STAT 3022 Homework 5

Problem 6.22.

Source	DF	SS	MS	F	p-value
Face(Yes/No)	1	12915	12915	129.15	0
Gender(M/F)	1	2500	2500	25.0	2.580991e-16
Interaction	1	400	400	4.0	0.04832569
Residuals	96	9600	100		
Total	99	25415			

```
> 1-pf(129.15, 1, 96)

[1] 0

> 1-pf(25.0, 1, 96)

[1] 2.580991e-06

> 1-pf(4.0, 1, 96)

[1] 0.04832569
```

```
Problem 6.25.
> library(Stat2Data)
> data(Alfalfa)
> aggregate(Ht4~Row, data = Alfalfa,FUN= "mean" )
   Row Ht4
    a 1.16
1
2
    b 1.57
3
    c 1.25
4
    d 2.26
5
    e 2.46
## 6.25 (a): means of each row of cups
> aggregate(Ht4~Acid, data = Alfalfa,FUN= "mean" )
          Ht4
  Acid
1 1.5HCl 1.466
2 3.0HCl 1.084
   water 2.670
## 6.25 (a): means of each row of treatment
> mean(Alfalfa$Ht4)
[1] 1.74
> sd(Alfalfa$Ht4)
[1] 1.105396
## 6.25 (a): mean and standard deviation for the growth in all cups
> lm1 = aov(Ht4~Acid+Row, data=Alfalfa)
> summary(lm1)
             Df Sum Sq Mean Sq F value Pr(>F)
Acid
                           3.426
                                     4.513 0.0487 *
                 6.852
Row
               4
                 4.183
                           1.046
                                     1.378 0.3235
                  6.072
Residuals
               8
                           0.759
Signif. Codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## 6.25 (b): two-way ANOVA table for differences in average growth due to acid using rows as a
blocking variable.
> par(mfrow = c(2, 2))
> plot(lm1)
                                     Residuals vs Fitted
                                                                   Normal Q-Q
                                                                    00000000
                                                        Standardized
                              0.0
                                                          0
                                      0
                                           00
                                         0
                                0.5
                                   1.0
                                      1.5 2.0 2.5 3.0 3.5
                                                                 -1
                                                                      0
                                                                  Theoretical Quantiles
                                        Fitted values
                                                                 Constant Leverage:
                                                               Residuals vs Factor Levels
                                       Scale-Location
                           (Standardized residuals)
                              1.5
```

6.25 (c): From the normal q-q plot, the normality is not very good for it shows a general linear pattern while there exists a curve. The residuals vs fitted value plot shows that the zero mean assumption (equal variances) holds. So generally, this model is acceptable.

1.5 2.0 2.5 3.0 3.5

1.0

0.5

0.0

0.5 1.0

6.25 (d): Yes. Because the p-value of acid is 0.0487 < 0.05 which indicates that Acid effect is significant, and the observed variability is because of the treatment.

Standardized residuals

0

Acid : 1.5HCI

00

water

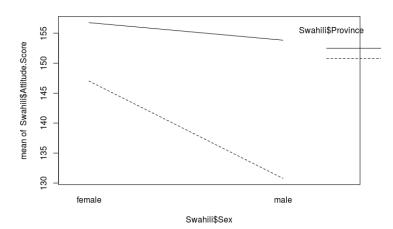
3.0HCI

Factor Level Combinations

6.25 (e): No. Because the p-value of Row is 0.3235 > 0.05 which indicates that distance effect is not significant, and the observed variability is not because of the distance.

Problem 6.28

- > data(Swahili)
- > par(mfrow = c(1, 1))
- > interaction.plot(Swahili\$Sex, Swahili\$Province, Swahili\$Attitude.Score)



> lm2=aov(Attitude.Score~as.factor(Province) * as.factor(Sex), data = Swahili)

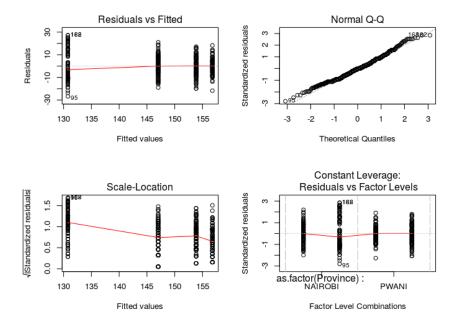
> summary(lm2)

```
Df Sum Sq Mean Sq F value
                                                                < 2e-16 ***
as.factor(Province)
                                         32275
                                                 32275 349.82
                                                        119.45 < 2e-16 ***
as.factor(Sex)
                                      1
                                         11021
                                                 11021
as.factor(Province):as.factor(Sex)
                                      1
                                          5320
                                                  5320
                                                         57.66 1.66e-13 ***
Residuals
                                    476
                                         43917
```

- - -

Signif. Codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
6.28 (a): The plot shows that the average of Nairobi is lower than the average of Pwani.
Male has lower average than female. The difference between male and female is larger in Nairobi than in Pwani. The table shows that both p-value of province factor and sex factor are very smaller than 0.05, which indicates that both these two factor are very important to this model.

