

STOCHASTIC ANALYSIS OF REAL AND VIRTUAL STORAGE IN THE SMART GRID

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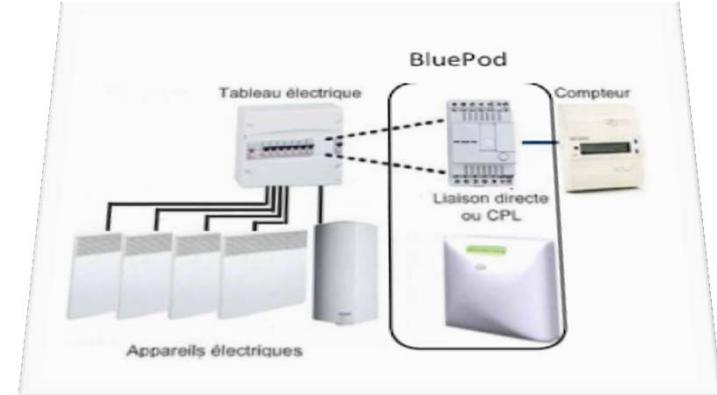
1.

A MODEL OF DEMAND RESPONSE

Le Boudec, Tomozei, *Satisfiability of Elastic Demand in the Smart Grid*, Energy 2011
and ArXiv.1011.5606

Demand Response

- = distribution network operator may interrupt / modulate power
- elastic loads support graceful degradation
- Thermal load (Voltalis), washing machines (Romande Energie«commande centralisée») e-cars,



Voltalis Bluepod switches off thermal load for 60 mn



Our Problem Statement

■ Does demand response work ?

- ▶ Delays
- ▶ Returning load

■ **Problem Statement**

Is there a control mechanism that can stabilize demand ?

■ We leave out for now the details of signals and algorithms

Macroscopic Model of Cho and Meyn [1], non elastic demand, mapped to discrete time

Step 1: Day-ahead market

- Forecast demand:

$$D^f(t)$$

control

- Forecast supply:

$$G^f(t) = D^f(t) + \varepsilon_0$$

deterministic

Step 2: Real-time market

- Actual demand

$$D^a(t) = D(t) + D^f(t)$$

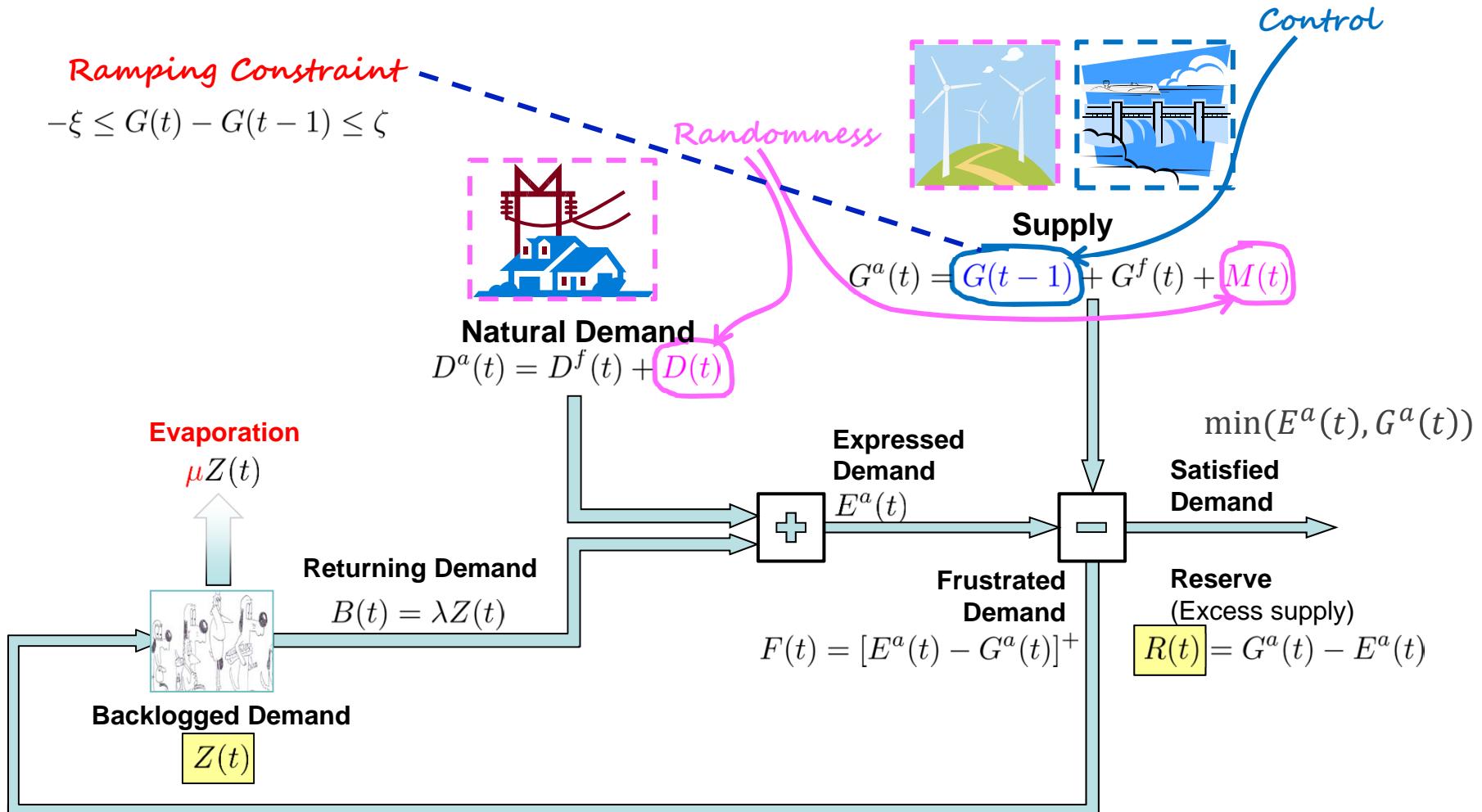
random

- Actual supply

$$G^a(t) = G(t-1) + G^f(t) + M(t)$$

- We now add the effect of elastic demand / flexible service
Some demand can be «frustrated» (delayed)

