# ECE324 Lectures

## Hanhee Lee

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### 1 Why Systems Software?

#### 1.0.1 Learning algorithm

#### 1.0.2 Linear regression

#### Example:

$$W \cdot x = y \tag{1}$$

- E: x, y
- P: Error rate (e.g. mean squared error)
- T: Predict y from x (i.e.  $\hat{y}$ )
- M: Linear model (W)
- Learn:

#### 1.1 Linear transformations

**Definition**: Transform from one vector space to another.

 $W \cdot x$ 

**Example**: Linear transformations warped to a prediction target.

$$Link(W \cdot x) = y$$

- x: Input features
- y: Output / target
- W: Linear transformation
- Link: Warping function
- If x has dim 50 and W projects to dimension 100, what is the shape of W?  $100 \times 50$ .
- If W is learnable, how many parameters does W have?  $100 \times 50 = 5000$ .

#### 1.2 How does a generalized linear model make a prediction?

Definition: By either mapping to a line (regression) or separating data by a line (i.e. hyperplane) (classification).

#### 1.3 Representation

#### **Definition:**

- Feature vectors
- Embeddings
- Latent codes
- Intermediate activations, etc.

#### 1.4 Neural networks

**Definition**: Learnable (optimizable) transformations of data

#### 1.4.1 2-Layer Neural Net (MLP)

**Example**: By stacking linear transforms with activation functions.

$$Link(W_2 \cdot relu(W_1 \cdot x)) = y$$

• E: x and y

- $\bullet\,$  P: Mean squared error
- $\bullet\,$  T: Predict y from x
- M: Neural net  $(W_1, W_2)$
- Learn: Gradient descent

#### 1.4.2 Encoder-Decoder View of Neural Networks

$$x \xrightarrow{\text{Encode}} z \xrightarrow{\text{Decode}} \hat{x}'$$

Language translation via text encoder/decoders.

Example: Using learned representations for new problems

Encoder and decoder view of Supervised Learning.

Example: PCA

### 1.5 Specifying an ML task

### 1.6 Landscape of tools and approaches

# 2 Kernels