

SENSORS





---

## *Robotics 1*

# **Robot components: Introduction, Actuators, Transmissions**

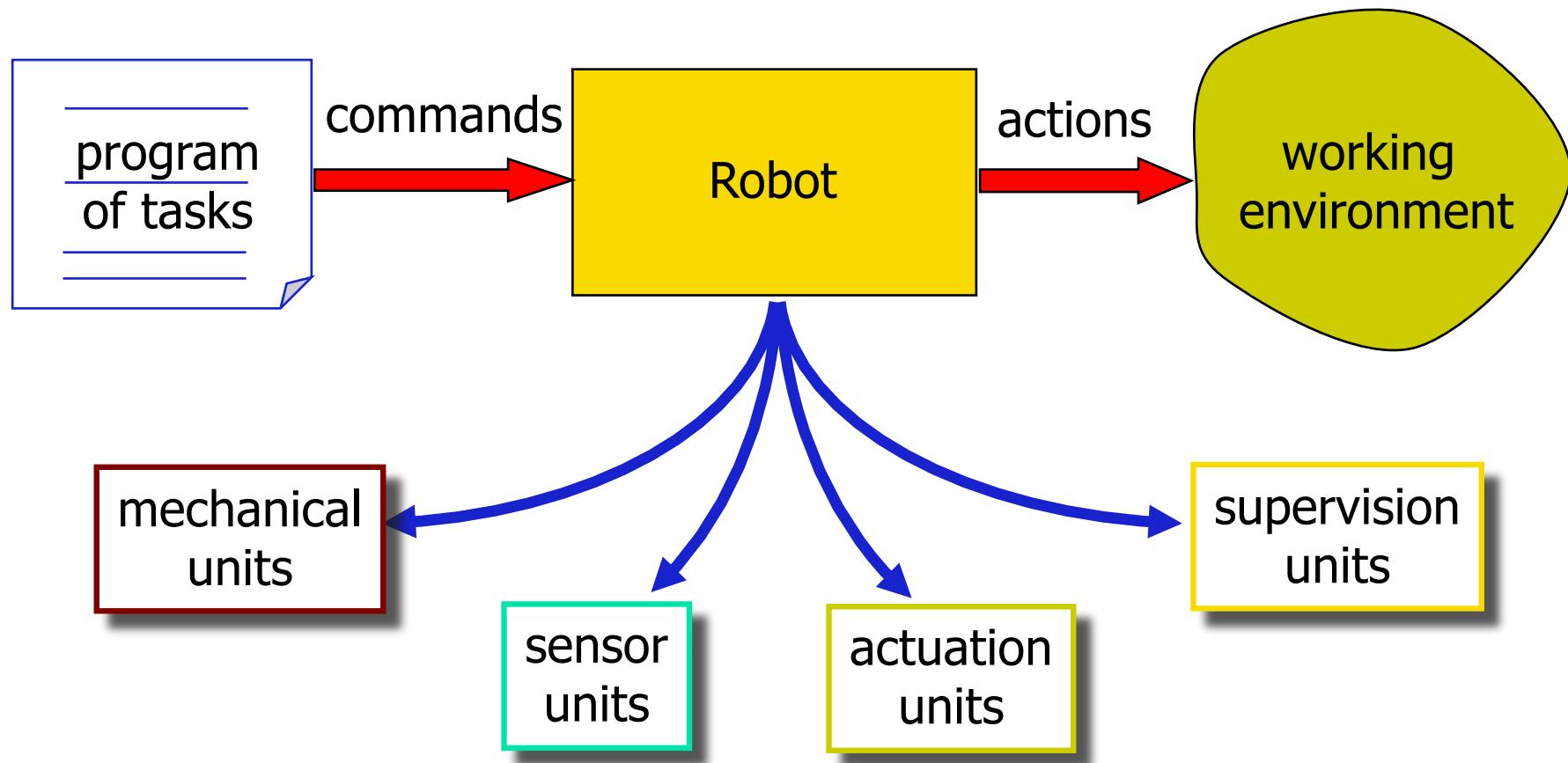
Prof. Alessandro De Luca

DIPARTIMENTO DI INGEGNERIA INFORMATICA  
AUTOMATICA E GESTIONALE ANTONIO RUBERTI





# Robot as a system





# Functional units of a robot

---

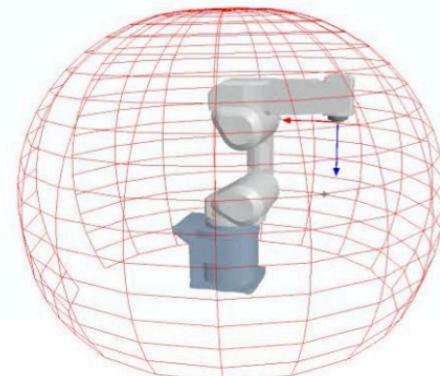
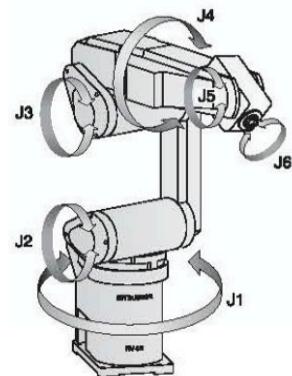
- mechanical units (robot arms)
  - serial manipulators: rigid links connected via **rotational** or **prismatic** joints (each giving 1 degree of freedom = DOF)
  - **supporting structure** (mobility), **wrist** (dexterity), **end-effector** (for task execution, e.g., manipulation)
- actuation units
  - motors (**electrical**, **hydraulic**, **pneumatic**) and transmissions
  - motion control algorithms
- sensor units
  - **proprioceptive** (internal robot state: position and velocity of the joints)
  - **exteroceptive** (external world: force and proximity, vision, ...)
- supervision units
  - task **planning** and **control**
  - artificial intelligence and reasoning



# Arrangement of mechanical links

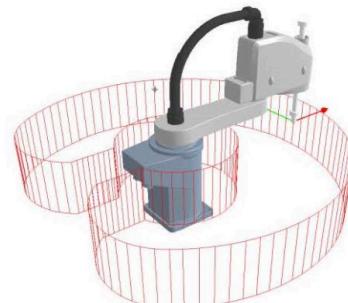
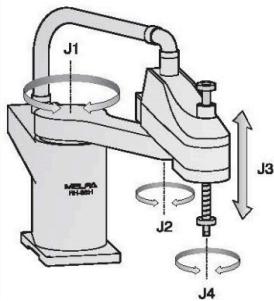
4, 5, or 6 joints  
(DOFs)

Articulated Robot

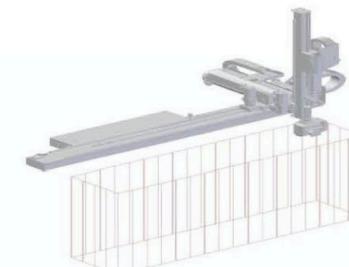
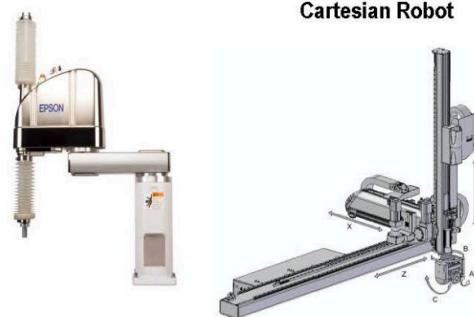


different kinematic types of robot arms

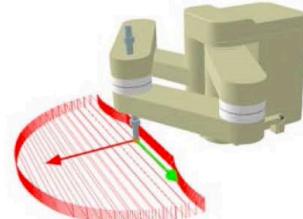
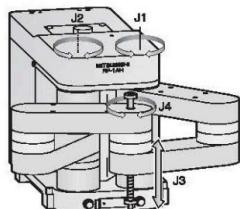
SCARA Robot



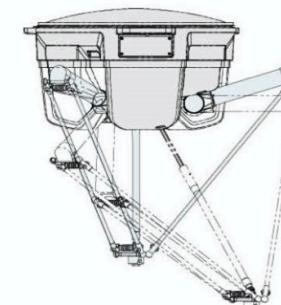
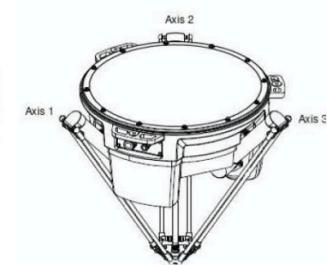
Cartesian Robot



SCARA Robot



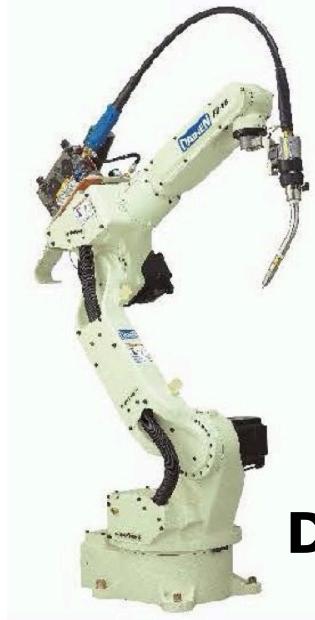
Parallel/Delta Robot



# Examples of industrial robots with brands



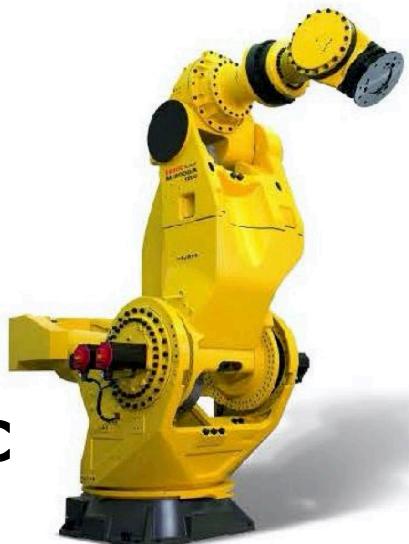
**ABB**



**DAIHEN**



**EPSON**



**FANUC**



**KUKA**



**NAICHI**

# Bi-manual industrial robots with brands

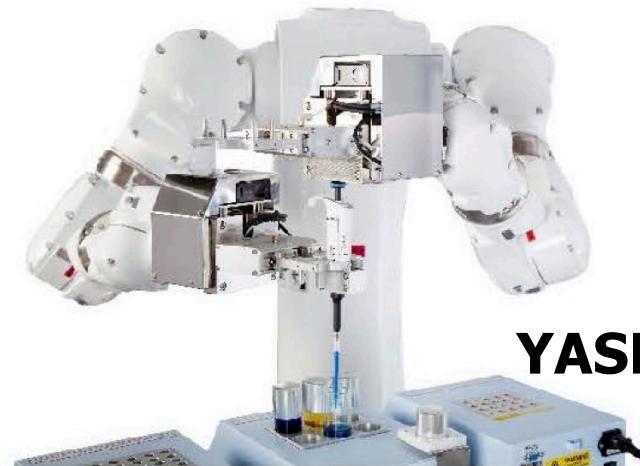
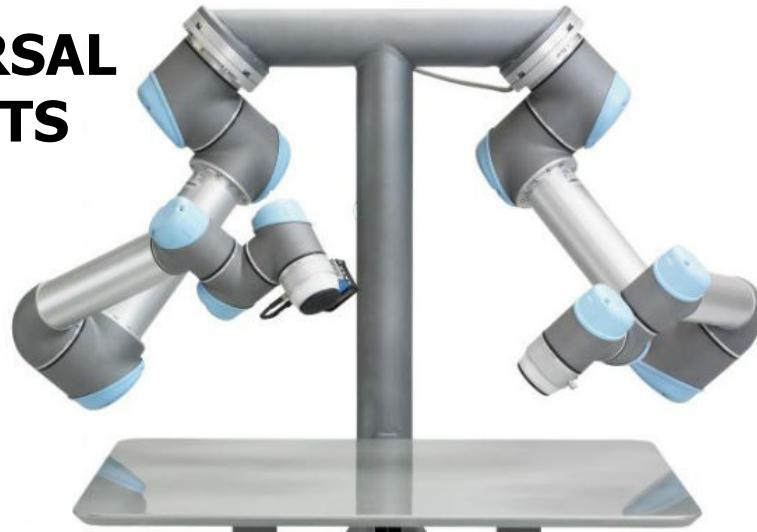


**ABB**



**COMAU**

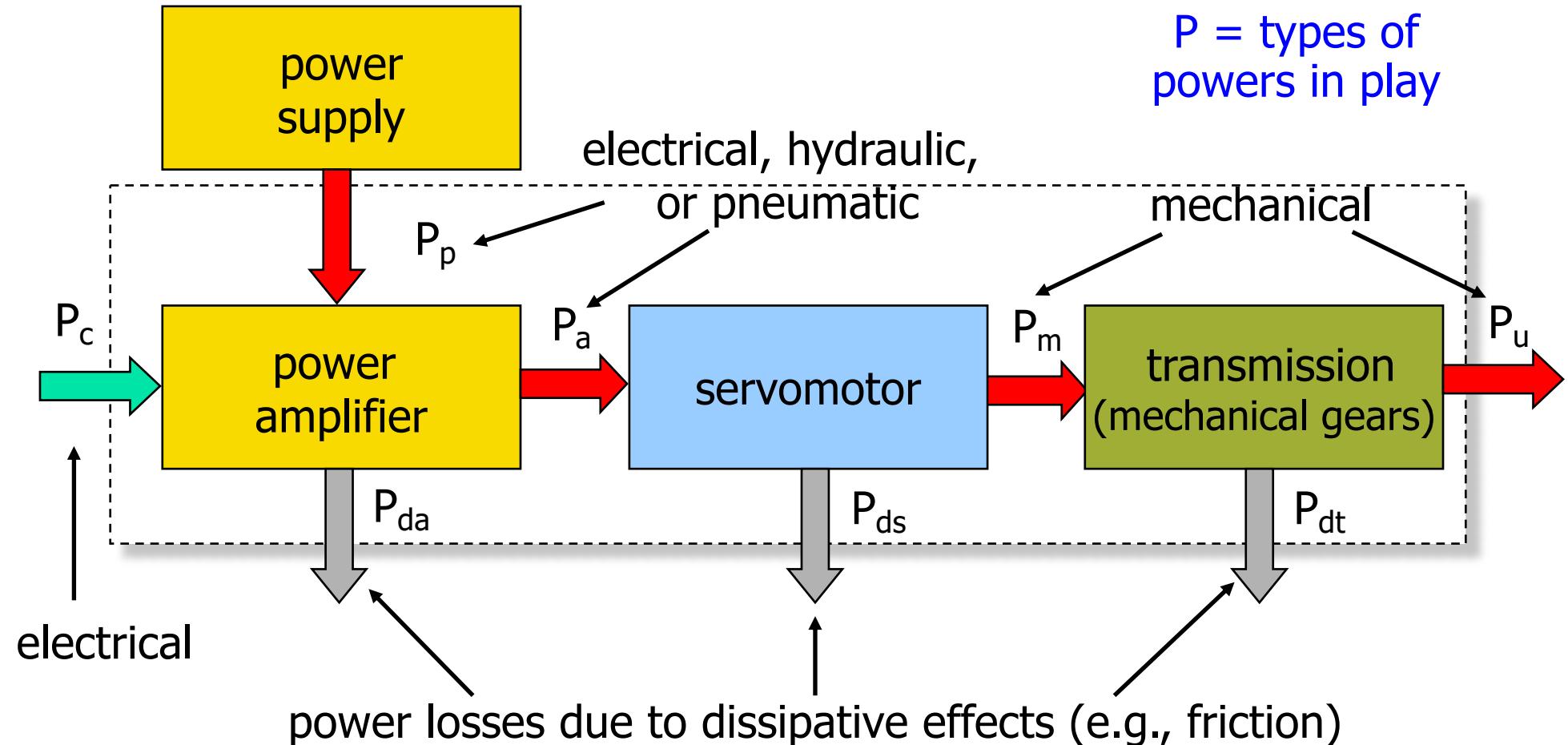
**UNIVERSAL  
ROBOTS**



**YASHKAWA**



# Actuation systems



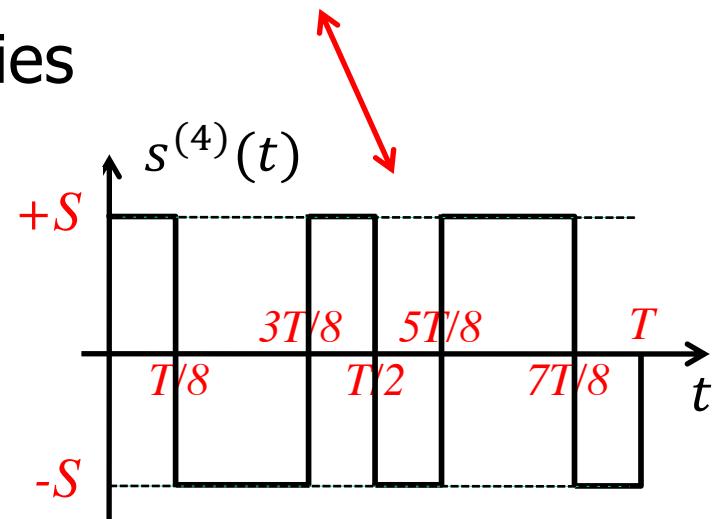
power = voltage · current = pressure · flow rate = force · speed = torque · angular speed [W, Nm/s]

efficiency = power out/power in [%]   energy ~ work = power · time [kWh, Nm, J]



# Desired characteristics for robot servomotors

- low inertia
- high power-to-weight ratio
- high acceleration capabilities
  - variable motion regime, with several stops and inversions
- large range of operational velocities
  - 1 to 2000 rpm (round per min)
- high accuracy in positioning
  - at least 1/1000 of a turn
- low torque ripple
  - continuous rotation at low speed
- power: 10 W to 10 kW





# Servomotors

- **pneumatic:** pneumatic energy (compressor) → pistons or chambers → mechanical energy
  - difficult to control accurately (change of fluid compressibility) → no trajectory control
  - used for opening/closing grippers
  - ... or as artificial muscles (McKibben actuators)
- **hydraulic:** hydraulic energy (accumulation tank) → pumps/valves → mechanical energy
  - **advantages:** no static overheating, self-lubricated, inherently safe (no sparks), excellent power-to-weight ratio, large torques at low velocity (w/o reduction)
  - **disadvantages:** needs hydraulic supply, large size, linear motion only, low power conversion efficiency, high cost, increased maintenance (oil leaking)





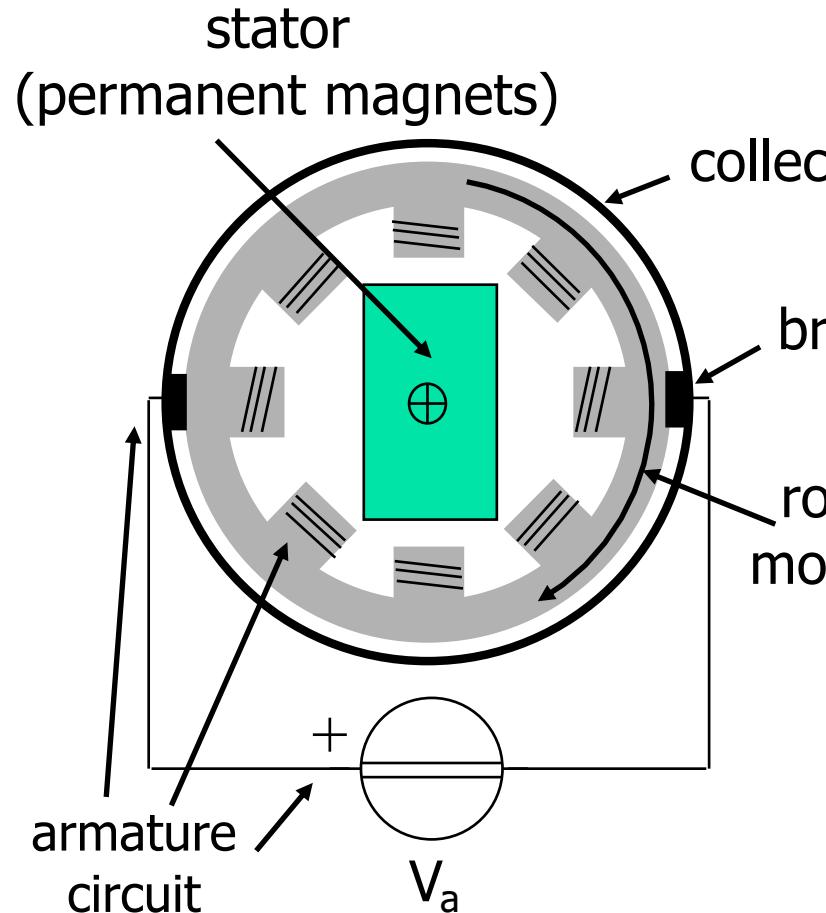
# Electrical servomotors

---

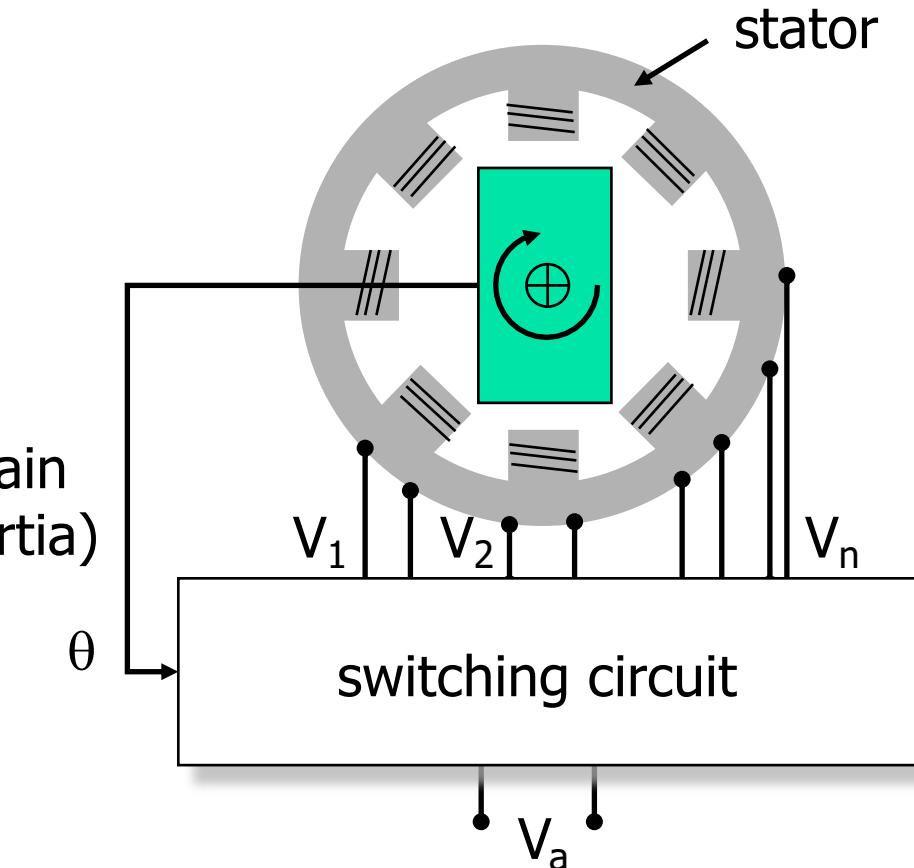
- **advantages**
  - power supply available everywhere
  - low cost
  - large variety of products
  - high power conversion efficiency
  - easy maintenance
  - no pollution in working environment
- **disadvantages**
  - overheating in static conditions (in the presence of gravity)
    - use of (emergency) brakes
  - need special protection in flammable environments
  - some advanced models require more complex control laws



# Electrical servomotors for robots



direct current (DC) motor



with electronic switches (brushless)



# Advantages of brushless motors

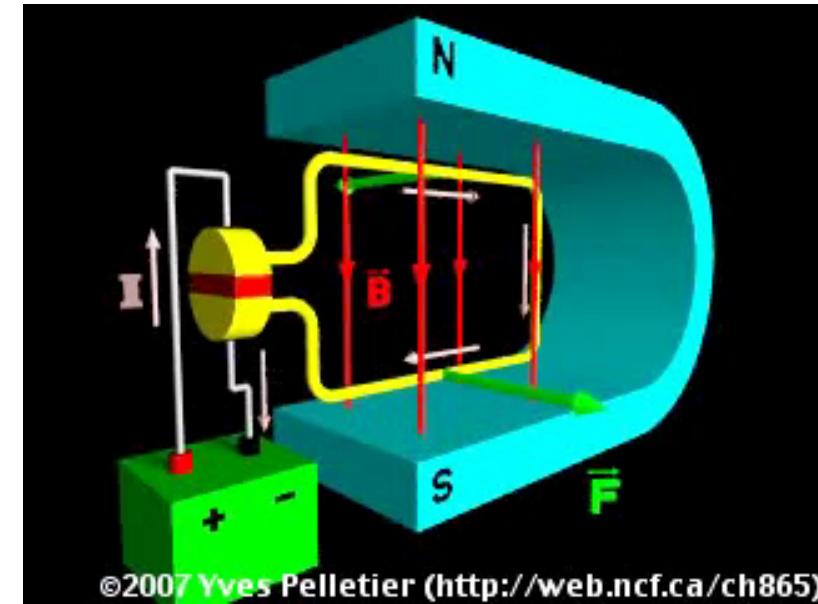
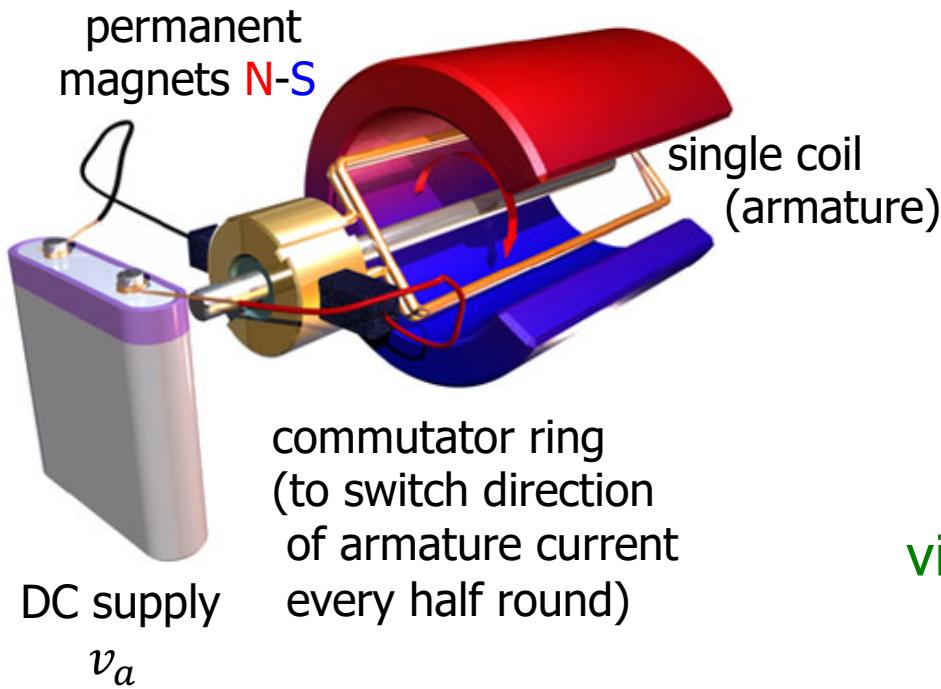
---

- reduced losses, both electrical (due to tension drops at the collector-brushes contacts) and mechanical (friction)
- reduced maintenance (no substitution of brushes)
- easier heat dissipation
- more compact rotor (less inertia and smaller dimensions)

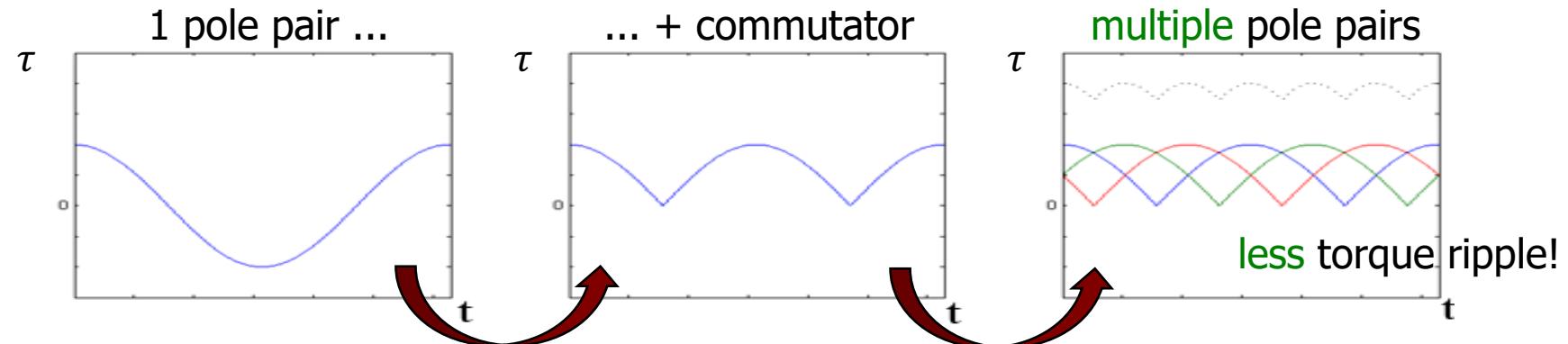
... but indeed a higher cost!