Our Macroscopic Model with Elastic Demand

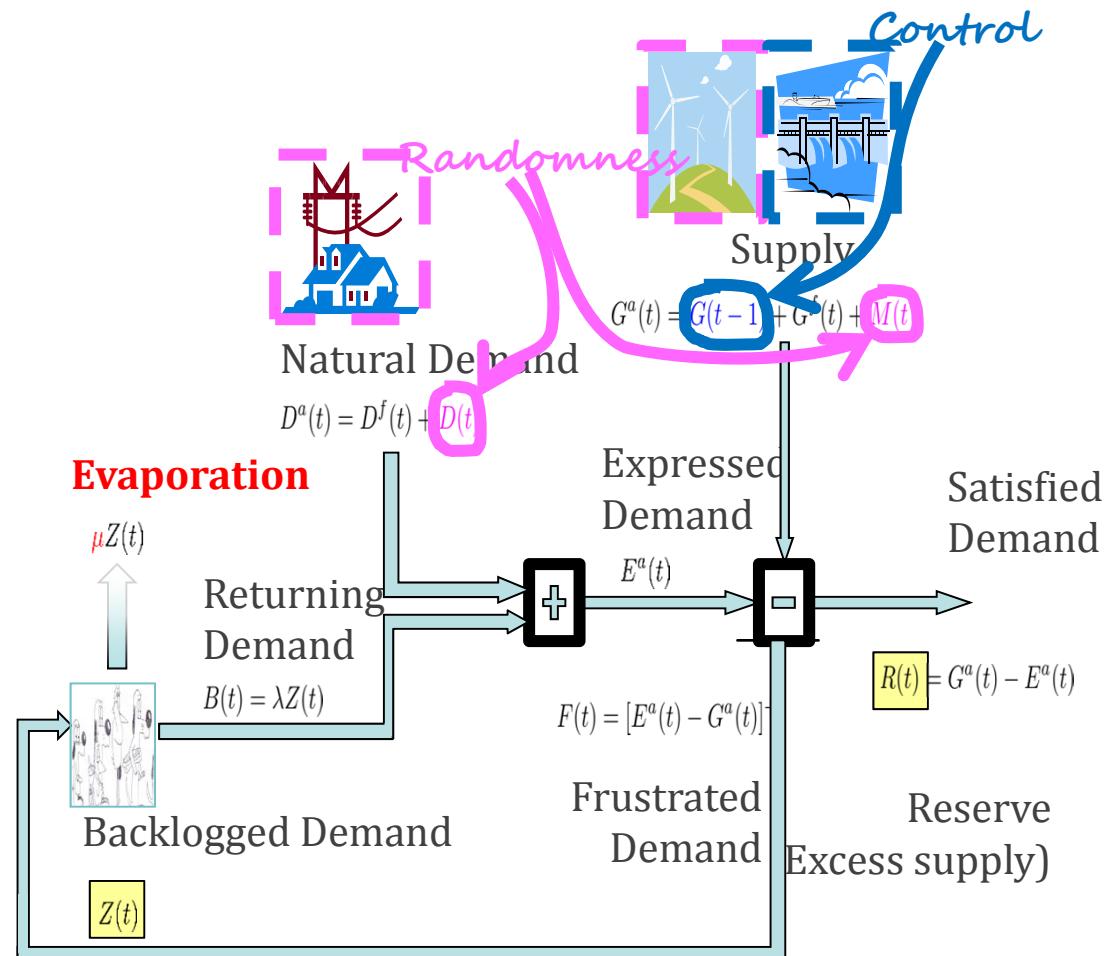


$$R(t) = G(t-1) - \lambda Z(t) + M(t) - D(t) + r_0$$

$$Z(t) = Z(t-1) - \lambda Z(t) - \mu Z(t) + \mathbb{1}_{\{R(t)<0\}} |R(t)|$$

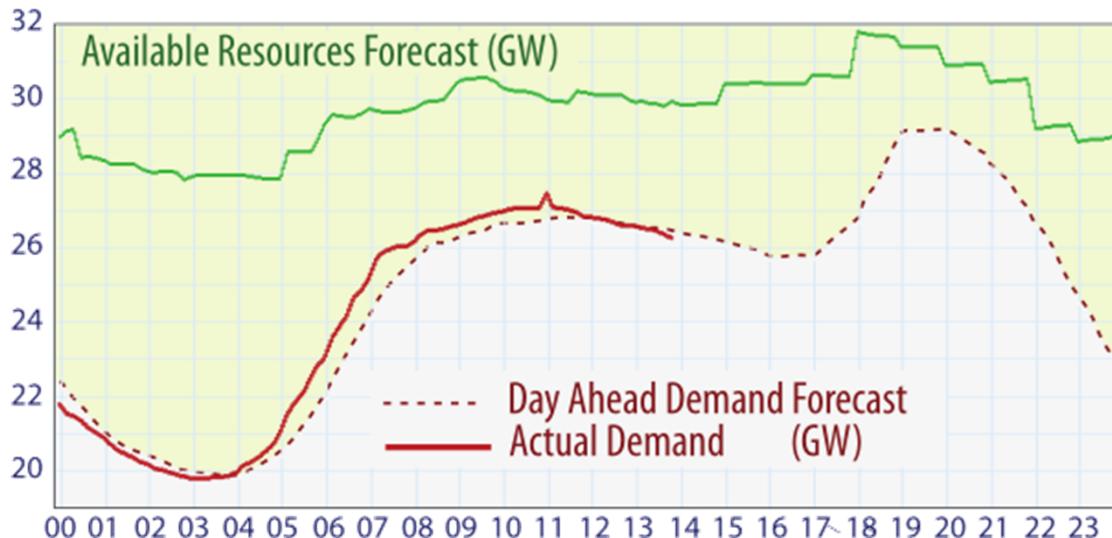
Backlogged Demand

- We assume backlogged demand is subject to two processes: update and re-submit
- Update term (evaporation) $\mu Z dt$ with $\mu > 0$ or $\mu < 0$ μ is the evaporation rate (proportion lost per time slot)
- Re-submission term $\lambda Z dt$ $1/\lambda$ (time slots) is the average delay



Macroscopic Model, continued

- Assumption : $(M - D) = \text{ARIMA}(0, 1, 0)$
typical for deviation from forecast
$$(M(t + 1) - D(t + 1) - M(t) - D(t)) := N(t + 1) \sim N(0, \sigma^2)$$



S. Meyn
“Dynamic Models and Dynamic Markets
for Electric Power Markets”

- 2-d Markov chain on continuous state space

$$R(t + 1) = R(t) + \Delta G(t) + N(t + 1) - \lambda[Z(t + 1) - Z(t)]$$
$$Z(t + 1) = (1 - \lambda - \mu)Z(t) + \mathbb{1}_{\{R(t) < 0\}}R(t)$$

The Control Problem

- Control variable:

$$G(t - 1)$$

production bought one time slot ago in real time market

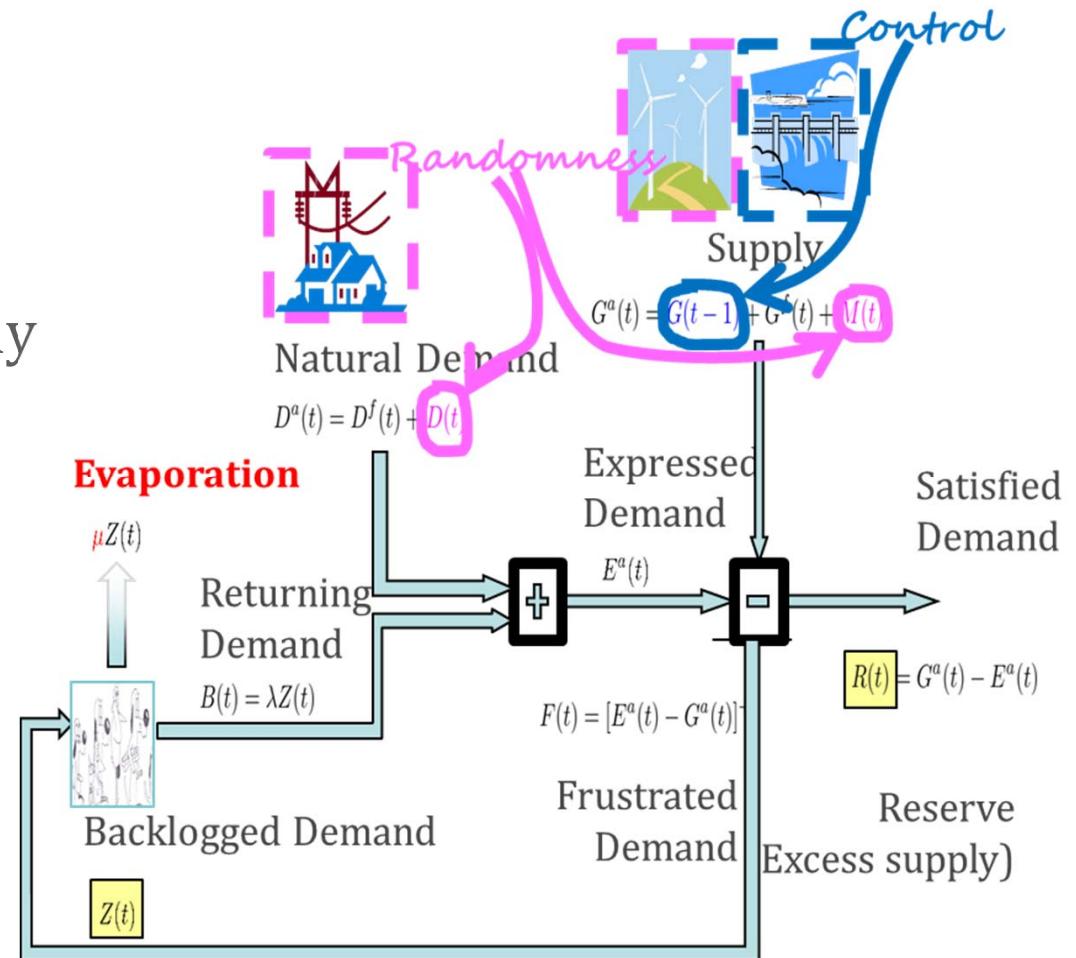
- Controller sees only supply $G^a(t)$ and expressed demand $E^a(t)$

