,D)
 \tkzLabelLine[pos=1.25,below left](A,B){$(1_1)$}
 \time [pos=1.2,right](C,D){$(1_2)$}
 \tkzLabelLine[pos=1.25,left](C,c){$\delta$}
 \tkzMarkRightAngle(C,I,B)\tkzMarkRightAngle(I,C,D)
\end{tikzpicture}
```

2.2 Tangent to a Circle: \tkzDefTangent

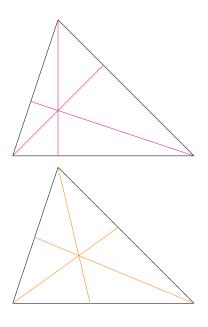


```
\begin{tikzpicture}[scale=.75]
  \tkzDefPoint(0,0){0}
  \tkzDefRandPointOn[circle=center 0 radius 2]
  \tkzGetPoint{A}
  \tkzDrawSegment(0,A)
  \tkzDrawCircle(0,A)
  \tkzDefTangent[at=A](0)   \tkzGetPoint{h}
  \tkzDrawPoints[size=1.5pt](A,0,h)
  \tkzDrawLine[add = 2 and 2.5](A,h)
  \tkzMarkRightAngle[fill=red!30](0,A,h)
  \tkzLabelPoints[above right](A)  \tkzLabelPoints[left](0)
  \end{tikzpicture}
```

2.3 Median, Altitude, and Bisector



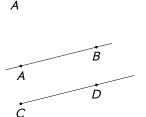
```
\begin{tikzpicture}[scale=1.2]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(4,0){B}
  \tkzDefPoint(1,3){C}
  \tkzDrawPolygon(A,B,C)
  \tkzSetUpLine[color=blue]
  \tkzDefSpcTriangle[medial,name=M](A,B,C){_A,_B,_C}
  \tkzDrawSegments(A,M_A B,M_B C,M_C)
\end{tikzpicture}
```

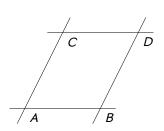


```
\begin{tikzpicture}[scale=1.2]
 \tkzDefPoint(0,0){A}
 \tkzDefPoint(4,0){B}
 \tkzDefPoint(1,3){C}
 \tkzDrawPolygon(A,B,C)
 \tkzSetUpLine[color=magenta]
 \tkzDefSpcTriangle[orthic,name=H](A,B,C){_A,_B,_C}
 \tkzDrawSegments(A,H_A B,H_B C,H_C)
\end{tikzpicture}
\begin{tikzpicture}[scale=1.2]
 \tkzDefPoint(0,0){A}
 \tkzDefPoint(4,0){B}
 \tkzDefPoint(1,3){C}
 \tkzDrawPolygon(A,B,C)
 \tkzSetUpLine[color=orange]
 \tkzDefSpcTriangle[in,name=I](A,B,C){_A,_B,_C}
 \tkzDrawSegments(A,I_A B,I_B C,I_C)
\end{tikzpicture}
```

2.4 Drawing: \tkzDrawSegment and \tkzDrawLine

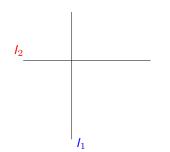
В



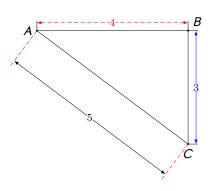


```
\begin{tikzpicture}[scale=1.5]
   \tkzDefPoint(0,0){A}
   \tkzDefPoint(2,1){B}
   \tkzDrawSegment[color=red,thin](A,B)
   \tkzDrawPoints(A,B)
   \tkzLabelPoints(A,B)
\end{tikzpicture}
 \begin{tikzpicture}
   \tkzDefPoint(0,0){A}
   \tkzDefPoint(2,0.5){B}
   \t \DefPoint(0,-1) \{C\} \t \DefPoint(2,-0.5) \{D\}
   \tkzDrawLine(A,B)
   \t DrawLine[add = 0 and .5](C,D)
   \tkzDrawPoints(A,B,C,D) \tkzLabelPoints(A,B,C,D)
 \end{tikzpicture}
 \begin{tikzpicture}
   \tkzDefPoint(0,0){A}
   \tkzDefPoint(2,0){B}
   \tkzDefPoint(1,2){C}
   \tkzDefPoint(3,2){D}
   \tkzDrawLines(A,B C,D A,C B,D)
   \tkzLabelPoints[below right](A,B,C,D)
 \end{tikzpicture}
```

2.4.1 Labeling: \tkzLabelLine

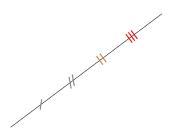