# Principle of operation of a DC motor



$$\vec{F} = L(\vec{i} \times \vec{B}) \quad \tau = d|\vec{F}|$$





# DC electrical motor

## mathematical model (in the time domain)

**electrical balance**  
(on the equivalent armature circuit)

$$v_a(t) = R_a i_a(t) + L_a \frac{di_a(t)}{dt} + v_{emf}(t)$$

$$v_{emf}(t) = k_v \omega(t)$$

(back emf)

**mechanical balance**  
(Newton law on torques)

$$\tau_m(t) = I_m(t) \frac{d\omega(t)}{dt} + F_m \omega(t) + \tau_{load}(t)$$

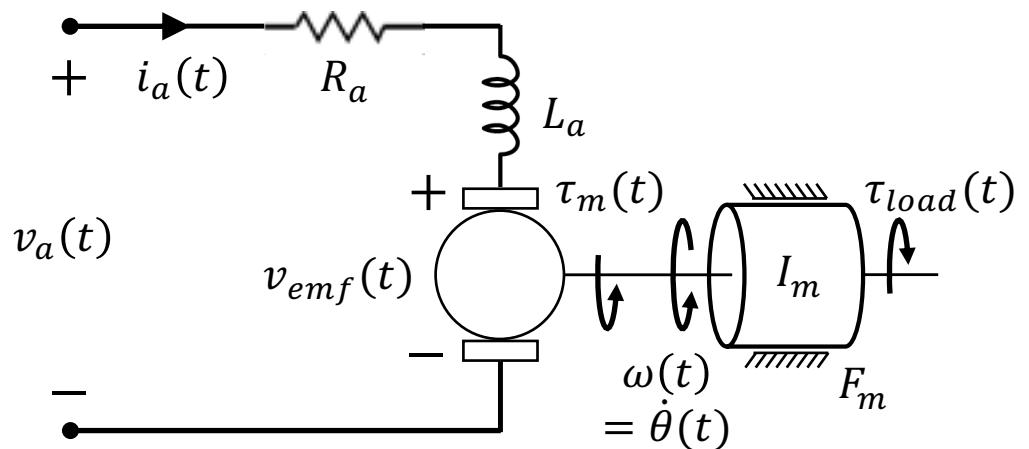
$$\tau_m(t) = k_t i_a(t)$$

(motor torque)

in the absence of losses, **conservation of power** holds in energy transformations

$$P_{elec} = v_{emf} i_a = \tau_m \omega = P_{mecc}$$

$$\Rightarrow k_v = k_t \quad (\text{in SI units})$$



using Laplace transform, differential equations become **algebraic relations!**

$$X(s) = \mathcal{L}[x(t)] = \int_0^\infty x(t) e^{-st} dt$$

# DC electrical motor

## mathematical model for command and control



### electrical balance

$$V_a = (R_a + sL_a) I_a + V_{\text{emf}}$$

$$V_{\text{emf}} = k_v \Omega$$

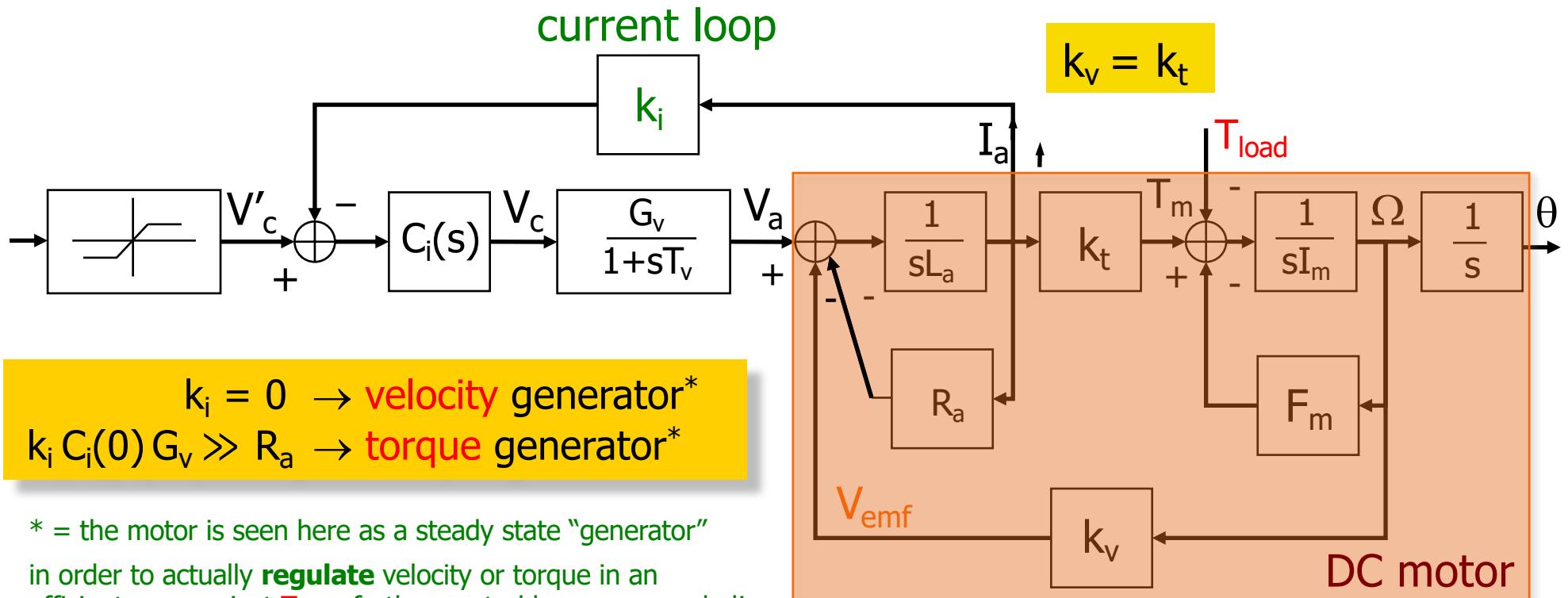
### Laplace domain (transfer functions)

$$\tau_{\text{elec}} = \frac{L_a}{R_a} \ll \frac{I_m}{F_m} = \tau_{\text{mecc}}$$

### mechanical balance

$$T_m = (sI_m + F_m) \Omega + T_{\text{load}}$$

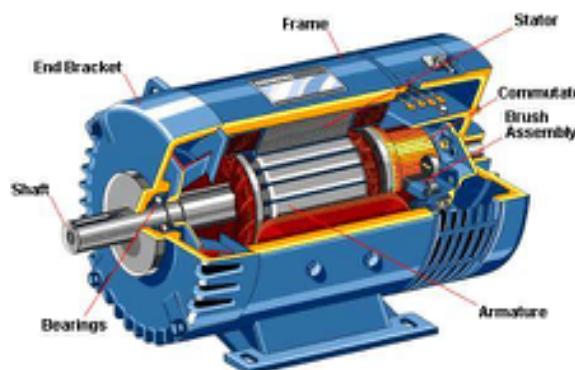
$$T_m = k_t I_a$$



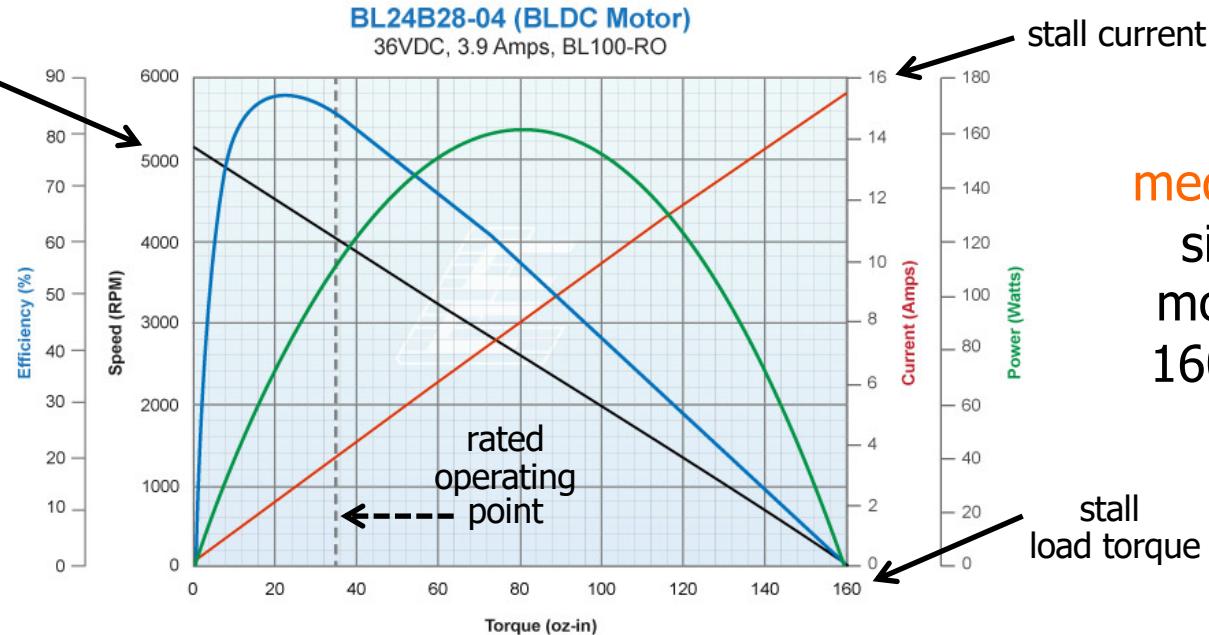


# Characteristic curves of a DC motor

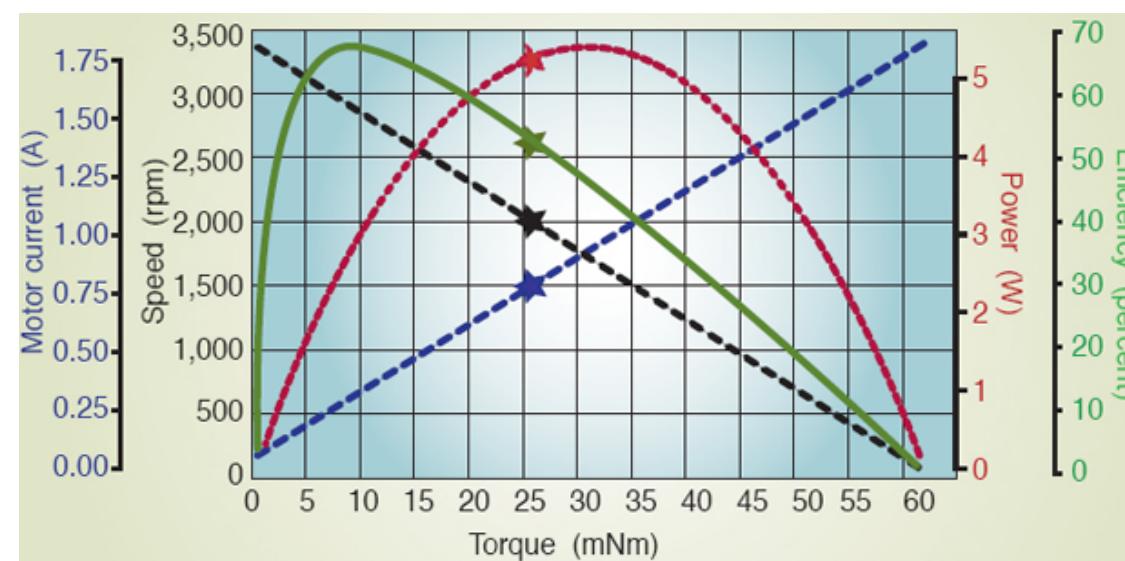
at steady-state,  
for **constant**  
applied tension  $v_a$



no-load  
max speed



conversion SI  $\Leftrightarrow$  US  
unit systems (!!)  
 $1 \text{ Nm} = 141.61 \text{ oz-in}$   
 $100 \text{ oz-in} = 0.70 \text{ Nm}$





# Data sheet electrical motors

- DC drives



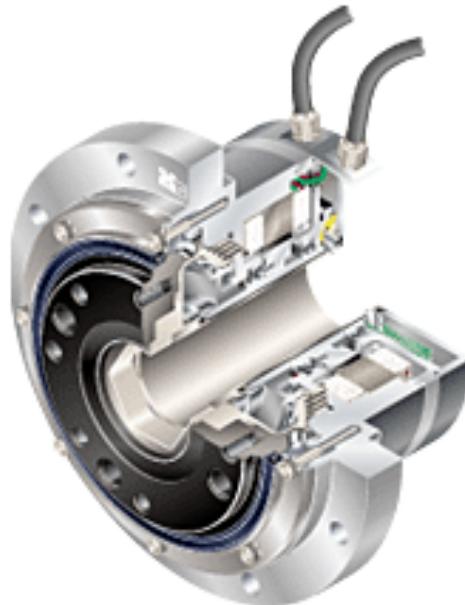
Model of actuator	RHS-14		RHS-17		RHS-20/RFS-20				RHS-25/RFS-25				RHS-32/RFS-32				
	6003	3003	6006	3006	6007	3007	6012	3012	6012	3012	6018	3018	6018	3018	6030	3030	
Rated Torque	Inlb	48	69	87	177	106	212	177	266	177	354	266	531	266	531	443	885
	Nm	5.4	7.8	9.8	20	12	24	20	30	20	40	30	60	30	60	50	100
Rated Speed of Rotation	rpm	60	30	60	30	60	30	60	30	60	30	60	30	60	30	60	30
Max. Instant. Torque	Inlb	159	248	301	478	504	743	504	743	885	1416	885	1416	1947	3009	1947	3009
	Nm	18	28	34	54	57	84	57	84	100	160	100	160	220	340	220	340
Max. Speed of Rotation	rpm	100	50	80	40	80	40	80	40	80	40	80	40	80	40	80	40

nominal/peak torques and speeds



# Data sheet electrical motors

## ■ AC drives



	unit	HKM-20-60	HKM-20-30	HKM-25-60	HKM-25-30
Rated Power	Watts	100		200	
Rated Torque	in-lb	115	223	233	440
	N-m	13	26	26	50
Maximum Torque	in-lb	345	700	830	1330
	N-m	39	79	94	150
Rated Speed	r/min	60	30	60	30
Maximum Speed	r/min	80	40	80	40
Current Rated	A	1.8	1.4	4.8	3
Current Max	A	5	4	14	9
Thermal Time Constant	min.				
Gear Reduction Ratio	R:1	50	100	50	100
Output Resolution	P/rev	50,000	100,000	75,000	150,000
	arc sec	26	13	17	9
Absolute Accuracy	+/- arc sec	75	40	60	40

- for applications requiring a rapid and accurate response (in robotics!)
- induction motors driven by alternate current (AC)
- small diameter rotors, with low inertia for fast starts, stops, and reversals



# Motion transmission gears

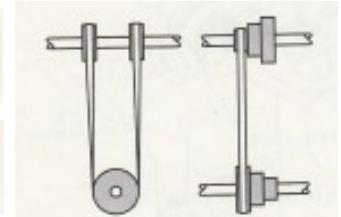
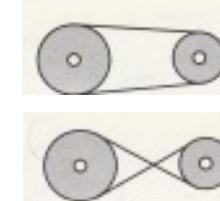
---

- optimize the transfer of mechanical torque from actuating motors to driven links
- quantitative transformation (from **low torque/high velocity** to **high torque/low velocity**)
- qualitative transformation (e.g., from **rotational** motion of an electrical motor to a **linear** motion of a link along the axis of a prismatic joint)
- allow improvement of static and dynamic performance by reducing the weight of the actual robot structure in motion (locating the motors remotely, closer to the robot base)



# Transmissions in robotics

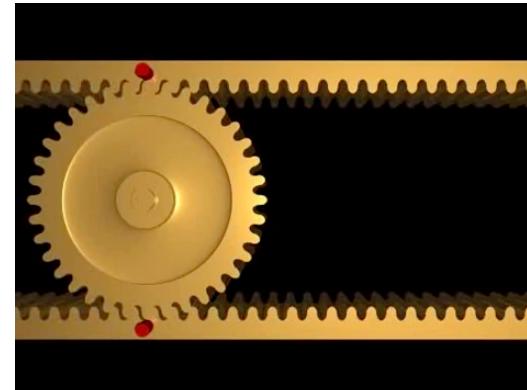
- **spur gears:** modify direction and/or translate axis of (rotational or translational) motor displacement
  - problems: **deformations, backlash**
- **lead screws, worm gearing:** convert rotational into translational motion (prismatic joints)
  - problems: **friction, elasticity, backlash**
- **toothed belts and chains:** dislocate the motor w.r.t. the joint axis
  - problems: **compliance** (belts) or **vibrations** induced by larger mass at high speed (chains)
- **harmonic drives:** compact, in-line, power efficient, with high reduction ratio (up to 150-200:1)
  - problems: **elasticity**
- **transmission shafts:** long, inside the links, with flexible couplings for alignment



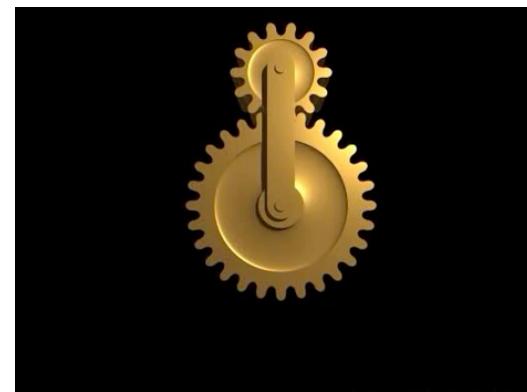


# Transmission gears in motion

- racks and pinion
  - one rack moving (or both)
- epi-cycloidal gear train
  - or hypo-cycloidal (small gear inside)
- planetary gear set
  - one of three components is locked:  
sun gear, planet carrier, ring gear



video



video

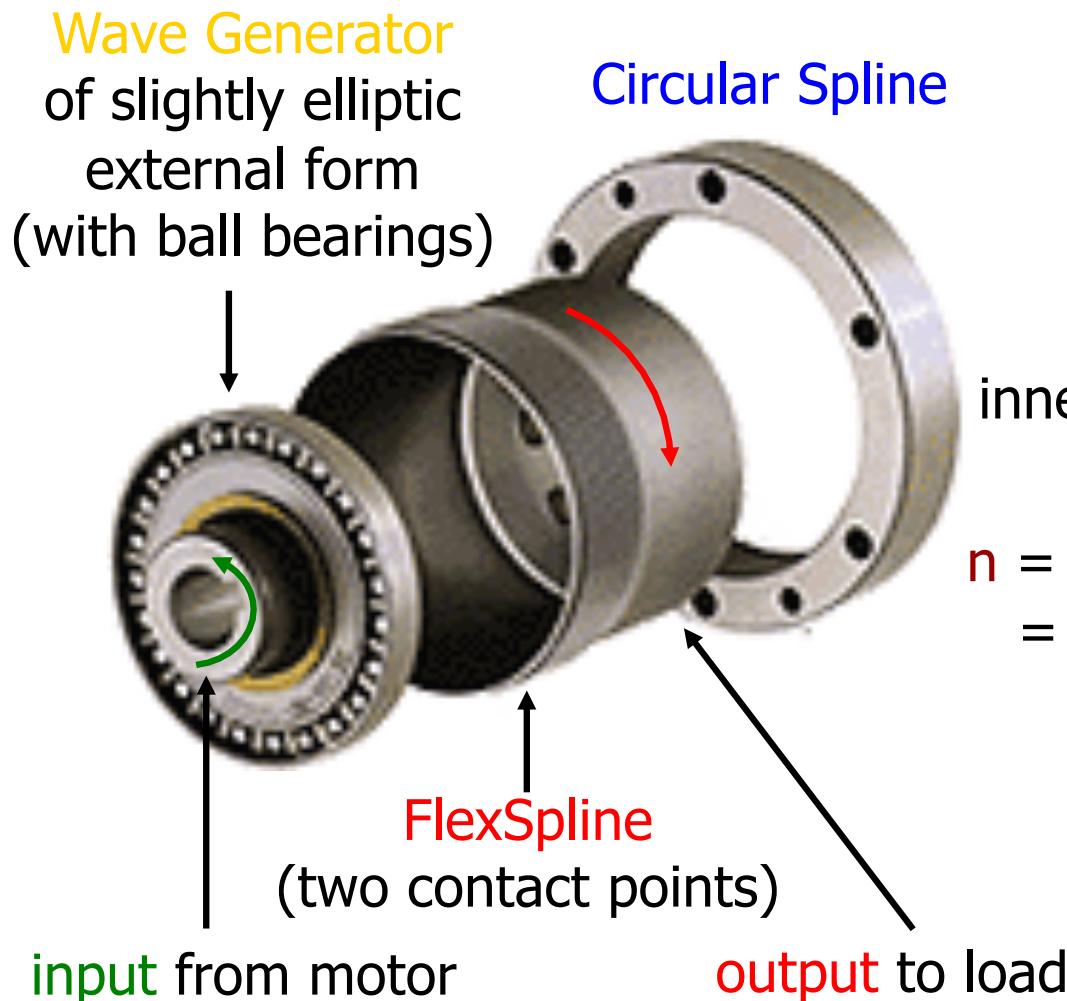


video



# Harmonic drives

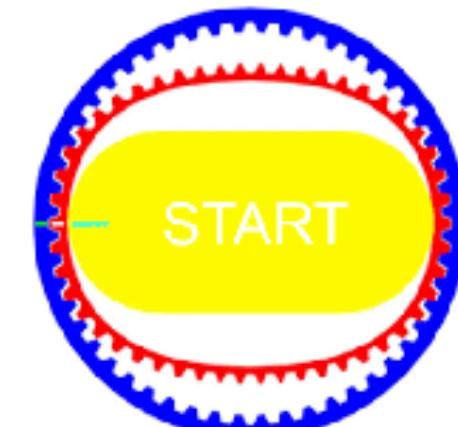
[video](#)



$$\text{inner \#teeth CS} = \text{outer \#teeth FS} + 2$$

reduction ratio

$$n = \frac{\#\text{teeth FS}}{(\#\text{teeth CS} - \#\text{teeth FS})} = \frac{\#\text{teeth FS}}{2}$$





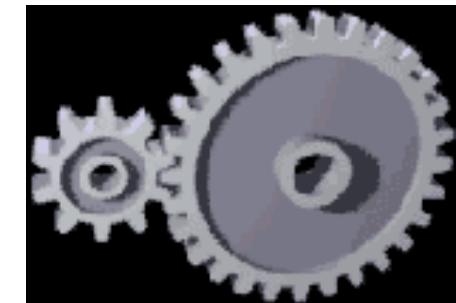
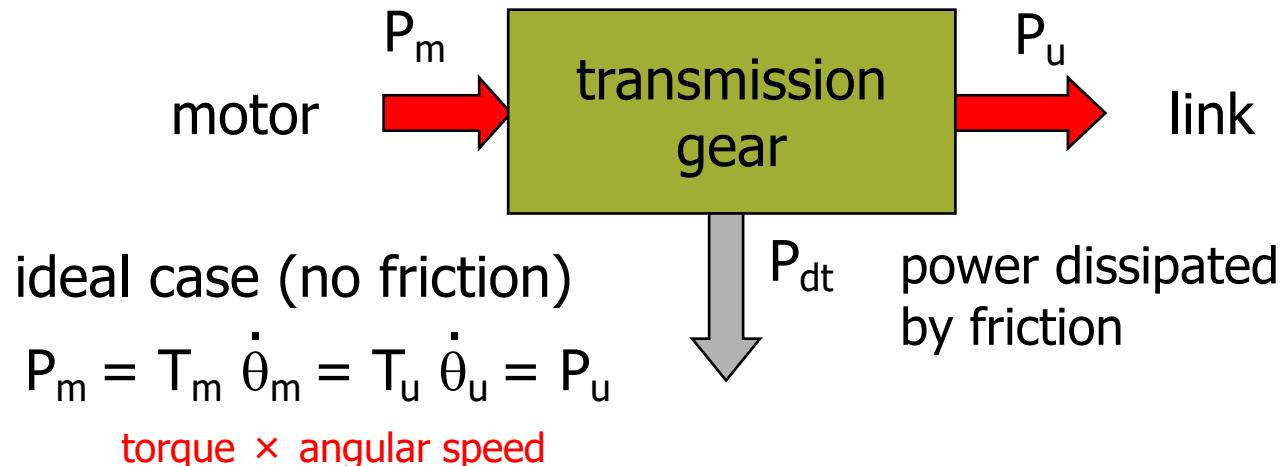
# Operation of an harmonic drive

Harmonic Drive Gearing  
**PRINCIPLE <sup>of</sup> OPERATION**

commercial video by Harmonic Drives AG  
(<https://www.youtube.com/watch?v=bzRh672peNk>)



# Optimal choice of reduction ratio



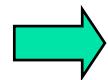
$$n = \text{reduction ratio } (\gg 1) \quad \dot{\theta}_m = n \dot{\theta}_u \quad \rightarrow \quad T_u = n T_m$$

to have  $\ddot{\theta}_u = a$  (thus  $\ddot{\theta}_m = n a$ ), the motor should provide a torque

$$T_m = J_m \ddot{\theta}_m + 1/n (J_u \ddot{\theta}_u) = (J_m n + J_u/n) a$$

inertia × angular acceleration

for minimizing  $T_m$ , we set:  $\frac{\partial T_m}{\partial n} = (J_m - J_u/n^2) a = 0$



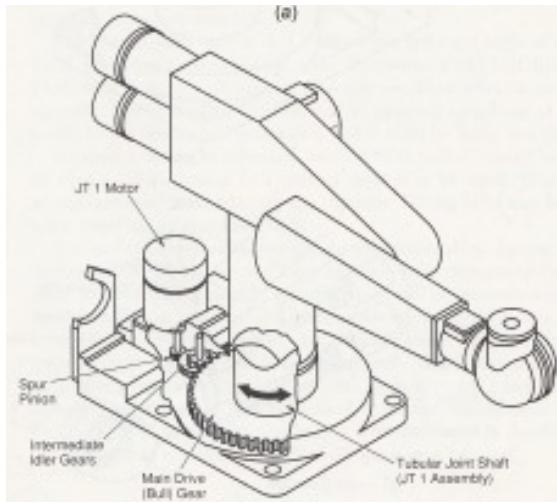
$$n = (J_u / J_m)^{1/2}$$

"matching" condition between inertias

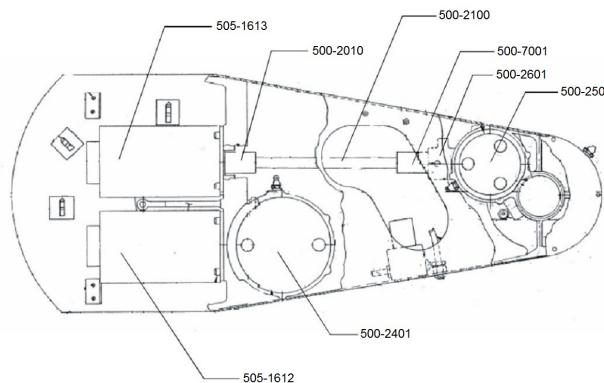
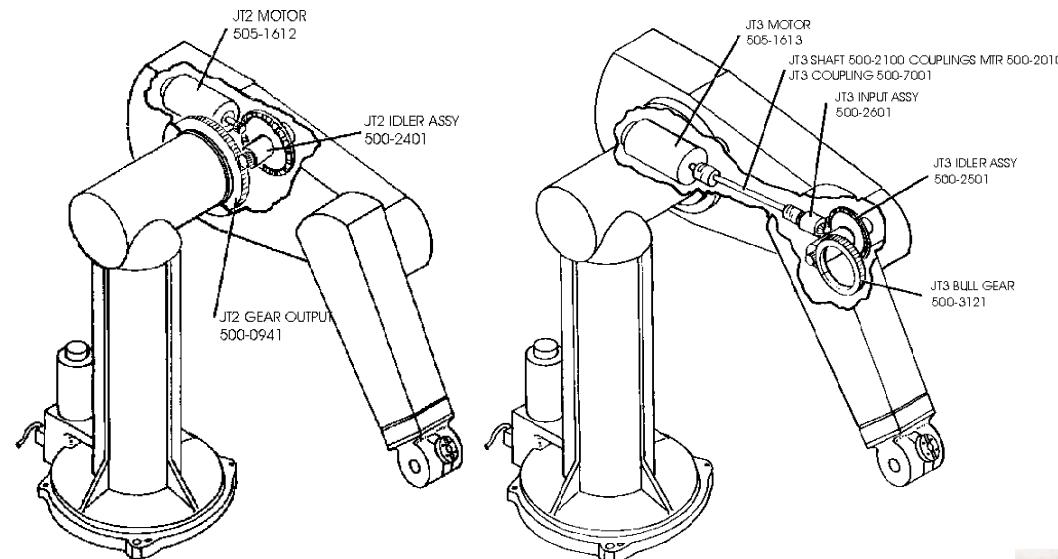