- Our Problem:

keep backlog $Z(t)$ stable

- Ramp-up and ramp-down constraints

$$\xi \leq G(t) - G(t - 1) \leq \zeta$$



Threshold Based Policies

$$G^f(t) = D^f(t) + r_0$$

Forecast supply is adjusted to forecast demand

$$R(t) = G^a(t) - E^a(t)$$

$R(t)$:= reserve = excess of demand over supply

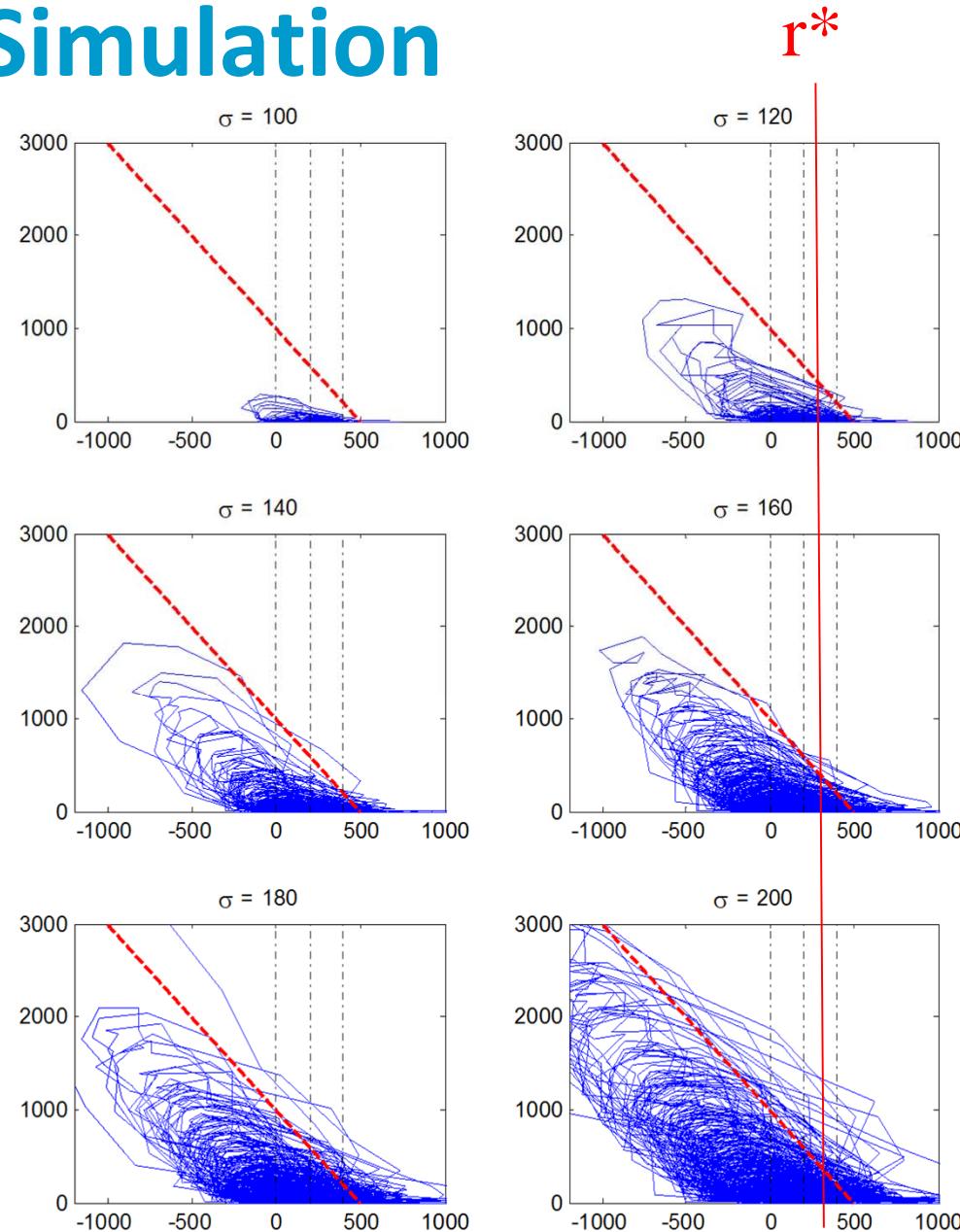
Threshold policy:

if $R(t) < r^*$ increase supply to come as close to r^* as possible (considering ramp up constraint)

else decrease supply to come as close to r^* as possible (considering ramp down constraint)

Simulation

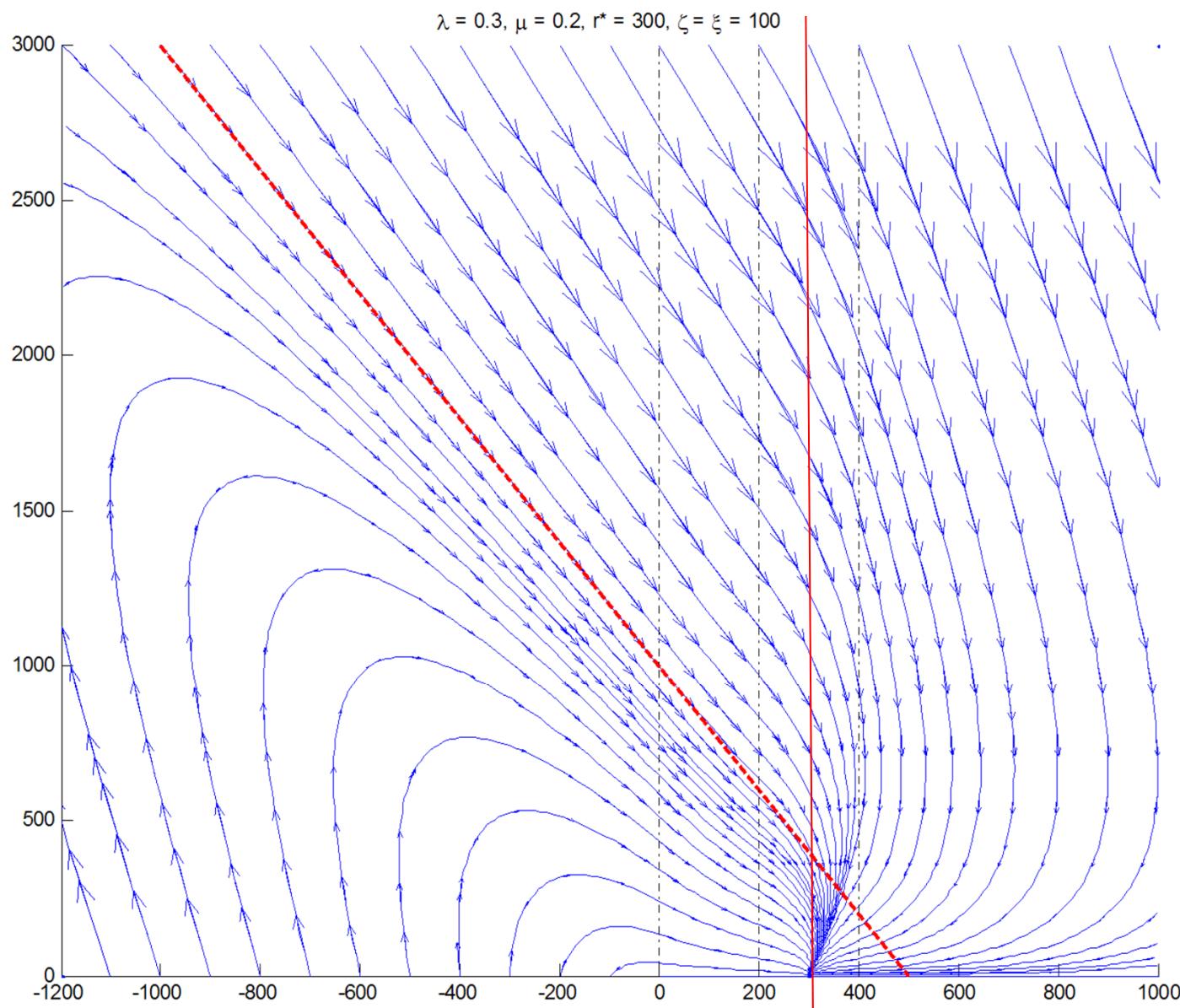
- Large excursions into negative reserve and large backlogs are typical



