

# Variational Curriculum Reinforcement Learning for Unsupervised Discovery of Skills

Seongun Kim<sup>\*1</sup>, Kyowoon Lee<sup>\*2</sup>, Jaesik Choi<sup>1</sup>

<sup>\*</sup>Equal Contribution    <sup>1</sup>KAIST    <sup>2</sup>UNIST

## Motivation

How can we train robot policies efficiently

- without crafting the order of training skills and
- without manually engineering objective functions
- to achieve complex skills for our learning agent?

## Contributions

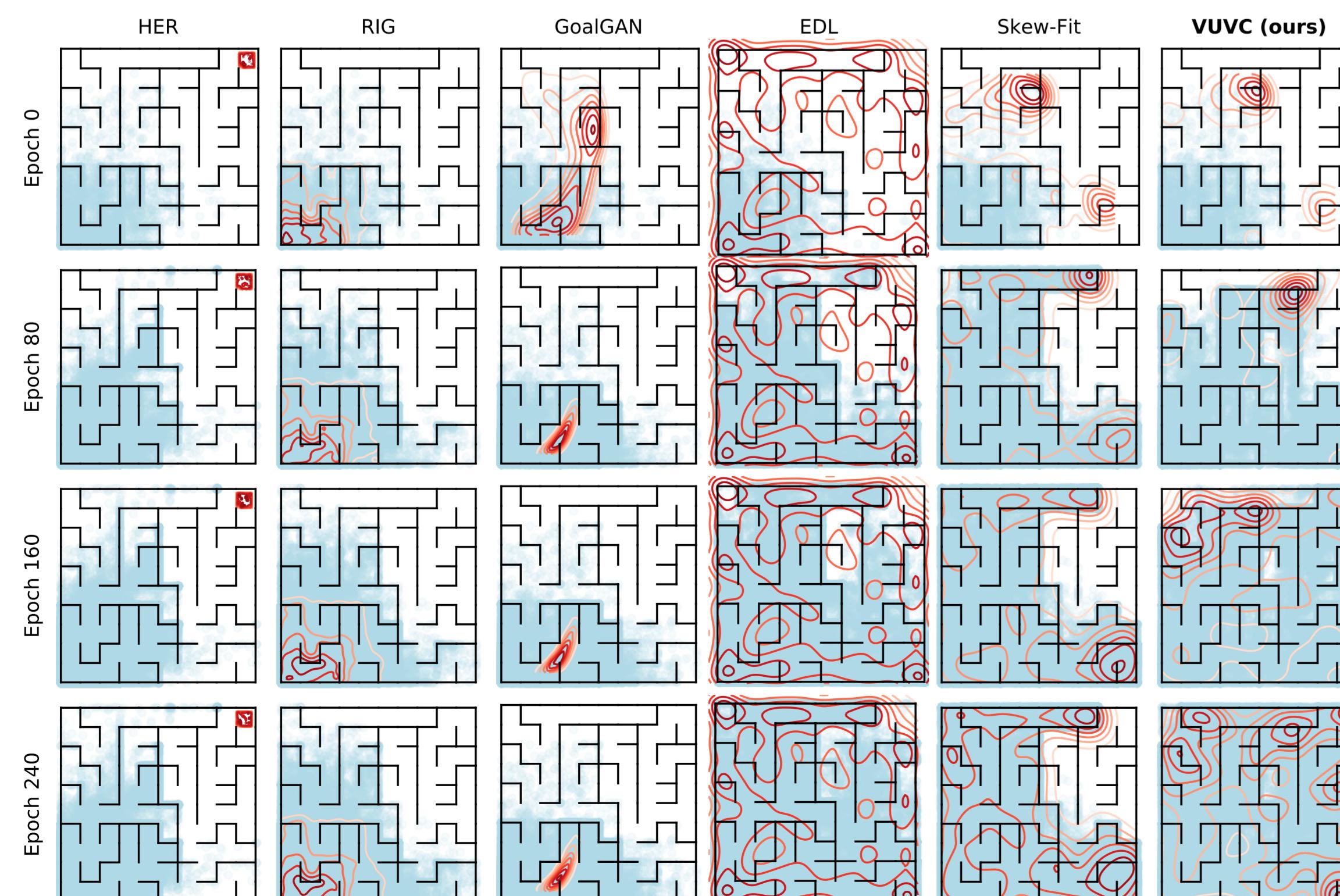
- Provide the unifying framework Variational Curriculum Reinforcement Learning (VCRL) encapsulating most of the prior mutual information based approaches.
- Propose Value Uncertainty Variational Curriculum (VUVC), a value uncertainty based approach to information-theoretic skill discovery.

