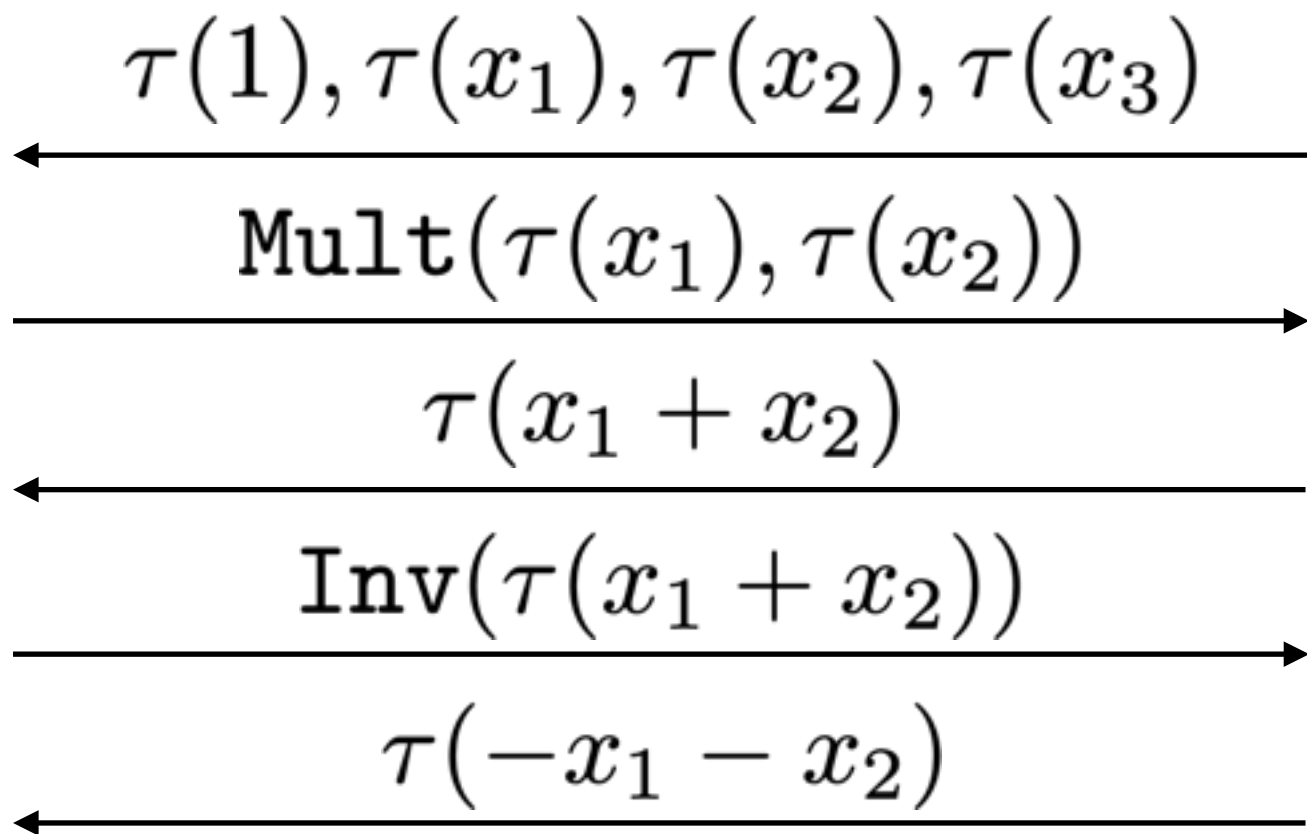


Bridge-Finding Game

in the Generic Group Model



$$(x_1, x_2, x_3)$$

$$y = \vec{a} \cdot \vec{x} + b$$

\mathcal{L}

$\tau(y)$	\vec{a}	b
$\tau(1)$	$(0, 0, 0)$	1
$\tau(x_1)$	$(1, 0, 0)$	0
$\tau(x_2)$	$(0, 1, 0)$	0
$\tau(x_3)$	$(0, 0, 1)$	0
$\tau(x_1 + x_2)$	$(1, 1, 0)$	0
$\tau(01101101)$	$(-1, -1, 0)$	0
$\tau(x_1 + 1)$	$(1, 0, 0)$	1
η	$(0, 0, 0)$	7
01101101	$(0, 1, 0)$	7
...