T=10000 iterations, $\xi=\zeta=100$, $r^*=300$, $\lambda=0.3$, $\mu=0.2$

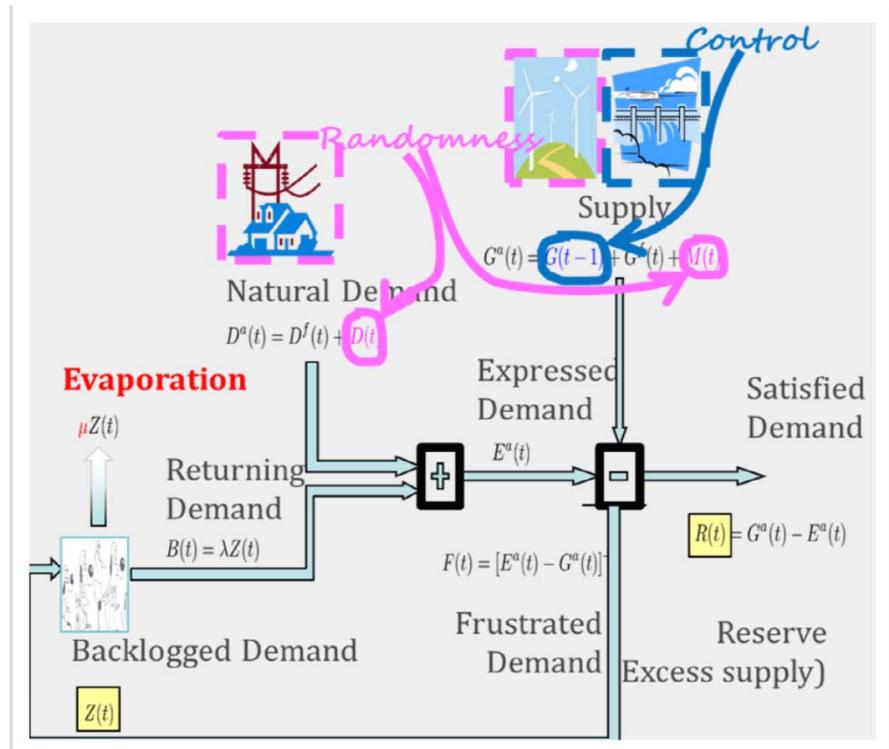
ODE Approximation

r^*



Findings : Stability Results

- If evaporation μ is positive, system is stable (ergodic, positive recurrent Markov chain) for any threshold r^*
- If evaporation μ is negative, system unstable for any threshold r^*
- Delay does not play a role in stability
- Nor do ramp-up / ramp down constraints or size of reserve



Evaporation

■ *Negative evaporation μ means: delaying a load makes the *returning load* larger than the original one.*

■ Could this happen ?

Q. Does letting your house cool down now imply spending more heat in total compared to keeping temperature constant ?

■ \neq return of the load:
Q. Does letting your house cool down now imply spending more heat later ?

A. Yes

(you will need to heat up your house later -- delayed load)

■ Assume the house model of [6]

heat provided to building $d(t)\epsilon = K(T(t) - \theta(t)) + C(T(t) - T(t-1))$

leakiness outside inertia

efficiency $\epsilon \sum_{t=1}^{\tau} d(t) = K \sum_{t=1}^{\tau} (T(t) - \theta(t)) + C(T(\tau) - T(0))$

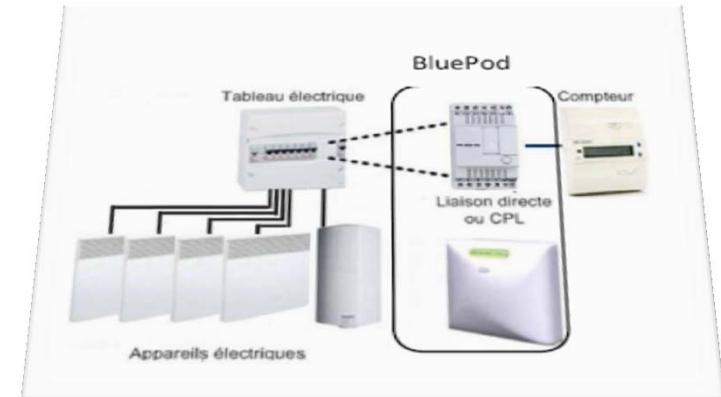
E, total energy provided achieved t^0

<i>Scenario</i>	<i>Optimal</i>	<i>Frustrated</i>
Building temperature	$T^*(t), t = 0 \dots \tau$	$T(t), t = 0 \dots \tau,$ $T(t) \leq T^*(t)$
Heat provided	$E^* = \frac{1}{\epsilon} \left(K \sum_{t=1}^{\tau} (T^*(t) - \theta(t)) + C(T^*(\tau) - T^*(0)) \right)$	$E < E^*$

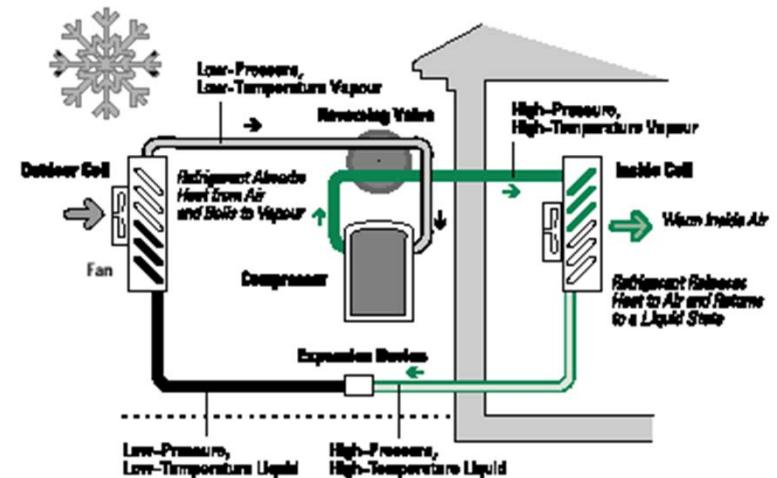
Findings

- Resistive heating system:
evaporation is positive.