## Variational Curriculum Reinforcement Learning (VCRL)

- Recast variational empowerment as curriculum learning in goal-conditioned RL.
- Objective of variational empowerment is to maximize a variational lower bound:

$$\mathcal{F}(\theta, \lambda) = \mathbb{E}_{\substack{g \sim p(g), \\ s \sim \rho^{\theta}(s|g)}} [\log q_{\lambda}(g|s) - \log p(g)], \quad (1)$$

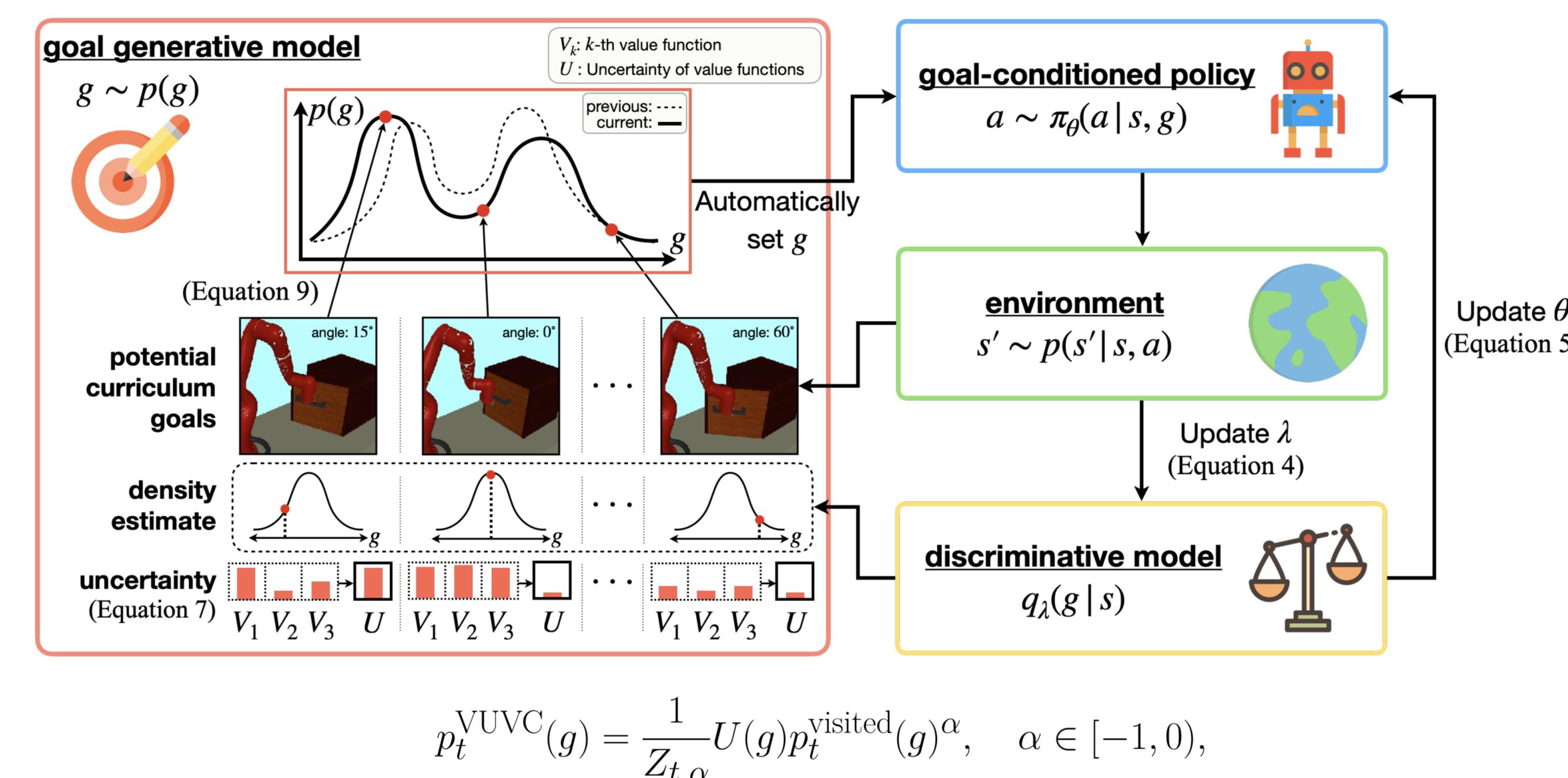
Methods	$q_{\lambda}(g s)$	$p(g)$	Non-stationary goal distribution
GCRL (w/ sparse reward)	$\frac{1}{Z} \exp(1 - 2\delta_g \mathcal{U}_{[s \pm \delta_g]})$	$p_{\text{target}}(g)$	✗
GCRL (w/ dense reward)	$\mathcal{N}(s, \sigma^2 I)$	$p_{\text{target}}(g)$	✗
EDL	$\mathcal{N}(\mu(s), \sigma^2 I)$	$p_{\text{explored}}(g)$	✗
RIG	$\mathcal{N}(\mu(s), \sigma^2 I)$	$p_t^{\text{visited}}(g)$	✓
Skew-Fit	$\mathcal{N}(\mu(s), \sigma^2 I)$	$\propto p_t^{\text{visited}}(g)^{\alpha}$	✓
<b>VUVC (ours)</b>	$\mathcal{N}(\mu(s), \sigma^2 I)$	$\propto U(g)p_t^{\text{visited}}(g)^{\alpha}$	✓