# Transmissions in industrial robots

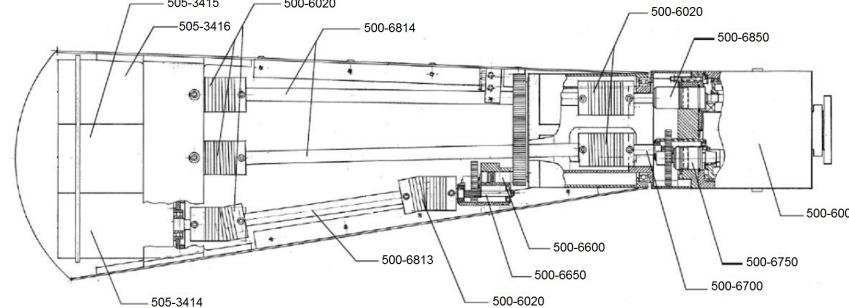
- transmissions used (inside) 6-dof Unimation industrial robots with serial kinematics



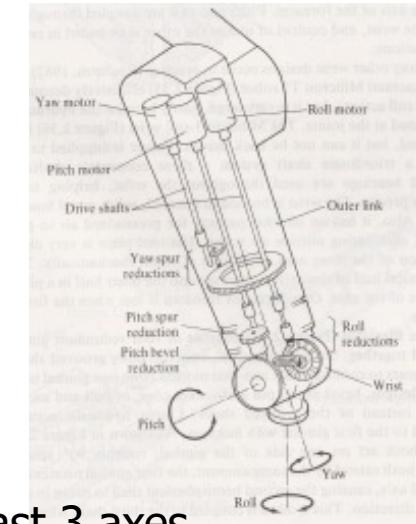
**PUMA 260:** 1<sup>st</sup> axis



**PUMA 560:** 2<sup>nd</sup> and 3<sup>rd</sup> axes



**PUMA 560:** inner and outer links



**PUMA 560:** last 3 axes

# Inside views on joint axes 4, 5 & 6 of an industrial KUKA robot

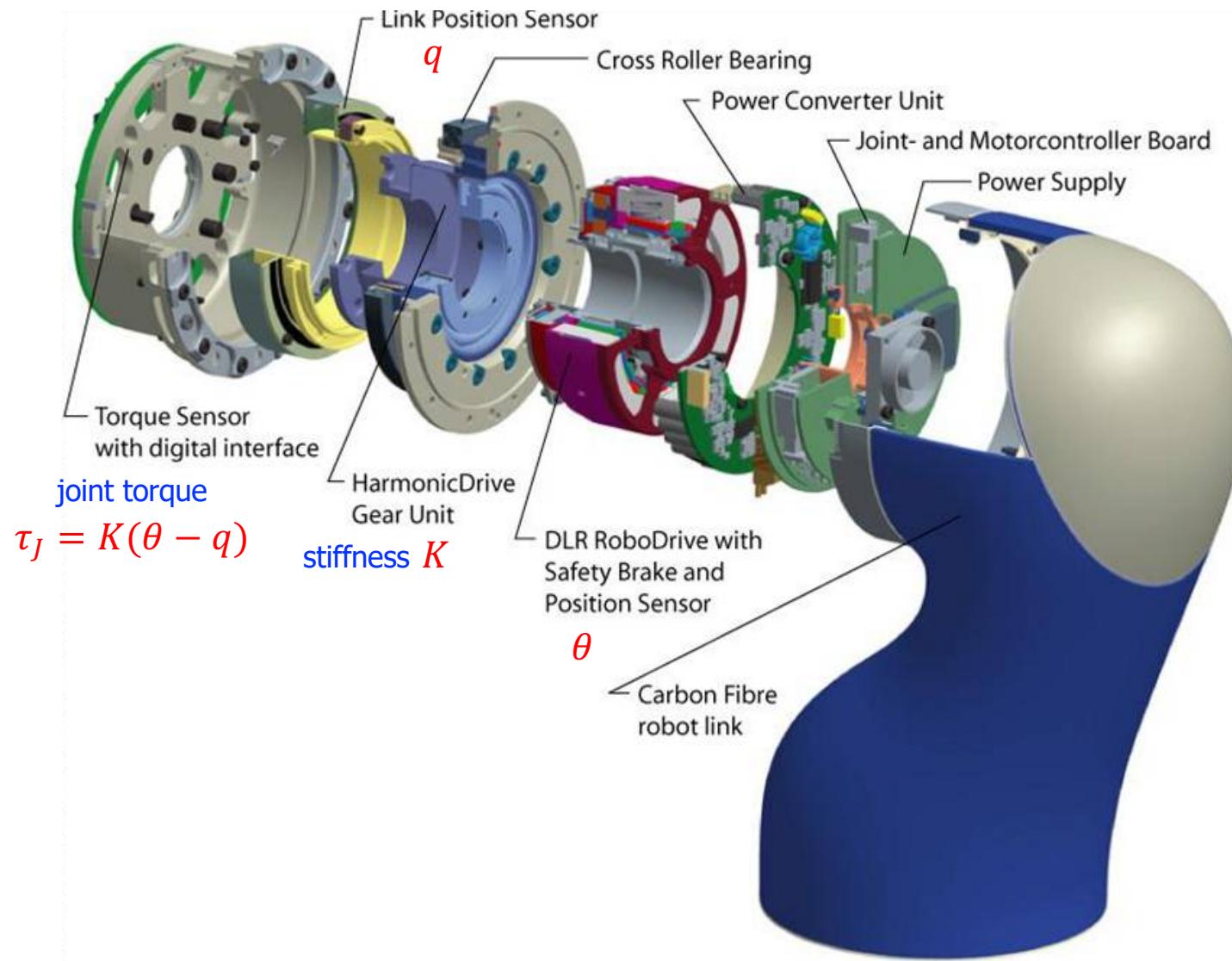


- looking inside the forearm to see the transmissions of the spherical wrist
- motor rotation seen from the encoder side (small couplings exist)





# Exploded view of a joint in the DLR-III robot





---

## *Robotics 1*

# Robot components: Proprioceptive sensors

Prof. Alessandro De Luca

DIPARTIMENTO DI INGEGNERIA INFORMATICA  
AUTOMATICA E GESTIONALE ANTONIO RUBERTI





# Properties of measurement systems - 1

---

- **accuracy**

agreement of measured values with a given reference standard (e.g., ideal characteristics)

- **repeatability**

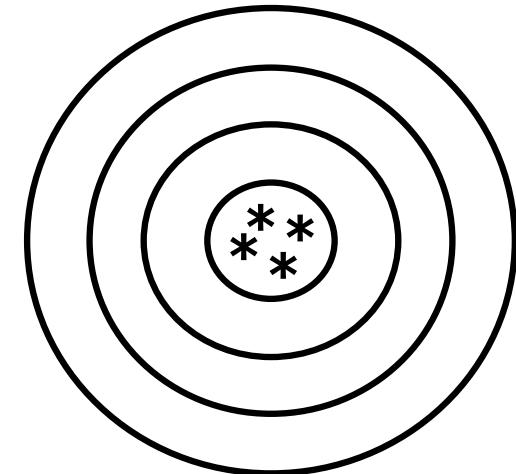
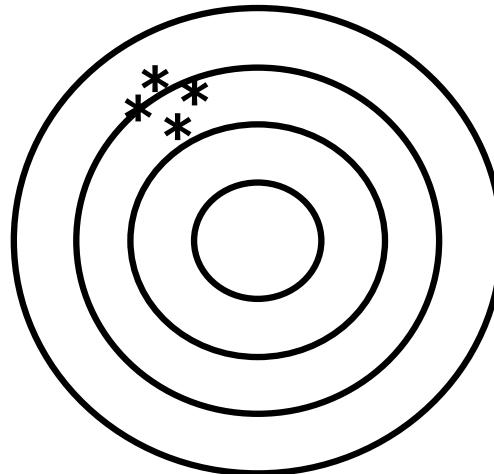
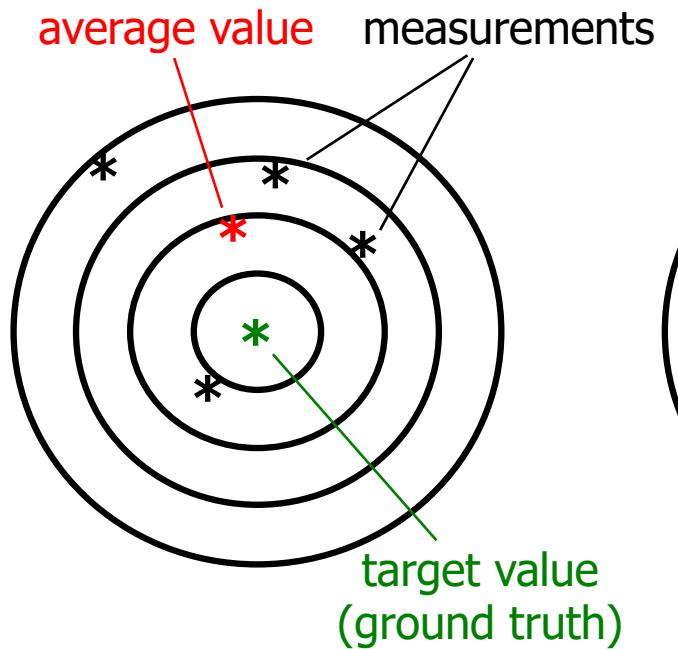
capability of reproducing as output similar measured values over consecutive measurements of the same constant input quantity

- **stability**

capability of keeping the same measuring characteristics over time/temperature (similar to accuracy, but in the long run)



# Accuracy and Repeatability



low accuracy  
low repeatability

low accuracy  
high repeatability

high accuracy  
high repeatability

better components!

calibration!

# Accuracy and Repeatability in robotics



- **accuracy** is how close a robot can come to a given point in its workspace
  - depends on machining accuracy in construction/assembly of the robot, flexibility effects of the links, gear backlash, payload changes, round-off errors in control computations, ...
  - can be improved by (**kinematic**) **calibration**
- **repeatability** is how close a robot can return to a previously taught point
  - depends only the robot controller/measurement resolution
- both may vary in different areas of the robot workspace
  - standard ISO 9283 defines conditions for assessing robot performance
  - limited to static situations (recently, interest also in dynamic motion)
  - robot manufacturers usually provide only data on “repeatability”

[video](#)



simple test on repeatability of a  
Fanuc ArcMate100i robot (1.3 m reach)



# Properties of measurement systems - 2

---

- **linearity** error

maximum deviation of the measured output from the straight line that best fits the real characteristics

- as % of the output (measurement) range

- **offset** error

value of the measured output for zero input

- sometimes not zero after an operation cycle, due to **hysteresis**

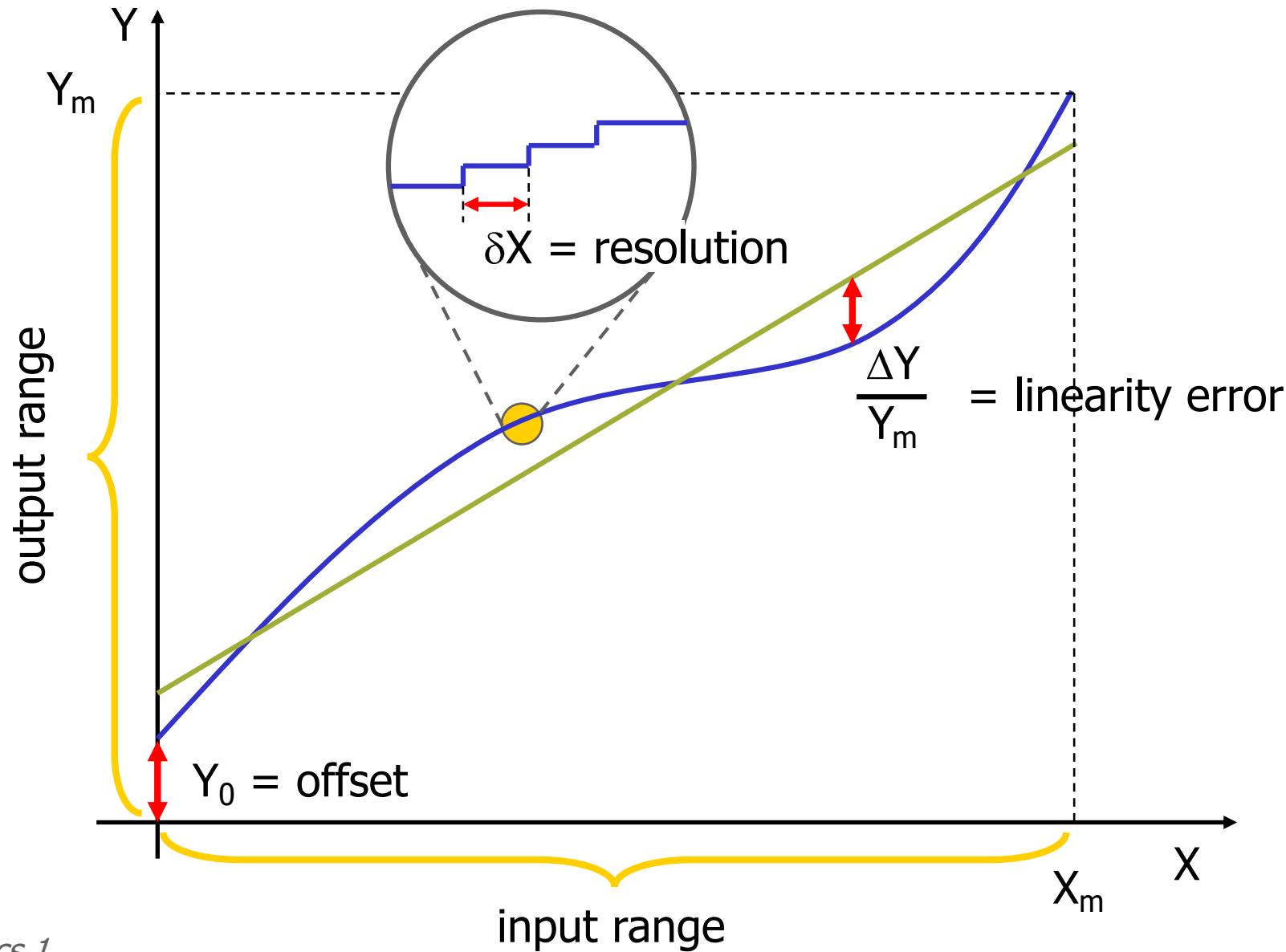
- **resolution** error

maximum variation of the input quantity producing no variation of the measured output

- in absolute value or in % of the input range



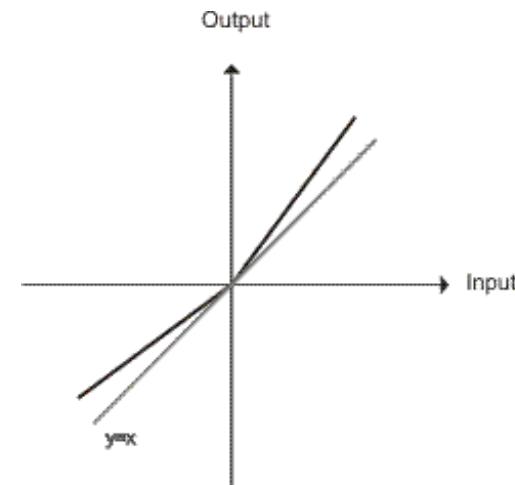
# Linearity, Offset, Resolution



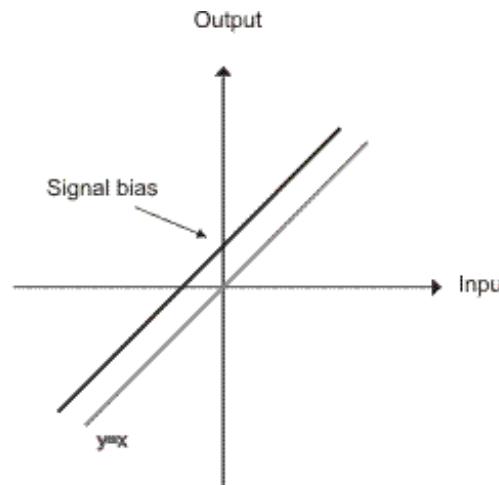


# Sensor measurements

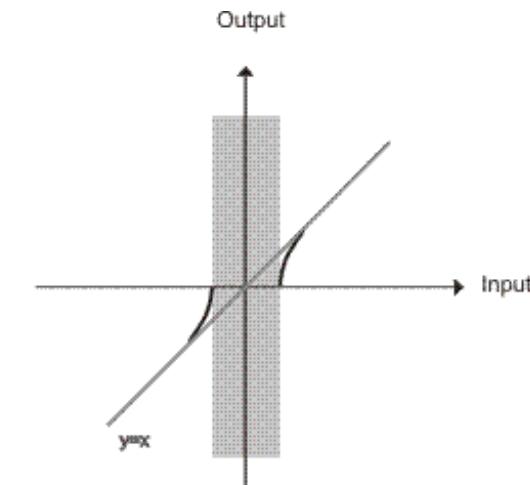
## some non-idealities



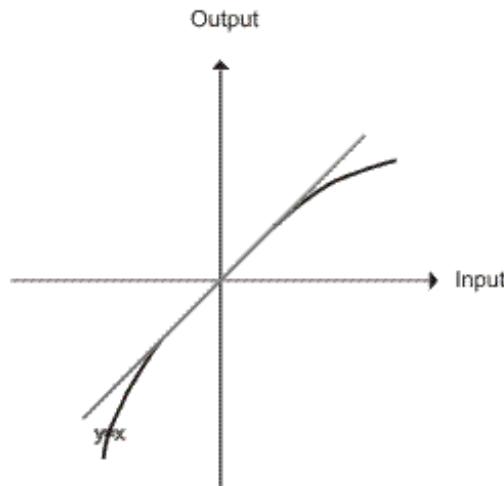
Asymmetry



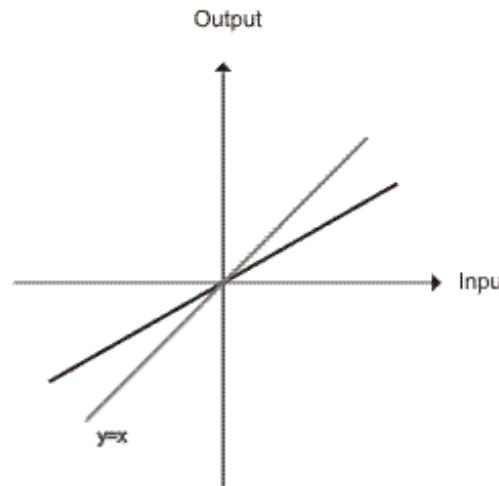
Bias



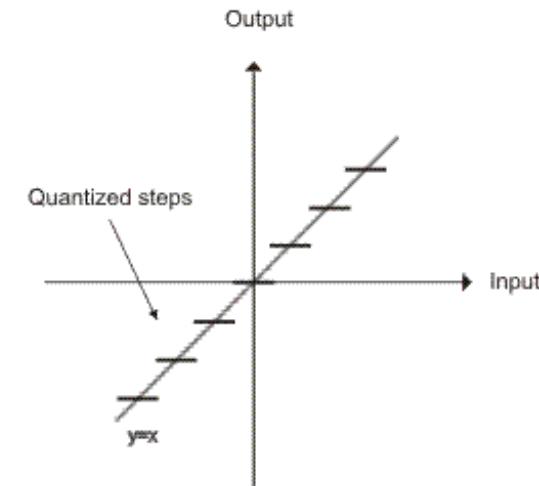
Dead zone



Nonlinearity



Scaling factor



Quantization



# Classes of sensors for robots

---

- **proprioceptive sensors** measure the internal state of the robot (**position and velocity of joints**, but also **torque at joints** or **acceleration of links**)
  - kinematic calibration, identification of dynamic parameters, control
- **exteroceptive sensors** measure/characterize robot interaction with the environment, enhancing its autonomy (**forces/torques**, **proximity**, **vision**, but also sensors for sound, smoke, humidity, ...)
  - control of interaction with the environment, obstacle avoidance in the workspace, presence of objects to be grasped, ...
  - mobile-base robots: localization in a map, navigation in unknown environments, ...



# Position sensors

- provide an **electrical signal proportional to the displacement** (linear or angular) of a mechanical part with respect to a reference position
- **linear** displacements: potentiometers, linear variable-differential transformers (LVDT), inductosyns
- **angular** displacements: potentiometers, resolvers, syncros (all analog devices with A/D conversion), optical **encoders (digital)**, Hall sensors, ...

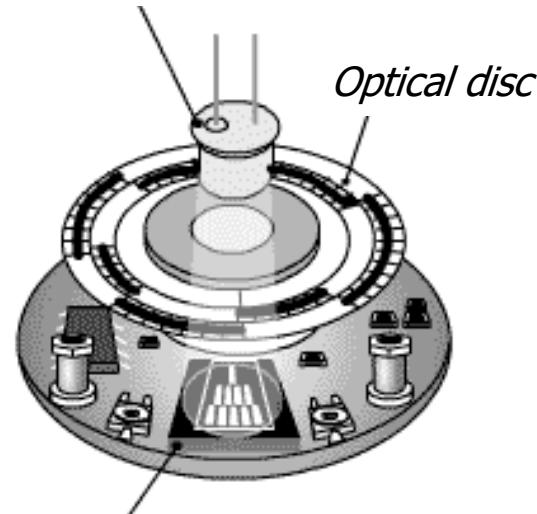
the most used in robotics, since also linear displacements are obtained through rotating motors and suitable transmissions





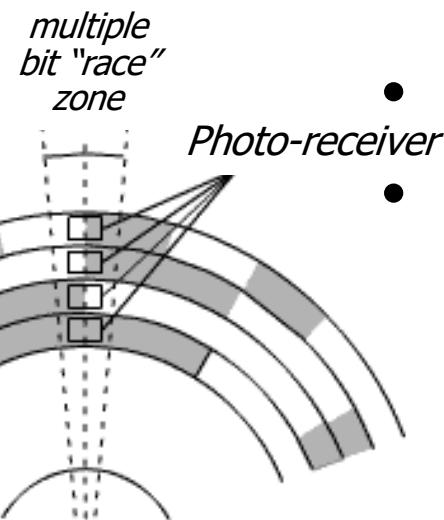
# Absolute encoders

*Photo-emitter*



*Photo-receiver*

$$N_t = \# \text{ tracks} = \# \text{ bits} \\ (\text{min } 12 \text{ in robotics})$$

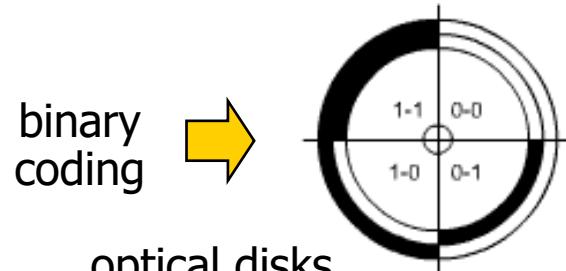


- rotating optical disk, with alternate transparent and opaque sectors on multiple concentric tracks
- (infrared) light beams are emitted by leds and sensed by photo-receivers
- light pulses are converted into electrical pulses, electronically processed and transmitted in output
- **resolution** =  $360^\circ / 2^{N_t}$
- digital encoding of **absolute** position

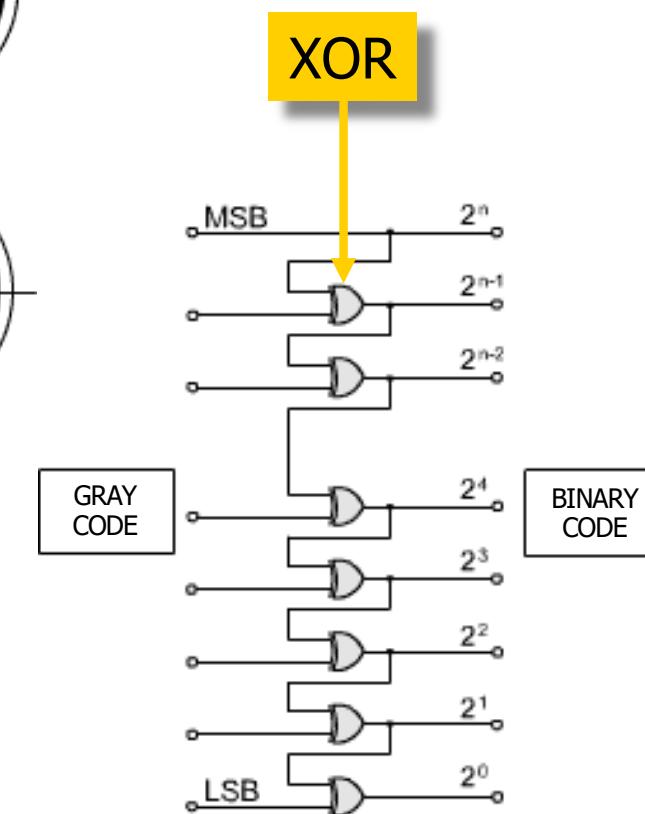
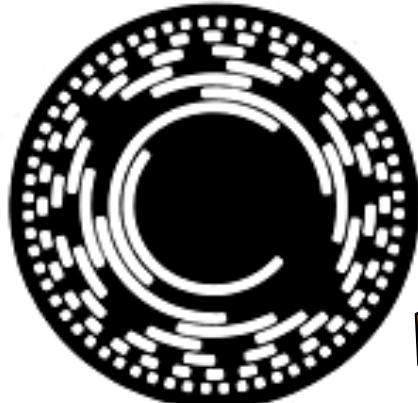
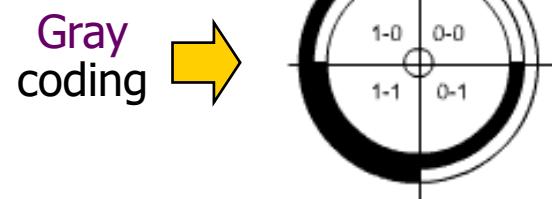
when the optical disk is rotating fast, the use of **binary coding** may lead to (large) reading errors, in correspondence to multiple transitions of bits