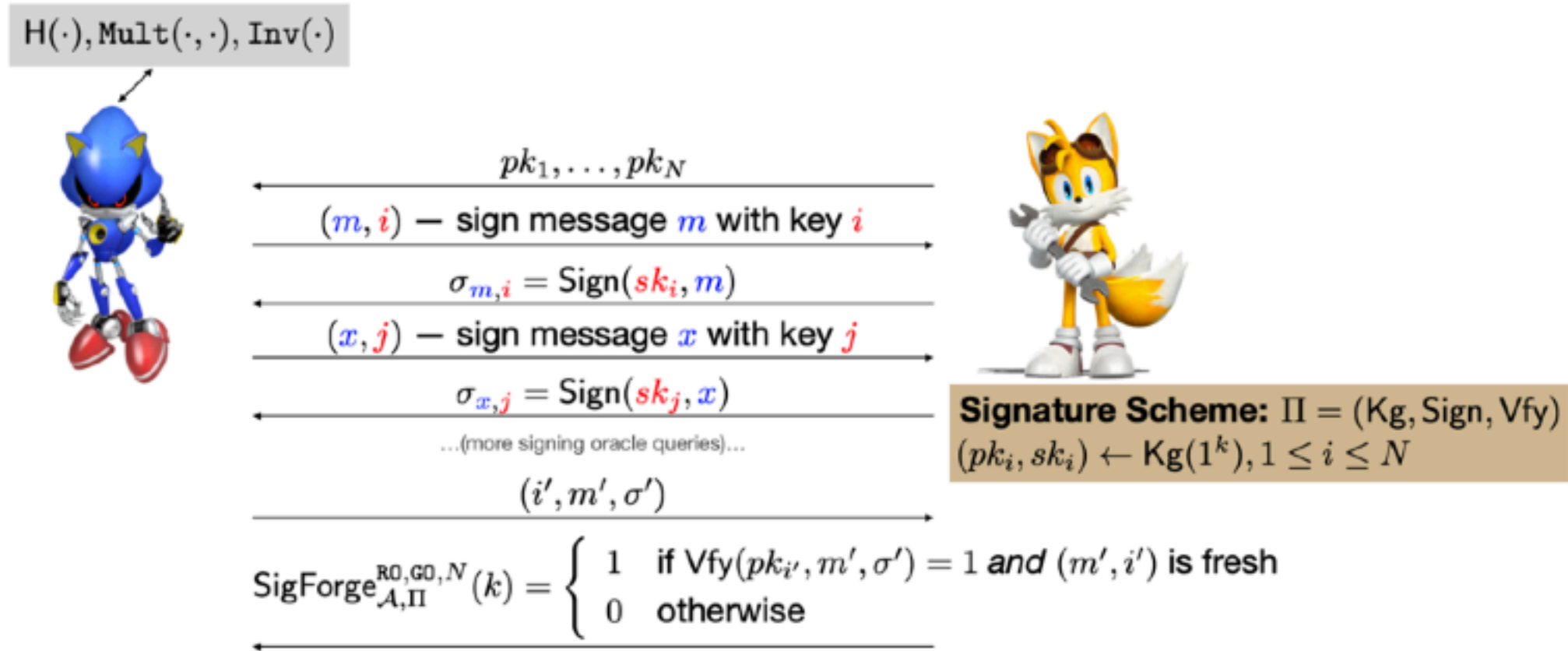
Bridge event since $\tau(-x_1 - x_2) = \tau(x_2 + 7) = 01101101$
but $((-1, -1, 0), 0) \neq ((0, 1, 0), 7)$

Then we learned

$$-x_1 - x_2 = x_2 + 7$$

Theorem (informal). $\Pr[\text{BRIDGE}] \leq \mathcal{O}\left(\frac{q^2 + qN}{p}\right).$

Multi-User Security of Short Schnorr Signatures in the ROM+GGM



$$\begin{aligned} \Pr \left[\text{SigForge}_{\mathcal{A}, \Pi}^{\text{RO}, \text{GO}, N}(k) = 1 \right] &\leq \Pr[\text{BRIDGE}] + \Pr[\text{Bad}] \\ &\leq \mathcal{O} \left(\frac{q^2 + qN}{p} + \frac{q}{2^k} \right) \\ &\leq \mathcal{O} \left(\frac{q + N}{2^k} \right), \end{aligned}$$

where $p \simeq 2^{2k}$.