

## 0.1 Learning representations of data

### 0.1.1 AI/MI/ML/DL

#### Definition:

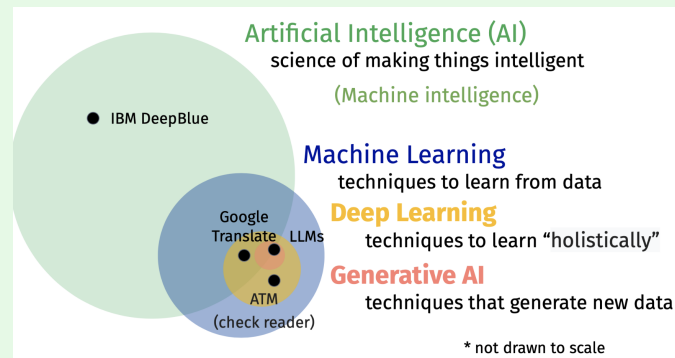


Figure 1:

### 0.1.2 Learning algorithms

**Definition:** “A **computer program M** is said to **learn** from **experience E** with respect to some class of **tasks T** and **performance measure P**, if its performance at **tasks in T**, as measured by **P**, improves with **experience E**”

- **experience E**  $\sim$  Data
- **performance measure P**  $\sim$  Loss function, evaluation metric
- **tasks T**  $\sim$  “Prediction problem”
- **computer program M**  $\sim$  Model
- **learn**  $\sim$  Optimize

### 0.1.3 Linear models

#### Example: Linear Regression

$$W \cdot x = y \quad (1)$$

- **E** (x and y)
- **P** mean squared error
- **T** Predict y from x
- **M** Linear model (W)
- **learn?** Analytical solution or gradient descent

#### Example: Generalized Linear models in equations

$$\text{Link}(W \cdot x) = y \quad (2)$$

- $x$ : Input features
  - $W$ : Linear transformation
  - $y$ : Output / target
  - $\text{Link}(x)$ : Warping function
1. If  $x$  has dim 50 and  $W$  projects to dimension 100, what is the shape of  $W$ ?
    - $W$  is a  $100 \times 50$  matrix
  2. If  $W$  is learnable, how many parameters does  $W$  have?
    - $100 \times 50 = 5000$  parameters

**Notes:** How does a generalized linear model make a prediction? By either mapping to a line or separating data by a line (hyperplane)

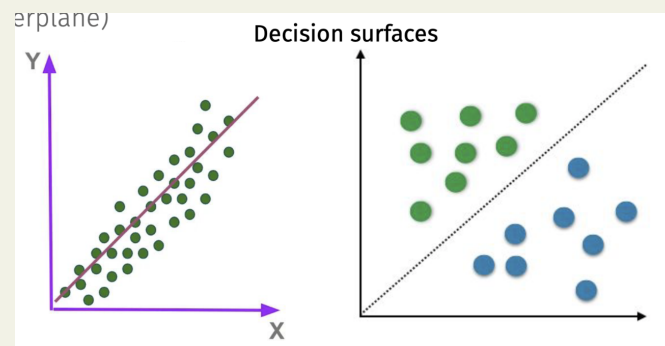


Figure 2:

**Notes:** What can we do when the data cannot be separated by a line? Resort to different decision surfaces.

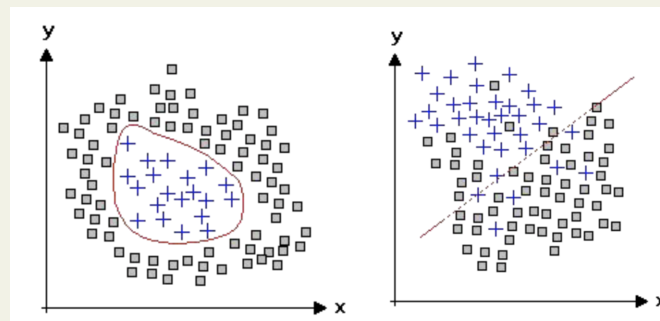


Figure 3:

### 0.1.4 Representations

**Notes:**

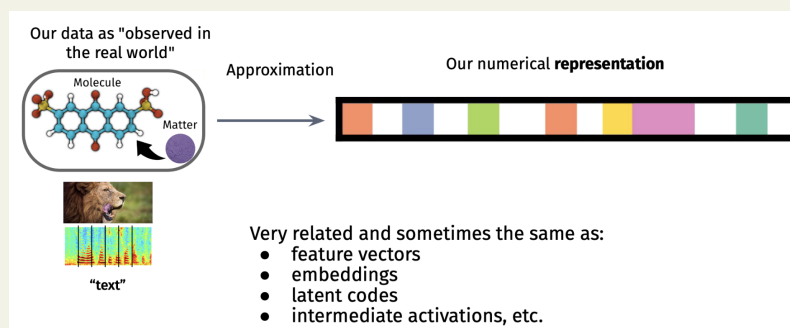


Figure 4:

## 0.2 Neural networks

**Definition:** Learnable (optimizable) transformations of data.

$$x \xrightarrow{\text{Model}} y \quad (3)$$

### 0.2.1 2-layer MLP

**Definition:**

$$\text{Link}(W_2 \cdot \text{relu}(W_1 \cdot x)) = y \quad (4)$$

- **E** (x and y)
- **P** ? mean squared error
- **T** ? Predict y from x
- **M** ? Neural net (W1, W2)
- **learn?** gradient descent

### 0.2.2 Geometric intuition

### 0.2.3 Encoder-Decoder view