# Absolute encoding



optical disks with **2 bits**



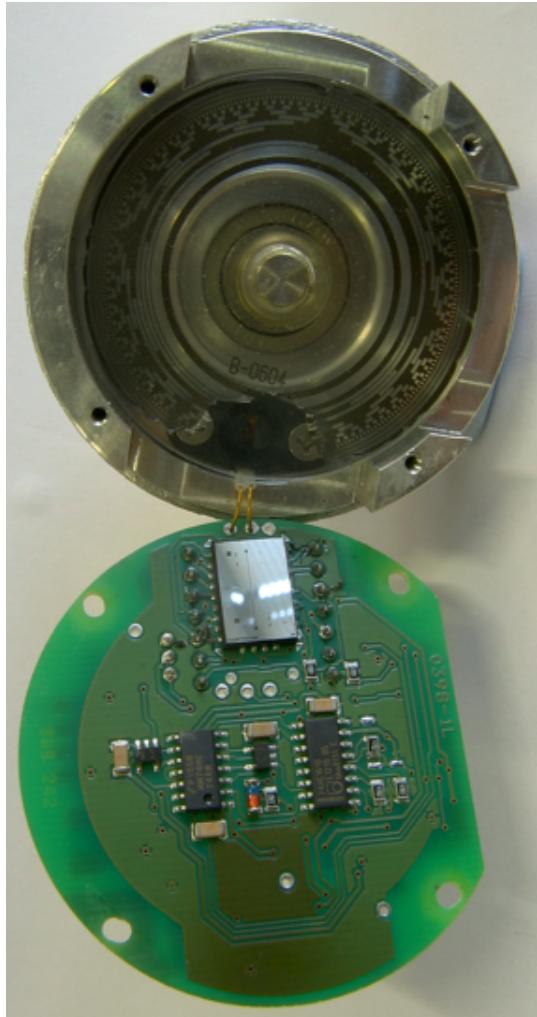
**8-bit** Gray-coded  
absolute encoder

DECIMAL	BINARY	GRAY
0	0000	0000
1	0001	0001
2	0010	0011
3	0011	0010
4	0100	0110
5	0101	0111
6	0110	0101
7	0111	0100
8	1000	1100
9	1001	1101
10	1010	1111
11	1011	1110
12	1100	1010
13	1101	1011
14	1110	1001
15	1111	1000

adjacent codes differ  
by just one bit



# Use of absolute encoders



13-bit absolute encoder opened:  
Gray-coded disk and electronics

- ready to measure at start (no “homing”)
- two modes for permanent operation
  - when switching off the drive, position parameters are saved on a flash memory (and brakes activated)
  - battery for the absolute encoder is always active, and measures position even when the drive is off
  - data memory > 20 years
- single-turn or multi-turn versions, e.g.
  - 13-bit single-turn has  $2^{13} = 8192$  steps per revolution (resolution =  $0.044^\circ$ )
  - 29-bit multi-turn has 8192 steps/revolution + counts up to  $2^{16} = 65536$  revolutions
- aluminum case with possible interface to field bus systems (e.g., CANopen or PROFIBUS)
- typical supply 5/28V DC @1.2 W



hollow shaft



round flange



multi-turn



# Incremental encoders

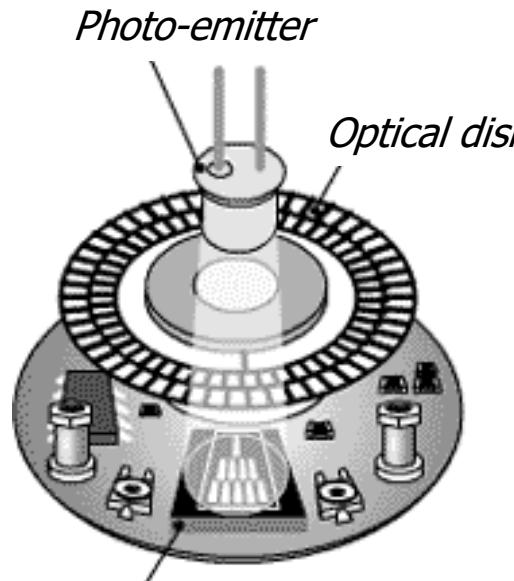
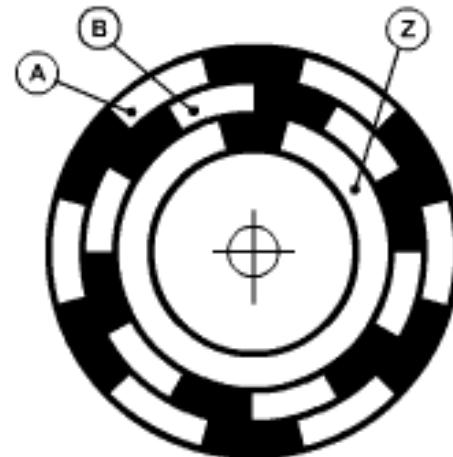


Photo-receiver

The three tracks  
on an optical disk  
(here  $N_e = 6$ )

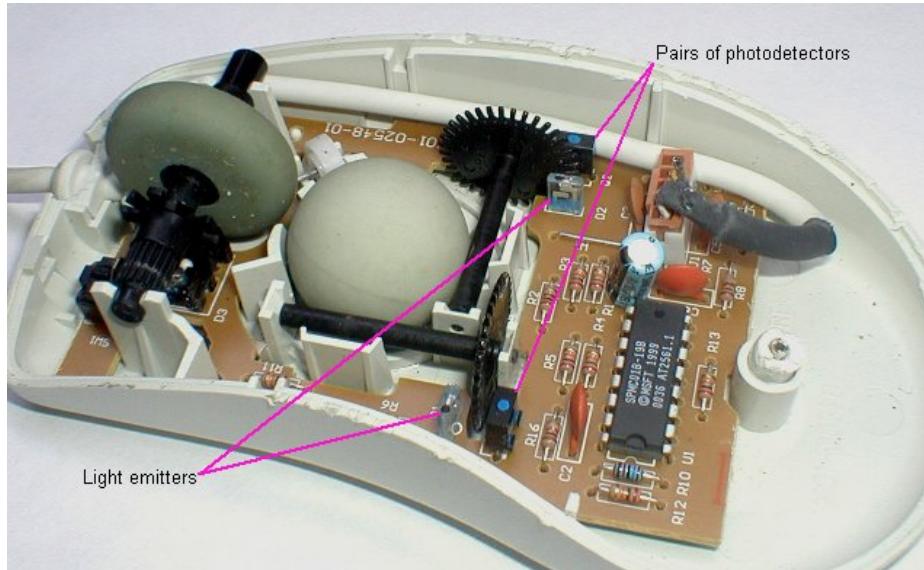


- optical rotating disk with three tracks, alternating transparent and opaque areas: measures **incremental** angular displacements by counting trains of  $N_e$  pulses ("counts") per turn ( $N_e = 100 \div 5000$ )
  - the two A and B tracks (**channels**) are in quadrature (phase shift of  $90^\circ$  electrical), allowing to detect the direction of rotation
  - a third track Z is used to define the "0" reference position, with a reset of the counter (**needs "homing"** at start)
  - some encoders provide as output also the three phases needed for the switching circuit of brushless motors



# Incremental encoders

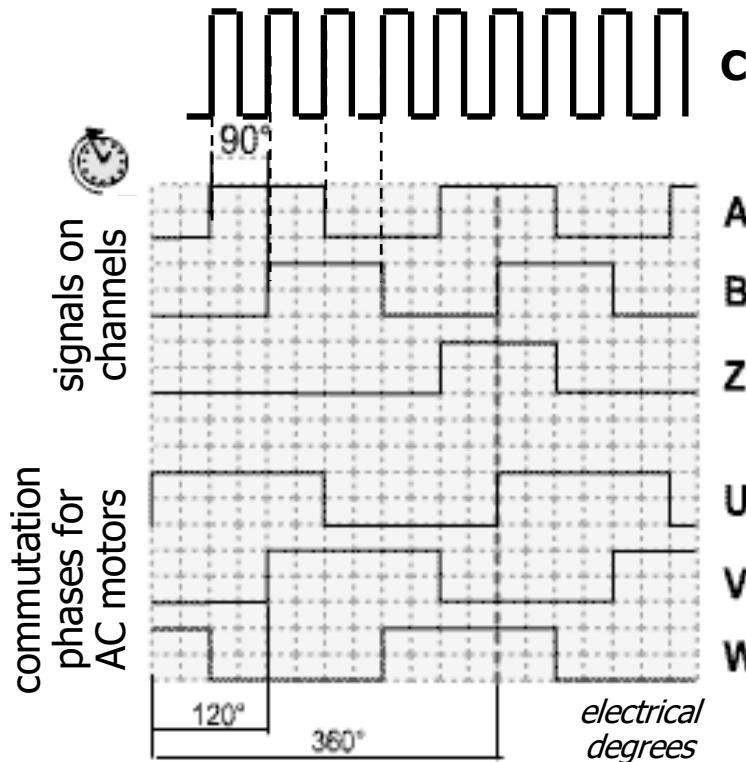
- two (cheap) incremental encoders inside a mouse
- a OMRON incremental encoder with 2000 pulses/turn



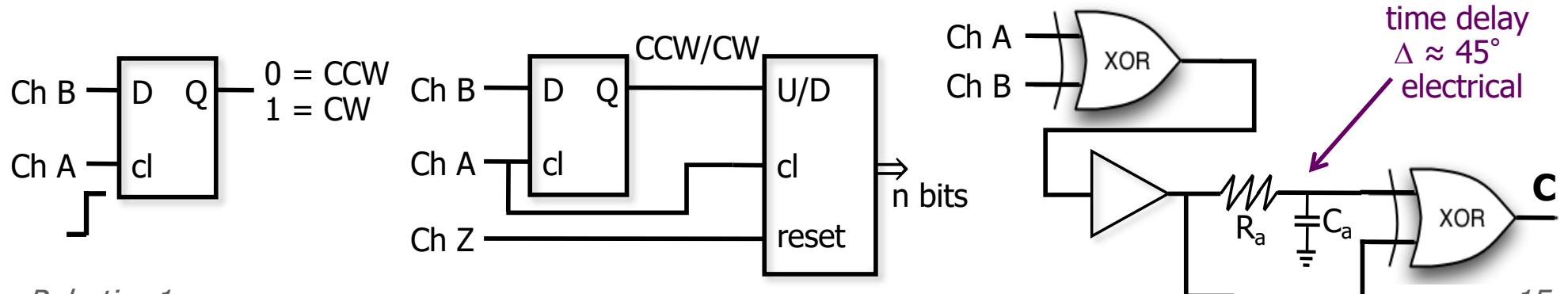
diameter  $\varnothing 40$  mm  
mass  $m \approx 100$  g  
inertia  $J = 1 \cdot 10^{-6}$  kg m<sup>2</sup>



# Signal processing



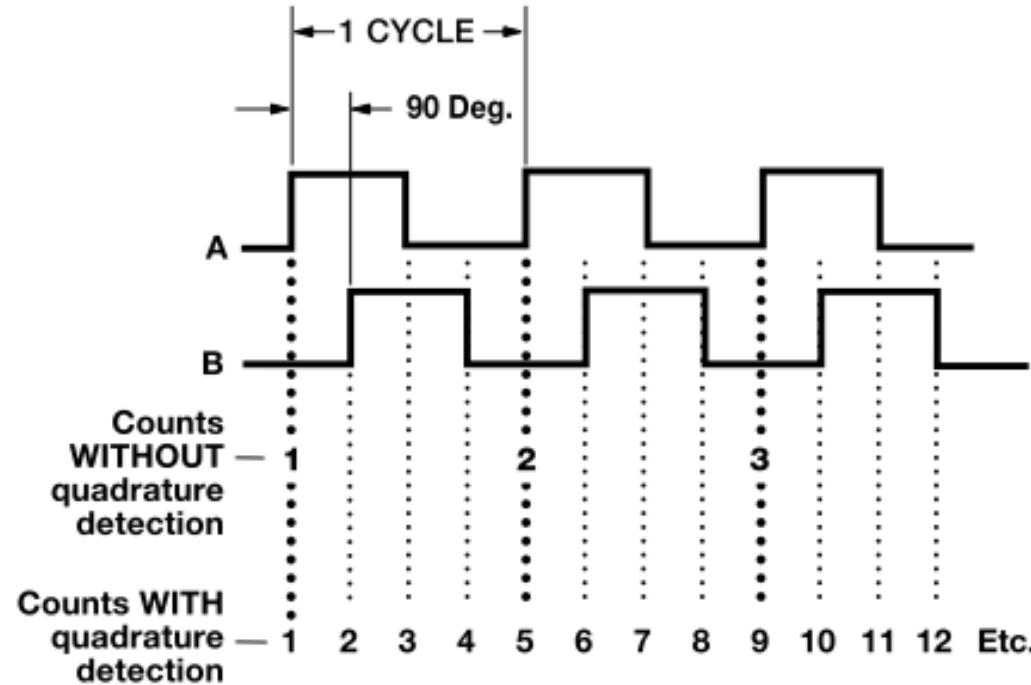
- c • “fractions of a cycle” of each pulse train are measured in “electrical degrees”
- A •  $1^\circ \text{ electrical} = 1^\circ \text{ mechanical}/N_e$   
 $360^\circ \text{ mechanical} = 1 \text{ turn}$
- B • signals are fed in a digital **counter**, with a **D-type** flip-flop to sense direction + **reset**
- Z • to **improve resolution** ( $4 \times$ ), the leading and trailing edges of signals A and B are used
- U • the sequence of pulses C will clock now the counter (**increments or decrements**)





# Count multiplication

## example of quadrature detection

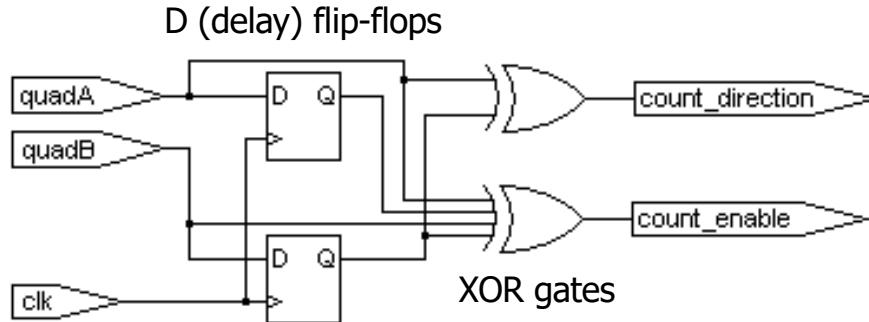


- an incremental encoder with  $N_e = 2000$  (electrical) cycles provides a count of  $N = 8000$  pulses/turn after electronic multiplication
- its final **resolution** is (mechanical)  $360^\circ/8000 = .045^\circ (= 0^\circ 2' 42'')$
- needs a 13-bit counter to cover a full turn without reset ( $2^{13} = 8192$ )

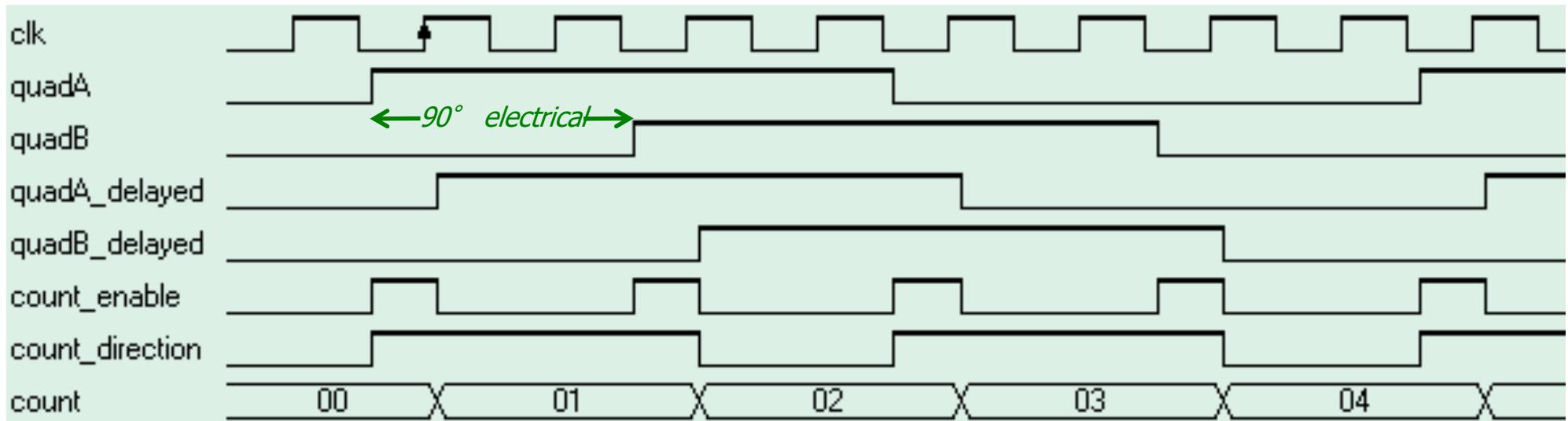


# Quadrature detection in incremental encoders

## a more complete implementation



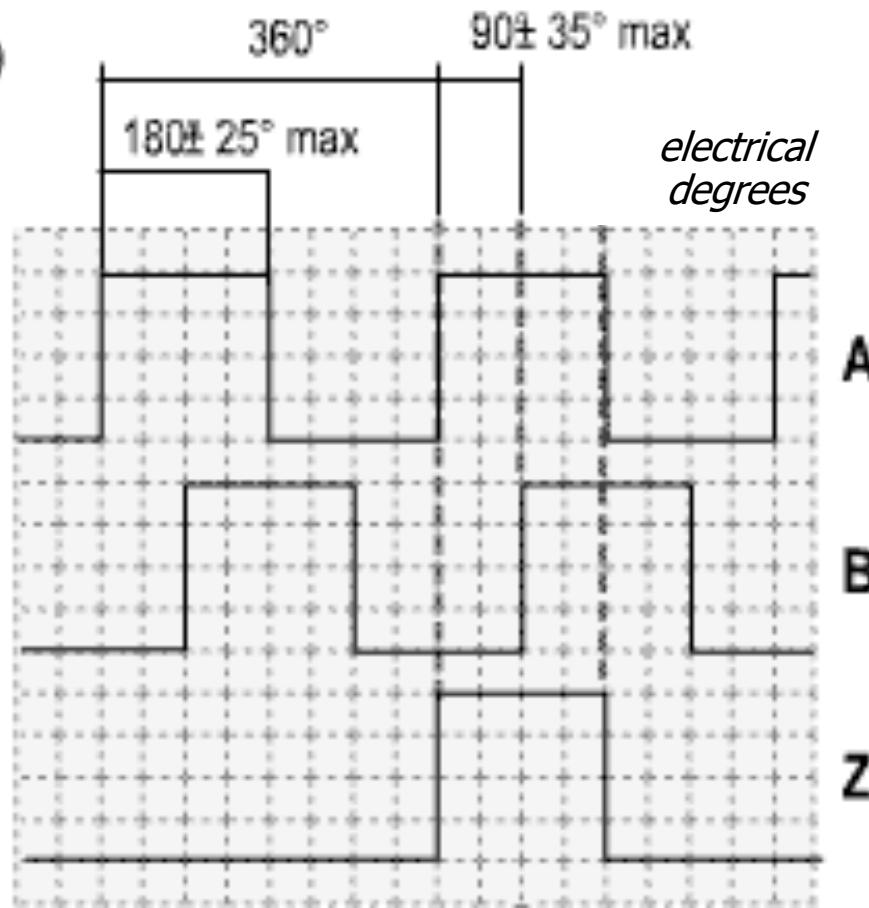
NOTE: since in practice A and B signals may **not** be synchronous to the clock signal, two extra D flip-flops per input should be used to avoid meta-stable states in the counters



- it is assumed that an oversampling clock "clk" (e.g., as provided by a FPGA) is available, which is faster than the two quadrature signals A and B
- the digital count output will have a **resolution** multiplied by 4



# Accuracy in incremental encoders



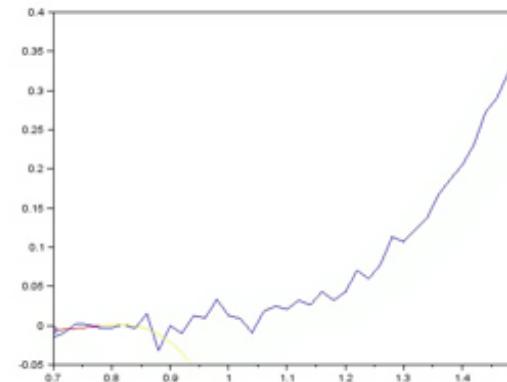
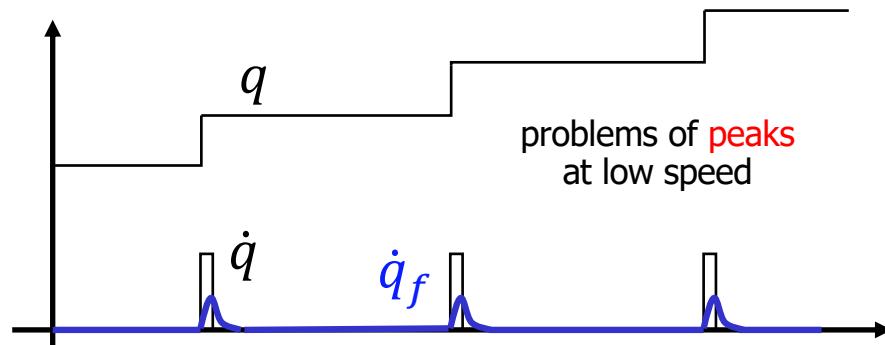
...apart from  
quantization errors

- division error: maximum displacement between two consecutive leading/trailing edges, typically within  $\max \pm 25^\circ$  electrical
- the phase shift of the two channels, nominally equal to 90° electrical, is typically within  $\max \pm 35^\circ$  electrical (quadrature error)



# Indirect measure of velocity

- numerical differentiation of digital measures of position
  - to be realized **on line** with Backward Differentiation Formulas (BDFs)
  - 1-step BDF (Euler):  $\dot{q}_k = \dot{q}(kT) = \frac{1}{T}(q_k - q_{k-1}) \Leftrightarrow \dot{q}_k = \frac{\Delta q_k}{T} \leftarrow$  directly from incremental encoder
  - 4-step BDF:  $\dot{q}_k = \frac{1}{T} \left( \frac{25}{12} q_k - 4q_{k-1} + 3q_{k-2} - \frac{4}{3} q_{k-3} + \frac{1}{4} q_{k-4} \right)$
- convolution **filtering** is needed because of noise and position quantization
  - use of **non-causal** filters (e.g., Savitzky-Golay) helps, **but** introduces delays
- **Kalman filter** for on line state estimation (**optimal**, assuming Gaussian noise)



**animation** of Savitzky-Golay filter  
with cubic polynomials



# Kinematic Kalman Filter for velocity estimation

motion and  
sensing  
discrete-time  
**model** for  
estimation

noisy position measure  
(encoder output)

$$\begin{aligned}\xi(k) &= \begin{pmatrix} 1 & T \\ 0 & 1 \end{pmatrix} \xi(k-1) + \mu \\ z(k) &= \begin{pmatrix} 1 & 0 \end{pmatrix} \xi(k) + \nu\end{aligned}$$

zero mean  
Gaussian noises  
with (co)variances  
 $Q$  (a matrix) and  $R$

$T$  = sampling time

$$\xi(k) = (x(k) \dot{x}(k))^T$$

actual state

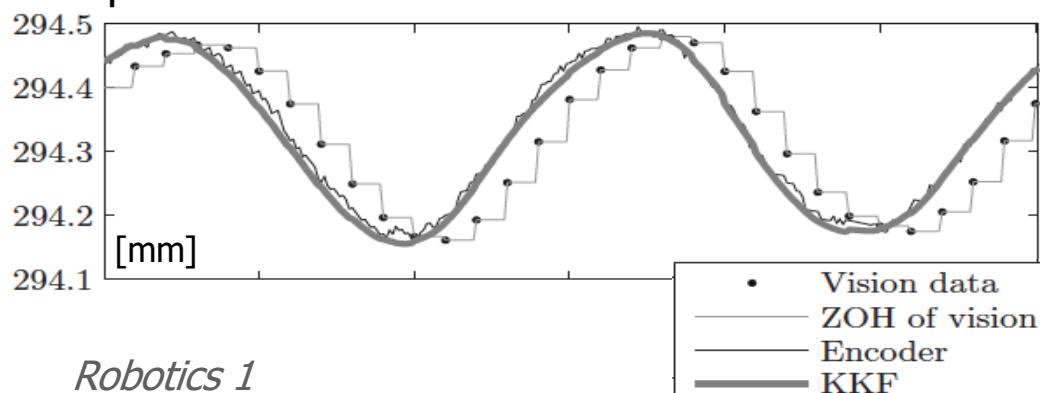
unmeasured  
velocity

design a (linear) **Kalman filter** providing an estimate  $\hat{\xi}(k)$  of the model state

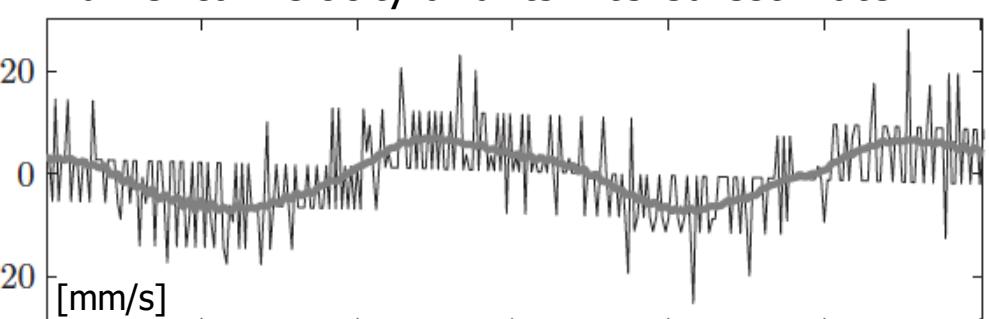
$$\hat{\xi}(k) = \underbrace{\begin{pmatrix} 1 & T \\ 0 & 1 \end{pmatrix} \hat{\xi}(k-1)}_{\text{(a priori) prediction}} + K_k \underbrace{\left( z(k) - \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} 1 & T \\ 0 & 1 \end{pmatrix} \hat{\xi}(k-1) \right)}_{\text{correction (based on the measured output)}}$$

using the optimal  
Kalman gain  $K_k$

position measure and its filtered version



numerical velocity and its filtered estimate

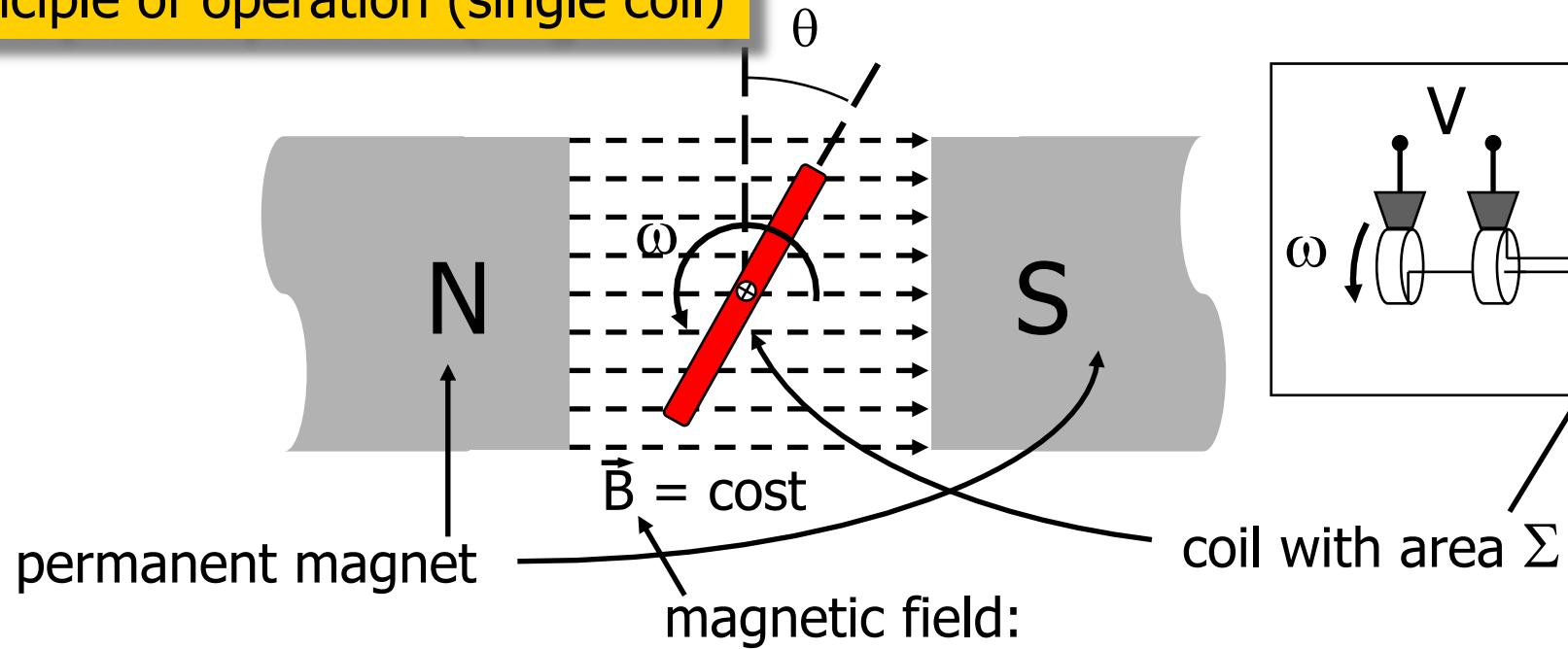




# Velocity sensor: Tachometer

always mounted on the (electrical) motor axis

principle of operation (single coil)



$$V = -d\Phi/dt = |\vec{B}|\Sigma \omega \sin \omega t$$

amplitude  $V \propto \omega$

⇒ to reduce ripples, use m coils rotated regularly by  $180^\circ/m$



# DC tachometer

## an example



- Servo-Tek Tach Generator (B series)
- bi-directional
- output voltage 11 ÷ 24 V @1000 RPM
- low ripple: < 3% peak-to-peak of DC value (with 72 KHz filter)
- weight = 113 g, diameter = 2.9 cm
- linearity error < 0.1% (at any speed)
- stability 0.1% (w.r.t. temperature)

### B-Series Specifications

Model Number	Mounting	Weight (approx)	Inertia (approx) oz · in.-sec <sup>2</sup>	V/1,000 RPM	RPM (max)	Driving Torque (max)	Arm R (ohms dynamic)	Arm Ind (h)
SA-740B-1*	Face	4.0 oz	$2.27 \times 10^{-4}$	20.8 V	8,000	0.25 oz-in.	1000	0.56
SB-740B-1*	Flange	4.0 oz	$2.27 \times 10^{-4}$	20.8 V	8,000	0.25 oz-in.	1000	0.56
SA-757B-1*	Face	4.0 oz	$2.27 \times 10^{-4}$	20.8 V	8,000	0.25 oz-in.	1000	0.56
SB-757B-1*	Flange	4.0 oz	$2.27 \times 10^{-4}$	20.8 V	8,000	0.25 oz-in.	1000	0.56