- > par(mfrow = c(2, 2))
- > plot(lm2)

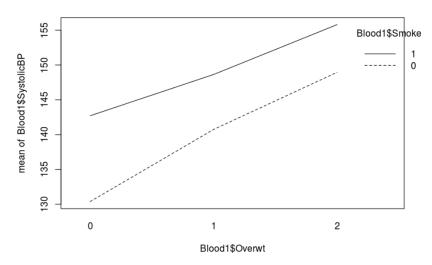


6.28 (b): The normal q-q plot shows a general linear pattern which indicates that the normality is met. The residuals vs fitted value plots shows that the zero mean assumption (equal variance) holds. So both normality and equal variance conditions are satisfied.

6.28 (c): The balanced design needs equal number of observations from two factors' each combinations of levels. In this problem, there is only one school from each province, which means if we have students from the school of one province as our observations, we will have no other observations (students) from both this school and the school in another province at same time. So this can't be a balanced complete factorial design.

Problem 7.12:

```
> data(Blood1)
> Blood1$Overwt = as.factor(Blood1$Overwt)
> Blood1$Smoke = as.factor(Blood1$Smoke)
> interaction.plot(Blood1$Overwt, Blood1$Smoke, Blood1$SystolicBP)
```



```
> lm3 = lm(SystolicBP ~ Smoke * Overwt, data = Blood1)
> anova(lm3)
Analysis of Variance Table
Response: SystolicBP
                Df Sum Sq Mean Sq F value
                                             Pr(>F)
               1 14635 14634.9 20.5255 7.387e-06 ***
Smoke
0verwt
                 23443 11721.6 16.4396 1.224e-07 ***
               2
Smoke:Overwt
               2
                    769
                          384.4 0.5391
                                          0.5836
Residuals
             494 352228
                          713.0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
> source("LSDtest.R")
 lout = LSDtest(Blood1$SystolicBP, Blood1$Overwt, alpha = 0.05)
 lout
  pair
              est
                        lwr
       -8.051464 -14.45261
  0~1
                            -1.650318
  0~2 -16.865865 -22.24359 -11.488141
  1~2 -8.814400 -15.11657 -2.512235
> subset(lout, sign(lwr)==sign(upr))
                        lwr
              est
  pair
       -8.051464 -14.45261
                            -1.650318
  0~1
  0~2 -16.865865 -22.24359 -11.488141
3 1~2 -8.814400 -15.11657 -2.512235
> ncomp = choose(nlevels(Blood1$0verwt), 2)
> bout = LSDtest(Blood1$SystolicBP, Blood1$Overwt, alpha = 0.05/ncomp)
> bout
  pair
              est
                        lwr
       -8.051464 -15.87754 -0.2253901
 0~1
 0~2 -16.865865 -23.44070 -10.2910325
 1~2 -8.814400 -16.51946 -1.1093404
> subset(bout, sign(lwr)==sign(upr))
              est
                        lwr
       -8.051464 -15.87754
 0~1
                            -0.2253901
2 0~2 -16.865865 -23.44070 -10.2910325
3 1~2 -8.814400 -16.51946 -1.1093404
## 7.12 (a): The Bonferroni intervals shows that there is not interval cover 0, so all
```

intervals are significant and that all weight groups are different from each other.

```
> lm4 = aov(SystolicBP ~ Overwt, data = Blood1)
> summary(lm4)
              Df Sum Sq Mean Sq F value Pr(>F)
Overwt
             2 27801
                       13900
                               19.02 1.1e-08 ***
           497 363274
Residuals
                          731
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
> TukeyHSD(lm4, "Overwt", data = Blood1)
  Tukey multiple comparisons of means
    95% family-wise confidence level
Fit: aov(formula = SystolicBP ~ Overwt, data = Blood1)
$0verwt
          diff
                     lwr
                              upr
                                      p adj
1-0 8.051464 0.3927115 15.71022 0.0366867
2-0 16.865865 10.4316024 23.30013 0.0000000
2-1 8.814400 1.2740746 16.35473 0.0170703
```

7.12 (b): The TukeyHSD shows that all weight groups are different from each other. And they are all significant.

7.12 (c): From the two table we knows that there is no significant difference between these two test.