This is why Voltalis bluepod is accepted by users



- If heat = heat pump, coefficient of performance ϵ may be variable
negative evaporation is possible
- Electric vehicle: delayed charge
may have to be faster, less efficient,
negative evaporation is possible



Conclusions

- A first model of demand response with volatile demand and supply
- Suggests that negative evaporation makes system unstable
Existing demand-response positive experience (with Voltalis/PeakSaver) might not carry over to other loads
- Model suggests that large backlogs are possible
Backlogged load is a new threat to grid operation
Need to measure and forecast backlogged load

2.

COPING WITH WIND VOLATILITY

Gast, Tomozei, Le Boudec. Optimal Storage Policies with Wind Forecast Uncertainties,
GreenMetrics 2012

Problem Statement

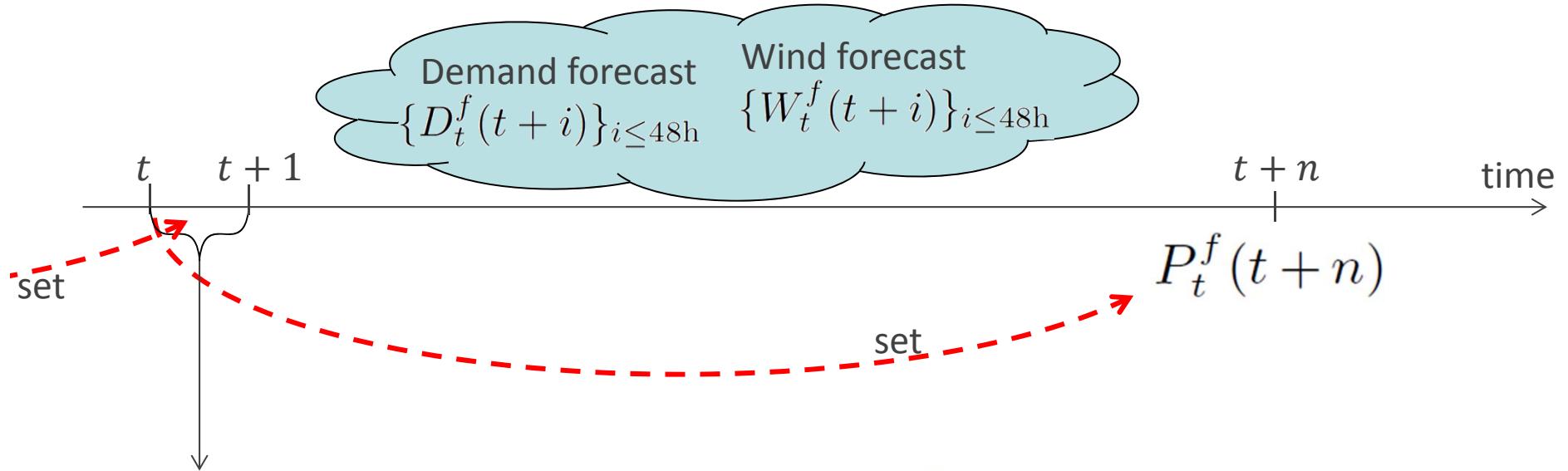
■ Model

- ▶ 20% wind penetration + prediction
- ▶ Schedule $P(t+n)$
- ▶ Imperfect storage (80% efficiency)

■ Questions:

- ▶ Optimal storage size
- ▶ Lower bound when efficiency < 100%.
- ▶ Scheduling policies with small storage

Storage Model, from [Bejan, Gibbens Kelly 2011]



■ Mismatch: $\Delta(t) := D(t) - W(t) - P_{t-n}^f(t)$.

To compensate the mismatch:

1. Storage system

$$B(t+1) = \begin{cases} \max(B - \min(\Delta, D_{\max}), 0) & \text{if } \Delta \geq 0, \text{ (discharge)} \\ \min(B + \eta \min(-\Delta, C_{\max}), B_{\max}) & \text{if } \Delta < 0. \text{ (charge)} \end{cases}$$

Efficiency of cycle (~70-80%)

Power constraints

Capacity constraints

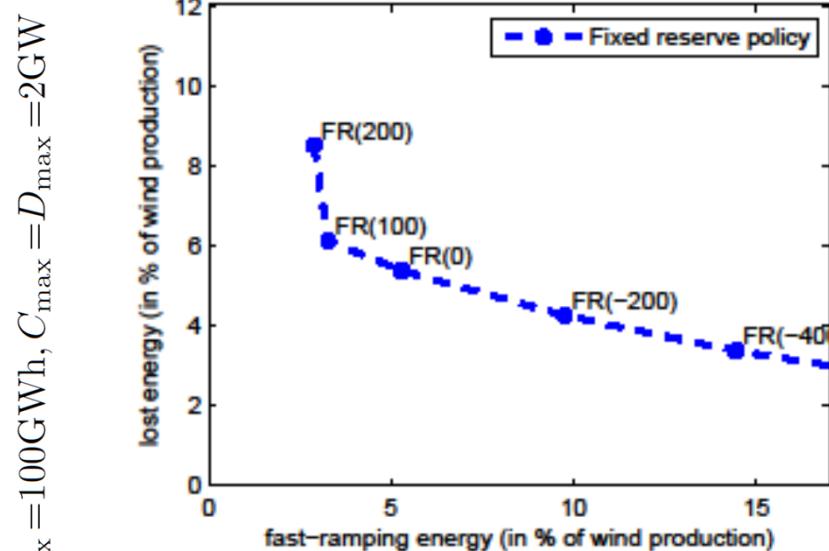
2. Fast-ramping generation (gas) / Loss

Basic scheduling policy & metrics

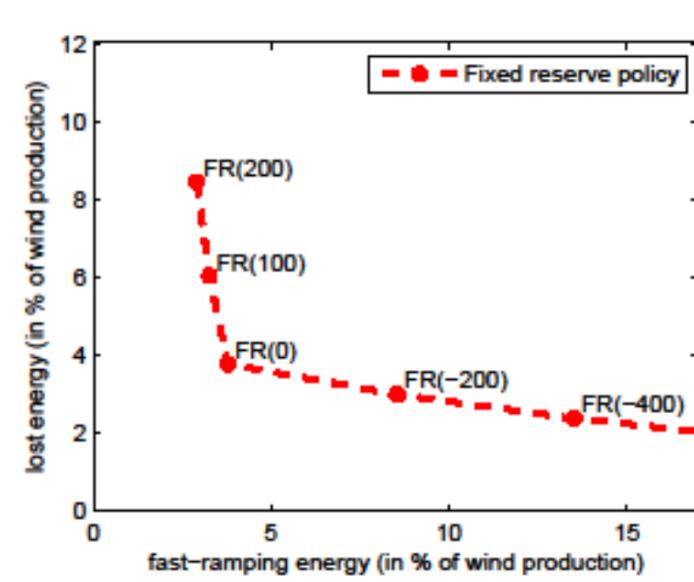
- ▶ Mismatch: $\Delta(t) := D(t) - W(t) - P_{t-n}^f(t).$
- ▶ Basic schedule: $P_t^f(t+n) := D_t^f(t+n) - W_t^f(t+n) + u_t^f(t+n)$

- Ex: **fixed reserve** $u_t^f(t+n) = x$

- Metric: Fast-ramping energy used (x-axis)
Lost energy (y-axis) = wind spill + storage inefficiencies



