

2 RVs:
Joint PMF: $P_{X,Y}(x,y) = P[X = x, Y = y]$
Joint PDF: $f_{X,Y}(x,y) = \frac{\partial^2}{\partial x \partial y} F_{X,Y}(x,y)$
* $P[(X,Y) \in A] = \int \int_{(x,y) \in A} f_{X,Y}(x,y) dx dy$
Expectation: $E[g(X,Y)] = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x,y) f_{X,Y}(x,y) dx dy$
Correlation: $E[XY]$
Covariance: $\text{Cov}[X,Y] = E[XY] - E[X]E[Y]$
Correlation Coefficient: $\rho_{X,Y} = \frac{\text{Cov}[X,Y]}{\sigma_X \sigma_Y}$
Bayes' Rule $f_{Y|X}(y|x) = \frac{f_{X,Y}(x,y)}{f_X(x)} = \frac{f_{X|Y}(x|y)f_Y(y)}{\int_{-\infty}^{\infty} f_{X|Y}(x|y')f_Y(y') dy'}$
Independent: $f_{X|Y}(x|y) = f_X(x) \forall y \Leftrightarrow f_{X,Y}(x,y) = f_X(x)f_Y(y)$
* If independent, then uncorrelated.
Uncorrelated: $\text{Cov}[X,Y] = 0 \Leftrightarrow \rho_{X,Y} = 0$
Orthogonal: $E[XY] = 0$
Conditional Expectation: $E[Y] = E[E[Y|X]]$ or $E[E[h(Y)|X]]$
* $E[E[Y|X]]$ w.r.t. $X \mid E[Y|X]$ w.r.t. Y .