

MTHM005: MATHEMATICAL SCIENCES PROJECT

Pricing Asian Options

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Abstract

November 16, 2022

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Chapter 1: Introduction

This report studies a vital financial derivative in today's markets, namely options. The importance of the option market has been shown by empirical studies which suggest that option trading improves information efficiency in the broader stock market [PP06; Li21], and also that firms with listed options experience lower implied cost of equity capital [NNT13]; indicating that options trading reduces the cost of capital [Li21]. The popularity of the options market can easily be seen in Figure 1.1, which shows the exponential growth in trading volume since standardized, exchange-traded stock options were first listed in The Chicago Board Options Exchange in 1973 [Mar02]. In 2020 single stock option trading volume became higher than the underlying stock volume for the first time ever [Fin20].

It is this explosive popularity and significance which have motivated this report. We will begin by describing standard options and explore popular methods that are used to price them. We will then move onto Asian options and look at the literature surrounding how to price them before implementing several pricing methods with the use of MATLAB. Furthermore, we will then take an analytical approach to determine how Asian options can be priced accurately and efficiently.

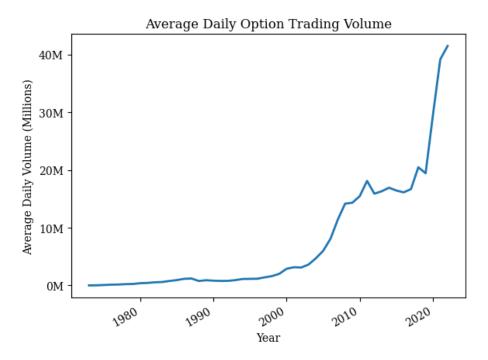


Figure 1.1: Time series plot of the average daily option trading volume per annum. Data provided by the Options Clearing Corporation (OCC) [Cor22]. Source code: Listing B.1

1.1 A brief overview of call and put options

Options are a particular type of financial derivative, a contract that details the conditions under which payments are made between two counterparties. They are purchased for a set fee, and in return the buyer is granted the right, but not the obligation to buy or sell an underlying asset — such as commodities, stocks or bonds — for a predetermined price (the strike price) on or before a determined date (the expiry date).

Call options allow the buyer to purchase an asset for the strike price at a future date. The buyer can make a return if the value of the asset is worth more than the strike price when exercised. Alternatively, put options allow the buyer to sell an asset for the strike price at a future date and the buyer can make a return if the value of the asset is less than the strike price when exercised.

The option market is widely considered a venue for informed trading [Li21; Hu14; CGM04], that is, investors trading with superior knowledge of the probability distribution of share prices, through either access to private information or skillful processing of public information [Gro75].

1.1.1 A short history of option trading

The history of financial options can be traced as far back as 6th century BCE when ancient Greek mathematician and philosopher Thales of Miletus predicted through his astrological knowledge there was going to be a great olive harvest. As he did not have much money, he used what he had as a deposit on the rights to the local olive presses; due to no competition he secured this at a relatively low price. When the harvest proved to be bountiful leading to high demand, Thales charged a high price for use of the presses and reaped a considerable profit. His deposit gave him the right but not the obligation to hire the presses, thus his losses were limited to his initial deposit [Ins12; Ari77].

Whilst this is quite a positive look on option trading, throughout history this has not always been the case. During the Dutch tulip bubble of the seventeenth century, tulips were seen as a status symbols which caused high demand and consequently drove their prices up, creating a bubble [Das11]. Tulip growers would buy puts to protect their profits in case the price of tulip bulbs went down and wholesalers would buy calls to protect against the risk of tulip bulbs going up. When the bubble eventually burst, there was no way to force investors to fulfil their obligations of the options contracts, due to the unregulated nature of the option market. This ultimately led to options gaining a dubious reputation and bans were later placed on them within Britain between 1733-1860 [Poi08].

During the late nineteenth century, brokers started to arrange deals between buyers and sellers of options for particular stocks at prices that were arranged between the two parties. Trades were arranged similarly until the 1960s when the options market started to become regulated by the Chicago Board of Trade. In 1973, the Chicago Board of Options Exchange (CBOE) began trading and for the first time options contracts were properly standardized. At the same time, the Options Clearing Corporation was established for centralized clearing and enforcing the proper fulfillment of contracts, ensuring that they were honored [Mar02].