## Value Uncertainty Variational Curriculum (VUVC)

- Approach for unsupervised discovery of skills which utilizes a value uncertainty for an increment in the entropy of the visited state distribution.

### Value Uncertainty Variational Curriculum



$$p_t^{\text{VUVC}}(g) = \frac{1}{Z_{t,\alpha}} U(g) p_t^{\text{visited}}(g)^{\alpha}, \quad \alpha \in [-1, 0], \quad (2)$$

where  $Z_{t,\alpha}$  is the normalizing coefficient.

### Definition: Expected Entropy Increment over Uniform Curriculum

Given the empirical distribution of the visited state

$$p_t^{\text{visited}}(s) = \sum_{i=1}^t \frac{\mathbb{I}(s_i = s)}{t}, \quad (3)$$

where  $\mathbb{I}(\cdot)$  is an indicator function, uniform curriculum goal distribution  $p_t^{\mathcal{U}}$  and value uncertainty-based curriculum goal distribution  $p_t^{\text{VU}}$  are defined as follows:

$$p_t^{\mathcal{U}}(g) = \mathcal{U}(\text{support}(p_t^{\text{visited}}))(g), \quad (4)$$

$$p_t^{\text{VU}}(g) = \frac{1}{Z_t} U(g) p_t^{\mathcal{U}}(g), \quad (5)$$

where  $Z_t$  is the normalizing coefficient,  $p_t^{\mathcal{U}}$  is uniform over the support of  $p_t^{\text{visited}}$  and  $U(g)$  is the value uncertainty. Then the expected entropy increment over uniform curriculum  $I_t$  is defined as

$$I_t = \mathbb{E}_{g \sim p_t^{\text{VU}}} [\mathcal{H}(p_{t+1}^{\text{visited}})] - \mathbb{E}_{g \sim p_t^{\mathcal{U}}} [\mathcal{H}(p_{t+1}^{\text{visited}})]. \quad (6)$$

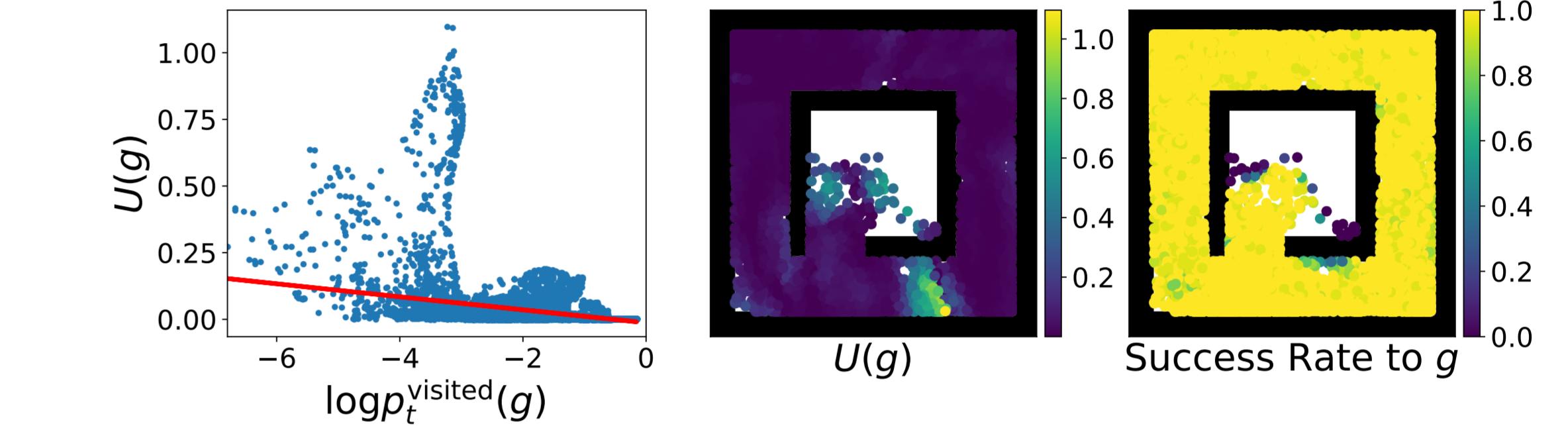
### Proposition: VUVC Is At Least Better Than The Uniform Curriculum

With an accurate goal-conditioned policy and the model of dynamics, VUVC accelerates the increase of entropy in the visited states compared to the uniform curriculum, if the uncertainty of the learned value functions  $U(g)$  and the log density of  $p_t^{\text{visited}}$  are negatively correlated.