```
\begin{tikzpicture}[scale=0.8]
  \tkzDefPoints{0/0/A,3/0/B,1/1/C}
  \tkzDefLine[perpendicular=through C,K=-1](A,B)
  \tkzGetPoint{c}
  \tkzDrawLines(A,B C,c)
  \tkzLabelLine[pos=1.25,blue,right](C,c){$1_1$}
  \tkzLabelLine[pos=-0.25,red,above](A,B){$1_2$}
\end{tikzpicture}
```



```
\begin{tikzpicture}
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(4,0){B}
  \tkzDefTriangle[pythagore](A,B) \tkzGetPoint{C}
  \tkzDrawPoints[size=1.5pt](A,B,C)
  \tkzDrawSegment[dim={$3$, 6pt, transform shape},
    dim style/.append style={blue}](B,C)
  \tkzDrawSegment[dim={$4$, 6pt, transform shape},
    dim style/.append style={densely dashed, red}](A,B)
  \tkzDrawSegment[dim={$5$, 1cm, transform shape},
    dim fence style/.style={red,densely dashed}](C,A)
  \tkzLabelPoints[left](A) \tkzLabelPoints[above right](B)
  \tkzLabelPoints[below](C)
  \end{tikzpicture}
```

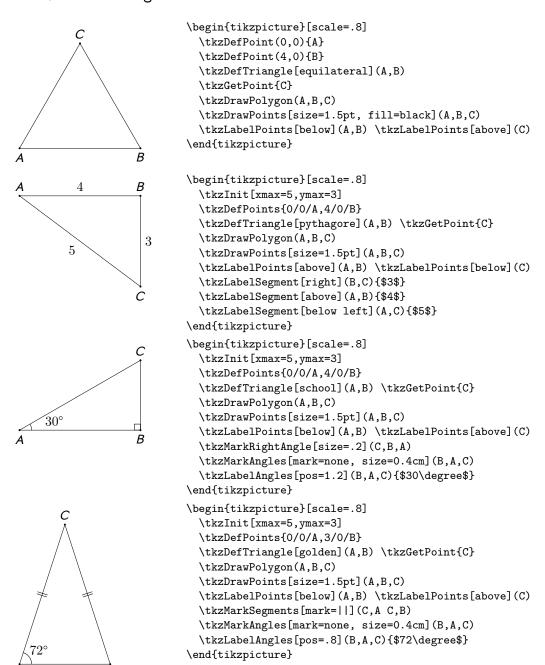
2.4.2 Marking: \tkzMarkSegment



```
\begin{tikzpicture}
  \tkzDefPoint(2,1){A}
  \tkzDefPoint(6,4){B}
  \tkzDrawSegment(A,B)
  \tkzMarkSegment[thick,color=gray,pos=0.2,mark=s|](A,B)
  \tkzMarkSegment[thick,color=gray,pos=0.4,mark=s|](A,B)
  \tkzMarkSegment[thick,color=brown,pos=0.6,mark=||](A,B)
  \tkzMarkSegment[thick,color=red,pos=0.8,mark=||](A,B)
  \tkzMarkSegment[thick,color=red,pos=0.8,mark=||](A,B)
  \end{tikzpicture}
```

3 Triangles

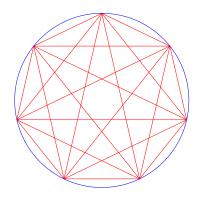
3.1 \tkzDefTriangle



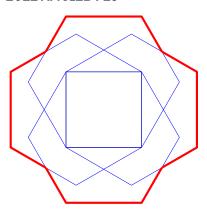
3.2 \tkzDefDefSpcTriangle

4 Miscellaneous

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```
\begin{tikzpicture}
 \tkzDefPoints{-1/-1/P_1,1/-1/P_2,0/0/0}
 \tkzDefRegPolygon[side, sides=4, name=P_](P_1,P_2)
 \tkzDrawPolygon(P_1,P_...,P_4)
 foreach i [evaluate=i as i using { <math>int(mod(i,4) + 1) }]
           in \{1, ..., 4\} {
   \t \DrawPolygon[blue](Q_{i_1},Q_{i_...,Q_{i_6})
 \begin{pgfinterruptboundingbox}
 \t = 2*sqrt(3), 2.1){A}
 \t C
 \tkzDefRectangle(A,C) \tkzGetPoints{B}{D}
 \foreach \i in \{1, ..., 4\} {
   \begin{scope}
    \tkzDefPointsBy[rotation=center 0 angle 90](A,B,C,D)
                 \{A,B,C,D\}
    \tkzClipPolygon(A,B,C,D)
    \end{scope}
 \end{pgfinterruptboundingbox}
\end{tikzpicture}
```