1.1.2 Standard options

A standard option comes in two styles; European: which restricts the holder of the option to only exercise the option on the expiry date, and American: which allows the holder to exercise the option at anytime up till or on the expiry date. They will take the current value of the underlying asset as the spot price — that is the price that the asset can be purchased for on the open market. The payoff in this case then becomes the difference between the spot price and strike price.

1.1.3 Asian options

Whilst standard options involve using the spot price as the underlying value of the asset; this is not always the case with so-called exotic options. Exotic options differ in their payment structures, expiration dates, and/or strike prices. In the case of exotic fixed-strike price Asian options, the average price of the asset is used in place of the underlying asset value. This differs from fixed-price Asian options which instead use the average price of the asset to take place of the strike price. These are the two main variations of Asian style options but both of these can be varied further in how the averaging is calculated, for example: geometrically, arithmetically, average taken every day or average taken at the start of each month and so on. They can be varied further by having an expiry structure matching a European or American style option.

1.2 Market definition and assumptions

To begin pricing options we must first establish assumptions on the value of assets and the market in which they are traded. We will consider a market in which there are two classes of assets; risk-free assets and risky assets. We allow derivatives to exist on risky assets.

1.2.1 Asset definitions

We define our two classes of assets with the following assumptions:

Risk-free assets

Risk-free assets are assumed to have no uncertainty in regard to their future value and defined as returning interest continuously compounded at a fixed rate r. Hence, an investment of A made at time t will return $A^{r(T-t)}$ at time T > t with no uncertainty. These can be positive e.g., making an investment, or negative e.g., taking out a loan. Risk-free assets are akin to fixed rate investments at a well-know bank or government bonds. However, even sovereign nations have been known to default on their bond repayments so in reality are not truly risk-free, but instead considered low-risk [Kit+15].

Risky assets

Risky assets are assets in which the future value can not be determined without at least some uncertainty. These are typically shares in a company or commodities such as gold or oil. These assets are traded on the open market and their value is heavily dependent on the balance of supply and demand of the asset; this in turn is dependent on so many variables that we assume their future value to be a random process. Depending on our model we can make different assumptions on the distribution of the process and thus how the value evolves over a time period. In practice there are people who argue that future value of risky assets are truly random [Fam65], whilst others believe they can be at least partly deterministic where patterns and trends exists [SP85].

1.2.2 Market Assumptions

We shall assume that an investor may hold any quantity (including negative and/or fractional) of an asset, known as divisibility and short-selling assumption. We will also assume that our market is frictionless — that is that any quantity of assets can be bought and sold at the same price with no transaction cost and are entirely liquid meaning there is always a buver for every seller and vice versa.

In practice these assumptions do not accurately represent the real markets, for example it is common place for markets to have bid-ask spreads which represents the different in price at which you can buy and sell assets for. Furthermore, transaction costs are impossible to fully eliminate — even in scenarios with no tax or commission fees, buying or selling assets (especially in large quantities) will in theory have an effect on the supply and demand of that asset; this introduces market impact costs [Mor+09]. There are other transaction fees to also consider such as: time spent deciding what assets to buy, computing power costs and their associated opportunity costs.

No-Arbitrage assumption

Perhaps our most important market assumption is the No-Arbitrage principle; sometimes referred to as the no free-lunch principle. This assumption states that there can be no risk-free way to get a better rate of return than the market risk-free interest rate, r. The logic behind this assumption is that if there exists a way to earn a higher rate of return than r with no initial outlay; than other traders would employ the same method and market forces would eliminate the arbitrage opportunity. This assumption assumes that markets are perfectly efficient meaning all traders have access to the same information and that market adjustments to supply and demand happen instantaneously, which we know not to be true in practice.

1.3 Asset pricing models

Having now established our market assumptions, we must now define our assumptions on the random process which describes how the asset value may evolve over a specified time period. We will first introduce the mathematical concepts in which these models are built upon. Then we will introduce a simple asset model and one which has more assumptions in hopes of better describing the future asset value in practice.

1.4 Pricing options

Since the holder of the contract is not obliged to exercise the contract at the expiry time, they do not hold any liability in the absence of a price to purchase the option. The problem then becomes, what is the correct price to charge the holder of the option to balance this inequality of liability.