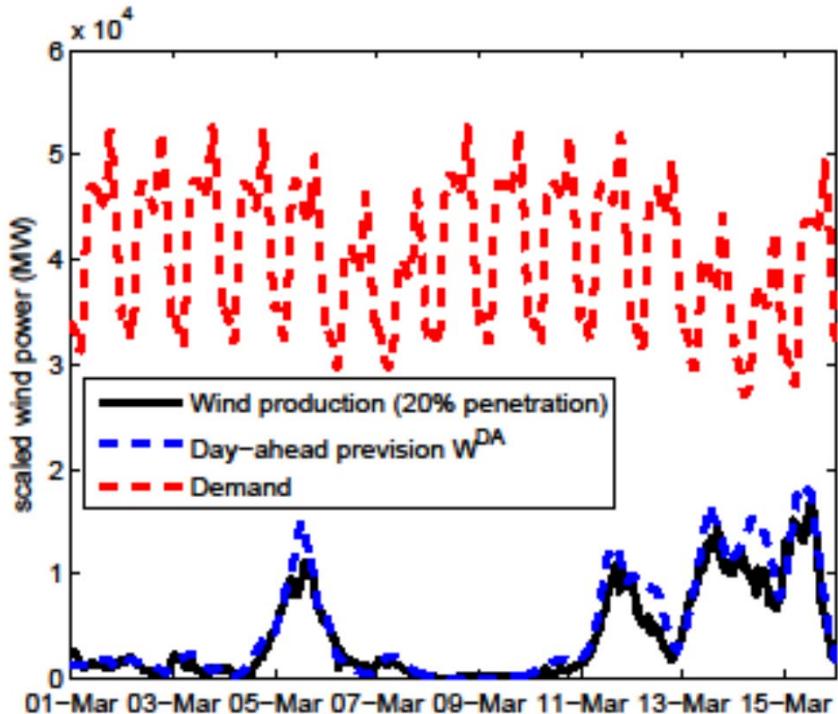
$$\eta = 0.8$$



$$\eta = 1$$

Wind data & forecasting

- Aggregate data from UK (BMRA data archive <https://www.elexonportal.co.uk/>)



- Demand perfectly predicted
- 3 years data
- Scale wind production to 20% (max 26GW)
$$W(t) := \frac{\text{production}(t)}{\text{total wind capacity at time } t} \times 26\text{GW}.$$
- Relative error $\frac{\sum_t |W_t^f(t+n) - W(t+n)|}{\sum_t W(t)}$
- Day ahead forecast = 24%
- Corrected day ahead forecast = 19%

- Key parameter: prediction error $e(t+n) = W(t+n) - W_t^f(t+n)$

A lower bound

■ **Theorem.** Assume that the error $e(t+n) = W(t+n) - W_t^f(t+n)$ conditioned to \mathcal{F}_t is distributed as \mathcal{E} . Then:

$$(i) \bar{G} \geq \mathbb{E}[(\varepsilon + \bar{u})^-] - \text{ramp}(\bar{u})$$

$$\bar{L} \geq \mathbb{E}[(\varepsilon + \bar{u})^+] - \text{ramp}(\bar{u})$$

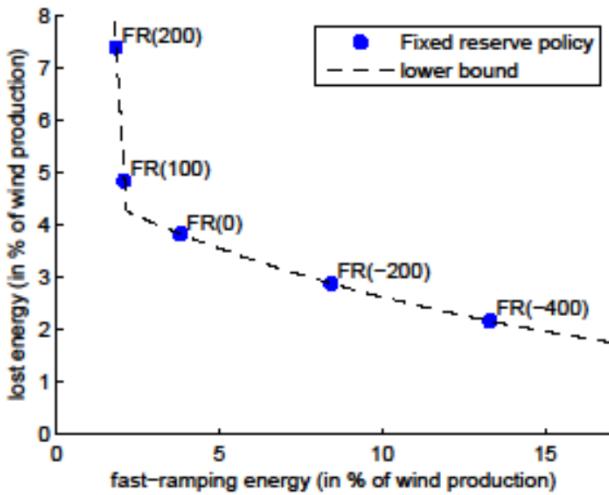
where $\text{ramp}(\bar{u}) := \mathbb{E}[\min(\eta(\varepsilon + \bar{u})^+, \eta C_{\max}, (\varepsilon + \bar{u})^-, D_{\max})]$

(ii) The lower bound is achieved by the Fixed Reserve when storage capacity is infinite.

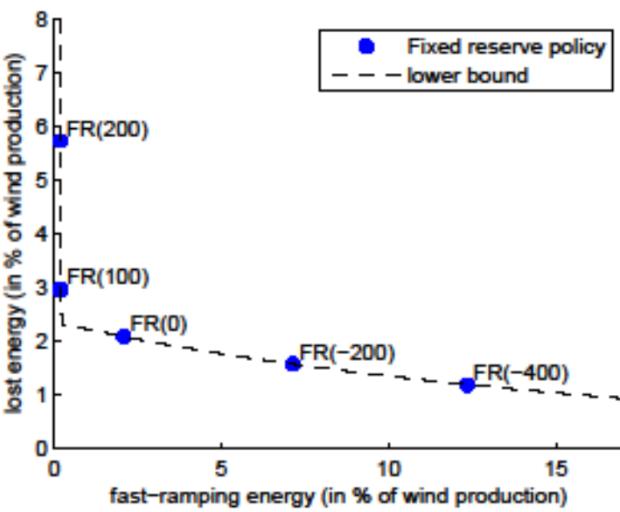
- ▶ Depends on storage characteristics
 - ▶ Efficiency, maximum power (but not on size)
- ▶ Assumption valid if prediction error is Arima

