

## Lab #4

### Objectives

- Analyze systems using Z-transform

### Report

1. Your report must include your answers in hand-written or computer-aid tools.
2. Do not share your report with your friends.
3. Finally, you upload your report to BKeL on time.

### Z-TRANSFORM EXERCISES

For each discrete-time signal  $x(n]$ , find the corresponding Z-Transform and its ROC

#### Exercise 1.

$$x(n) = 2\delta(n + 2) - 1\delta(n + 1) + 2\delta(n) - 3\delta(n - 1) + 4\delta(n - 2)$$

#### Exercise 2.

$$x(n) = 0.5^n u(n) + 0.4^n u(n)$$

#### Exercise 3.

$$x(n) = 0.5^n u(n) + 0.9^n u(-n - 1)$$

### ADDITIONAL SCILAB EXERCISES

#### Exercise 4.

Investigate the existing library or toolbox in Scilab to process audio data.

#### Exercise 5.

Investigate the existing library or or toolbox in Scilab for image processing. Then, you can do an example or a demo to show a simple manipulation (e.g., Histogram display, histogram equalization, blur, and watermarking) on a digital image.

#### Exercise 6.

Let there are two discrete signals  $x(n), h(n), n = 0, \pm 1, \pm 2, \dots$ , defined over the entire range of  $n$ . Then the linear convolution of discrete signals is  $y(n)$  of the form  $y(n) = \sum_{k=-\infty}^{\infty} h(k)x(n - k)$ .

- Deprive the signal  $y(n)$  such that  $y(n)$  converges in the following cases.
  - Both  $h(n)$  and  $x(n)$  are causal.

- The system has a finite impulse response such that  $h(n) = 0, n < 0 \vee n > M$ .
- Suppose the second case is hold, compute the convolution  $y(n)$  of  $x(n) = [1 \uparrow, 2, -3, 2, 1]$  and  $h(n) = [1 \uparrow, 0, -1]$  using “folding and shifting” method. Implement your answer with Scilab script.
- Suppose the second case is hold, compute the convolution  $y(n)$  of  $x(n) = [1 \uparrow, 2, -3, 2, 1]$  and  $h(n) = [1 \uparrow, 0, -1]$  using matrix method. Implement your answer with Scilab script.
- Drawing  $x(n)$ ,  $y(n)$  and energy of discrete signals in the same figure.

### Exercise 7.

For a periodic signal  $x(n)$  of length  $N$  and impulse response  $h(n)$  of length  $M$ , the circular convolution between  $x(n)$  and  $h(n)$  is defined as  $y(n) = \sum_{k=0}^{M-1} h(k)x[(n-k) \bmod N]$ . Explain why  $y(n)$  can be deprived that way.

- Compute the convolution  $y(n)$  of  $x(n) = [1 \uparrow, 2, -3, 2, 1]$  and  $h(n) = [1 \uparrow, 0, -1, -1, 1]$  using “folding and shifting” method. Implement your answer with Scilab script.
- Compute the convolution  $y(n)$  of  $x(n) = [1 \uparrow, 2, -3, 2, 1]$  and  $h(n) = [1 \uparrow, 0, -1, -1, 1]$  using matrix method. Implement your answer with Scilab script.
- Drawing  $x(n)$ ,  $y(n)$  and energy of discrete signals in the same figure.

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