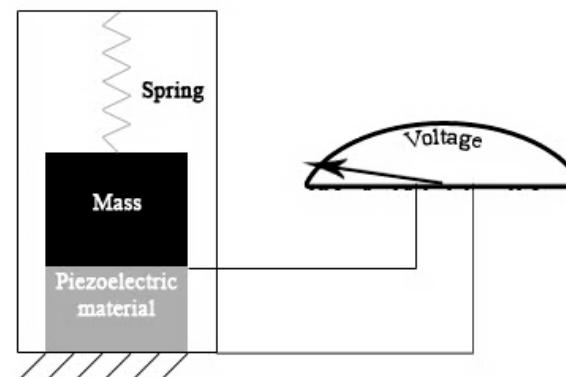
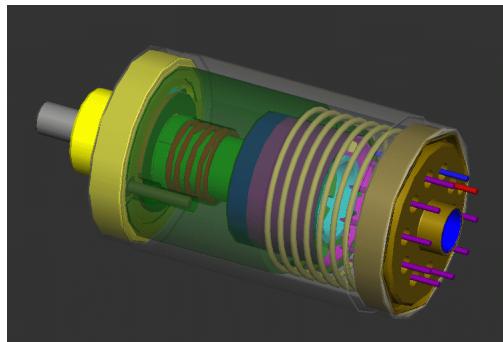


1.75 mNm (as a load)



# Accelerometers

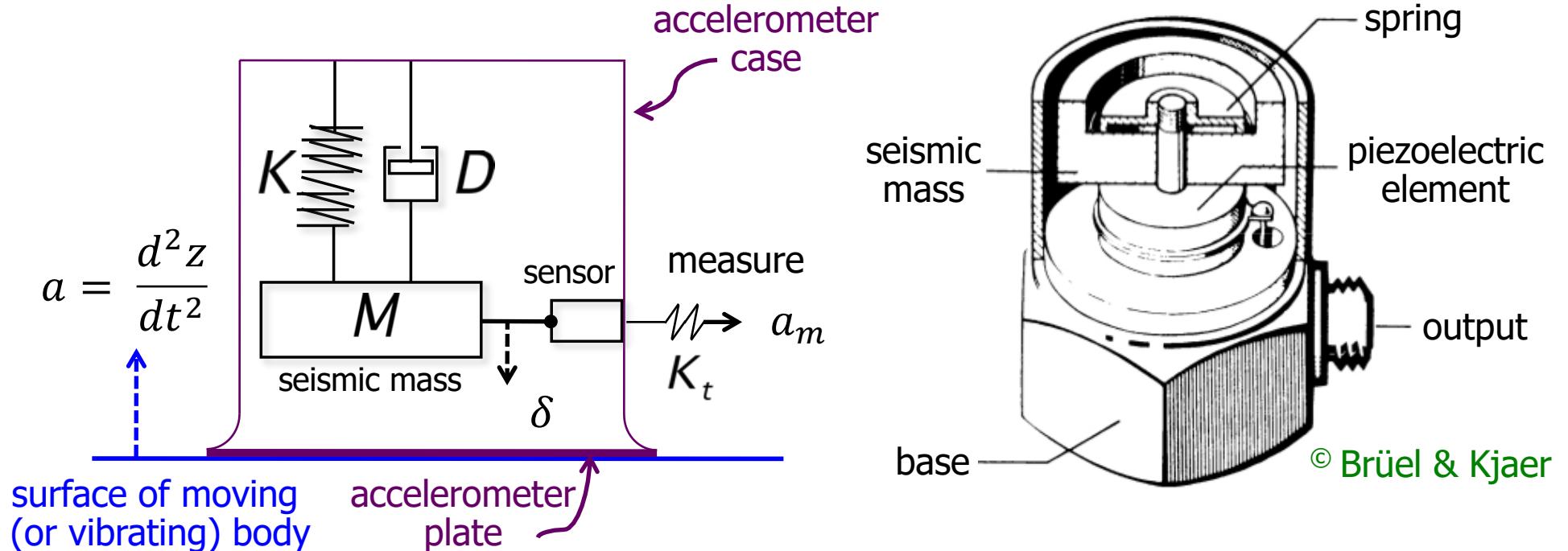
- measure of linear acceleration based on **inertial forces** (no “touch”)
  - units: [m/s<sup>2</sup>] or gravitational acceleration [g] (non-SI unit: 1g ≈ 9.81 m/s<sup>2</sup>)
- different principles for converting mechanical motion in an electrical signal
  - **piezoelectric**: piezoceramics (PZT) or crystals (quartz), better linearity & stability, wide dynamic range up to high frequencies, no moving parts, no power needed
  - **piezoresistive**: for high-shocks, measures also static acceleration ( $g_0$ ), needs supply
  - **capacitive**: silicon micro-machined sensing element, superior in static to low frequency range, can be operated in servo mode, cheap but limited resolution
  - modern solution: small **MEMS** (Micro Electro-Mechanical Systems)
- multiple applications: from vibration analysis to long range navigation



**animation** of  
measurement principle  
in a piezoelectric  
accelerometer



# Operation principle seismic accelerometer



$$Ma = M\ddot{\delta} + D\dot{\delta} + K\delta$$

by Laplace transform

$$a_m = K_t \delta$$

$$\frac{A_m(s)}{A(s)} = K_t \frac{M}{Ms^2 + Ds + K}$$

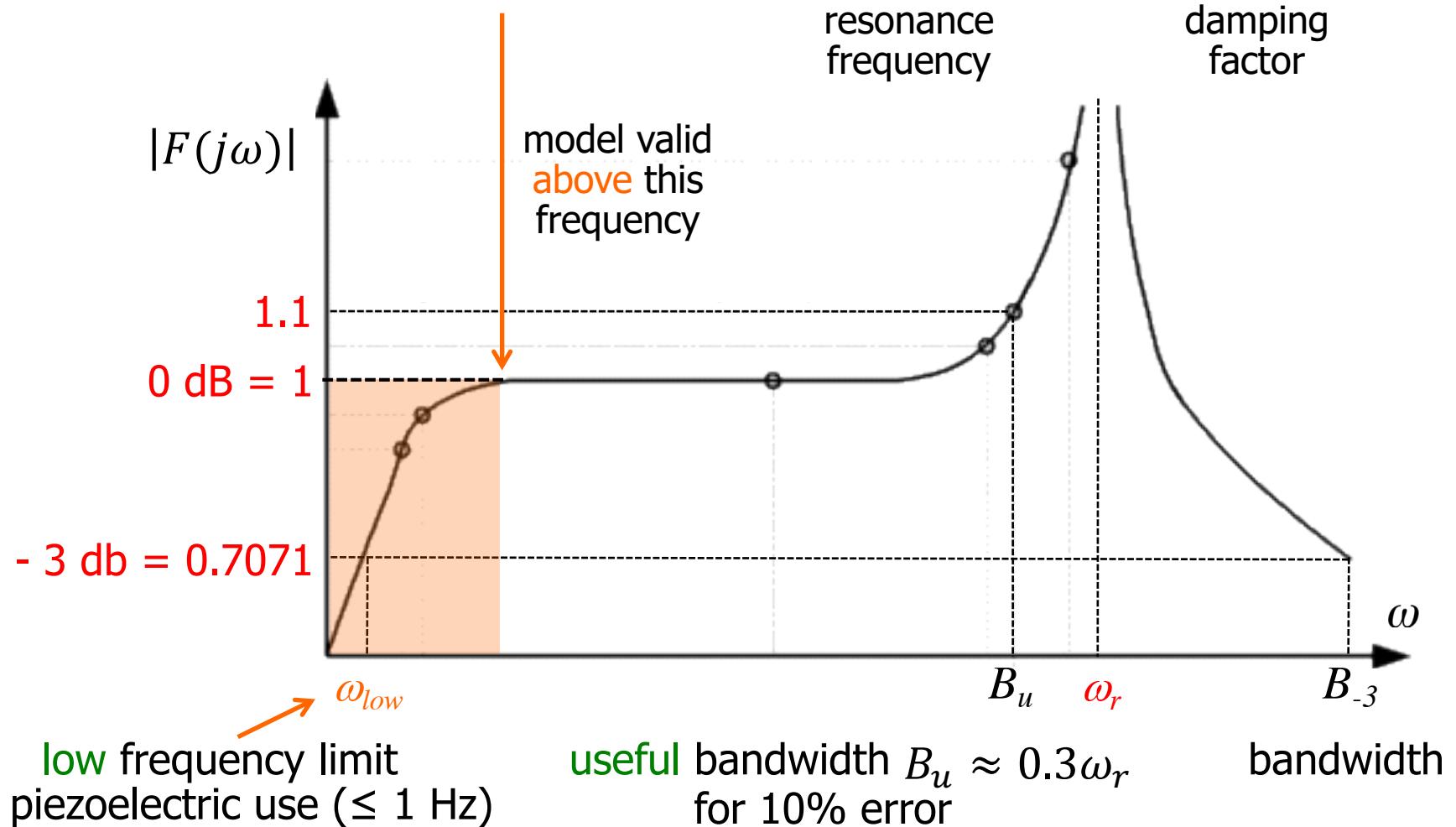
$$= \frac{K_t}{s^2 + (D/M)s + (K/M)}$$



# Frequency characteristics of a piezoelectric accelerometer

$$F(s) = \frac{A_m(s)}{A(s)} = \frac{K_t}{s^2 + (D/M)s + (K/M)}$$

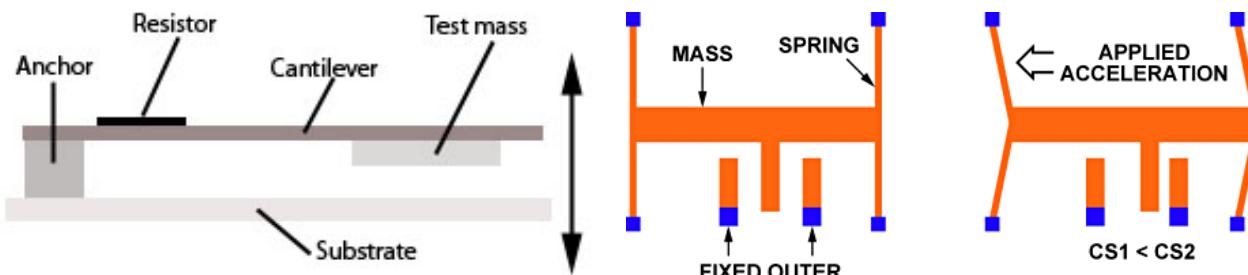
$$\omega_r = \sqrt{K/M} \quad \zeta = \frac{D}{2} \sqrt{1/KM}$$



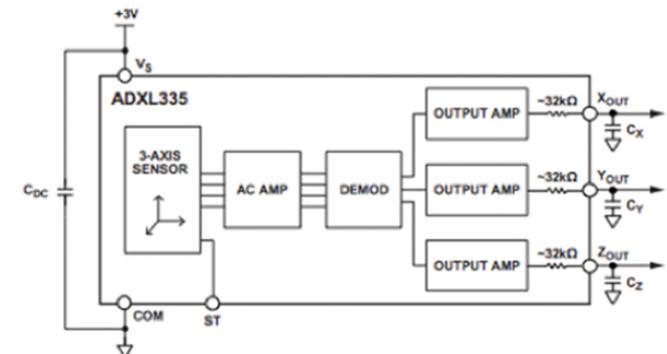
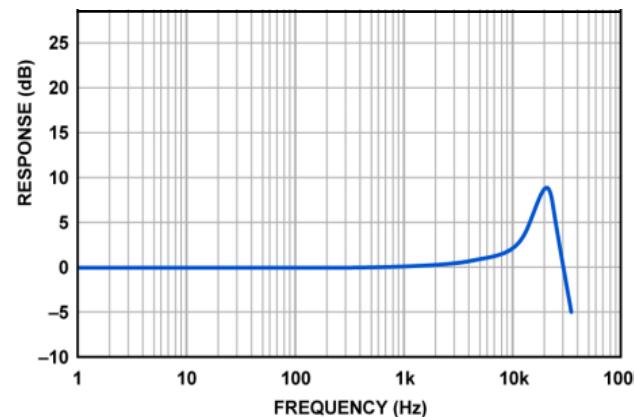
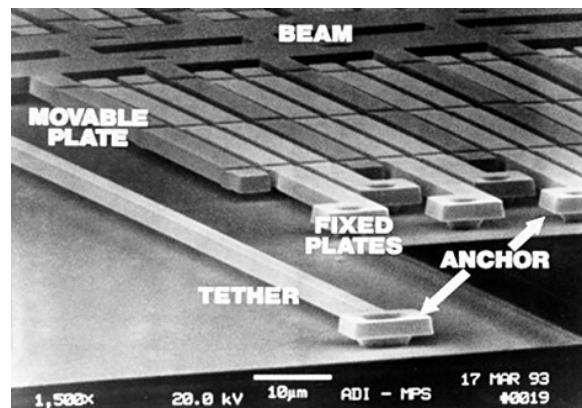


# MEMS accelerometers

- very simple MEMS (a **cantilever** beam with a **test mass**, with damping from the residual gas sealed in the device), single- or **tri-axial**, very small and light
- cross-couplings** among acceleration sensing directions should be limited  $\leq 3\%$

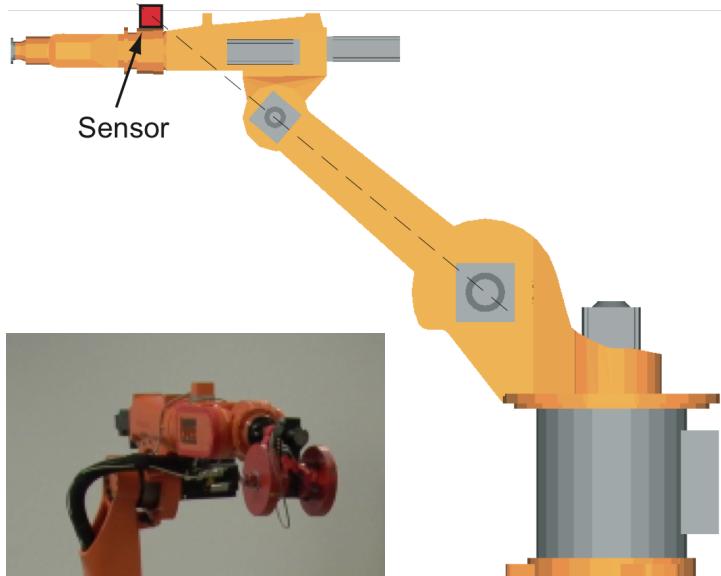


ADXL335 3-axis, small, low power,  $\pm 3g$ , with signal conditioned voltage outputs

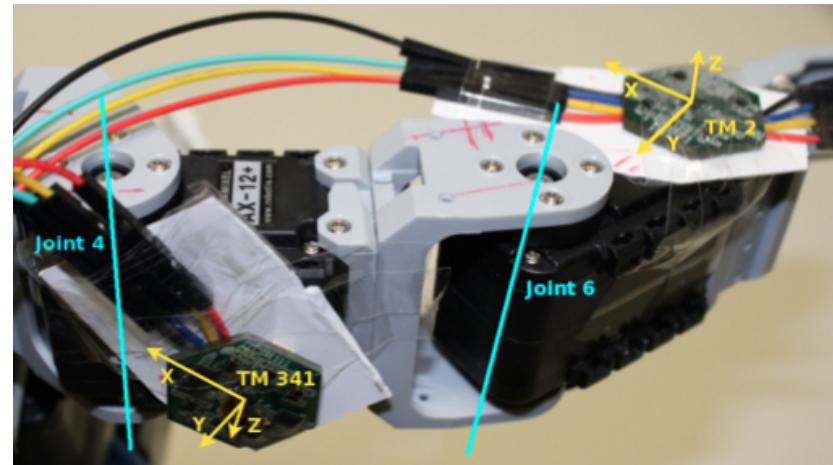




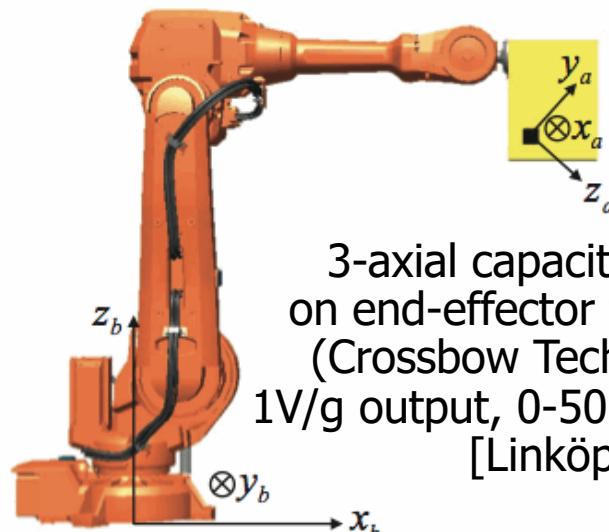
# Mounting accelerometers on robots



3-axisial MEMS  
accelerometer  
on the forearm  
of a [KUKA KR15/2](#)  
[DLR/Sapienza, 2007]



Bosch BMA 150 3-axial accelerometers  
integrated in two larger Tactile Modules on the  
links of a [Bioloid humanoid left arm](#) [TUM, 2011]



3-axisial capacitive accelerometer  
on end-effector tool of an [ABB robot](#)  
(Crossbow Technology: 2g range,  
1V/g output, 0-50 Hz,  $\pm 2^\circ$  align error)  
[Linköping, 2012]



---

## *Robotics 1*

# Robot components: Exteroceptive sensors

Prof. Alessandro De Luca

DIPARTIMENTO DI INGEGNERIA INFORMATICA  
AUTOMATICA E GESTIONALE ANTONIO RUBERTI





# Summary

---

- force sensors
  - strain gauges and joint torque sensor
  - 6D force/torque (F/T) sensor at robot wrist
  - RCC = Remote Center of Compliance (*not a sensor, but similar...*)
- proximity/distance sensors (⇒ moved to AMR course!)
  - infrared (IF)
  - ultrasound (US)
  - laser
  - with structured light
- vision
- examples of robot sensor equipment
- some **videos** intertwined, with applications

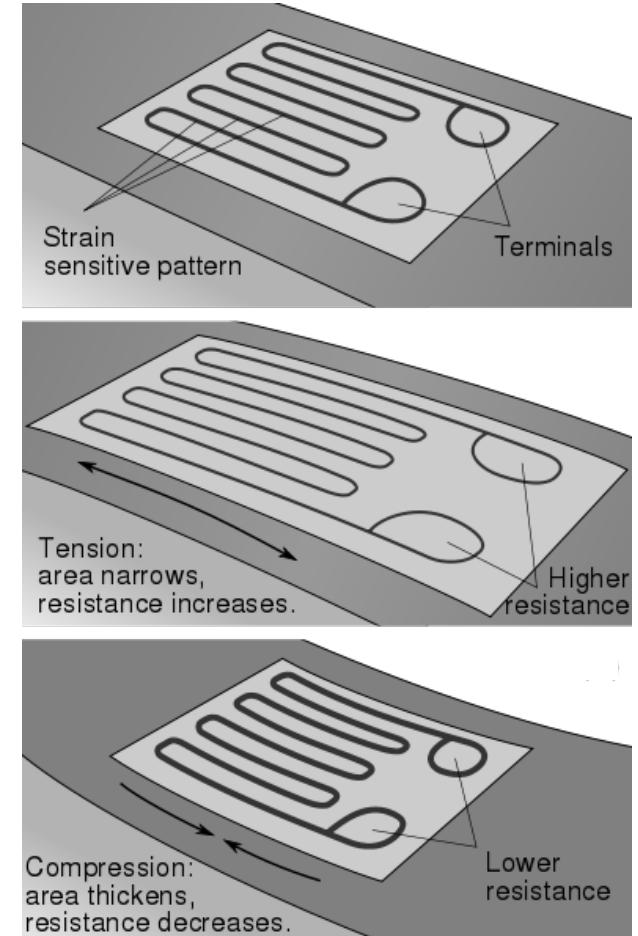


# Force/torque and deformation

- indirect information obtained from the measure of **deformation** of an elastic element subject to the force or torque to be measured
- basic component is a **strain gauge**: it uses the variation of the resistance  $R$  of a metal conductor when its length  $L$  and/or cross-section  $S$  vary

$$\frac{\partial R}{\partial L} > 0 \quad \frac{\partial R}{\partial S} < 0$$

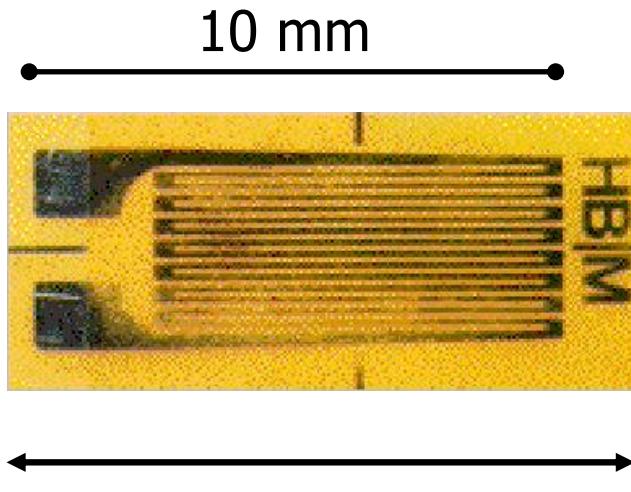
$$\frac{\partial R}{\partial T} \xleftarrow{\text{small}}$$



temperature



# Strain gauges



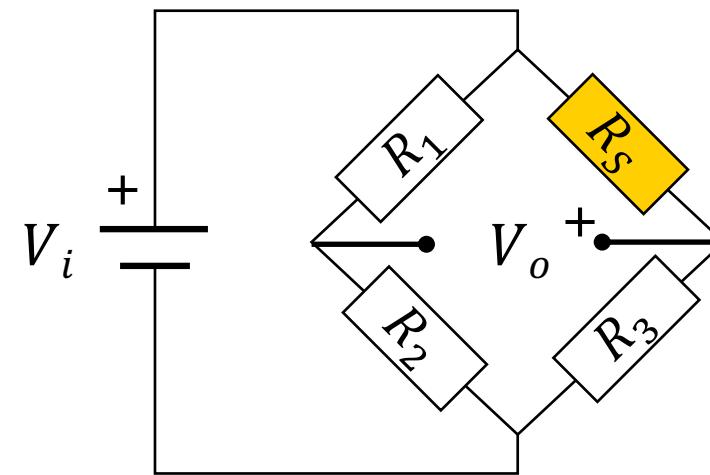
principal measurement axis

$$\text{Gauge-Factor} = \text{GF} = \frac{\Delta R / R}{\Delta L / L} \quad \text{strain } \varepsilon$$

(typically GF  $\approx 2$ , i.e., small sensitivity)

if  $R_1$  has the same dependence on  $T$  of  $R_s$   
thermal variations are automatically  
compensated

Wheatstone **single-point quarter-bridge**  
(for accurately measuring resistance)



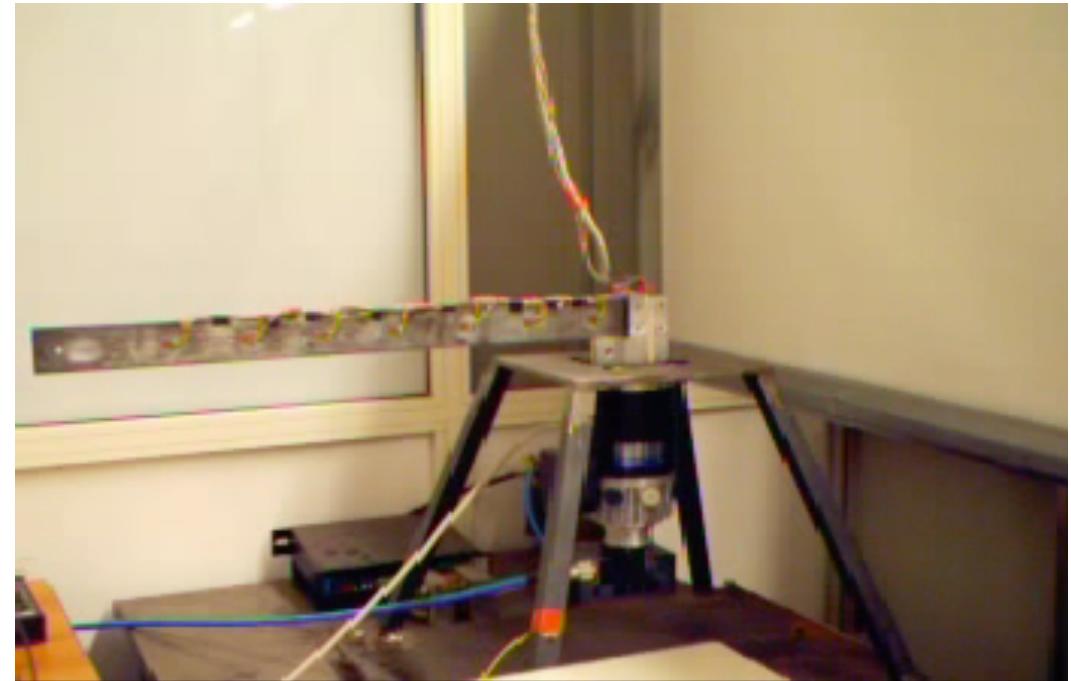
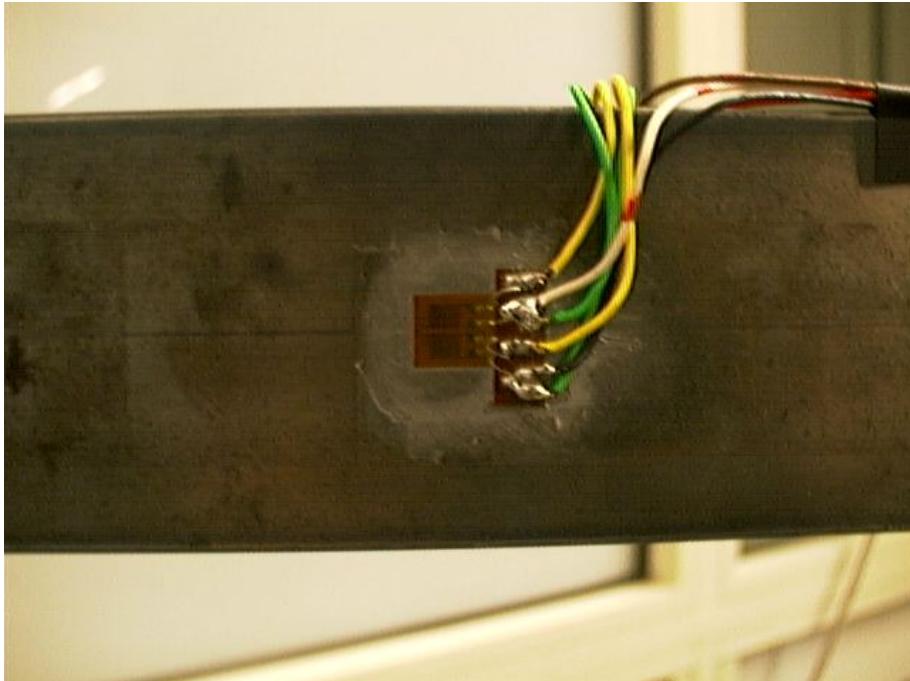
- $R_1, R_2, R_3$  very well matched ( $\approx R$ )
- $R_s \approx R$  at rest (no stress)
- **two-point** bridges have 2 strain gauges connected oppositely ( $\rightarrow$  sensitivity)

$$V_0 = \left( \frac{R_3}{R_3 + R_s} - \frac{R_2}{R_1 + R_2} \right) V_i$$



# Strain gauges in flexible arms

[video](#)