Lower bound is attained for $B_{\max} = 100 \text{GWh}$

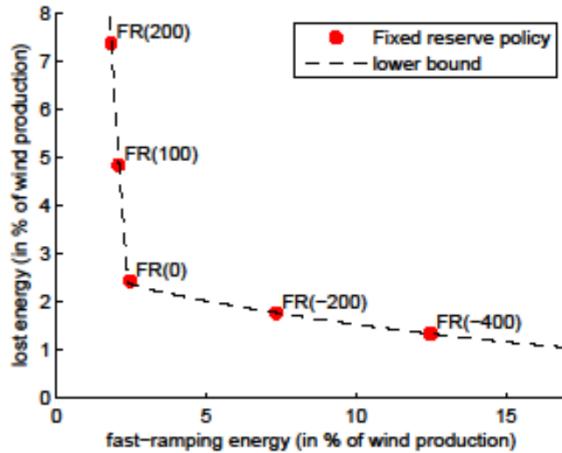
$C_{\max} = D_{\max} = 2 \text{GW}$



$C_{\max} = D_{\max} = 6 \text{GW}$



$$\eta = 0.8$$



$$\eta = 1$$

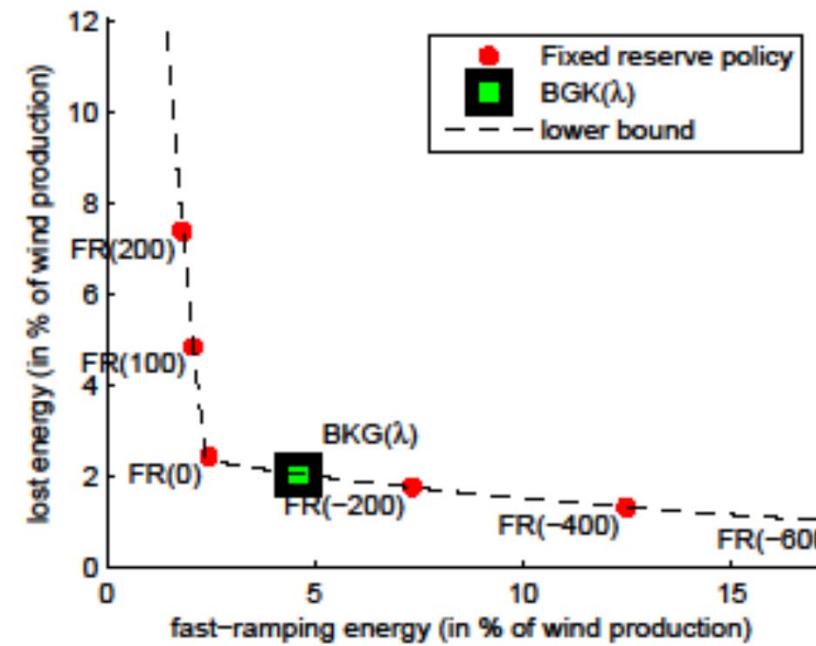
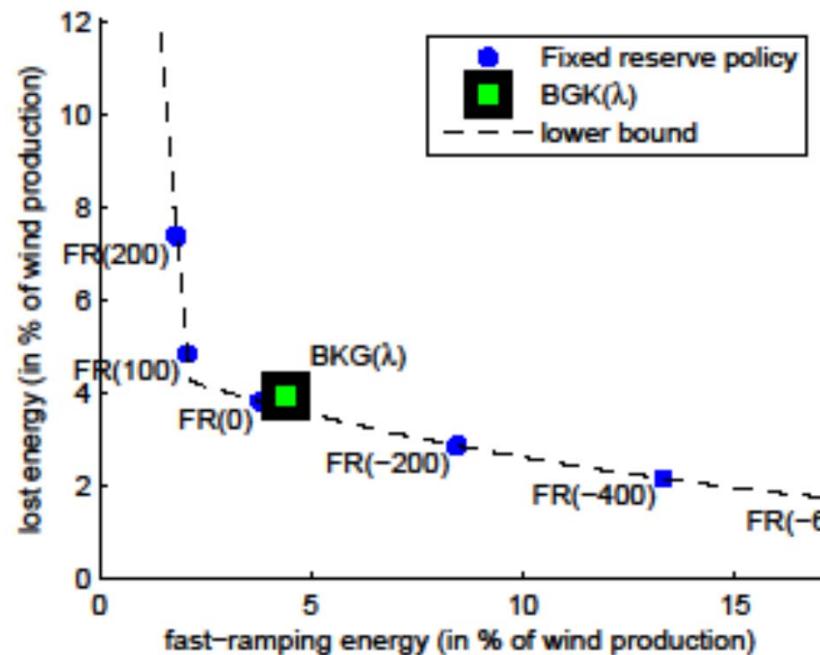
The BGK policy [Bejan, Gibbens, Kelly 2011]

- BGK [7] : try to **maintain storage in a fixed level** λB_{\max}

► Compute estimate of storage size $B_t^f(t+n)$

$$P_t^f(t+n) := D_t^f(t+n) - W_t^f(t+n) + u_t^f(t+n)$$

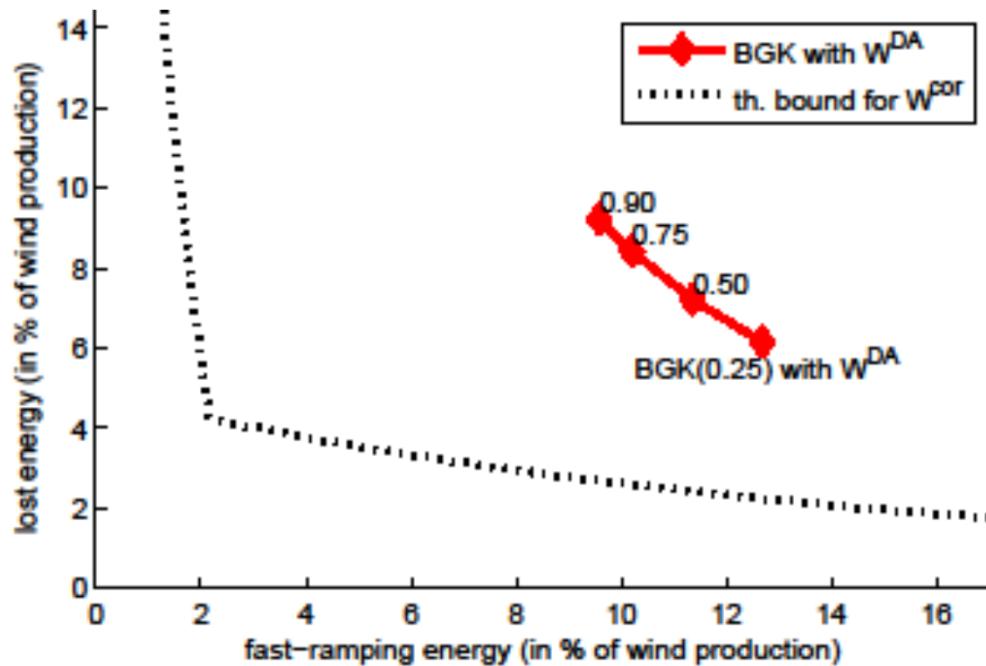
$$u_t^f(t+n) = \min\left(\frac{1}{\eta}(\lambda B_{\max} - B)^+, C_{\max}\right) - \min((\lambda B_{\max} - B)^-, D_{\max}).$$



- Close to lower bound for large storage

Small storage capacity?

- BGK is far from lower bound:



$$B_{\max} = 5 \text{ GWh}, C_{\max} = D_{\max} = 2 \text{ GW} \quad \eta = 0.8$$

Scheduling policies for small storage

$$P_t^f(t+n) := D_t^f(t+n) - W_t^f(t+n) + u_t^f(t+n)$$

- Fixed reserve $u_t^f(t+n) = x$
- BGK [7] : try to maintain storage in a fixed level λB_{\max}
 - ▶ Compute estimate of storage size $B_t^f(t+n)$

■ Dynamic reserve

- ▶ Based on a simplified Markov Decision Process (one time step evolution)

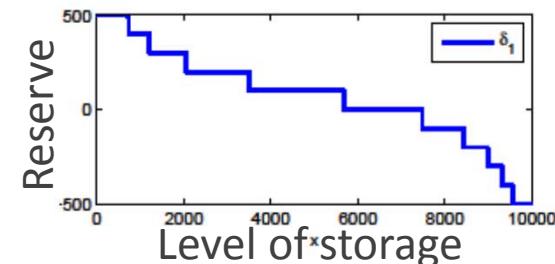
$$B(t+1) = \phi(B(t), -\varepsilon(t+1) - u(t)).$$

cost = energy loss + γ fast-ramping

- ▶ Optimal policy $\delta_\gamma(x) := \arg \min_{u \in \mathbb{R}} \{\mathbb{E} (c(x, u) + v(\phi(x, -u - \varepsilon)))\}.$

- ▶ Apply δ_γ to $B_t^f(t+n)$:

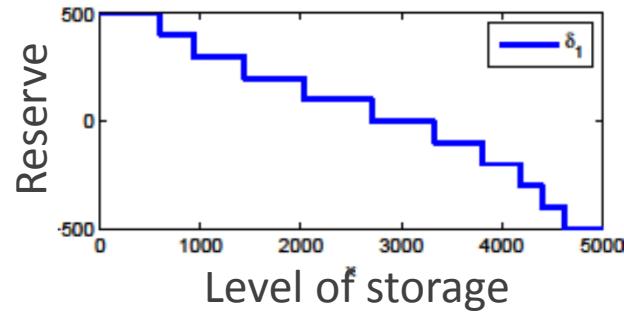
$$u_t^f(t+n) = \delta_\gamma(B_t^f(t+n))$$



