

scalar and matrix operation

$$5 + \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 6 & 7 \\ 8 & 9 \end{bmatrix} \quad (1)$$

$$a + \mathbf{B} = \mathbf{C}$$

$$5 - \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 4 & 3 \\ 2 & 1 \end{bmatrix} \quad (2)$$

$$a - \mathbf{B} = \mathbf{C}$$

$$5 \cdot \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 5 & 10 \\ 15 & 20 \end{bmatrix} \quad (3)$$

$$a \cdot \mathbf{B} = \mathbf{C}$$

$$12 \div \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 12 & 6 \\ 4 & 3 \end{bmatrix} \quad (4)$$

$$a \div \mathbf{B} = \mathbf{C}$$

matrix and matrix operation

$$\begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ 5 & 6 \end{bmatrix} \quad (5)$$

$$\mathbf{A} + \mathbf{B} = \mathbf{C}$$

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} - \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \quad (6)$$

$$\mathbf{A} - \mathbf{B} = \mathbf{C}$$

$$\begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 4 & 6 \\ 8 & 12 \end{bmatrix}$$

(7)

$$\mathbf{A}\mathbf{B} = \mathbf{C}$$

$$\begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix}^{-1} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

(8)

$$\mathbf{A}\mathbf{A}^{-1} = \mathbf{I}$$

Hadamard product

$$\begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} \odot \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 6 & 8 \end{bmatrix}$$

(9)

$$\mathbf{A} \odot \mathbf{B} = \mathbf{C}$$

Dot product

when $\mathbf{a} = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$ and $\mathbf{b} = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$

$$\mathbf{a} \cdot \mathbf{b} = \mathbf{a}^T \mathbf{b} = \begin{bmatrix} 1 & 2 \end{bmatrix} \begin{bmatrix} 3 \\ 4 \end{bmatrix} = 11$$

(10)

linear equation

$$\boldsymbol{A}\boldsymbol{x} = \boldsymbol{b} \tag{11}$$

$$\begin{bmatrix} a_0 & a_1 \\ a_2 & a_3 \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} = \begin{bmatrix} b_0 \\ b_1 \end{bmatrix} \tag{12}$$

$$\begin{aligned} b_0 &= a_0x_0 + a_1x_1 \\ b_1 &= a_2x_0 + a_3x_1 \end{aligned} \tag{13}$$

Linear Dependence and Span

$$equation \tag{14}$$

Norm

$$L^p = \|\boldsymbol{x}\| \tag{15}$$

$$L^2 = \boldsymbol{x}^T \boldsymbol{x} \tag{16}$$