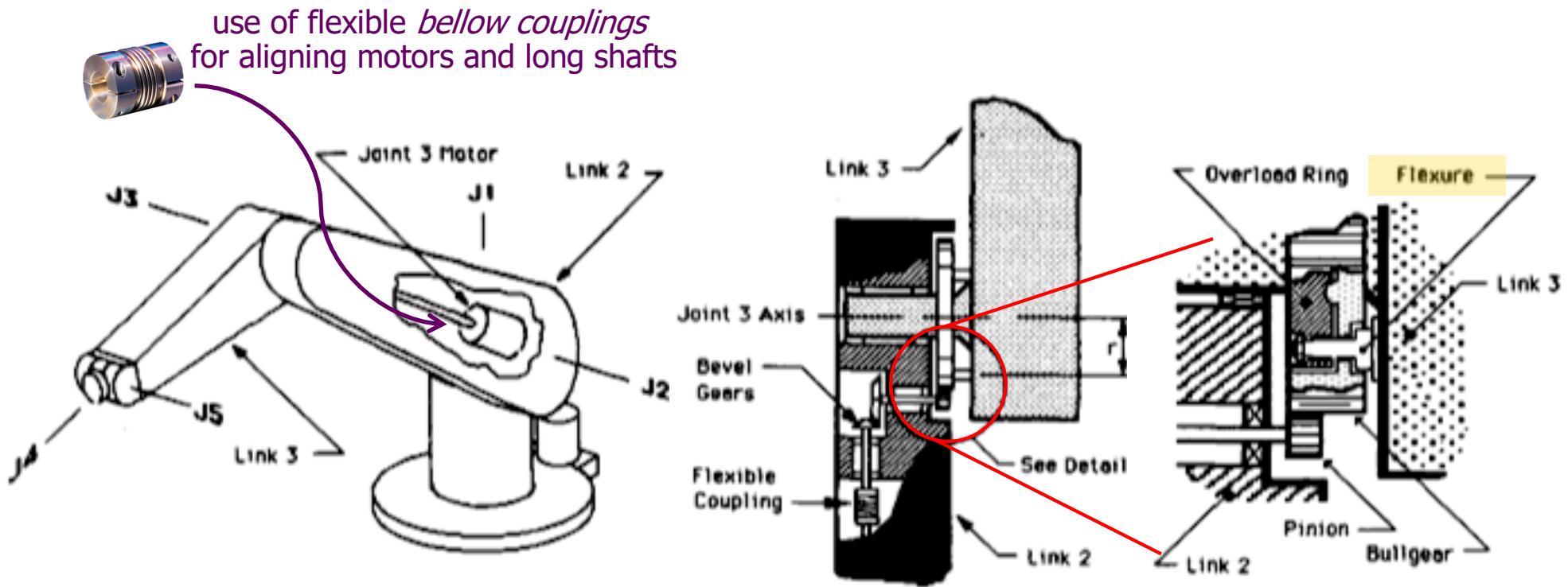


7 strain gauges glued<sup>(1)</sup> to a flexible aluminum beam (a robot “link”) measuring its local “curvature” in dynamic bending during slew motions (a **proprioceptive** use of these sensors)

<sup>(1)</sup> by cyanoacrylic glue



# Torque sensor at robot joints



strain gauge mounted to “sense” the axial deformation of the transmission shaft of joint #3 (elbow) in a PUMA 500 robot (again, a **proprioceptive** use of this sensor)



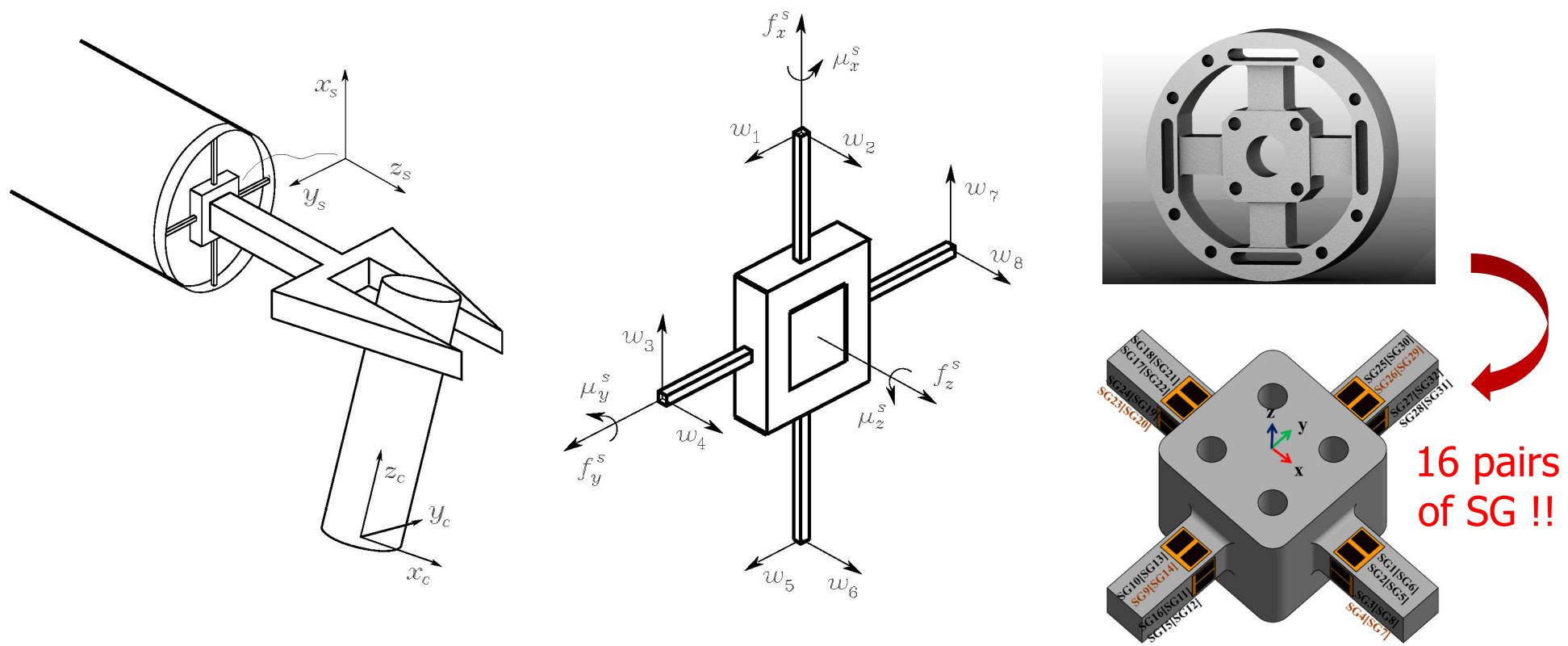
# Force/torque sensor at robot wrist

---

- a device (with the outer form of a cylinder), typically located between the last robot link and its end-effector
- top and bottom plates are mechanically connected by a number of **deformable elements** subject to **strain** under the action of forces and moments
- there should be at least one such element in any direction along/around which a force or torque measure is needed
- since a complete “decoupling” of these measurements is hard to obtain, there are  $N \geq 6$  such deformable elements
- on each element, a **pair of strain gauges** is glued so as to undergo opposite deformations (e.g., traction/compression) along the main axis of measurement



# Maltese-cross configuration



- diameter  $\approx 10$  cm
- height  $\approx 5$  cm
- $50 \div 500$  N (resolution 0.1%)
- $5 \div 70$  Nm (resolution 0.05%)
- sample frequency  $\approx 1$  KHz

- 4 deformable elements
- two pairs of strain gauges (**SG**) mounted on opposite sides of each element (**8 pairs**)
- the two gauges of each pair are placed adjacent on the same Wheatstone bridge



# 6D force/torque sensors

- ATI series
- cost (in 2016): about 6 K€ for Mini45 model + 700 € DAQ card

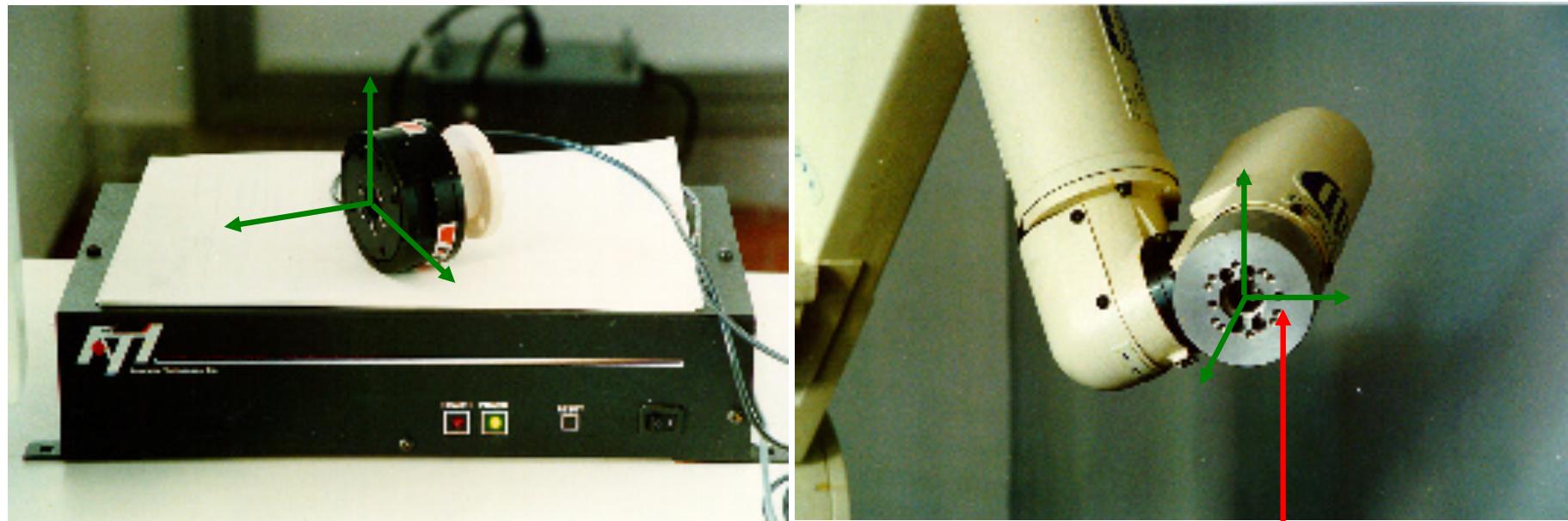


Model	Max Fx,Fy*	Max Tx,Ty*	Weight**	Diameter**	Height**
Nano17	±50 N	±500 N-mm	0.0091 kg	17 mm	14 mm
Nano25	±250 N	±6 N-m	0.064 kg	25 mm	22 mm
Nano43	±36 N	±500 N-mm	0.041 kg	43 mm	11 mm
Mini40	±80 N	±4 N-m	0.05 kg	40 mm	12 mm
Mini45	±580 N	±20 N-m	0.091 kg	45 mm	16 mm
Gamma	±130 N	±10 N-m	0.25 kg	75 mm	33 mm
Delta	±660 N	±60 N-m	0.91 kg	94 mm	33 mm
Theta	±2500 N	±400 N-m	5 kg	150 mm	61 mm
Omega160	±2500 N	±400 N-m	2.7 kg	160 mm	56 mm
Omega190	±7200 N	±1400 N-m	6.4 kg	190 mm	56 mm



# 6D force/torque sensor

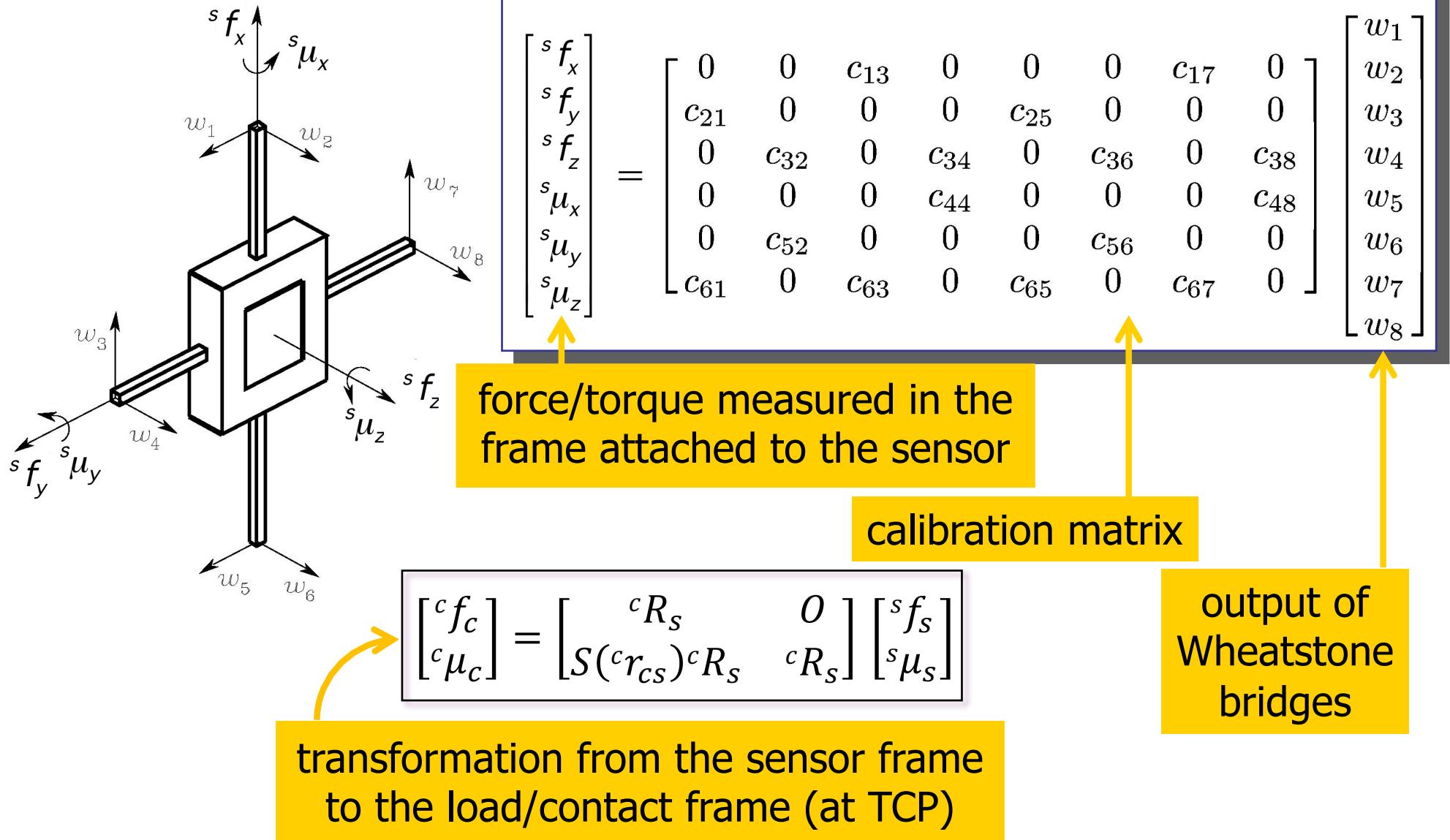
- electronic processing unit and mounting on an industrial robot (Comau Smart 3 robot, 6R kinematics)



mounting flange  
(on link 6 of the manipulator arm)

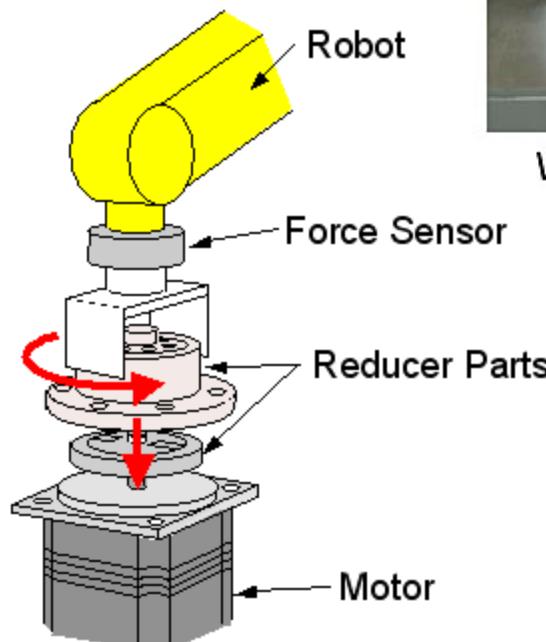


# 6D F/T sensor calibration

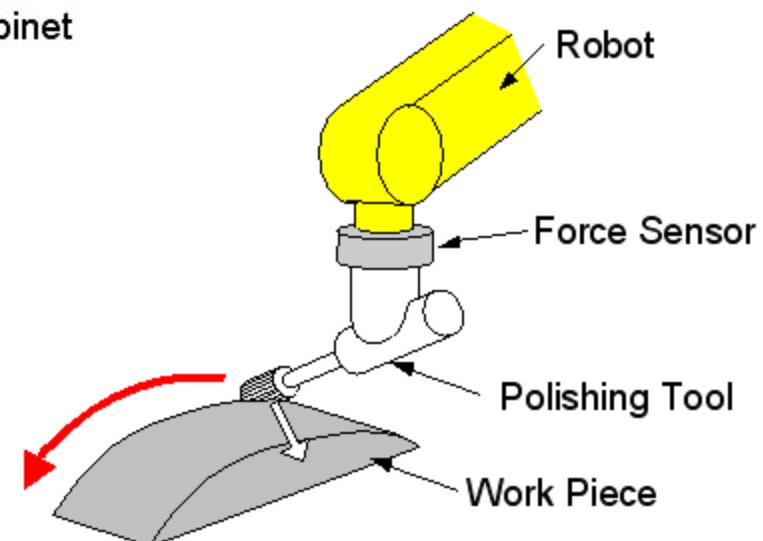
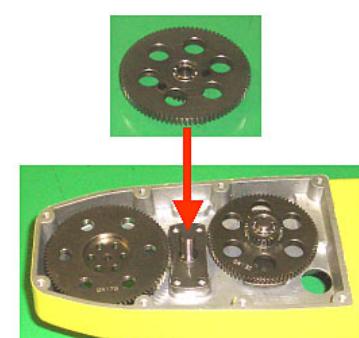




# Typical uses of a F/T sensor



Phase matching by force sensing



Following with constant pushing force



# Active assembly with F/T sensor

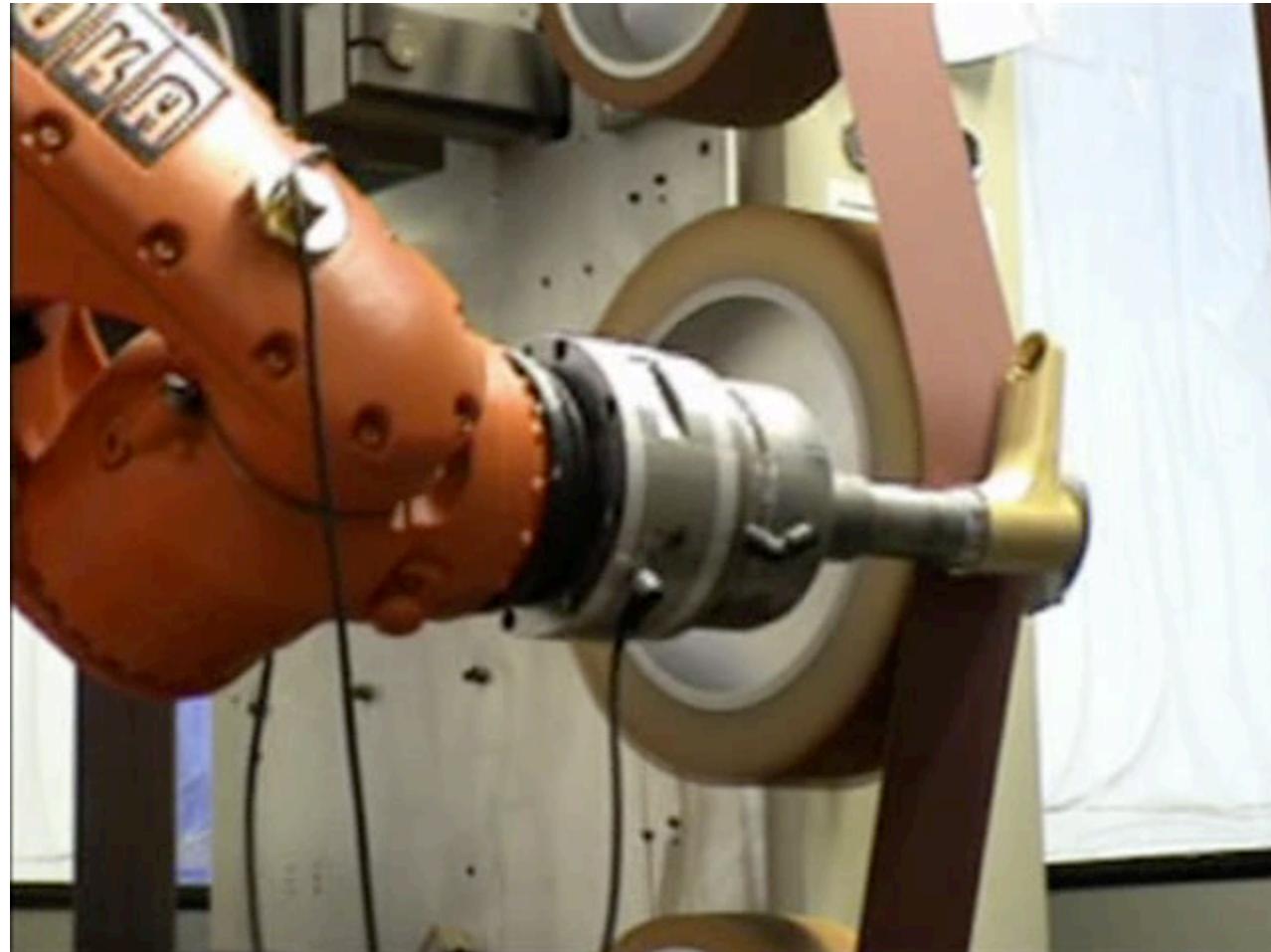


video

ABB robot with ATI F/T sensor



# Surface finishing with F/T sensor



video

KUKA robot with F/T sensor



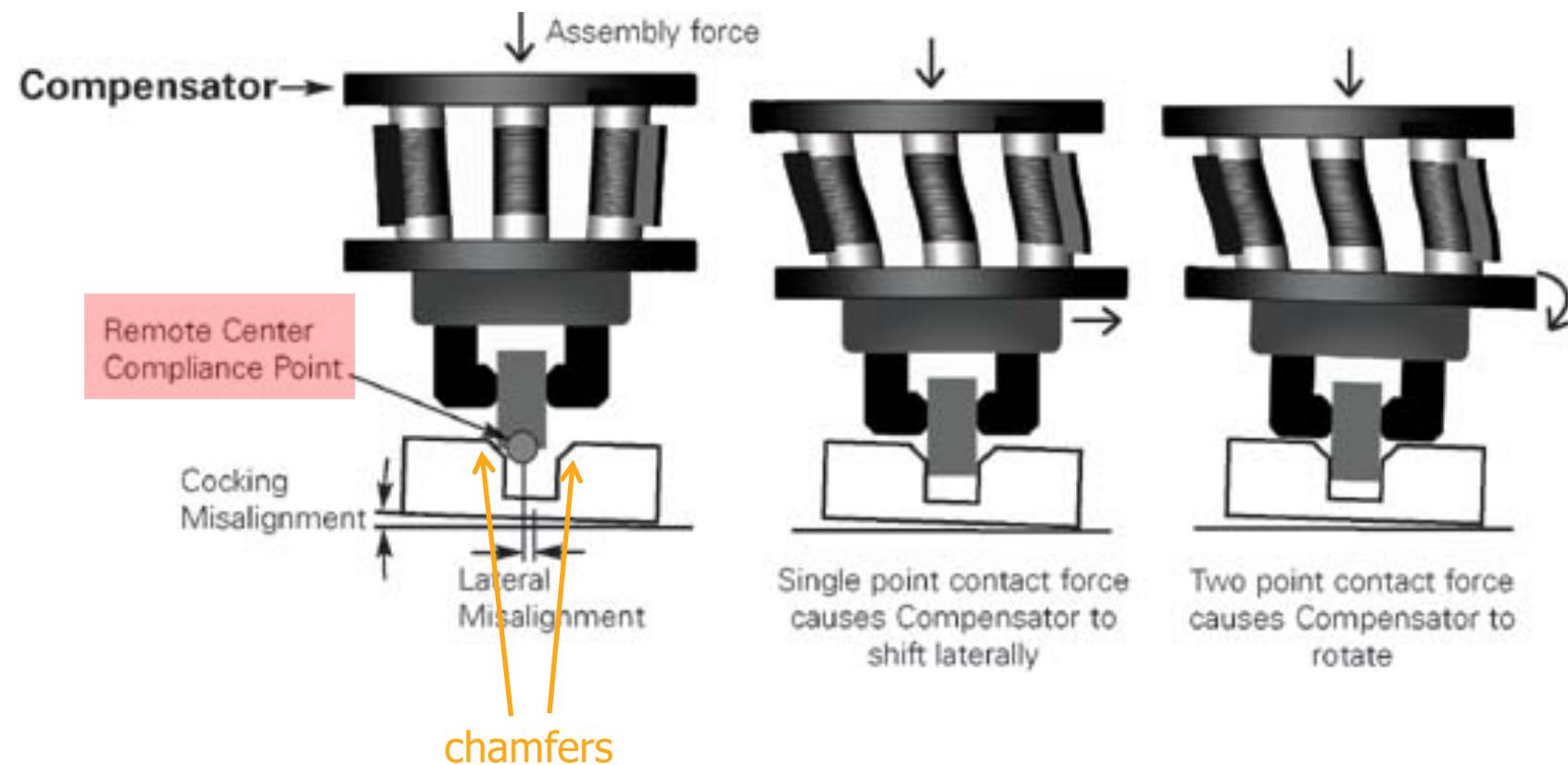
# Passive RCC device

- RCC = Remote Center of Compliance
- placed on the wrist so as to introduce **passive “compliance”** to the robot end-effector, in response to static forces and moments applied from the environment at the contact area
- mechanical construction yields “**decoupled**” linear/angular motion responses **if** contact occurs at or near the RCC point



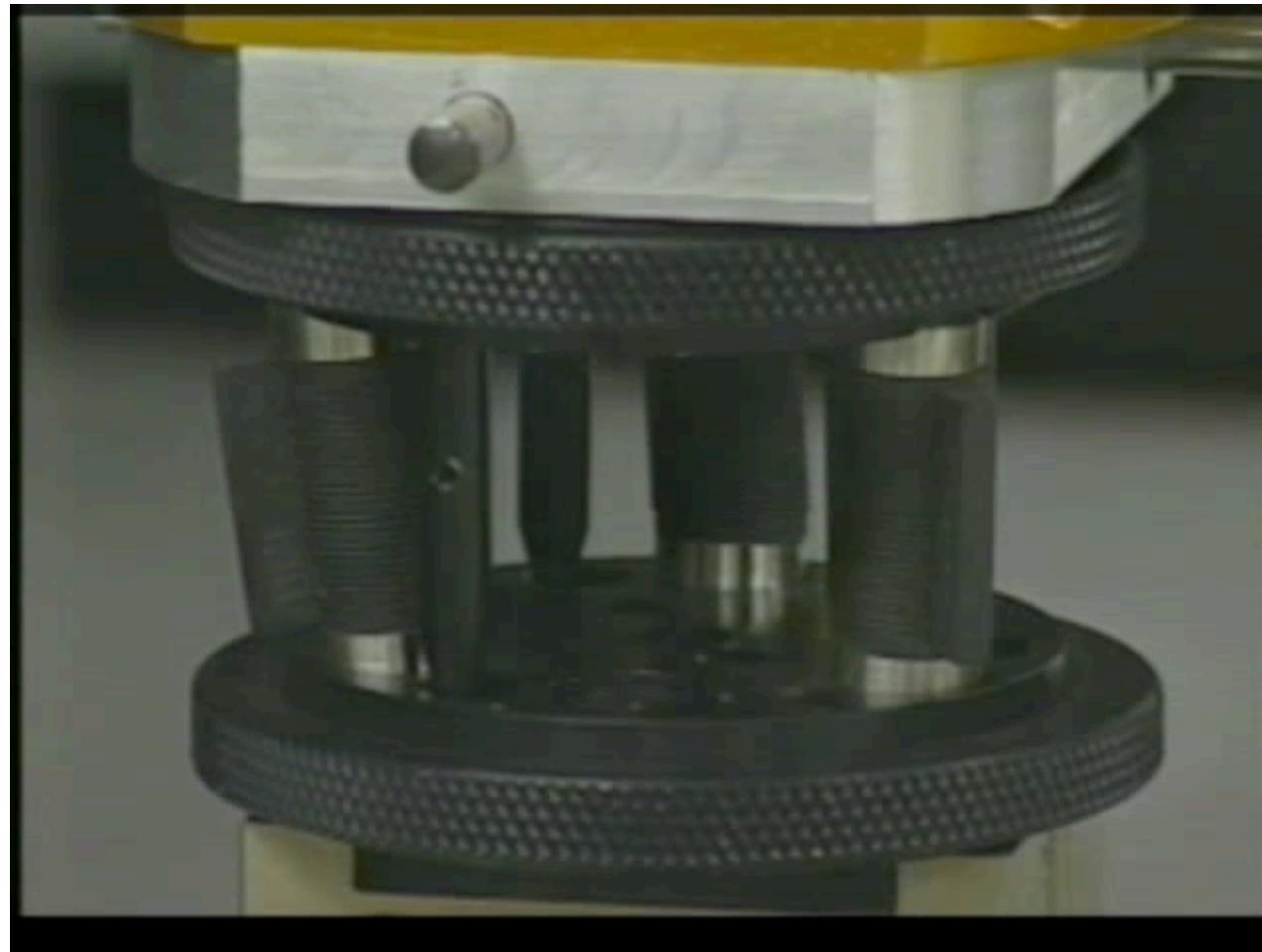


# Assembly with RCC





# Passive assembly with RCC



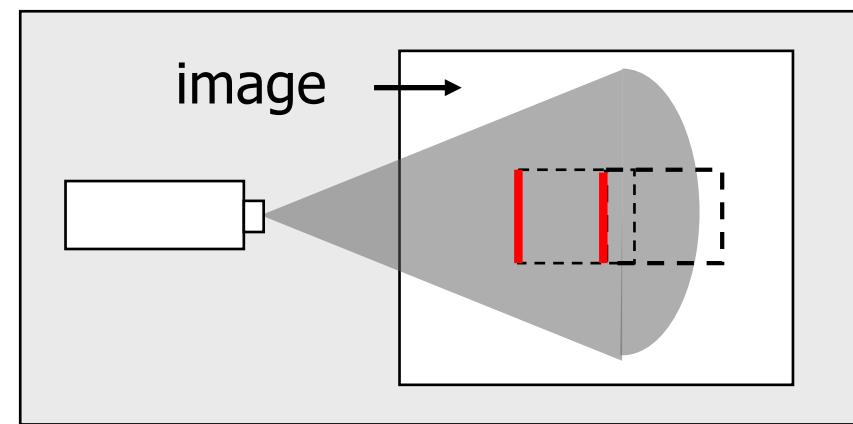
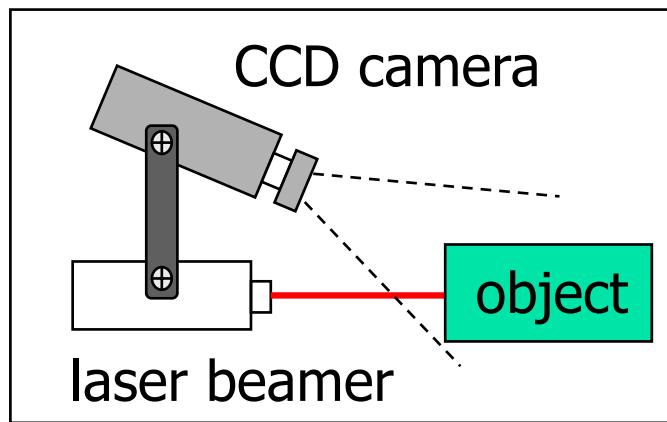
video