1.4.1 Pricing standard options

Binomial method

Black-Scholes Formula

1.4.2 Pricing Asian options

Hull-White model

Costabile adjusted binomial method

Analytical solution for geometric average Asian options

1.4.3 Monte-Carlo method

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Appendices

A Matlab Files

All files can be found: https://github.com/leele2/Mathematics-in-Business-Project/tree/master/MATLAB%20Files

Listing A.1: ../../MATLAB Files/BinoAsian.m

```
%function BinoAsian(SO,E,T,r,sigma,N,F)
   addpath('Functions')
   % Test
   \texttt{clear}\;;\;\;\texttt{tic}\;;\;\;S0=100;\;\;E=100;\;\;T=0.25;\;\;r=0.1;\;\;\texttt{sigma}=0.1;\;\;N=10;\;\;F=@(S,A)\max(A-E,0)\;;
   1 Function to evaluate European Call option by Binomial Method
         S0 = initial share price
         E = exercise price
        T = time to expiry
10 %
         r = riskfree interest rate
         sigma = volatility
   %
         N = Number of steps
         F = Option Payoff (European Call in given)
14 % Calculated parameters
   dt
          = exp(sigma*sqrt(dt));
                                           %Up price movement
   u
          = 1/u;
                                           %Down price movement
   disf = \exp(-r*dt);
                                           %Discount factor over each timestep
          = (1/disf - d)/(u-d);
                                           %Risk-neutral probability
   р
   % Initalizing Arrays and Functions
           = zeros(N+1,N+1);
                                       %Underlying Asset Price
                                       %S_max %% Cells are used so different sized vectors can be stored at each element in
           = \operatorname{cell}(N+1,N+1);
           cell array
   Α
           = zeros(N+1,N+1);
                                       %Average of Underlying Asset Price
                                       %Representitive averages
   A_k
           = cell(N+1,N+1);
           = zeros(N+1,N+1);
                                       %Price of Option
            = \operatorname{cell}(N+1,N+1); %Option price for given representitive avg = \operatorname{@}(S,A)\max(A-E,0); %Option Payoff (European Call)
26
   C_{-k}
           = \operatorname{cell}(N+1,N+1);
   30
   % Calculate Underlying asset price
   \quad \quad \text{for} \quad i \ = \ 0 : N
         for j = 0:i
              \ddot{S}(i+1,j+1) = S0*u^{(j)}*d^{(i-j)};
         end
36
   end
   % Calculating All S_max and Representitive Averages
   for i = 0:N
         \begin{array}{lll} \text{for } j=0\text{:}i \text{ \%j indexes at } j+1 \text{ due to matlab not allowing } C\text{-}k\left\{\text{:},0\right) \\ A\text{-}k\left\{\text{i}+1,j+1\right\} = zeros\left(j*(i-j)+1,1\right); \text{ \%Create Vector to hold rep avgs } S\text{-}k\left\{\text{i}+1,j+1\right\} = NaN\left(j*(i-j),1\right); \text{ \%Create Vector to hold } S\text{-max} \end{array}
40
                                                              \mbox{\ensuremath{\mbox{$\%$}}} Assign A\_{max} to first element in vector
              A_k\{i+1,j+1\}(1) = A_max(i,j);
              \% Paths with only up (i = j) or down movements (j = 0) or i = 1 will only have one representative
                    average
               if i < 1 | i == j | | j == 0
                    S_{-k}\{i+1,j+1\}(1) = S0*(u^j)*d^(i-j);
45
47
              end
              7 Filling S_max Vector
49
              \% Setting Paramaters
                                         %Size of vector
              n = j*(i-j);
               rep = min([j;i-j]); %Maximum element repetition in vector
51
              % Calculating unique elements in vector
               {\tt unique} \ = \ 2*{\tt numel} \, (\, 1\, \colon\! {\tt rep}\, -1) \ + \ (\, {\tt n} \ - \ (\, 2*{\tt sum} \, (\, 1\, \colon\! {\tt rep}\, -1)\, )\, )\, /\, {\tt rep} \, ;
