Value Conversion in IL1 after Lambda Hoisting

Given the closure-conversion and then hoisted restricted language IL1 detailed below

$$\begin{split} v &::= n \mid x \mid \mathsf{halt} \\ e &::= v \mid v_0 + v_1 \mid (v_0, \cdots, v_n) \mid \pi_n v \\ c &::= \mathsf{let} \, x = e \, \mathsf{in} \, c \mid v_0 \, v_1 \, v_2 \mid v_0 \, v_1 \end{split}$$

we want to "lift" numbers and halt into expressions (as Val used in bindings only) and leave only variables as values, so in effect our language will now look like

$$\begin{split} v &::= x \\ e &::= v \mid \mathsf{val}(n) \mid \mathsf{val}(\mathsf{halt})v_0 + v_1 \mid (v_0, \cdots, v_n) \mid \pi_n v \\ c &::= \mathsf{let} \ x = e \mathsf{in} \ c \mid v_0 \ v_1 \ v_2 \mid v_0 \ v_1 \end{split}$$

We want to define a set of "lowering" translation $\mathcal{LV}[v]$, $\mathcal{LE}[e]$, $\mathcal{LC}[c]$ that binds all non-variable values (integers and halts) into their own variables. Therefore, we need to have both the value and the expressions translation be able to be abstracted as bindings.

$$\begin{split} \mathcal{LV}[\![v]\!] : (\mathsf{var} \times e) \mathsf{list} \times \mathsf{var} \\ \mathcal{LE}[\![e]\!] : (\mathsf{var} \times e) \mathsf{list} \times \mathsf{e} \\ \mathcal{LC}[\![c]\!] : c \end{split}$$

We will use the notation

$$let x_i = e_i in x$$

to mean

$$([(x_i,e_i);\cdots(x_n,e_n)],x)$$

and respective syntax sugary for expressions.

1 Values

$$\begin{split} \mathcal{LV}[\![n]\!] &= \mathsf{let}\, x = n \, \mathsf{in}\, x \\ \mathcal{LV}[\![x]\!] &= ([],x) \\ \mathcal{LV}[\![\mathsf{halt}]\!] &= \mathsf{let}\, x = \mathsf{halt}\, \mathsf{in}\, x \end{split}$$