RCC by ATI Industrial Automation  
<http://www.ati-ia.com>

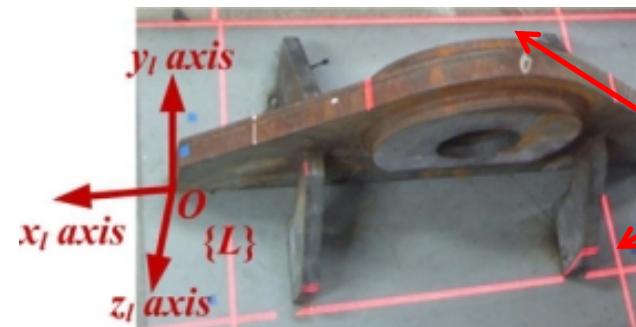


# Proximity/distance sensors - 4

- **structured light:** a laser beam (coherent light source) is projected on the environment, and its planar intersection with surrounding objects is detected by a (tilted) camera
- the position of the “red pixels” on the camera image plane is in **trigonometric** relation with the object distance from the sensor



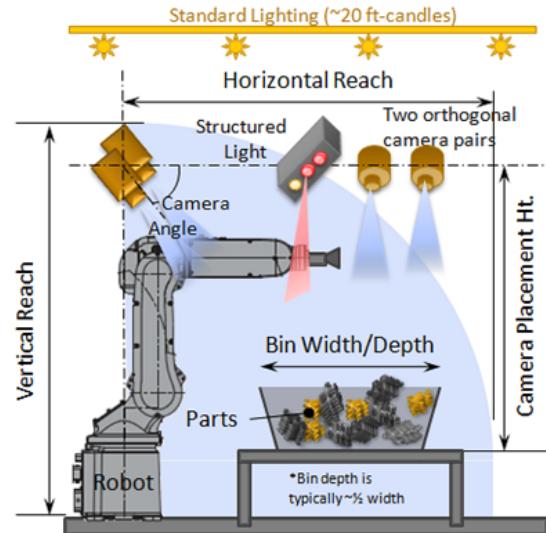
side view



top view



# Use of structured light sensors



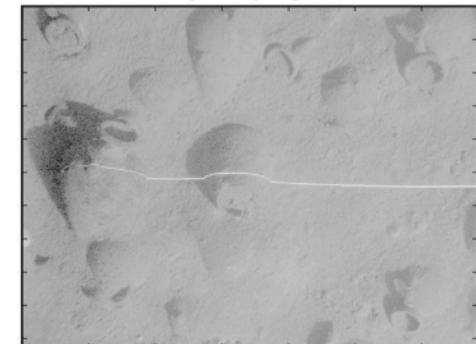
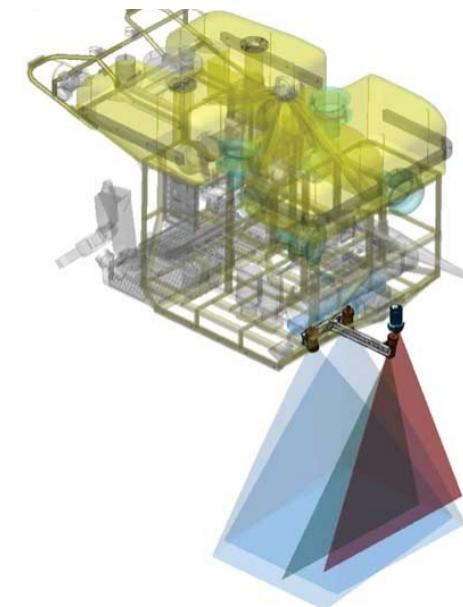
Random [bin picking](#) of 10-30 parts/minute (with surface inspection) with a 6R industrial robot, two pairs of cameras and a structured light sensor [Universal Robotics]



Structured light approach to best fit and [finish car bodies](#) (down to 0.1 mm) for reducing wind noise [Ford Motor Co.]



[Virtobot](#) system for post-mortem 3D optical scanning of human body & image-guided needle placement [Univ. Zürich]



[Hercules ROV](#) + structured-laser-light imaging system for high-resolution bathymetric underwater maps [Univ. Rhode Island]

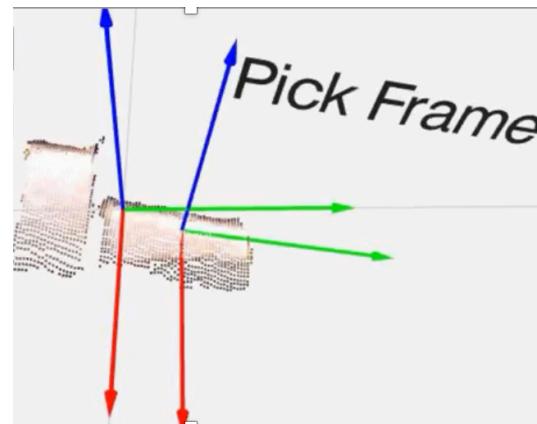


# Robotic bin picking using vision and structured light

video

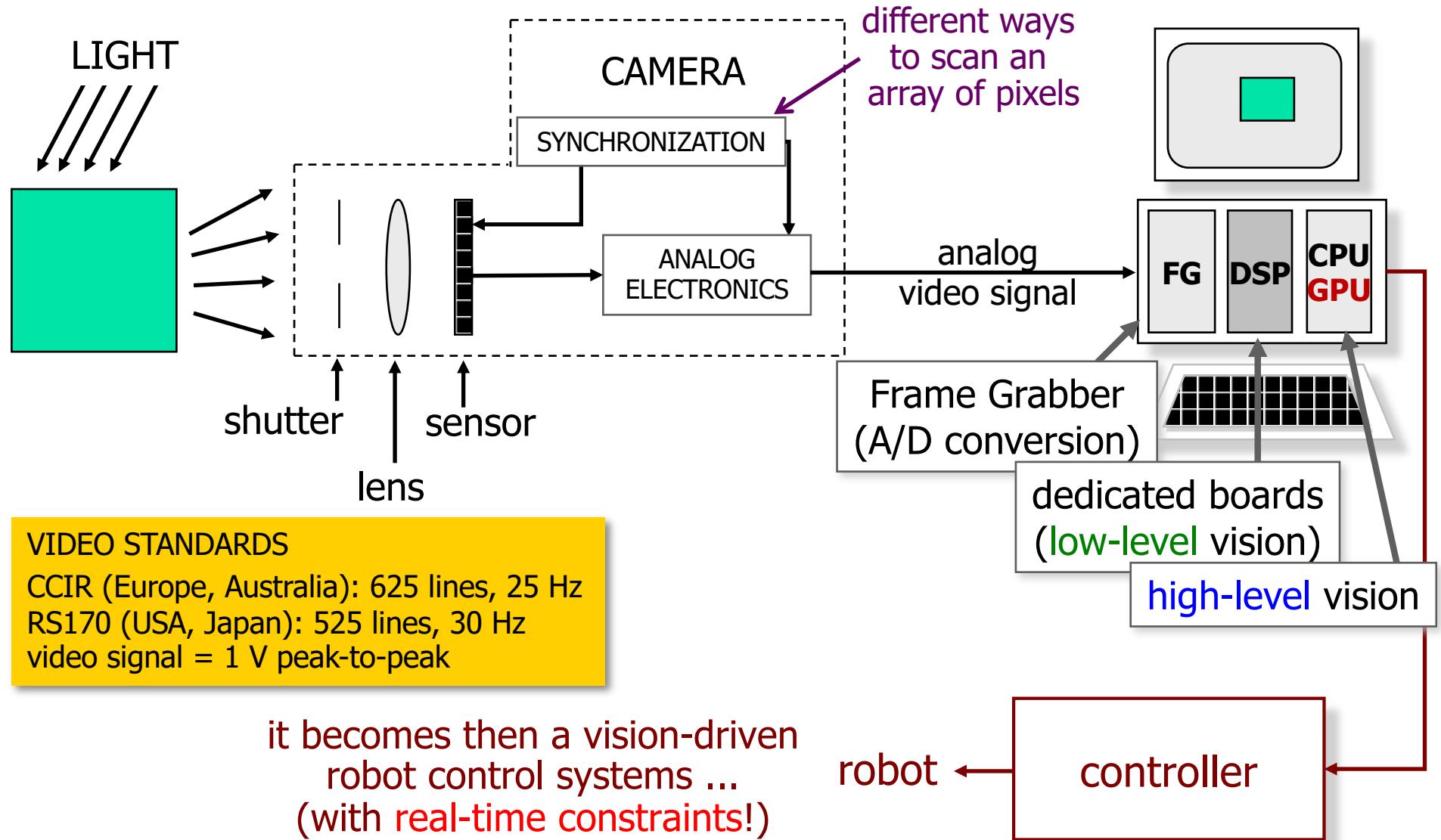


video





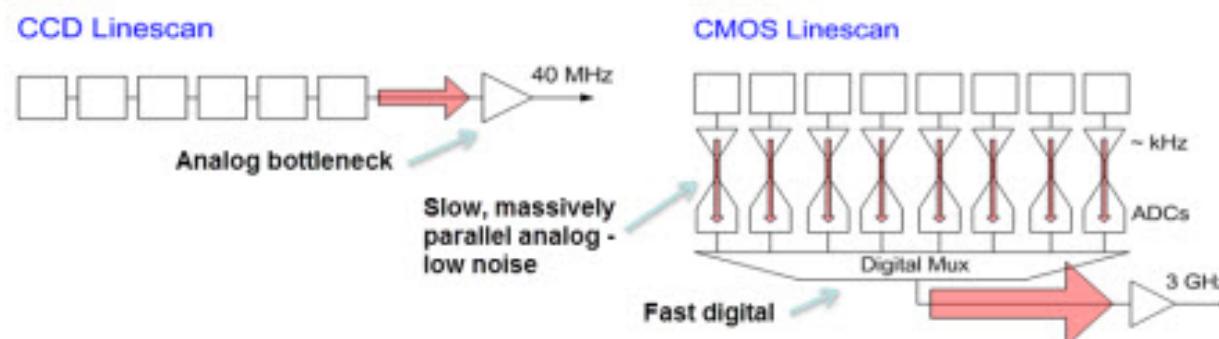
# Vision systems





# Sensors for vision

- arrays (spatial sampling) of photosensitive elements (**pixel**) converting light energy into electrical energy
- **CCD** (Charge Coupled Device): each pixel surface is made by a semiconductor device, **accumulating** free charge when hit by photons (**photoelectric effect**); “integrated” charges “read-out” by a sequential process (external circuitry) and transformed into voltage levels
- **CMOS** (Complementary Metal Oxide Semiconductor): each pixel is a **photodiode**, directly providing a voltage or current proportional to the **instantaneous** light intensity, with possibility of random access to each pixel





# CMOS versus CCD

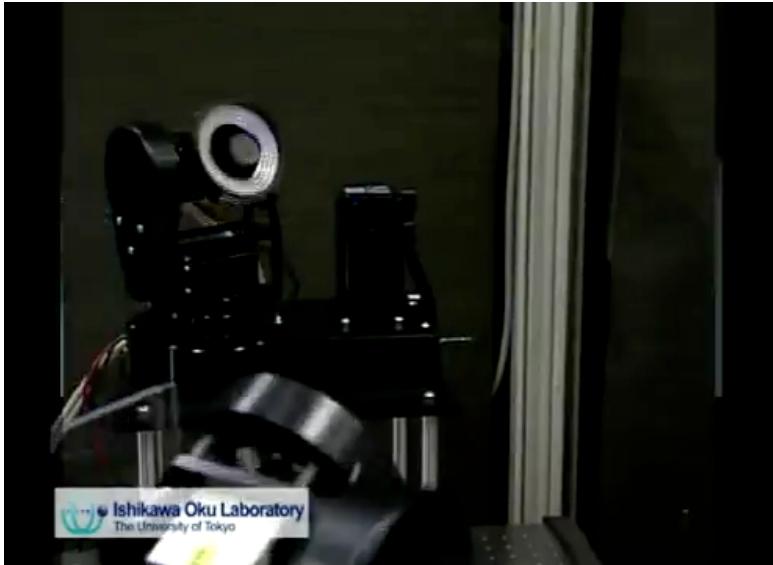
---

- reduction of fabrication costs of CMOS imagers
- better spatial resolution of elementary sensors
  - CMOS: 1M pixel, CCD:  $768 \times 576$  pixel
- faster processing speed
  - 1000 vs. 25 fps (frames per second)
- possibility of integrating “intelligent” functions on single chip
  - sensor + frame grabber + low-level vision
- random access to each pixel or area
  - flexible handling of ROI (Region Of Interest)
- possibly lower image quality w.r.t. CCD imagers
  - sensitivity, especially for applications with low S/N signals
- customization for small volumes is more expensive
  - CCD cameras have been on the market since much longer time



# Fast image processing for fast motion control

video



video



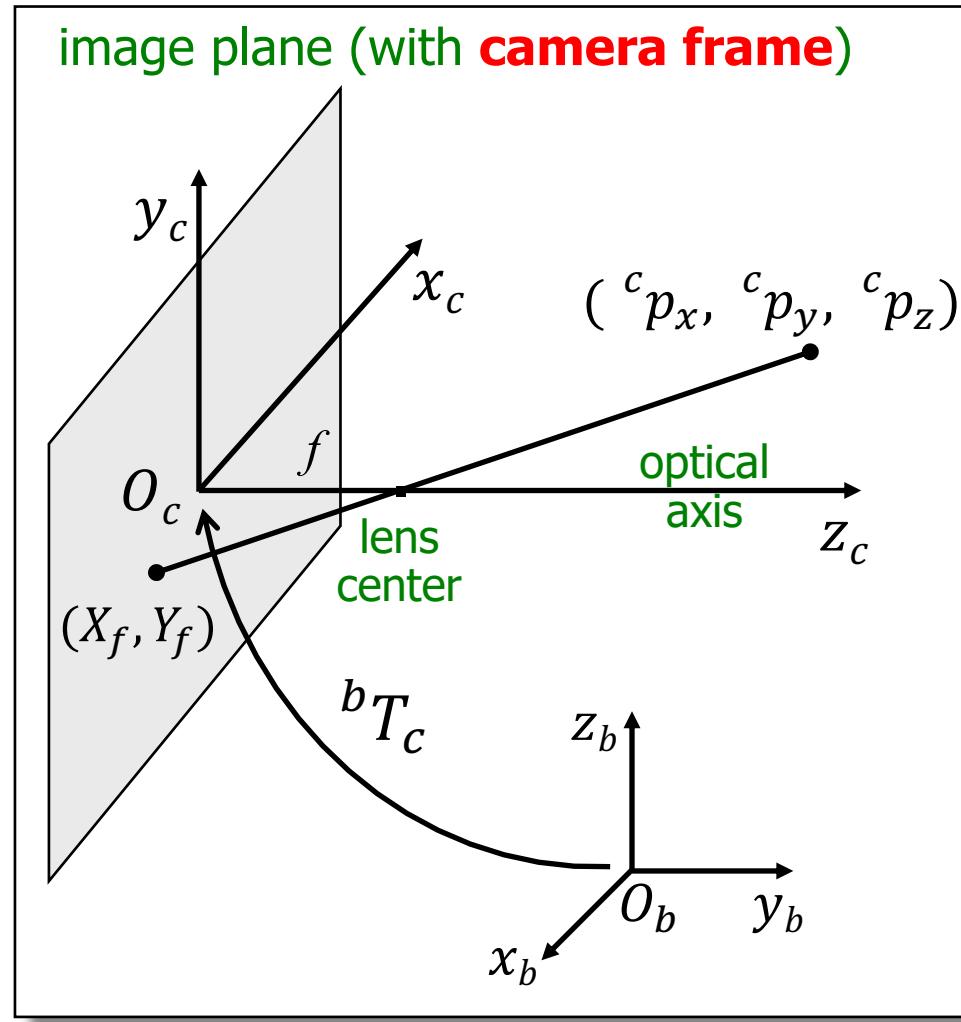
video

- 1 KHz vision frame rate
- 1 KHz robot control rate  
@ Ishikawa Lab – U Tokyo  
(2007-09)





# Perspective transformation with pinhole camera model



1. in metric units

$$X_f = \frac{f \ ^c p_x}{f - ^c p_z} \quad Y_f = \frac{f \ ^c p_y}{f - ^c p_z}$$

2. in pixel

$$X_I = \frac{\alpha_x f \ ^c p_x}{f - ^c p_z} + X_0$$

$$Y_I = \frac{\alpha_y f \ ^c p_y}{f - ^c p_z} + Y_0$$

pixel/metric scaling factor

3. LINEAR MAP in homogeneous coordinates

$$X_I = \frac{x_I}{z_I} \quad Y_I = \frac{y_I}{z_I} \quad \rightarrow \quad \begin{bmatrix} x_I \\ y_I \\ z_I \end{bmatrix} = \Omega \begin{bmatrix} ^c p_x \\ ^c p_y \\ ^c p_z \\ 1 \end{bmatrix}$$

$$\Omega = \begin{bmatrix} \alpha_x & 0 & X_0 & 0 \\ 0 & \alpha_y & Y_0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1/f & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

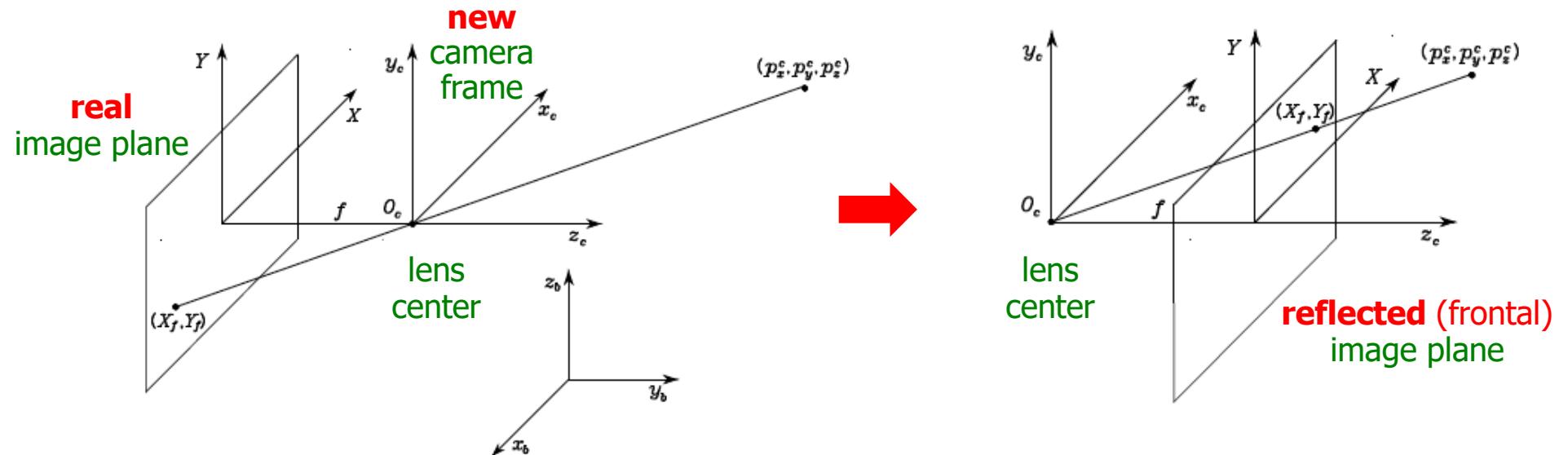
calibration  
matrix

$$H = \Omega \cdot {}^c T_b$$

intrinsic and extrinsic  
parameters



# Perspective transformation with camera frame at the lens center



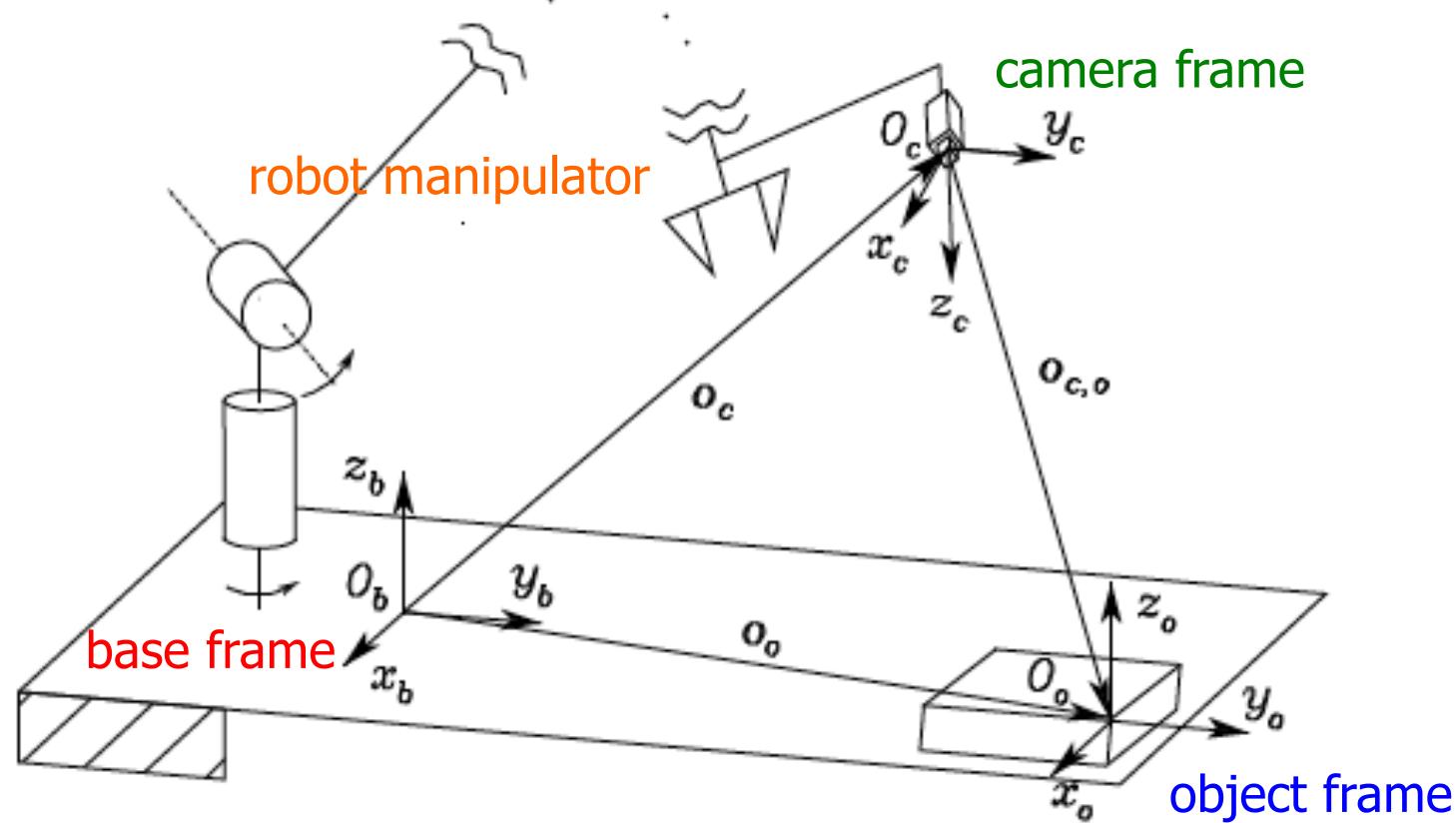
1. in metric units  $X_f = -\frac{f^c p_x}{c p_z} \quad Y_f = -\frac{f^c p_y}{c p_z}$   $\rightarrow \quad X_f = \frac{f^c p_x}{c p_z} \quad Y_f = \frac{f^c p_y}{c p_z}$

2. in pixel  $\dots$   $\rightarrow \quad X_I = \frac{\alpha_x f^c p_x}{c p_z} + X_0 \quad Y_I = \frac{\alpha_y f^c p_y}{c p_z} + Y_0$

3. LINEAR MAP in homogeneous coordinates  $\dots \rightarrow \begin{bmatrix} x_I \\ y_I \\ z_I \\ 1 \end{bmatrix} = \Omega \begin{bmatrix} c p_x \\ c p_y \\ c p_z \\ 1 \end{bmatrix} \quad \Omega = \begin{bmatrix} \alpha_x f & 0 & X_0 & 0 \\ 0 & \alpha_y f & Y_0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$



# Eye-in-hand camera



Relevant reference frames for visual-based tasks



# Kinect

## camera + structured light 3D sensor



- RGB camera (with  $640 \times 480$  pixel)
- depth sensor (by PrimeSense)
  - infrared laser emitter
  - infrared camera (with  $320 \times 240$  pixel)
- 30 fps data rate
- range:  $0.5 \div 5$  m
- depth resolution: 1cm@2m; 7cm@5m
- cost: < 90 €



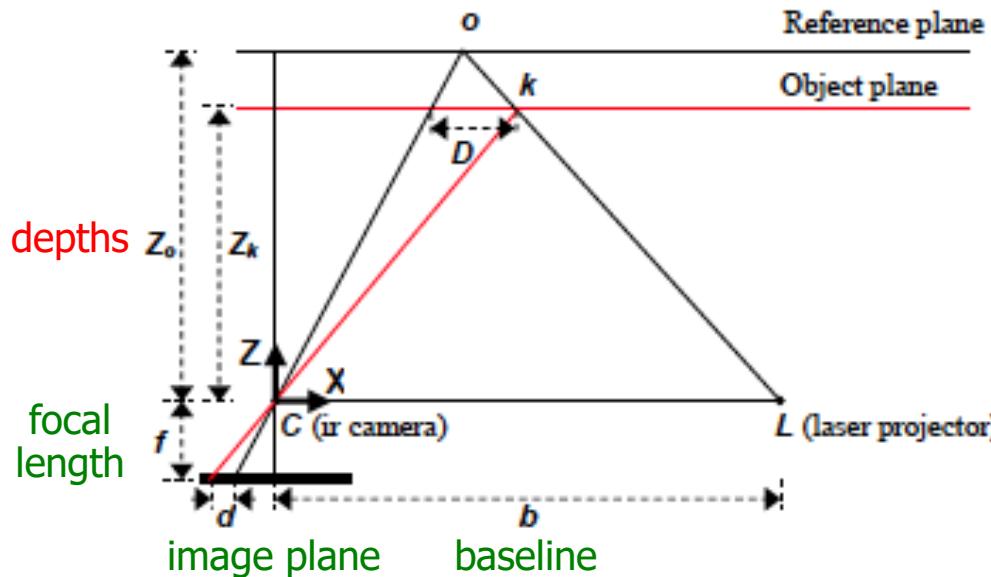
PrimeSense<sup>®</sup>  
Natural Interaction