54
              % First and last values
              \begin{array}{lll} S_{-k}\{\,i\!+\!1,j\!+\!1\}(1) &= S0 * (u \hat{\ } j)\,; \\ S_{-k}\{\,i\!+\!1,j\!+\!1\}(\text{end}) &= S0 * (u \hat{\ } (j-\text{unique}+1))\,; \end{array}
56
              if n = 2

% Ascending/Descending repeated values
k = 2; %iterator
count = 2; %Number of elements filled
58
59
60
                         % Filling from top
64
                         S_{-k}\{i+1,j+1\}(sum(1:k-1)+1:sum(1:k-1)+k) = repmat(S0*(u^(j-k+1)), k, 1);
                         % Filling from bottom
                         S_{-k}\{i+1,j+1\}(n-sum(1:k-1)+1-k:n-sum(1:k-1)) = repmat(S0*(u^(j-unique+k)), k, 1);
                         count = count + 2*k;
                         k = k + 1;
69
                    % "Middle" repeated values
                    for l = 0: (n-count)/rep - 1
                         S_{k}(i+1,j+1)(count/2+1+1*rep:end) = [repmat(S0*u^{(j-k+1)}, rep, 1);
                               S_k\{i+1,j+1\}(count/2+1+1*rep+rep:end)];
```

```
k = k + 1;
                      end
 76
 77
78
                % Calculating Representitive Averages Using S_max
                 A_{-k}\{i+1,j+1\}(j*(i-j)+1) = A_{-min}(i,j); \text{ $\%$ Assign $A_{-min}$ to last element in vector } in \text{ $A_{-k}(i+1,j+1)$} 
                 for k = 2 : j * (i-j)
 80
                       A_{-}k\{\,i\,+\!1,\,\dot{j}\,+\!1\,\!\bigr\}(k)\ =\ A_{-}k\{\,i\,+\!1,\,j\,+\!1\}(k\!-\!1)\ -\ (1/(\,i\,+\!1))\,*\ \dots
81
                             (S_{k}\{i+1,j+1\}(k-1) - S_{k}\{i+1,j+1\}(k-1)*(d^{2}));
82
                 end
83
           \quad \text{end} \quad
84
     end
85
    7% Pricing Option Value at Final Time (N)
86
     for
          i = 0:N
87
           C_{-k}\{N+1, j+1\} = F(S(N+1, j+1), A_{-k}\{N+1, j+1\});
88
     end
    %% Pricing Option
89
90
     err = 1e-3:
     for i = N-1:-1:0
           \begin{array}{ll} \text{for } j = 0 \colon i \\ & \text{C-k}\{i\!+\!1, j\!+\!1\} = z \text{eros}\left(j * (i\!-\!j)\!+\!1, 1\right); \\ & \text{for } k = 1 \colon j * (i\!-\!j)\!+\!1 \end{array}
                      % Find K_u
                      \begin{array}{lll} Ku & = & (& (\,i\,+1)\,*\,A_-k\,\{\,i\,+1\,,\,j\,+1\}(\,k\,) & + & u\,*\,S\,(\,i\,+1\,,\,j\,+1) & )\,\,/\,(\,i\,+2)\,; \end{array}
96
                      [loc, ubound, lbound] = findInSorted(Ku, A_k{i+2,j+2},err); % If found set accordingly
                       if loc > 0
                             Cu = C_k\{i+2,j+2\}(loc);
                       else
                            \% If not found, interpolate between closest values
                             Cu = C_k\{i+2,j+2\}(lbound) + (Ku-A_k\{i+2,j+2\}(lbound)) * (...
                                   \begin{array}{l} (C_{-k}\{\,i+2,j+2\}(ubound)-C_{-k}\{\,i+2,j+2\}(lbound))/...\\ (A_{-k}\{\,i+2,j+2\}(ubound)-A_{-k}\{\,i+2,j+2\}(lbound)))\,; \end{array}
                      % Find K_d
                      Kd = ((i+1)*A_k\{i+1,j+1\}(k) + d*S(i+1,j+1))/(i+2);
                       [loc, ubound, lbound] = findInSorted(Kd, A_k\{i+2, j+1\}, err);
                      %If found set accordingly
                       if loc > 0
                             Cd = C_{-k}\{i+2,j+1\}(loc);
                            %If not,
114
                                          interpolate between closest values
                             Cd = C_k\{i+2,j+1\}(lbound)+(Kd-A_k\{i+2,j+1\}(lbound))*(...
                                   (C_k\{i+2,j+1\}(ubound)-C_k\{i+2,j+1\}(lbound))/...
                                   (A_k\{i+2,j+1\}(ubound)-A_k\{i+2,j+1\}(lbound));
118
119
                      % Calculate option value at previous node (i, j decreasing)
                       C_{k}\{i+1,j+1\}(k) = disf*(p*Cu + (1-p)*Cd);
     disp(C-k{1,1})
    toc;
```