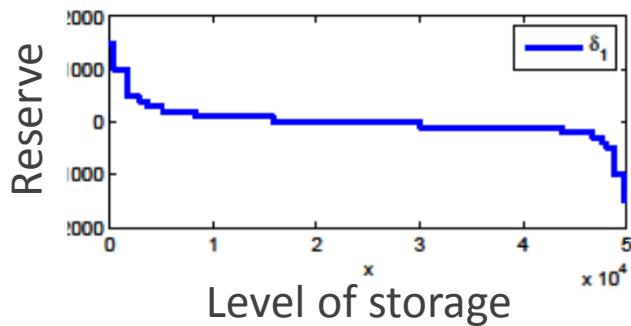
Control law for the Dynamic Reserve

- Effective algorithm to the Dynamic Reserve policy

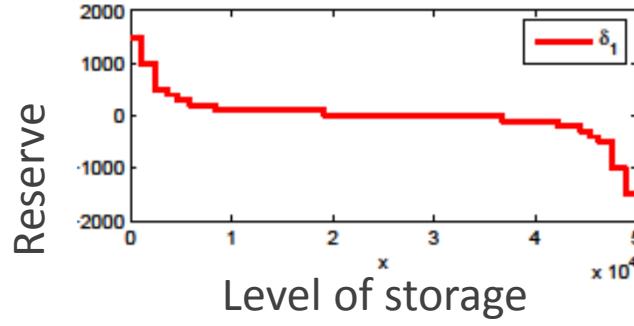
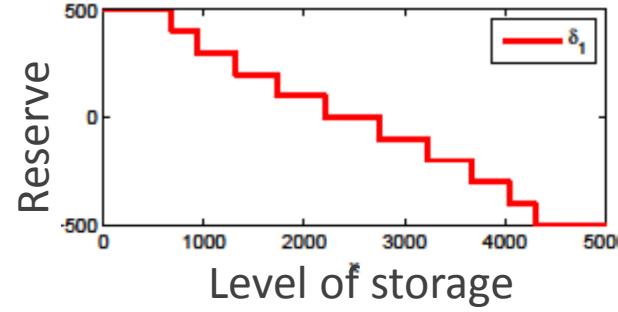
$B_{\max} = 5 \text{ GWh}$, $C_{\max} = D_{\max} = 2 \text{ GW}$



$B_{\max} = 50 \text{ GWh}$, $C_{\max} = D_{\max} = 6 \text{ GW}$



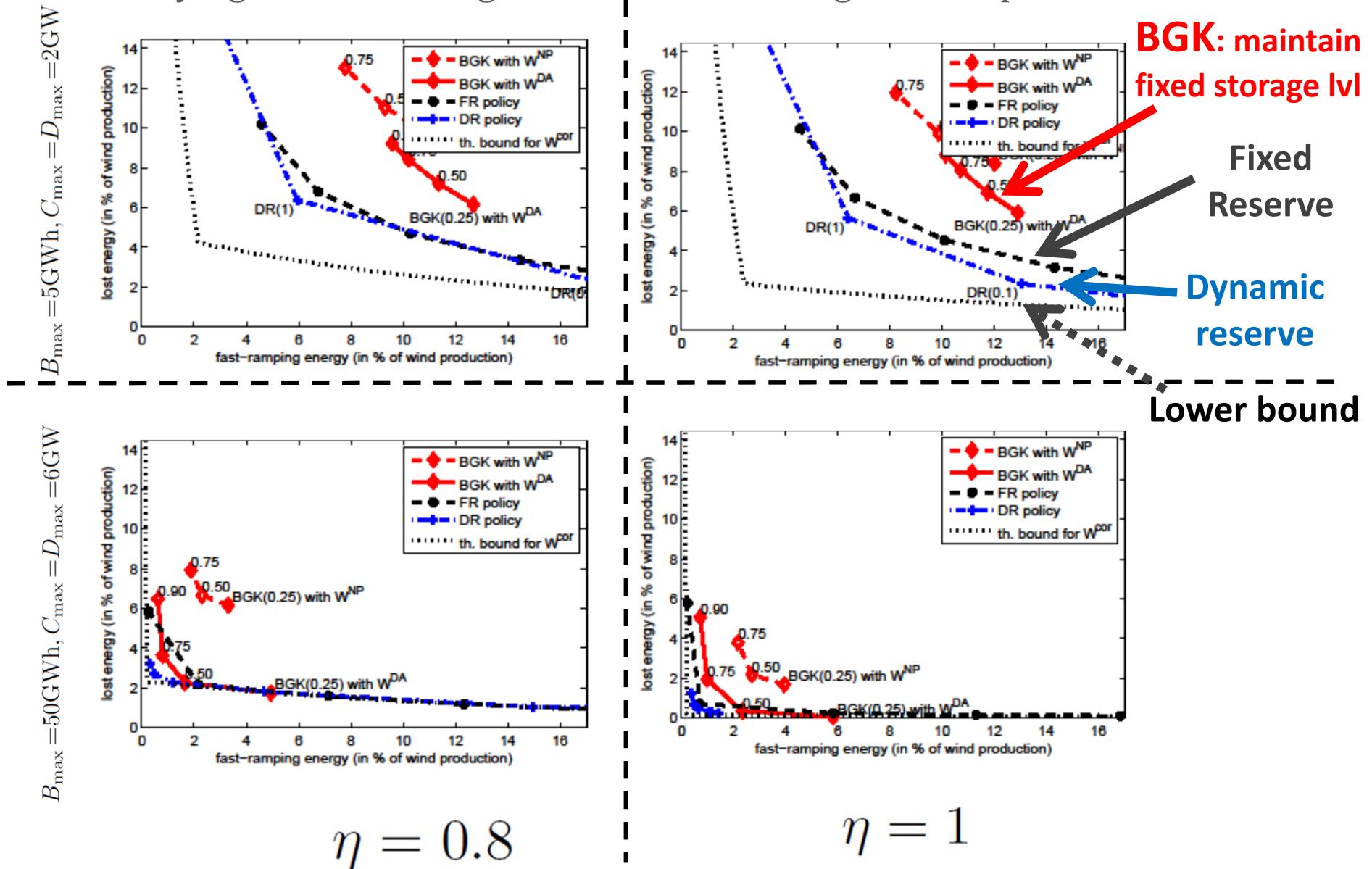
$$\eta = 0.8$$



$$\eta = 1$$

The Dynamic Reserve policies outperform BGK

- Trying to maintaining a fixed level of storage is not optimal



Conclusion

- Maintain storage at **fixed level**: not optimal
 - ▶ worse for low capacity
 - ▶ There exist better heuristics
- **Lower bound** (valid for any type of policy)
 - ▶ depends on η and maximum power
 - ▶ **Tight** for large capacity ($>50\text{GWh}$)
 - ▶ Still **gap for small capacity**
- 50GWh and 6GW is enough for 26GW of wind
- Quality of prediction matters

Questions ?

- [1] Cho, Meyn – *Efficiency and marginal cost pricing in dynamic competitive markets with friction*, Theoretical Economics, 2010
- [2] Le Boudec, Tomozei, *Satisfiability of Elastic Demand in the Smart Grid*, Energy 2011 and ArXiv.1011.5606
- [3] Le Boudec, Tomozei, *Demand Response Using Service Curves*, IEEE ISGT-EUROPE, 2011
- [4] Le Boudec, Tomozei, *A Demand-Response Calculus with Perfect Batteries*, WoNeCa, 2012
- [5] Papavasiliou, Oren - *Integration of Contracted Renewable Energy and Spot Market Supply to Serve Flexible Loads*, 18th World Congress of the International Federation of Automatic Control, 2011
- [6] David MacKay, *Sustainable Energy – Without the Hot Air*, UIT Cambridge, 2009
- [7] Bejan, Gibbens, Kelly, *Statistical Aspects of Storage Systems Modelling in Energy Networks*. 46th Annual Conference on Information Sciences and Systems, 2012, Princeton University, USA.