











verified,

**Digital Signatures**













Fail!



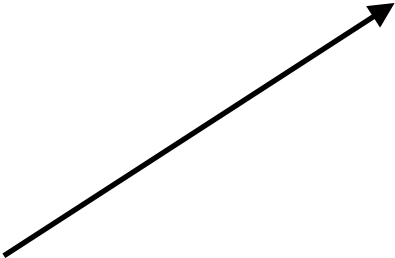






















verified,









Pass!

Desiderata

Security

Efficiency

**k bits of (multi-user)  
security**

**preprocessing attacks**

efficient signing/  
verification

**short signatures**



**Short Signature Schemes:**



**RSA-FDH**

**ECDSA**

**Schnorr**

**Short Schnorr**

**BLS**

**iO-based**

$w(k)$  bits

4k bits

$4k$  bits

$3k$  bits

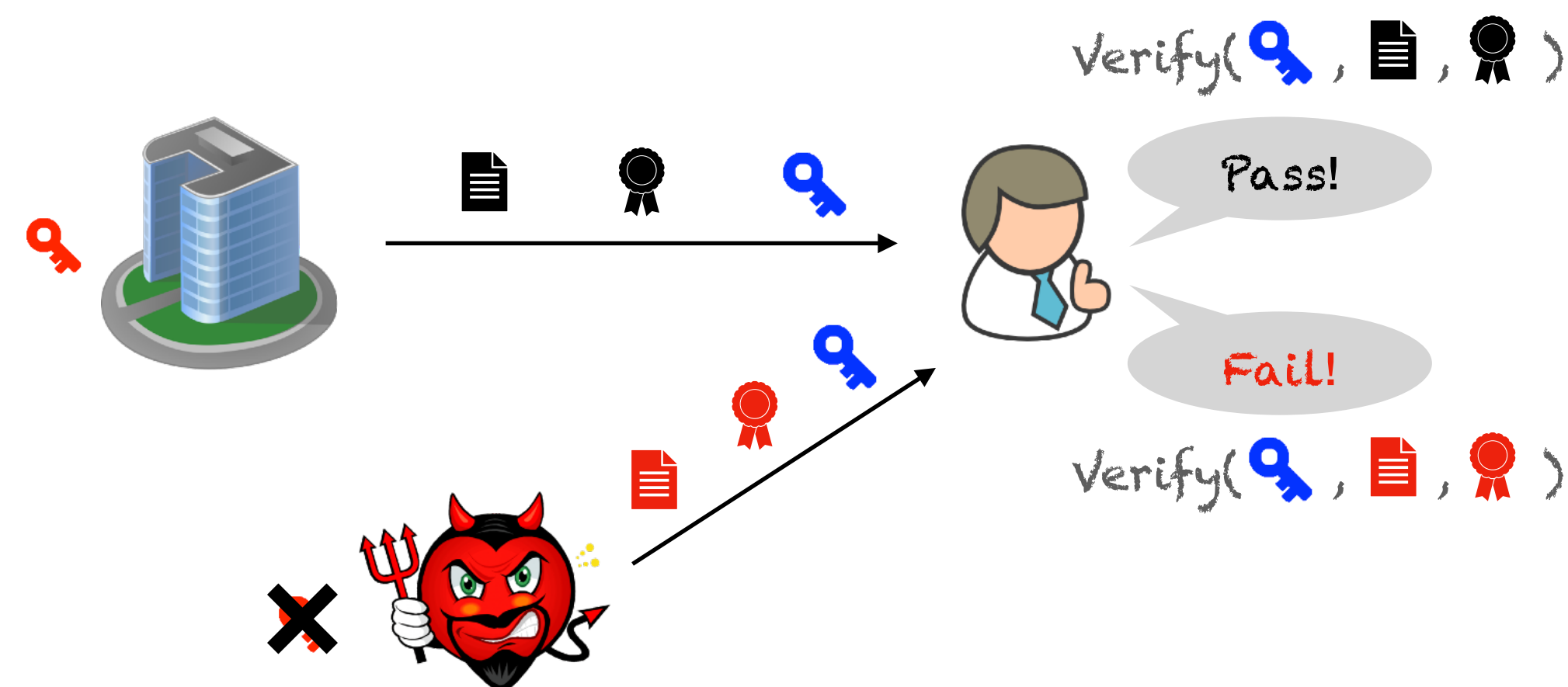
$2^k$  bits

$2^k$  bits



*k* bits

# Digital Signatures



Desiderata	
Security	Efficiency
k bits of (multi-user) security  preprocessing attacks	efficient signing/ verification  <b>short signatures</b>

## Short Signature Schemes:

RSA-FDH	<div></div>	$\omega(k)$ bits
ECDSA	<div></div>	$4k$ bits
Schnorr	<div></div>	$4k$ bits
Short Schnorr	<div></div>	$3k$ bits
BLS	<div></div>	$2k$ bits
iO-based	<div></div>	$k$ bits

# The (Short) Schnorr Signature Scheme

- **Public parameters:**

- ▷ Group  $G = \langle g \rangle$  of size  $p \approx 2^{2k}$ , where  $k$  is the security parameter
- ▷ Hash function  $H : \{0, 1\}^* \rightarrow \mathbb{Z}_p$

$\text{Kg}(1^k)$	$\text{Sign}(sk, m)$	$\text{Vfy}(pk, m, \sigma)$
1: $sk \leftarrow \mathbb{Z}_p$ 2: $pk \leftarrow g^{sk}$ 3: <b>return</b> $(pk, sk)$	1: $r \xleftarrow{\$} \mathbb{Z}_p; I \leftarrow g^r$ 2: $e \leftarrow H(I    m)$ 3: $s \leftarrow r + sk \cdot e \bmod p$ 4: <b>return</b> $\sigma = (s, e)$	1: $R \leftarrow g^s \cdot pk^{-e}$ 2: <b>if</b> $H(R    m) = e$ <b>then</b> 3: <b>return</b> 1 4: <b>else return</b> 0

1110101101101100011010101101011010101101

$2k$  bits

1010101101110101010101101011010010000010

$2k$  bits