Listing A.2: ../../MATLAB Files/Functions/findInSorted.m

```
function [loc, A, B] = findinSorted(x, range, err)
  \% x = value to find
  % range = (sorted) vector to search
  % err = tolerence on search
  % Outputs
  A
                    %left boundary
     = 1;
     = numel(range); %right boundary
                    %initially set to 0 implying not found
  loc = 0:
  % Binary Search Algorithm
  while B-A > 1
      mid = floor((A\!\!+\!\!B)/2);
      if x > range (mid)
B = mid;
      else
         A = mid;
      end
18
  end
  MR Returning returned value if found (within tolerance)
  if abs(range(A) - x) < err
      loc = A;
23
      return
  elseif abs(range(B) - x) < err
      loc = B;
      return
  end
```

B Python Files

All files can be found: https://github.com/leele2/Mathematics-in-Business-Project/tree/master/Python%20Files

Listing B.1: ../../Python Files/OptionVolume.py

```
#_-*- coding: utf-8 -*-
   Created on Wed Jun 8 18:05:55 2022
  Scraping and plotting data from theocc.com
   @author: leele2
  \begin{array}{ll} import & \text{pandas} & as & \text{pd} \\ import & \text{matplotlib} & as & \text{mpl} \end{array}
   import matplotlib.pyplot as plt
   import matplotlib.dates as mdates
   from datetime import datetime
  from bs4 import BeautifulSoup
13
   from os import listdir
  from pathlib import Path
14
   def string_to_int(string):
       if not string:
17
18
           return 0
       if string [0] == "$":
19
           string = string[1:]
       return int(string.replace(',','))
21
23
  \# Ensuring html file is on path
   html file taken from:
  https://www.\ theocc.com/Market-Data/Market-Data-Reports/Volume-and-Open-Interest/Historical-Volume-Statistics
  html_file = [f for f in listdir('.') if f.endswith('.html')]
   if len(html_file) != 1:
       raise ValueError ('should be exactly one html file in the current directory')
  # Importing html file
31
  with open(html_file[0], 'r', encoding='utf-8') as file:
       soup = BeautifulSoup(file, 'lxml')
33
  # Finding Table
  table = soup.find_all("table")
35
  # Selecting Data
table_data = table[0].find_all("tr")
# Finding Table Names
36
37
  table_names = []
39
  for names in table_data[0]:
40
       table_names.append(str(names.find("span").string))
41
   del table_names [0]
42
  del table_names [-1]
43
  # Finding Headers
44
  headers = []

for header in table_data[1]:
45
46
       headers.append(str(header.find("span").string))
47
  # Populating Data
48
  Data = \{\}
49
  for rows in table_data[2:]:
      50
51
52
53
54
       Date = datetime.strptime(temp["Date"], "%\")

del temp["Date"]
55
56
       Data[Date] = \{k: string\_to\_int(v) \text{ for } k, v \text{ in } temp.items()\}
57
58
   # Converting data into pandas dataframes
  Data = pd.DataFrame.from_dict(Data, orient="index")
60
  # Plotting time-series
  plt.rc('font', family='serif')
  fig , ax1 = plt.subplots()
  plt.gcf().set_size_inches (6, 4.5)
ax1.plot(Data['Options']/1e6, linewidth=2, zorder=1, label="Options")
# ax1.plot(Data[Data['Futures'] != 0]['Futures']/1e6, linewidth=2, zorder=1, label="Futures")
   # ax1.legend()
  axl.set_title('Average Daily OptionS Trading Volume')
axl.set_xlabel('Year')
  ax1.xaxis.set_minor_formatter(mdates.DateFormatter("%Y"))
  ax1.set_ylabel('Average Daily Volume (Millions)'
  ax1.yaxis.set_major_formatter(mpl.ticker.StrMethodFormatter('{x:,.0f}M'))
  fig.autofmt_xdate()
  plt.tight_layout()
  plt.show()
  # Saving plot
```