“skeleton” extraction and  
human motion tracking



# Kinect

## Depth sensor operation



- stereo triangulation based on IR source emitting pseudo-random patterns
- reference pattern on IR camera image plane acquired in advance from a plane at known distance and coded in H/W
- correlating the disparity  $d$  (10 bits) of reference and received object patterns provides the object depth  $z_k$

1. triangulation equations (by similarity of triangles)

$$\frac{D}{b} = \frac{z_0 - z_k}{z_0} \quad \& \quad \frac{d}{f} = \frac{D}{z_k} \rightarrow z_k = \frac{z_0}{1 + \frac{d}{fb} z_0} \quad \begin{matrix} \xrightarrow{\text{green}} & x_k = -\frac{z_k}{f} (X_k - X_0 + \delta X) \\ \xrightarrow{\text{green}} & y_k = -\frac{z_k}{f} (Y_k - Y_0 + \delta Y) \end{matrix}$$

2. accurate calibration of sensor

baseline length  $b$ , depth of reference  $z_0$  + camera intrinsic parameters  
(focal length  $f$ , lens distortion coefficients  $\delta X, \delta Y$ , center offsets  $X_0, Y_0$ )



# How Kinect works (a 2-minute illustration...)

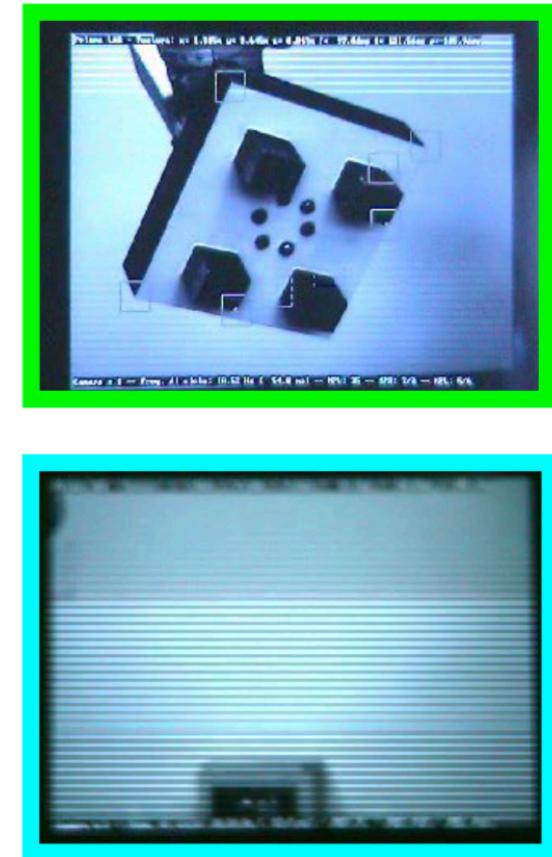
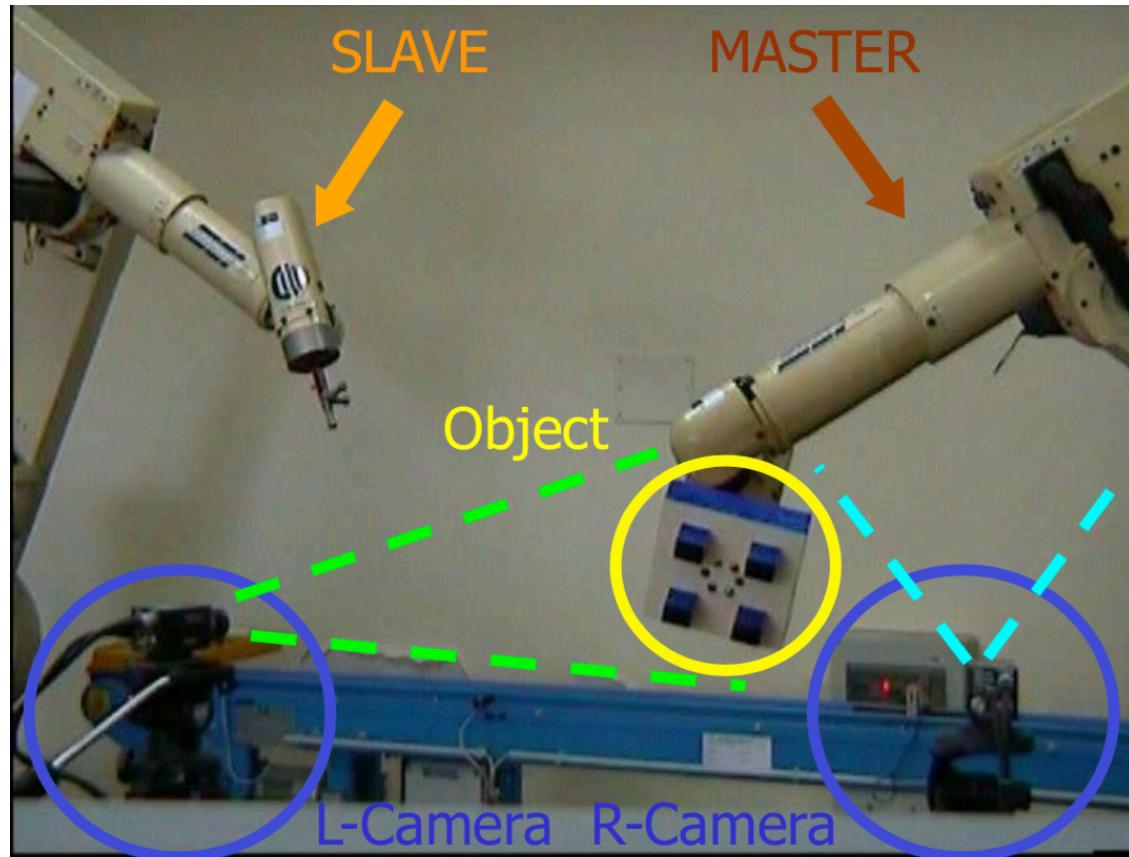


<http://youtu.be/uq9SEJxZiUg>



# Manipulators and vision systems

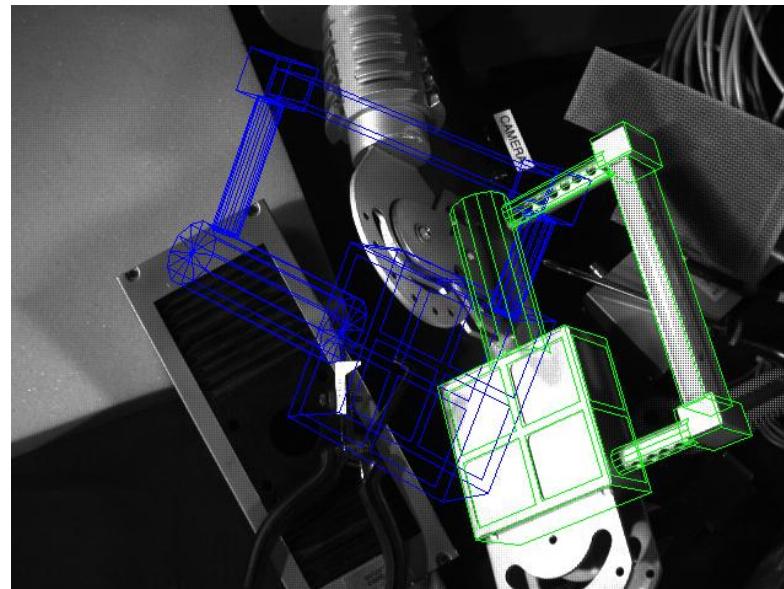
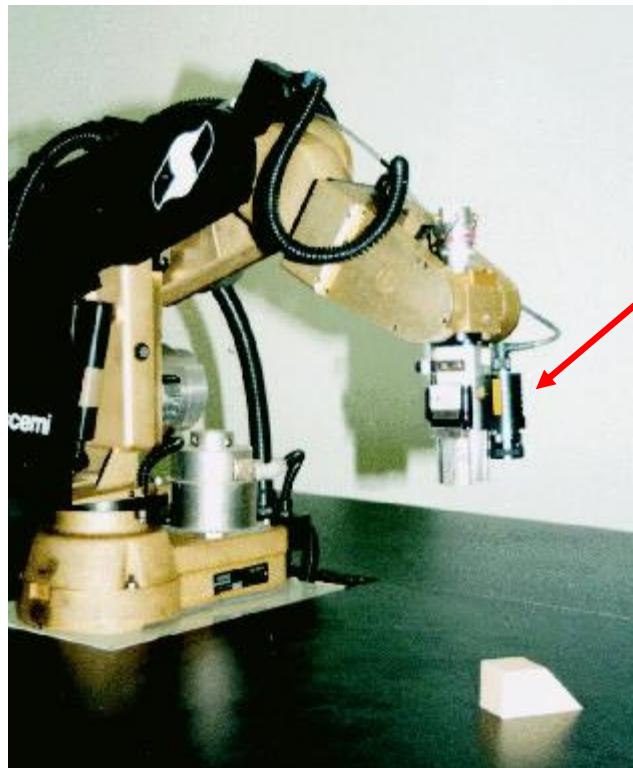
- stereovision with two external cameras, fixed in the environment (**eye-to-hand**)





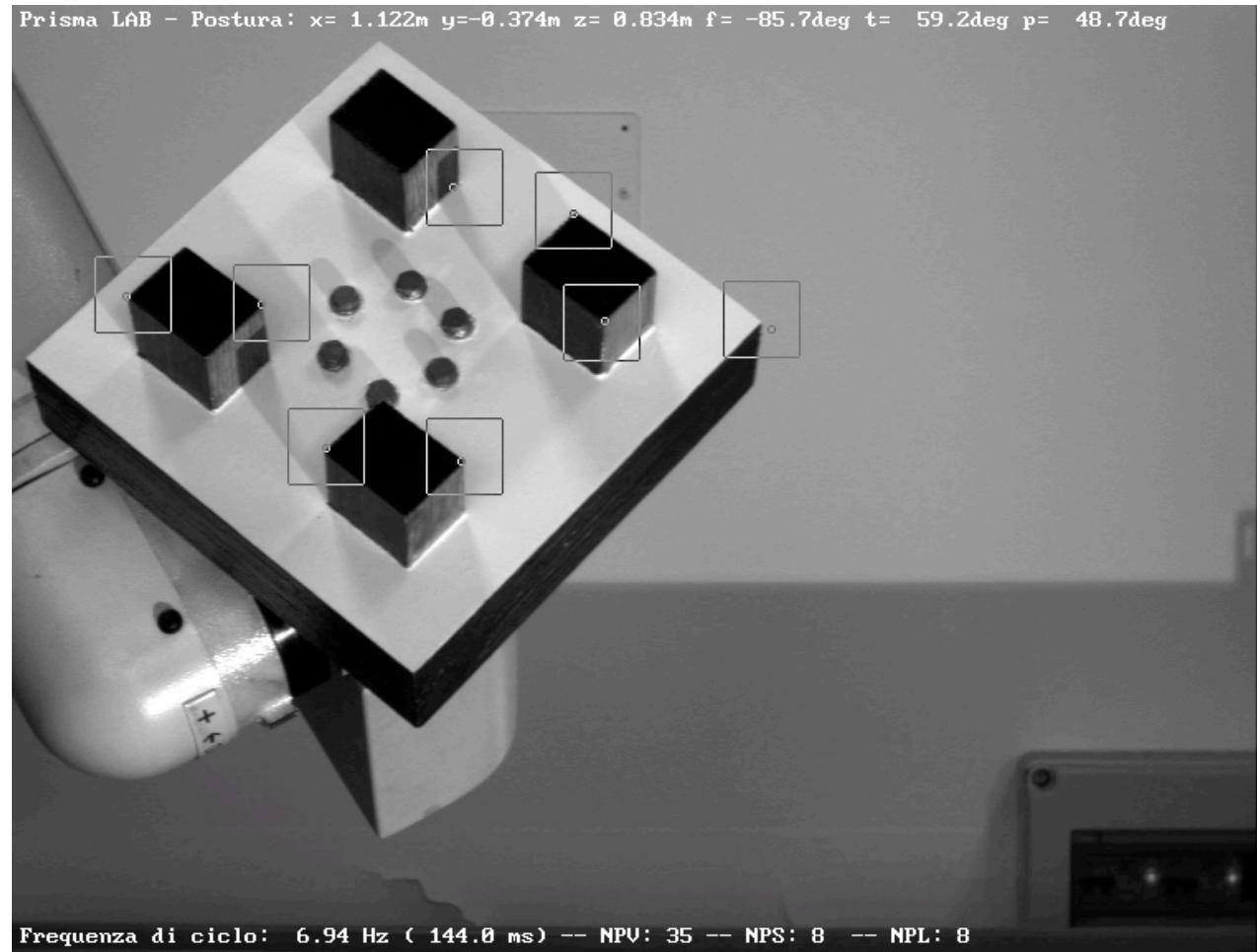
# Manipulators and vision systems

- CCD camera mounted on the robot for controlling the end-effector positioning (**eye-in-hand**)





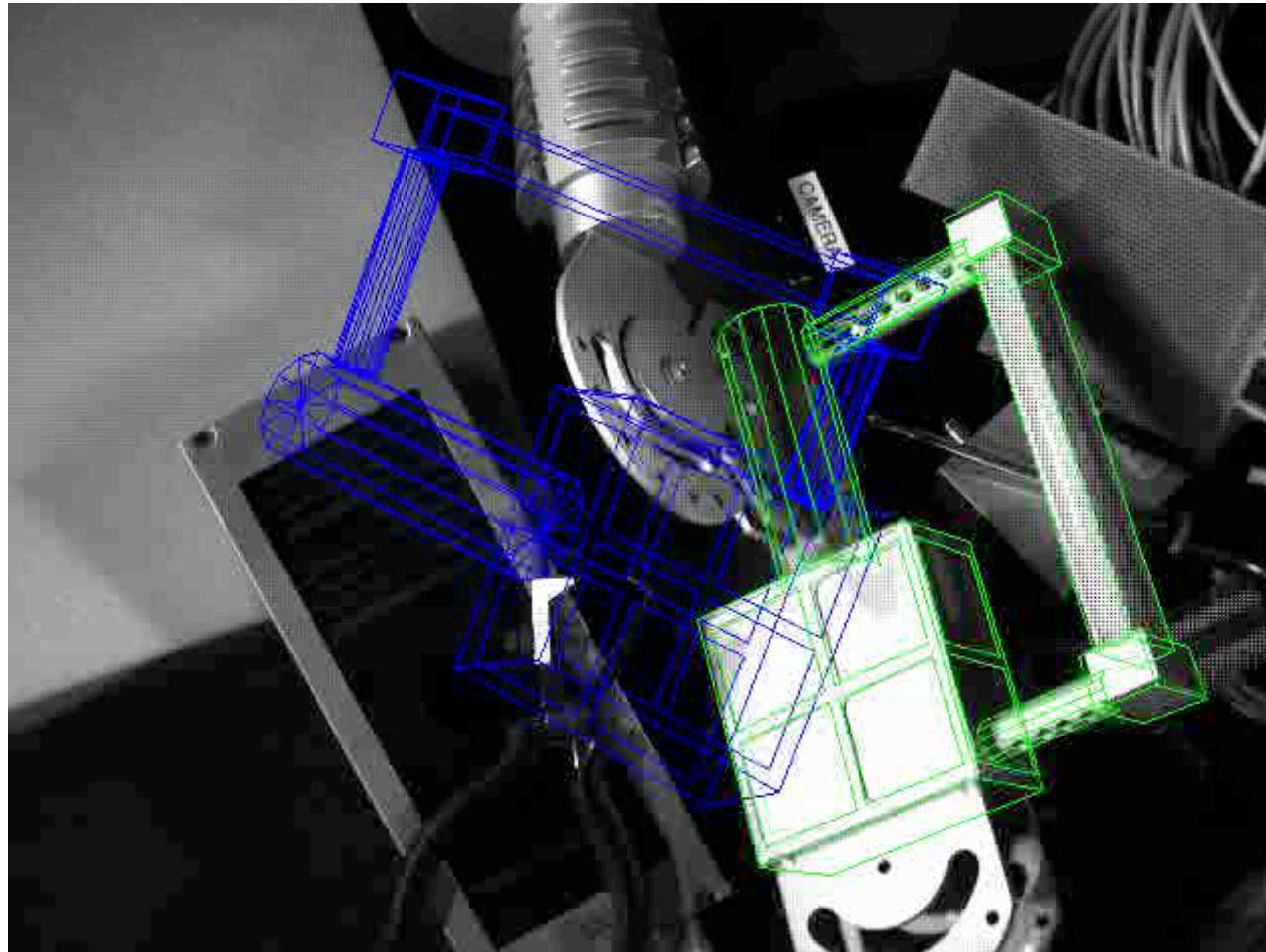
# Visual tracking eye-to-hand



COMAU robot with position-based 6D tracking from external camera  
(DIS, Università di Napoli Federico II)



# Visual servoing eye-in-hand

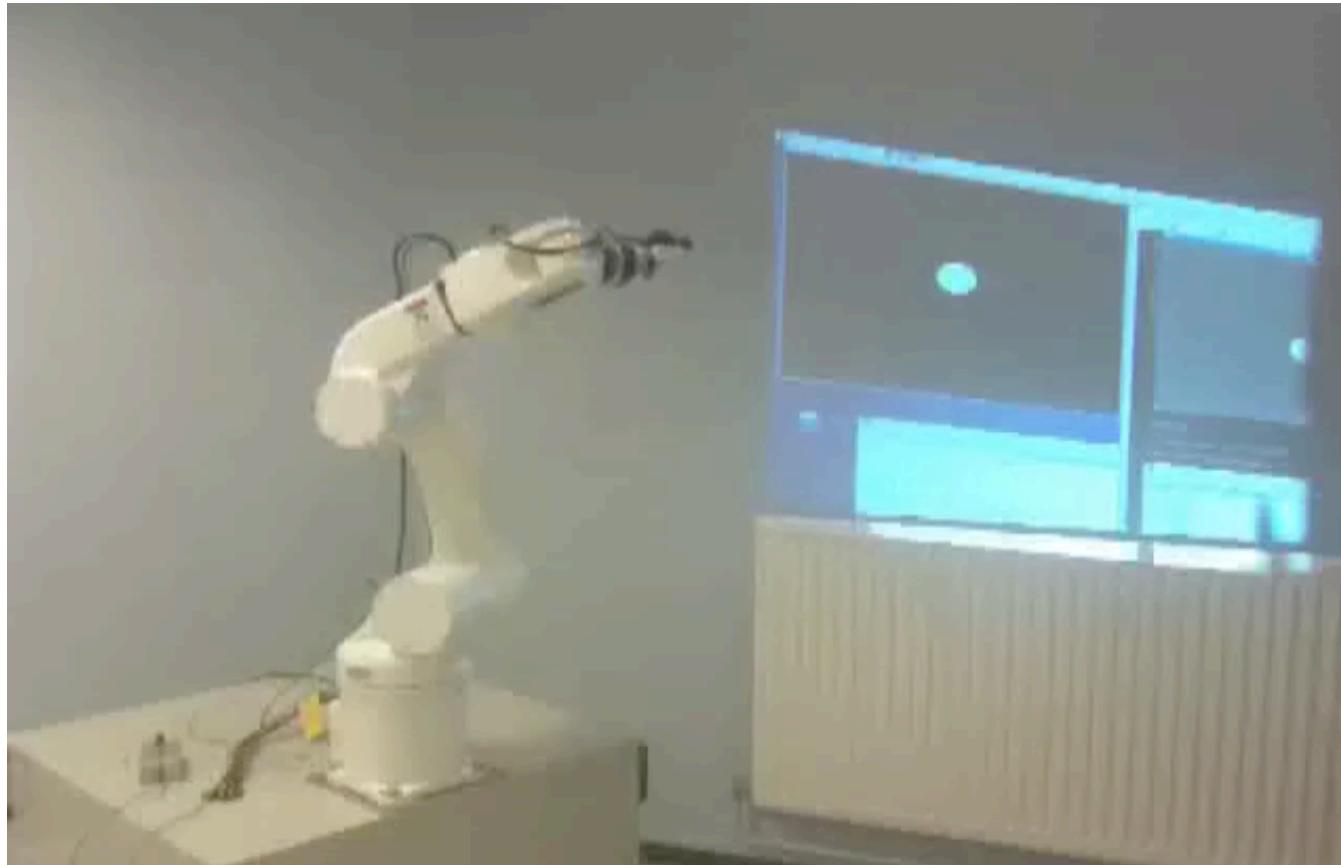


video

Image-based servoing with camera mounted on the robot end-effector  
(IRISA/INRIA, Rennes)



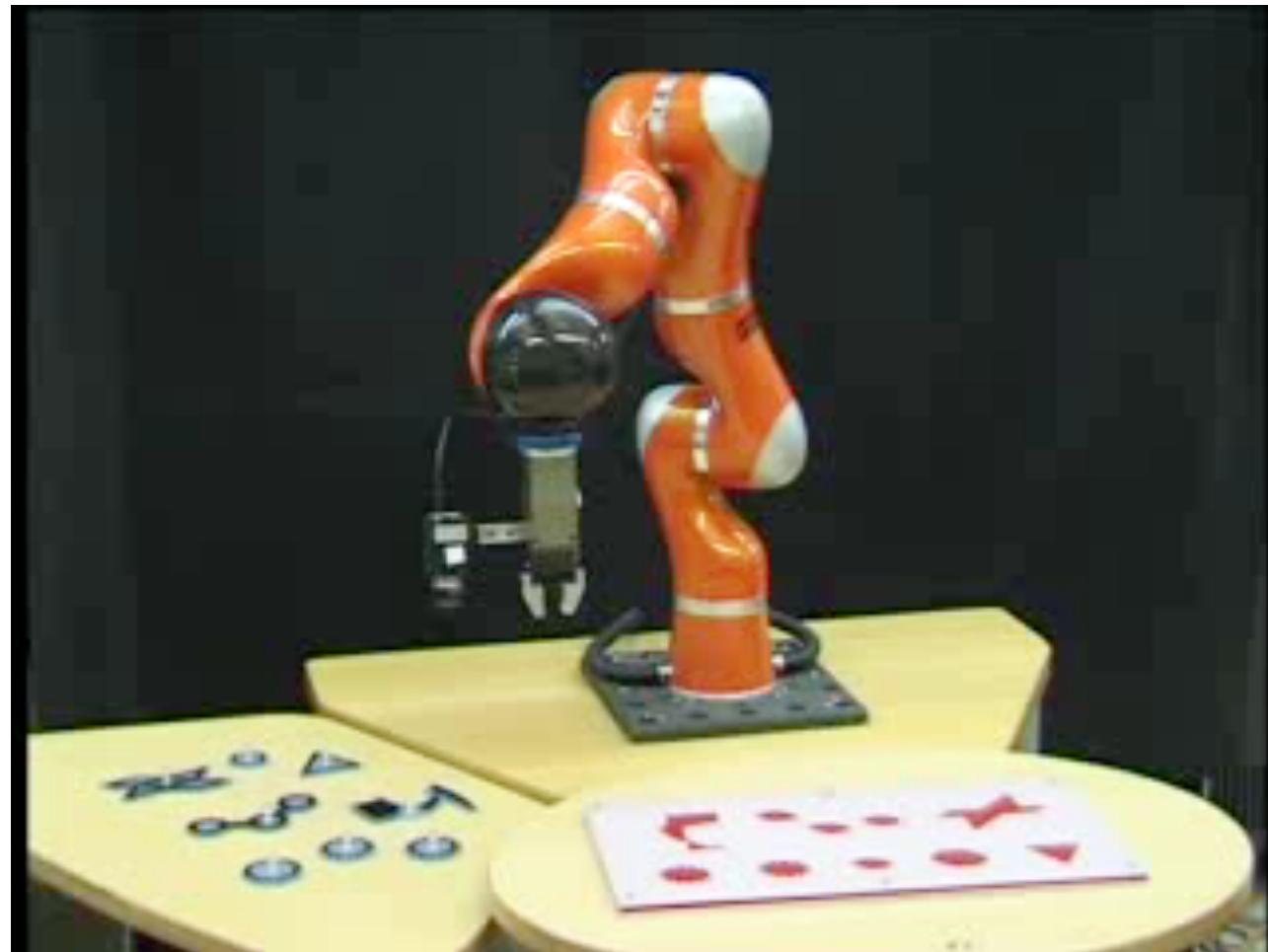
# Visual servoing and redundancy



visual servoing of circle feature ( $m = 3: p_x, p_y, r$ ) by Adept Viper robot ( $n = 6$ ):  
redundancy is used for avoiding joint range limits (IRISA/INRIA, Rennes)



# Combined visual/force assembly



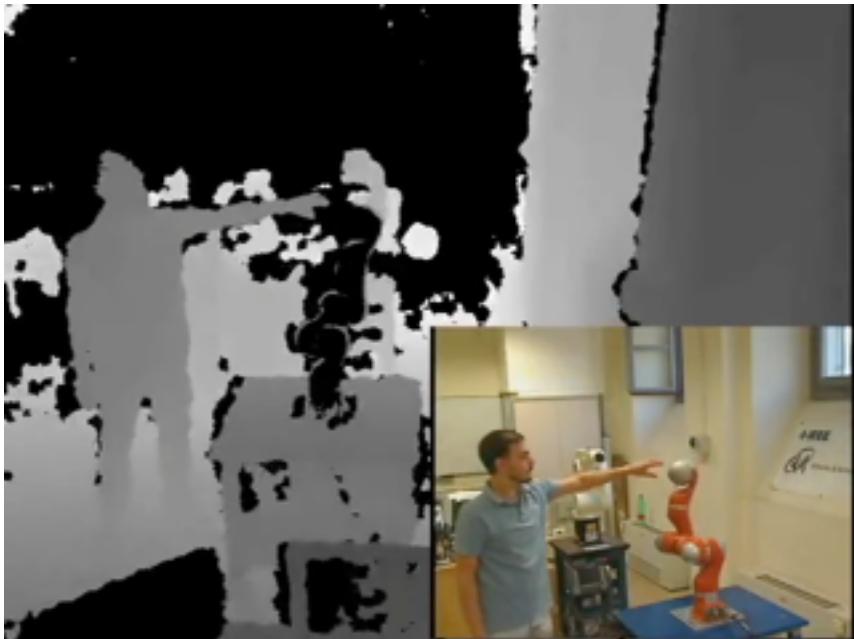
video

KUKA LWR with eye-in-hand camera and F/T sensor  
(DLR, IEEE ICRA'07 demo in Roma)

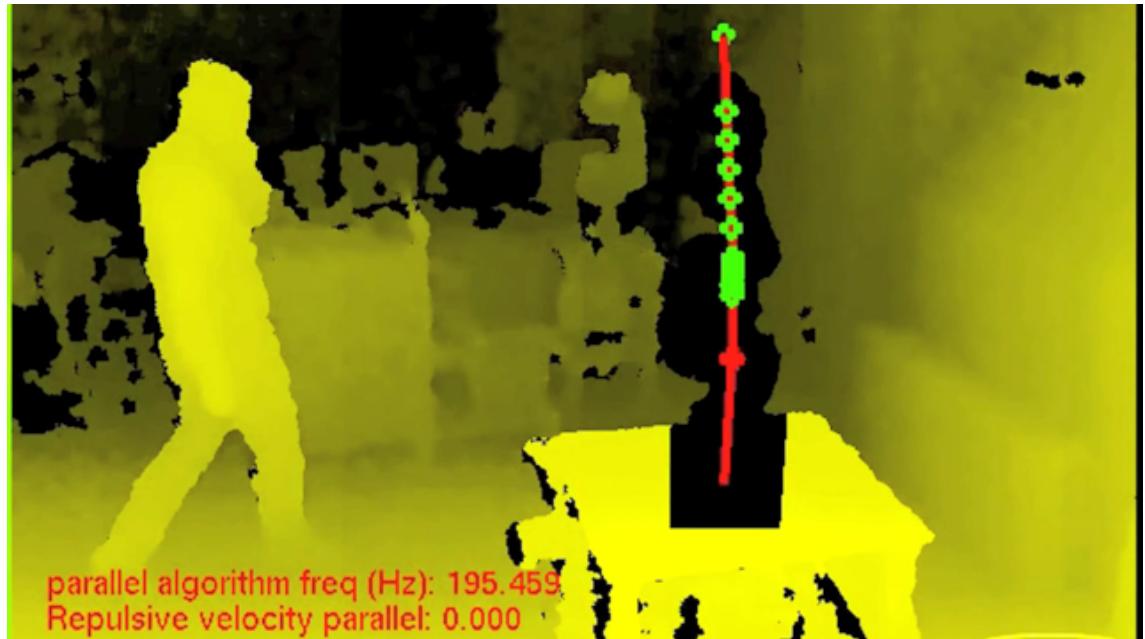
# On-line distance computation and human-robot coexistence



video



monitoring **left-** and **right-hand**  
distance to the robot (at same time)



several **control points** on robot **skeleton**  
used to compute distances and control motion

KUKA LWR with a Kinect monitoring its workspace  
(DIAG Robotics Laboratory, EU project SAPHARI, 2013)