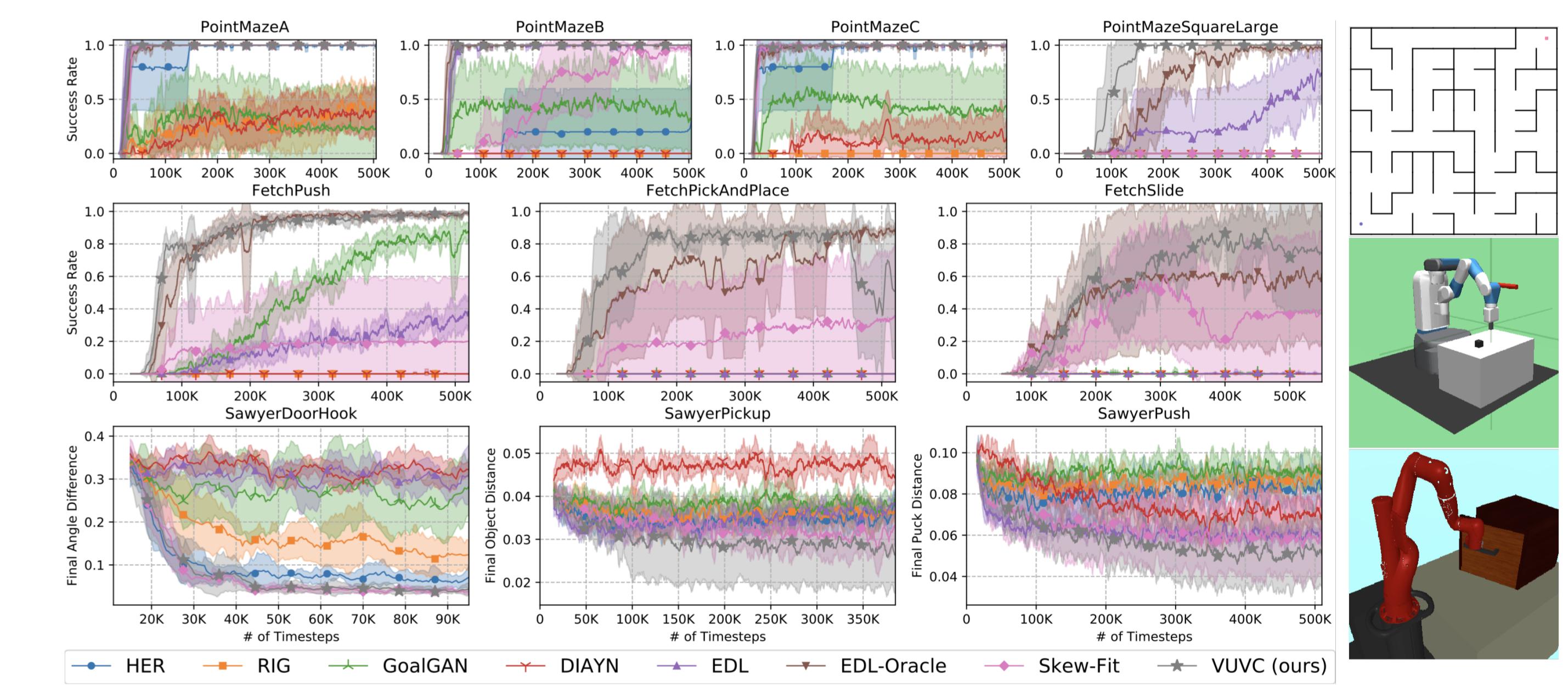
**Proof Sketch.** We begin by deriving a next step empirical distribution of the visited state given a curriculum goal  $g$  and a stationary state distribution induced by the policy  $\rho^{\pi_{\theta}}(s|g)$ , which can be written as  $p_{t+1}^{\text{visited}}(s) = \frac{p_t^{\text{visited}}(s) + \epsilon \rho^{\pi_{\theta}}(s|g)}{1+\epsilon}$ . Plugging this back into above Definition, we analyze asymptotic behavior of the expected entropy increment and obtain the conclusion.

## Experiments

### Impact of Value Uncertainty



### Comparison of Sample Efficiency



### Deploying Skills on the Real-world Robot

